

## Problem Set 5, Part I

### Problem 1: Sorting practice

1-1)

{3, 4, 18, 24, 33, 40, 8, 10, 12}

1-2)

{4, 10, 18, 24, 33, 40, 8, 3, 12}

1-3)

{4, 10, 18, 8, 3, 12, 24, 33, 40}

1-4)

{10, 18, 4, 24, 12, 3, 8, 40, 33}

1-5)

{10, 8, 4, 3, 12, 24, 18, 40, 33}

1-6)

{4, 10, 18, 24, 33, 40, 8, 3, 12}

### Problem 2: Practice with big-O

2-1)

| function                  | big-O expression |
|---------------------------|------------------|
| $a(n) = 5n + 1$           | $a(n) = O(n)$    |
| $b(n) = 5 - 10n - n^2$    | $b(n) = O(n^2)$  |
| $c(n) = 4n + 2\log(n)$    | $c(n) = O(n)$    |
| $d(n) = 6n\log(n) + n^2$  | $d(n) = O(n^2)$  |
| $e(n) = 2n^2 + 3n^3 - 7n$ | $e(n) = O(n^3)$  |

2-2)

$O(n^2)$

The “i” loop iterates 3 times. The “j” loop iterates n times. The “k” loop iterates  $(n+1)/2$  times. All in all, they iterate  $3n(n+1)/2$  times, which is  $O(n^2)$ .

2-3)

$O(n\log(n))$

The outer loop (noted by i) iterates n times, while the iterating times of the inner loop is the power of 2, which means it iterates  $\log(n)$  times. Combining them, we get  $n \cdot \log(n)$  times.

### Problem 3: Comparing two algorithms

*worst-case time efficiency of algorithm A:  $O(n^2)$*

explanation: when every element in the `arr[]` are the same, `numDups++` needs to run  $(n+1) \cdot n/2$  times, which is  $O(n^2)$

*worst-case time efficiency of algorithm B:  $O(n\log(n))$*

explanation: the time efficiency of merge sort is  $n\log(n)$ , which is more complicated than the following loop whose time efficiency is n.

#### Problem 4: Practice with references

4-1)

| Expression       | Address | Value |
|------------------|---------|-------|
| n                | 0x100   | 0x712 |
| n.ch             | 0x712   | 'n'   |
| n.prev           | 0x718   | 0x064 |
| n.prev.prev      | 0x070   | 0x360 |
| n.prev.next.next | 0x714   | Null  |
| n.prev.prev.next | 0x362   | 0x064 |

4-2)

x.next= n.prev.prev.next.next;

x.prev= n.prev.prev.next;

n.prev.next=x;

n.prev=x;

4-3)

```
public static void initPrevs(DNode n) {  
    DNode trav = n;  
    while (trav != null) {  
        trav.next.prev = trav;  
        trav = trav.next;  
    }  
}
```