

Figure 1: Most likely sequence

The sequence is $\mathbf{gangnamstyle}$

The following is the Matlab source code

```
//
// main.cpp
// cs_hw5_verbiti
//
// Created by Ning Ma on 2/23/13.
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//
#include <iostream>
#include <fstream>
#include <sstream>// for istringstream
#include <vector>
#include <set>
#include <algorithm>
#include <cmath>

using namespace std;
```

```
//read initial data from the txt files
void initialize(string a, vector<vector<double>>& matrix)
                   vector <double > row;
    string line;
    double number = 0;
    ifstream myfile;
    myfile.open(a);
    if (! myfile)
        cout << "can't open or find the file" << endl;
        exit (1);
    while (getline (myfile, line))//get next line from the file
        if (line.empty())
            continue;
        istringstream inputstream (line);//separtae the line based on the spaces between
        row.clear();
        while( inputstream >> number )
            //cout << number << " ";
            row.push_back(number);//get a row of matrix
        // cout << endl;
        matrix.push_back(row);//get the matrix
    myfile.close();
}
int main(int argc, const char * argv[])
    //L_matrix : compute the matrix L_it;
    //Theta_matrix : the matrix which record the most likely transition
    vector<vector<double>> Ini_state, A_transition, B_emission, O_observation;
    vector < double > temp_column;
    vector<vector<double> >::iterator iter_r;
    vector < double > :: iterator iter;
    double max_value;
    typedef const vector<double>::size_type CONST_vec_sz;
    typedef const vector<vector<double> >::size_type CONST_vec_vec_sz;
    typedef vector < double >:: size_type vec_sz;
    typedef vector<vector<double> >::size_type vec_vec_sz;
```

```
vec_vec_sz j, i;
vec_sz t, max_index;
initialize ("emissionMatrix.txt", B_emission);
initialize("initialStateDistribution.txt", Ini_state);
initialize ("transitionMatrix.txt", A_transition);
initialize("observations.txt",O_observation);
CONST_vec_vec_sz N_state = Ini_state.size();//number of states
CONST_{vec\_sz} T = O_{observation}[0]. size(); //number of observations
cout << N_state << " " << T << endl;
vector<vector<double>>L_matrix(N_state, vector<double>(T));
vector < vec_sz > S_star(T);
vector < vec_sz >> Theta_matrix (N_state, vector < vec_sz > (T));
temp_column.clear();
for (i = 0; i < N_state; i++)
    L_matrix[i][0] = log( Ini_state[i][0] ) + log( B_emission[i][O_observation[0]
    //cout << L_matrix[i][0] << endl;
for (t = 1; t < T; t++)
    for ( j = 0; j < N_state; j++)
        for (i = 0; i < N_state; i++)
            temp\_column.push\_back(L\_matrix[i][t-1] + log(A\_transition[i][j]));
            //cout << temp_column[i] <<endl;</pre>
        }
        iter = max_element( temp_column.begin(),temp_column.end() );
        max_index = iter - temp_column.begin();
        max_value = *iter;
        L_{matrix}[j][t] = \max_{value} + \log(B_{emission}[j][O_{observation}[0][t]]);
        Theta_matrix [j][t] = \max_{i=1}^{n} dex;
        temp_column.clear();
        //cout << Theta_matrix[j][t] << endl;
    }
//cout << Theta_matrix[16][2] << endl;
for (i = 0; i < N_state; i++)
    temp_column.push_back(L_matrix[i][T-1]);
iter = max_element( temp_column.begin(),temp_column.end() );
\max_{i=1}^{n} idex = iter - temp_{column.begin}();
```

```
S_{star}[T-1] = max_{index}+1;
cout \ll S_star[T-1] \ll endl;
for (t = T-2; t > 0; t--)
     \begin{array}{l} S_{-}star\,[\,t\,] \;=\; Theta_{-}matrix\,[\,S_{-}star\,[\,t+1]-1][\,t+1]+1;\\ //\,cout \;<<\; S_{-}star\,[\,t\,] \;<<\; "\;\; <<\; t\; <<\; endl\,; \end{array}
S_{star}[0] = Theta_{matrix}[S_{star}[1]][1];
/*for(i = 0; i < O_observation.size(); i++)
     row = O_observation[i];
     for (j = 0; j < row.size(); j++)
          cout << row[j] << " ";
     }
     cout << endl;</pre>
}*/
ofstream outfile;
outfile.open("S_star.txt");
if (!outfile)
     cout << "can't open a file" <<endl;</pre>
for (t = 0; t < T; t++)
     outfile << S_star[t] << endl;
outfile.close();
return 0;
```

}