aml-hw1-solutions-yx2845

September 28, 2023

0.1 Homework 1: Applied Machine Learning

This assignment covers contents of the first three lectures.

The emphasis for this assignment would be on the following: 1. Data Visualization and Analysis 2. Linear Models for Regression and Classification 3. Support Vector Machines

```
[2]: import warnings

def fxn():
    warnings.warn("deprecated", DeprecationWarning)

with warnings.catch_warnings():
    warnings.simplefilter("ignore")
    fxn()
```

```
import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
from matplotlib.lines import Line2D
from numpy.linalg import inv
%matplotlib inline
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler, OneHotEncoder, OrdinalEncoder
from sklearn.metrics import r2_score
from sklearn.svm import LinearSVC, SVC
from google.colab import drive
drive.mount('/content/drive')
```

Mounted at /content/drive

0.2 Part 1: Data Visualization and Analysis

Data visualization comes in handy when we want to understand data characteristics and read patterns in datasets with thousands of samples and features.

Note: Remember to label plot axes while plotting.

0.2.1 The dataset to be used for this section is bike_rental.csv.

```
[4]: # Load the dataset
     bike_rental_df = pd.read_csv('/content/drive/My_Drive/bike_rental.csv')
     bike_rental_df
[4]:
                                       weekday working day weather
             month season holiday
                                                                         temp \
                                                            cloudy
                                                                    0.344167
     0
           January
                    winter
                                No
                                      Saturday
                                                        No
     1
           January
                    winter
                                No
                                        Sunday
                                                        No
                                                            cloudy
                                                                    0.363478
     2
           January
                    winter
                                No
                                        Monday
                                                       Yes
                                                             clear
                                                                    0.196364
     3
                                       Tuesday
                                                                    0.200000
           January
                    winter
                                No
                                                       Yes
                                                             clear
     4
           January
                    winter
                                No
                                    Wednesday
                                                       Yes
                                                             clear 0.226957
     . .
                                                             •••
     726
          December
                    winter
                                No
                                      Thursday
                                                       Yes
                                                            cloudy 0.254167
     727
          December
                    winter
                                No
                                        Friday
                                                            cloudy 0.253333
                                                       Yes
     728
         December winter
                                No
                                      Saturday
                                                        No
                                                            cloudy 0.253333
     729
          December winter
                                No
                                        Sunday
                                                        No
                                                             clear
                                                                    0.255833
     730
         December winter
                                No
                                        Monday
                                                       Yes cloudy 0.215833
          feels temp humidity
                                windspeed
                                            casual registered
                                                               count
     0
            0.363625 0.805833
                                 0.160446
                                               331
                                                                  985
                                                           654
     1
                                                           670
                                                                  801
            0.353739 0.696087
                                 0.248539
                                               131
     2
            0.189405 0.437273
                                 0.248309
                                               120
                                                          1229
                                                                  1349
     3
            0.212122 0.590435
                                 0.160296
                                               108
                                                          1454
                                                                  1562
     4
            0.229270 0.436957
                                                82
                                 0.186900
                                                          1518
                                                                  1600
     726
            0.226642 0.652917
                                 0.350133
                                               247
                                                          1867
                                                                  2114
     727
            0.255046 0.590000
                                                          2451
                                                                  3095
                                 0.155471
                                               644
     728
            0.242400 0.752917
                                 0.124383
                                               159
                                                          1182
                                                                  1341
```

[731 rows x 13 columns]

0.231700 0.483333

0.223487 0.577500

729

730

1.1 Create a bar chart to compare the average bike rental count on holiday and non-holiday week-days. Are there differences in rental patterns?

364

439

1432

2290

1796

2729

0.350754

0.154846

```
[17]: ### Code here
# Define colors and their labels
colors = ['Salmon', 'skyblue']
labels = ['Non-Holiday', 'Holiday']

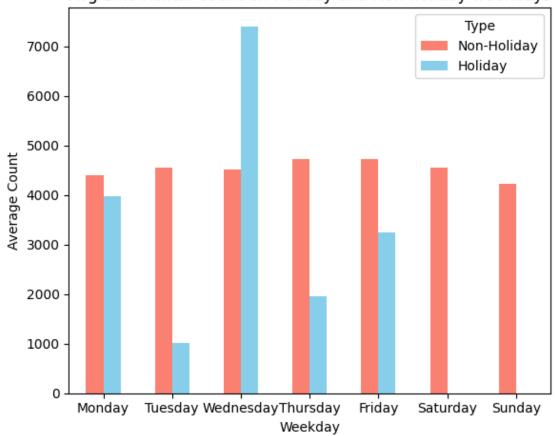
# Prepare data for plotting
avg_counts = bike_rental_df.groupby(['weekday','holiday'])['count'].mean().
ounstack()
order = ['Monday', 'Tuesday', 'Wednesday', 'Thursday', 'Friday', 'Saturday',
o'Sunday']
avg_counts = avg_counts.reindex(order)
```

```
# Create the plot
fig, ax = plt.subplots(figsize=(6, 5))
avg_counts.plot(kind='bar', color=colors, ax=ax)

# Setting the title and labels for the plot
ax.set_title("Avg Bike Rental Count on Holiday and Non-holiday weekdays")
ax.set_xlabel("Weekday")
ax.set_ylabel("Average Count")
ax.legend(title="Type", labels=labels)
ax.set_xticklabels(order, rotation=0)

# Adjust layout and display
plt.tight_layout()
plt.show()
```





[18]: | ### Comment here

```
# The graph provides a breakdown for individual weekdays. Notably, for non-holidays,

# the average bike rental counts consistently hover above 4,000 across all weekdays, showcasing limited variation.

# However, holidays present a different narrative. On Wednesdays that fall on holidays, the average bike rental

# count significantly surpasses its non-holiday counterpart. For other days, the average bike rental count on holidays

# is less than the average bike rental count when it is not holiday. In particular, the bike rental

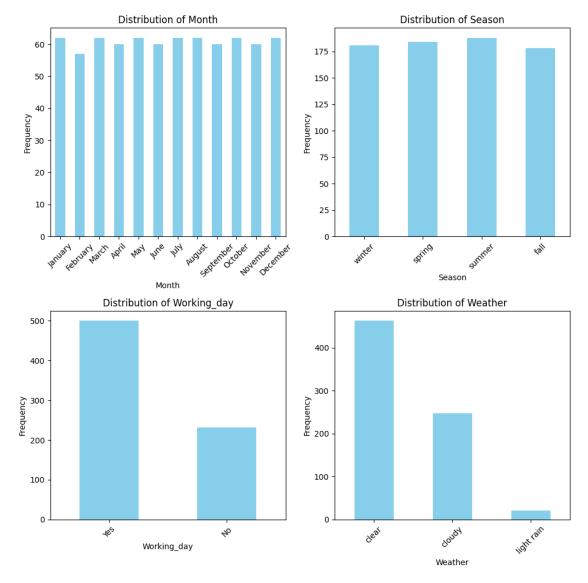
# average count on Tuesdays that are holidays are the lowest among all, followed by Thursday and Friday.
```

1.2 Plot a small multiple of bar charts to understand data distribution of the following categorical variables. 1. month 2. season 3. working day 4. weather

```
[19]: ### Code here
      # List of categorical variables
      variables = ['month', 'season', 'working_day', 'weather']
      # Order month and season chronologically
      month_order = ['January', 'February', 'March', 'April', 'May', 'June', 'July', |
       →'August', 'September', 'October', 'November', 'December']
      season_order = ['winter', 'spring', 'summer', 'fall']
      # Setting up the figure and axes
      fig, axs = plt.subplots(nrows=2, ncols=2, figsize=(10, 10))
      for ax, variable in zip(axs.ravel(), variables):
          # Count the frequency of each category
          freq = bike_rental_df[variable].value_counts()
          # Ordering by specific sequence or by size
          if variable == 'month':
              freq = freq.reindex(month_order)
          elif variable == 'season':
              freq = freq.reindex(season_order)
          else:
              # For 'working_day' and 'weather'
              freq = freq.sort_values(ascending=False)
          # Plot bar chart
          freq.plot(kind='bar', ax=ax, color='skyblue')
          # Set title and labels
          ax.set_title(f'Distribution of {variable.capitalize()}')
          ax.set_ylabel('Frequency')
```

```
ax.set_xlabel(variable.capitalize())
ax.tick_params(axis='x', rotation=45)

# Adjust layout
plt.tight_layout()
plt.show()
```

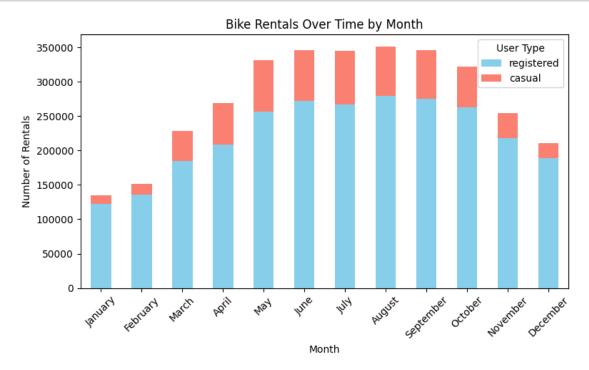


1.3 Compare the number of registered and casual bike rentals over time by month. Create a stacked bar chart to show the contributions of each user type.

```
[21]: ### Code here
# Ensure month ordering
```

```
bike_rental_df['month'] = pd.Categorical(bike_rental_df['month'],_
 ⇔categories=month_order, ordered=True)
# Group by month and sum 'registered' and 'casual' columns
monthly_data = bike_rental_df.groupby('month').agg({'registered': 'sum',_
 # Plotting
monthly_data.plot(kind='bar', stacked=True, figsize=(8, 5), color=['skyblue',_

¬'salmon'])
# Set titles and labels
plt.title('Bike Rentals Over Time by Month')
plt.ylabel('Number of Rentals')
plt.xlabel('Month')
plt.xticks(rotation=45)
plt.legend(title='User Type')
# Adjust layout
plt.tight_layout()
plt.show()
```

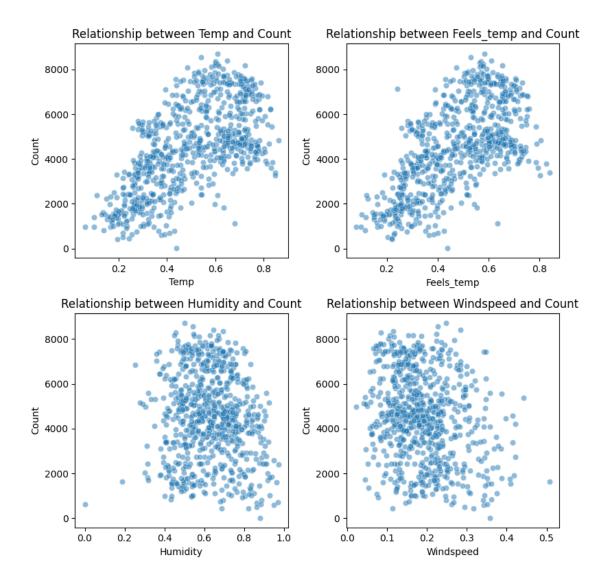


1.4 Plot relationships between the following features and the target variable count as a small multiple of scatter plots.

- 1. temp
- 2. feels_temp
- 3. humidity
- 4. windspeed

```
[22]: ### Code here
      # List of features
      features = ['temp', 'feels_temp', 'humidity', 'windspeed']
      # Setting up the figure and axes
      fig, axs = plt.subplots(nrows=2, ncols=2, figsize=(8, 8))
      for ax, feature in zip(axs.ravel(), features):
          # Scatter plot
          ax.scatter(bike_rental_df[feature], bike_rental_df['count'], alpha=0.5,_

→edgecolors='w', linewidth=0.5)
          # Set title and labels
          ax.set_title(f'Relationship between {feature.capitalize()} and Count')
          ax.set_ylabel('Count')
          ax.set_xlabel(feature.capitalize())
      # Adjust layout
      plt.tight_layout()
      plt.show()
```



0.3 Part 2: Linear Models for Regression and Classification

In this section, we will be implementing three linear models linear regression, logistic regression, and SVM. We will see that despite some of their differences at the surface, these linear models (and many machine learning models in general) are fundamentally doing the same thing that is, optimizing model parameters to minimize a loss function on data.

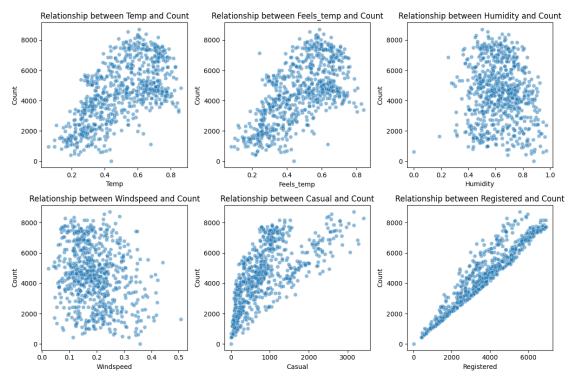
0.3.1 2.1 Linear Regression

The objective of this dataset is to predict the count of bike rentals based on weather and time. We will use linear regression to predict the count using weather and time.

```
[23]: # split data into features and labels
bike_rental_X = bike_rental_df.drop(columns=['count'])
bike_rental_y = bike_rental_df['count']
```

2.1.1 Plot the relationships between the label (count) and the continuous features (temp, feels_temp, humidity, windspeed, casual, registered) using a small multiple of scatter plots. Make sure to label the axes.

```
[24]: ### Code here
      # List of continuous features
      features = ['temp', 'feels_temp', 'humidity', 'windspeed', 'casual', __
       # Setting up the figure and axes
      fig, axs = plt.subplots(nrows=2, ncols=3, figsize=(12, 8)) # Adjusted for 6
       \hookrightarrow features
      for ax, feature in zip(axs.ravel(), features):
          # Scatter plot
          ax.scatter(bike_rental_X[feature], bike_rental_y, alpha=0.5,_
       ⇔edgecolors='w', linewidth=0.5)
          # Set title and labels
          ax.set_title(f'Relationship between {feature.capitalize()} and Count')
          ax.set_ylabel('Count')
          ax.set_xlabel(feature.capitalize())
      # Adjust layout
      plt.tight_layout()
      plt.show()
```



2.1.2 From the visualizations above, do you think linear regression is a good model for this problem? Why and/or why not? Please explain.

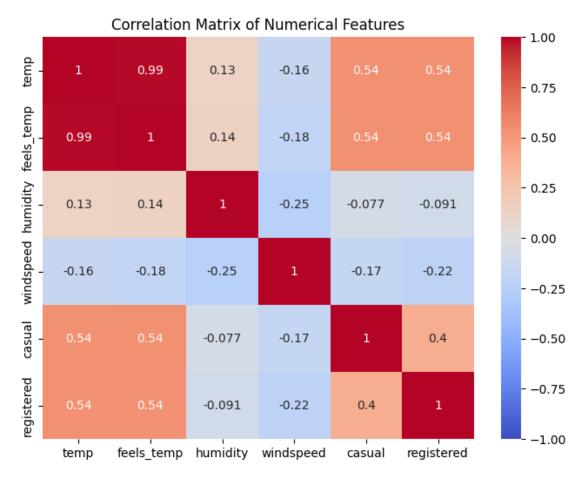
0.3.2 Data Preprocessing

Before we can fit a linear regression model, there are several pre-processing steps we should apply to the datasets:

- 1. Encode categorial features appropriately.
- 2. Remove highly collinear features by reading the correlation plot.
- 3. Split the dataset into training (60%), validation (20%), and test (20%) sets.
- 4. Standardize the columns in the feature matrices X_train, X_val, and X_test to have zero mean and unit variance. To avoid information leakage, learn the standardization parameters (mean, variance) from X_train, and apply it to X_train, X_val, and X_test.
- 5. Add a column of ones to the feature matrices X_train, X_val, and X_test. This is a common trick so that we can learn a coefficient for the bias term of a linear model.
- 2.1.3 Encode the categorical variables of the Bike Rental dataset.

2.1.4 Plot the correlation matrix, and check if there is high correlation between the given numerical features (Threshold >=0.9). If yes, drop one from each pair of highly correlated features from the dataframe. Why is necessary to drop those columns before proceeding further?

```
[28]: ### Code here
# Selecting only the numerical features for the correlation matrix
```



```
[29]: ### Code here

to_drop = set() # to store features to drop

for i in range(len(correlation_matrix.columns)):

    for j in range(i):

        if abs(correlation_matrix.iloc[i, j]) >= 0.9:

            colname_i = correlation_matrix.columns[i] # getting the name of occlumn i
```

```
colname_j = correlation_matrix.columns[j] # getting the name of of the column j

to_drop.add(colname_i) # add one of them to the drop list

# Drop the identified columns
bike_rental_encoded_X = bike_rental_encoded_X.drop(columns=to_drop)
```

```
[30]: ### Comment here
      # The regression coefficient for an independent variable represents the mean
      ⇔change in
      # the dependent variable for a one-unit change in that independent variable,
      ⇔holding all
      # other independent variables constant. However, when independent variables are
      ⇒highly correlated,
      # one unit changes in one variable will also cause shifts in its correlated \Box
      ⇔variables. This will make
      # model difficult to estimate the coefficients, thereby increasing the
       ⇔complexity of the model.
      # In the mean time, it can create noise and make the coefficient estimates,
      →unstable (high variance). Last but not least,
      # dropping one of the two highly correlated models will not worsen the
      →performance the model, because it
      # does not bring additional information to the model.
```

2.1.5 Split the dataset into training (60%), validation (20%), and test (20%) sets.

```
[31]: #Drop register and casual bike_rental_encoded_X.drop(columns=['registered',u \( \text{`casual'} \)])
```

2.1.6 Standardize the columns in the feature matrices.

```
[33]: ### Code here
# Initialize the scaler using the training data
scaler = StandardScaler()
```

```
# Initalize and fit the scaler only using the training data
scaler.fit(bike_rental_X_train)

# Standardize them in train, val and test sets
bike_rental_X_train = scaler.transform(bike_rental_X_train)
bike_rental_X_val = scaler.transform(bike_rental_X_val)
bike_rental_X_test = scaler.transform(bike_rental_X_test)
```

```
[34]: # Adding a column of ones to the feature matrices for the bias term.
bike_rental_X_train = np.hstack([np.ones((bike_rental_X_train.shape[0], 1)),
bike_rental_X_train])
bike_rental_X_val = np.hstack([np.ones((bike_rental_X_val.shape[0], 1)),
bike_rental_X_val])
bike_rental_X_test = np.hstack([np.ones((bike_rental_X_test.shape[0], 1)),
bike_rental_X_test])
```

At the end of this pre-processing, you should have the following vectors and matrices: -Bike Rental Prediction dataset: bike_rental_X_train, bike_rental_X_val, bike_rental_X_test, bike_rental_y_train, bike_rental_y_test

0.3.3 Implement Linear Regression

Now, we can implement our linear regression model! Specifically, we will be implementing ridge regression, which is linear regression with L2 regularization. Given an $(m \times n)$ feature matrix X, an $(m \times 1)$ label vector y, and an $(n \times 1)$ weight vector w, the hypothesis function for linear regression is:

$$y = Xw$$

Note that we can omit the bias term here because we have included a column of ones in our X matrix, so the bias term is learned implicitly as a part of w. This will make our implementation easier.

Our objective in linear regression is to learn the weights w which best fit the data. This notion can be formalized as finding the optimal w which minimizes the following loss function:

$$\min_{w} \|Xw - y\|_2^2 + \alpha \|w\|_2^2$$

This is the ridge regression loss function. The $||Xw - y||_2^2$ term penalizes predictions Xw which are not close to the label y. And the $\alpha ||w||_2^2$ penalizes large weight values, to favor a simpler, more generalizable model. The α hyperparameter, known as the regularization parameter, is used to tune the complexity of the model - a higher α results in smaller weights and lower complexity, and vice versa. Setting $\alpha = 0$ gives us vanilla linear regression.

Conveniently, ridge regression has a closed-form solution which gives us the optimal w without having to do iterative methods such as gradient descent. The closed-form solution, known as the Normal Equations, is given by:

$$w = (X^T X + \alpha I)^{-1} X^T y$$

2.1.7 Implement a LinearRegression class with two methods: train and predict.

Note: You may NOT use sklearn for this implementation. You may, however, use np.linalg.solve to find the closed-form solution. It is highly recommended that you vectorize your code.

```
[35]: class LinearRegression():
            Linear regression model with L2-regularization (i.e. ridge regression).
            Attributes
            _____
            alpha: regularization parameter
            w: (n x 1) weight vector
            def __init__(self, alpha=0):
                self.alpha = alpha
                self.w = None
            def train(self, X, y):
                '''Trains model using ridge regression closed-form solution
                (sets w to its optimal value).
                Parameters
                X : (m x n) feature matrix
                y: (m \ x \ 1) label vector
                Returns
                _____
                None
                # Identity matrix of shape (n, n)
                I = np.identity(X.shape[1])
                # Compute the weight using the closed-form solution
                self.w = np.linalg.solve(X.T @ X + self.alpha * I, X.T @ y)
                return None
            def predict(self, X):
                '''Predicts on X using trained model.
```

```
Parameters
------
X: (m x n) feature matrix

Returns
-----
y_pred: (m x 1) prediction vector
'''
return X @ self.w
```

0.3.4 Train, Evaluate, and Interpret LR Model

2.1.8 Train a linear regression model ($\alpha = 0$) on the bike rental training data. Make predictions and report the R^2 score on the training, validation, and test sets. Report the first 3 and last 3 predictions on the test set, along with the actual labels.

```
R2 score for Training set: 0.5990
R2 score for Validation set: 0.5326
R2 score for Test set: 0.5422
           Prediction Actual
Position
          4787.265096
                         3940
2
          5733.895508
                         7132
3
          2174.857758
                          705
145
          5504.144799
                         7534
146
          3951.633970
                         4118
147
          2167.033838
                          1834
```

2.1.9 As a baseline model, use the mean of the training labels (bike_rental_y_train) as the prediction for all instances. Report the R^2 on the training, validation, and test sets using this baseline.

This is a common baseline used in regression problems and tells you if your model is any good. Your linear regression R^2 should be much higher than these baseline R^2 .

```
[40]: ### Code here
    # Calculate the mean of the training labels
    mean_train = np.mean(bike_rental_y_train)

# Use this mean as the prediction for all instances
    train_pred = [mean_train] * len(bike_rental_y_train)
    val_pred = [mean_train] * len(bike_rental_y_val)
    test_pred = [mean_train] * len(bike_rental_y_test)

# Compute the R2 score
    r2_train = r2_score(bike_rental_y_train, train_pred)
    r2_val = r2_score(bike_rental_y_val, val_pred)
    r2_test = r2_score(bike_rental_y_test, test_pred)

# Report the results
    print(f"R2 score using mean baseline for Training set: {r2_train:.4f}")
    print(f"R2 score using mean baseline for Test set: {r2_test:.4f}")
    print(f"R2 score using mean baseline for Test set: {r2_test:.4f}")
```

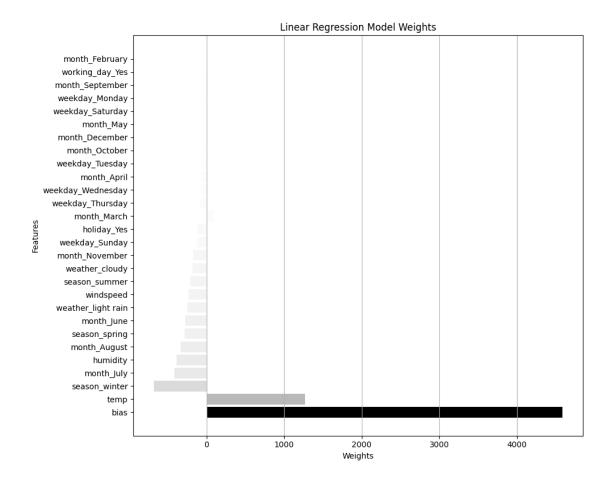
```
R2 score using mean baseline for Training set: 0.0000 R2 score using mean baseline for Validation set: -0.0209 R2 score using mean baseline for Test set: -0.0048
```

2.1.10 Interpret your model trained on the bike rental dataset using a bar chart of the model weights. Make sure to label the bars (x-axis) and don't forget the bias term!

```
[41]: ### Code here
weights = model.w

# Extracting feature names
```

```
# Add 'bias' for the bias term at the start
features = ['bias'] + bike_rental_encoded_X.columns.values.tolist()
# Creating a DataFrame for sorting
df_weights = pd.DataFrame({
    'Features': features,
    'Weights': weights
})
# Sorting by absolute weight value
df_weights = df_weights.reindex(df_weights.Weights.abs().
sort_values(ascending=False).index)
# Plotting
# Create a color map
cmap = plt.get_cmap('binary')
# Normalize values to 0-1
norm = plt.Normalize(df_weights.Weights.abs().min(), df_weights.Weights.abs().
 \rightarrowmax())
# Apply the color map
colors = cmap(norm(df_weights.Weights.abs()))
plt.figure(figsize=(10, 8))
plt.barh(df_weights['Features'], df_weights['Weights'], color=colors) # barh_
⇔is for horizontal bar chart
plt.xlabel('Weights')
plt.ylabel('Features')
plt.title('Linear Regression Model Weights')
plt.grid(axis='x')
plt.tight_layout()
plt.show()
```



2.1.11 According to your model, which features are the greatest contributors to the car price?

```
[42]: ### Comment here

# Based on the graph above, we can see that temp has the largest weight among_
all,

# therefore, it is the greatest contributor to the rental count, followed by

# season_winter, mnth_July and humidity. This is becasue increasing these_
afeatures by

# one unit, changes the rental count by their weights. The higher the weight,

# the greater contribution they affect the dependent variable count.
```

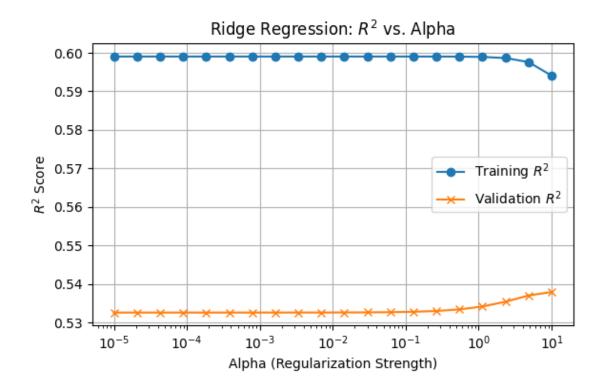
0.3.5 Hyperparameter Tuning (α)

Now, let's do ridge regression and tune the α regularization parameter on the bike rental dataset.

2.1.12 Sweep out values for α using alphas = np.logspace(-5, 1, 20). Perform a grid search over these α values, recording the training and validation R^2 for each α . A simple grid search is fine, no need for k-fold cross validation. Plot the training and validation R^2 as a function of α on a single figure. Make sure to label the axes and the

training and validation R^2 curves. Use a log scale for the x-axis.

```
[43]: ### Code here
      alphas = np.logspace(-5, 1, 20) # Values for alpha
      train_scores = [] # List to store R^2 values on the training set
      val scores = [] # List to store R^2 values on the validation set
      # Loop through the alpha values
      for alpha in alphas:
          # Create and train a model with the current alpha
          model = LinearRegression(alpha=alpha)
          model.train(bike_rental_X_train, bike_rental_y_train)
          # Predict on training set and compute R^2
          train_pred = model.predict(bike_rental_X_train)
          train_r2 = r2_score(bike_rental_y_train, train_pred)
          train_scores.append(train_r2)
          # Predict on validation set and compute R^2
          val_pred = model.predict(bike_rental_X_val)
          val_r2 = r2_score(bike_rental_y_val, val_pred)
          val_scores.append(val_r2)
      # Plotting
      plt.figure(figsize=(6,4))
      plt.plot(alphas, train_scores, marker='o', label='Training $R^2$')
      plt.plot(alphas, val_scores, marker='x', label='Validation $R^2$')
      plt.xscale('log')
      plt.xlabel('Alpha (Regularization Strength)')
      plt.ylabel('$R^2$ Score')
      plt.title('Ridge Regression: $R^2$ vs. Alpha')
      plt.legend()
      plt.grid(True)
      plt.tight_layout()
      plt.show()
```



2.1.13 Explain your plot above. How do training and validation R^2 behave with decreasing model complexity (increasing α)?

```
[44]: | ### Comment here
      # As alpha increases, it penalizes the magnitude of the coefficients in the
       → linear
      # regression model, and the model complexity decreases. Based on the graph_{\sqcup}
       ⇒above,
      # we can see that when alpha is still small, the penalty on the coefficients is i
       ⇔also small,
      # the training R squared did not change because the model's complexity is still_{\sqcup}
      # enough to fit the training data well. As alpha continues to increase, the
       \hookrightarrow training
      \# R squared starts to drop because the model becomes less flexible and will not \sqcup
      # fit the training data so well as before. However, the validation R squared
       ⇔starts to
      # increases, the gap between training R squared and validation R squared \Box
       ⇔becomes smaller,
      # this is because the model overfits when the alpha is very small. As_{\sqcup}
       \hookrightarrow regularization
      # increases, the model has lower variance and becomes less prone to overfitting.
```

```
# As alpha continues to increase, the training and validation R squared will_

meet, and
# drops together when the model starts to underfit.
```

0.3.6 2.2 Logistic Regression

2.2.1 Load the dataset, the dataset to be used is loan_data.csv

```
[45]: ### Code here
loan_data_df = pd.read_csv('/content/drive/My Drive/loan_data.csv')

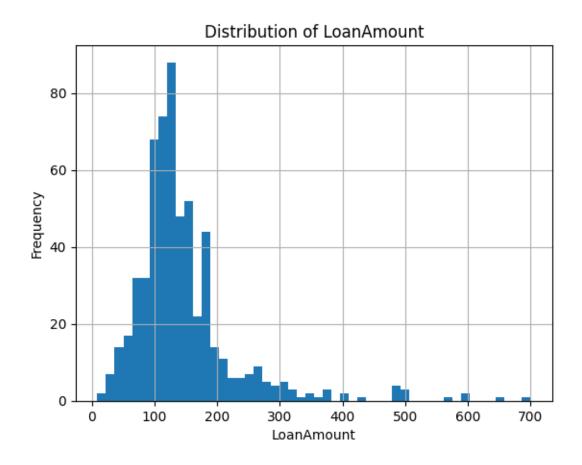
[46]: loan_data_df = loan_data_df.drop(columns=['Loan_ID'])
```

```
2.2.2 Are there any missing values in the dataset? If so, what is the best way to deal with it and why?
```

```
[47]: ### Code here
missing_values = loan_data_df.isnull().sum()
print(missing_values)

#Check the distribution for 'LoanAmount'
loan_data_df['LoanAmount'].hist(bins=50)
plt.xlabel('LoanAmount')
plt.ylabel('Frequency')
plt.title('Distribution of LoanAmount')
plt.show()
```

Gender 13 Married 3 Dependents 15 Education 0 Self_Employed 32 ApplicantIncome 0 CoapplicantIncome 0 LoanAmount 22 Loan Amount Term 14 Credit_History 50 Property_Area 0 Loan_Status 0 dtype: int64



```
[49]: ### Comment here
# For Married, since only 3 values are missing, just drop the rows, and we will

→not miss much data.

# For categorical features, we replace the missing values with mode. This is

→because
```

```
# it is simple and fast, and it keeps the data consistent and does not usintroduce new values.

# Although 'Load_Amount_Term' are numbers, but we treat it as categorical here, usince

# it only contain certain values, and we do not want to introduct new values.

# Note: This is under the assumption that they are missing completely at random.

# For the numerical feature 'LoanAmount', we replace it with the median instead of mean, because

# it is right skewed, and median is more robust to outliers than mean.
```

2.2.3 Encode the categorical variables.

2.2.4 Do you think that the distribution of labels is balanced? Why/why not? Hint: Find the probability of the different categories.

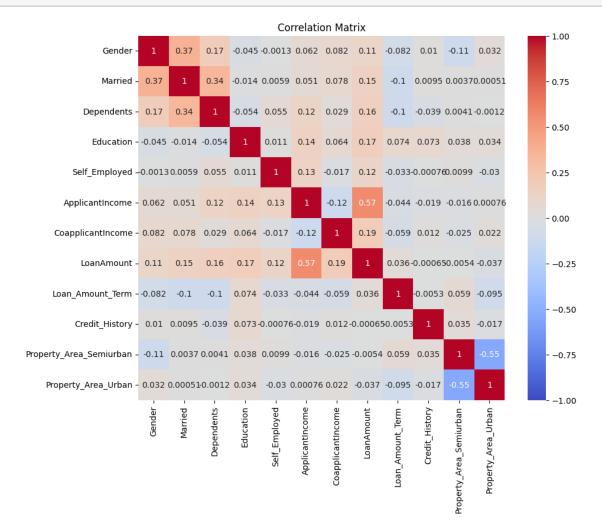
```
# ~31.4% of the dataset. In a balanced dataset, each class should have a 50-50 _{\rm L\!I} _{\odot} split.
```

2.2.5 Plot the correlation matrix (first separate features and Y variable), and check if there is high correlation between the given numerical features (Threshold >=0.9). If yes, drop those highly correlated features from the dataframe.

```
X = loan_data_df.drop('Loan_Status', axis=1)
y = loan_data_df['Loan_Status']

[54]: ### Code here
correlation_matrix = X.corr()
plt.figure(figsize=(10, 8))
sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm', vmin=-1, vmax=1)
plt.title('Correlation Matrix')
plt.show()
```

[53]: ### Code here



2.2.6 Apply the following pre-processing steps:

- 1. Convert the label from a Pandas series to a Numpy (m x 1) vector. If you don't do this, it may cause problems when implementing the logistic regression model.
- 2. Split the dataset into training (60%), validation (20%), and test (20%) sets.
- 3. Standardize the columns in the feature matrices. To avoid information leakage, learn the standardization parameters from training, and then apply training, validation and test dataset.
- 4. Add a column of ones to the feature matrices of train, validation and test dataset. This is a common trick so that we can learn a coefficient for the bias term of a linear model.

```
[56]: ### Code here
      y = np.array(y).reshape(-1, 1)
      # Split the dataset
      X_temp, X_test, y_temp, y_test = train_test_split(X, y, test_size=0.2,_
       →random_state=42)
      X_train, X_val, y_train, y_val = train_test_split(X_temp, y_temp, test_size=0.
       425, random_state=42) # 0.25 * 0.8 = 0.2
      # Standardize the columns
      scaler = StandardScaler()
      X_train = scaler.fit_transform(X_train)
      X_val = scaler.transform(X_val)
      X_test = scaler.transform(X_test)
      # Add a column of ones to the feature
      X_train = np.hstack([np.ones((X_train.shape[0], 1)), X_train])
      X_val = np.hstack([np.ones((X_val.shape[0], 1)), X_val])
      X_test = np.hstack([np.ones((X_test.shape[0], 1)), X_test])
```

0.3.7 Implement Logisitc Regression

We will now implement logistic regression with L2 regularization. Given an $(m \times n)$ feature matrix X, an $(m \times 1)$ label vector y, and an $(n \times 1)$ weight vector w, the hypothesis function for logistic regression is:

$$y = \sigma(Xw)$$

where $\sigma(x) = \frac{1}{1+e^{-x}}$, i.e. the sigmoid function. This function scales the prediction to be a probability between 0 and 1, and can then be thresholded to get a discrete class prediction.

Just as with linear regression, our objective in logistic regression is to learn the weights w which best fit the data. For L2-regularized logistic regression, we find an optimal w to minimize the following loss function:

$$\min_{w} \ -y^T \ \log(\sigma(Xw)) \ - \ (\mathbf{1} - y)^T \ \log(\mathbf{1} - \sigma(Xw)) \ + \ \alpha \|w\|_2^2$$

Unlike linear regression, however, logistic regression has no closed-form solution for the optimal w. So, we will use gradient descent to find the optimal w. The (n x 1) gradient vector g for the loss function above is:

$$g = X^T \Big(\sigma(Xw) - y \Big) + 2\alpha w$$

Below is pseudocode for gradient descent to find the optimal w. You should first initialize w (e.g. to a (n x 1) zero vector). Then, for some number of epochs t, you should update w with w - g \$, where η is the learning rate and g is the gradient. You can learn more about gradient descent here.

$$w = \mathbf{0}$$
 for $i = 1, 2, ..., t$ \$ w = w - g \$

A LogisticRegression class with five methods: train, predict, calculate_loss, calculate_gradient, and calculate_sigmoid has been implemented for you below.

```
self.alpha = alpha
    self.t = t
    self.eta = eta
    self.w = None
def train(self, X, y):
    '''Trains logistic regression model using gradient descent
    (sets w to its optimal value).
    Parameters
    _____
    X : (m \times n) feature matrix
    y: (m \ x \ 1) label vector
    Returns
    _____
    losses: (t x 1) vector of losses at each epoch of gradient descent
    loss = list()
    self.w = np.zeros((X.shape[1],1))
    for i in range(self.t):
        self.w = self.w - (self.eta * self.calculate_gradient(X, y))
        loss.append(self.calculate_loss(X, y))
    return loss
def predict(self, X):
    '''Predicts on X using trained model. Make sure to threshold
    the predicted probability to return a 0 or 1 prediction.
    Parameters
    X : (m \times n) feature matrix
    Returns
    _____
    y_pred: (m x 1) 0/1 prediction vector
    y_pred = self.calculate_sigmoid(X.dot(self.w))
    y_pred[y_pred >= 0.5] = 1
    y_pred[y_pred < 0.5] = 0
    return y_pred
def calculate_loss(self, X, y):
    '''Calculates the logistic regression loss using X, y, w,
    and alpha. Useful as a helper function for train().
```

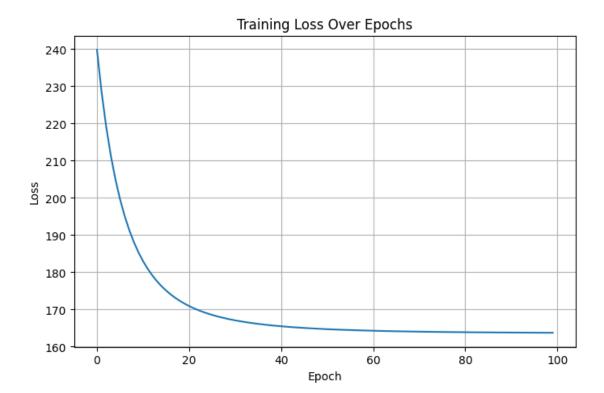
```
Parameters
       _____
      X : (m \times n) feature matrix
      y: (m x 1) label vector
      Returns
      loss: (scalar) logistic regression loss
      return -y.T.dot(np.log(self.calculate_sigmoid(X.dot(self.w)))) - (1-y).
→T.dot(np.log(1-self.calculate_sigmoid(X.dot(self.w)))) + self.alpha*np.
⇒linalg.norm(self.w, ord=2)**2
  def calculate_gradient(self, X, y):
       '''Calculates the gradient of the logistic regression loss
      using X, y, w, and alpha. Useful as a helper function
      for train().
      Parameters
      X : (m \times n) feature matrix
      y: (m x 1) label vector
      Returns
      gradient: (n x 1) gradient vector for logistic regression loss
      return X.T.dot(self.calculate sigmoid( X.dot(self.w)) - y) + 2*self.
⇒alpha*self.w
  def calculate_sigmoid(self, x):
       '''Calculates the sigmoid function on each element in vector x.
      Useful as a helper function for predict(), calculate_loss(),
      and calculate_gradient().
      Parameters
      x: (m \ x \ 1) \ vector
      Returns
      sigmoid_x: (m x 1) vector of sigmoid on each element in x
      return (1)/(1 + np.exp(-x.astype('float')))
```

2.2.7 Plot Loss over Epoch and Search the space randomly to find best hyperparame-

ters.

- i) Using your implementation above, train a logistic regression model (alpha=0, t=100, eta=1e-3) on the loan training data. Plot the training loss over epochs. Make sure to label your axes. You should see the loss decreasing and start to converge.
- ii) Using alpha between (0,1), eta between (0, 0.001) and t between (0, 100), find the best hyperparameters for LogisticRegression. You can randomly search the space 20 times to find the best hyperparameters.
- iii) Compare accuracy on the test dataset for both the scenarios.

```
[58]: ### Code here
      # Assuming the training data is split into train_loan_X (features) and_
       ⇔train_loan_y (labels)
      # Instantiate the model
      model_first = LogisticRegression(alpha=0, t=100, eta=1e-3)
      # Train the model
      losses = model_first.train(X_train, y_train)
      losses = np.array(losses).reshape(-1)
      # Plot the training loss
      plt.figure(figsize=(8,5))
      plt.plot(range(len(losses)), losses)
      plt.title('Training Loss Over Epochs')
      plt.xlabel('Epoch')
      plt.ylabel('Loss')
      plt.grid(True)
      plt.show()
```



```
[59]: ### Code here
      # Define the bounds for the hyperparameters
      alpha_bounds = [0, 1]
      eta_bounds = [0, 0.001]
      t_bounds = [0, 100]
      best model = None
      best acc = -float('inf') # Set an initial high loss value
      pred_values = []
      # Random search 20 times
      for _ in range(20):
          # Randomly sample hyperparameters within the bounds
          alpha = np.random.uniform(alpha_bounds[0], alpha_bounds[1])
          eta = np.random.uniform(eta_bounds[0], eta_bounds[1])
          t = np.random.randint(t_bounds[0], t_bounds[1])
          # Initialize and train model with the sampled hyperparameters
          model_second = LogisticRegression(alpha=alpha, t=t, eta=eta)
          model_second.train(X_train, y_train)
          # Evaluate on validation set
          y_pred_val = model_second.predict(X_val)
          pred_values.append(y_pred_val)
          # Calculate accuracy
          correct_predictions = (y_pred_val == y_val).sum()
```

```
acc_val = correct_predictions / len(y_val)
# Update best hyperparameters if this is the best model so far
if acc_val > best_acc:
    best_acc = acc_val
    best_model = model_second
```

```
[60]: ### Code here
pred_first = model_first.predict(X_test)
pred_sec = best_model.predict(X_test)
acc_first = np.mean(pred_first == y_test)
acc_sec = np.mean(pred_sec == y_test)
```

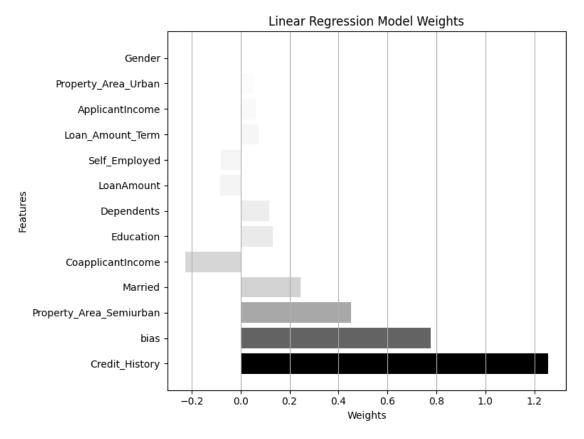
```
[61]: ### Code here
# Compare the accuracy for both scenarios
print(f"First case: {acc_first}, Second case: {acc_sec}")
```

First case: 0.8211382113821138, Second case: 0.8292682926829268

0.3.8 Feature Importance

2.2.8 Interpret your trained model using a bar chart of the model weights. Make sure to label the bars (x-axis) and don't forget the bias term!

```
[62]: ### Code here
      # Assuming best_model is the trained logistic regression model
      weights = best_model.w.ravel() # Flatten the weights for plotting
      # Add 'bias' for the bias term at the start
      features = ['bias'] + X.columns.values.tolist()
      # Creating a DataFrame for sorting
      df_weights = pd.DataFrame({
          'Features': features,
          'Weights': weights
      })
      # Sorting by absolute weight value
      df_weights = df_weights.reindex(df_weights.Weights.abs().
       ⇔sort_values(ascending=False).index)
      #Plotting
      # Create a color map
      cmap = plt.get cmap('binary')
      # Normalize values to 0-1
      norm = plt.Normalize(df_weights.Weights.abs().min(), df_weights.Weights.abs().
       \rightarrowmax())
```



```
[63]: ### Comment here

# Credit_History turns out to be the most important feature in predicting the
loan_status,

# followed by Property_area_semiurban and CoapplicantIncome.
```

0.3.9 2.3 Support Vector Machines

In this part, we will be using support vector machines for classification on the loan dataset.

0.3.10 Train Primal SVM

2.3.1 Train a primal SVM (with default parameters) on the loan dataset. Make predictions and report the accuracy on the training, validation, and test sets.

```
[64]: ### Code here
      from sklearn.metrics import accuracy_score
      # Separating features (X) and target label (y)
      X = loan data df.drop('Loan Status', axis=1)
      y = loan_data_df['Loan_Status']
      # Splitting the dataset
      X_temp, X_test, y_temp, y_test = train_test_split(X, y, test_size=0.2)
      X_train, X_val, y_train, y_val = train_test_split(X_temp, y_temp, test_size=0.
       425, random_state=42) # 0.25 * 0.8 = 0.2
      #Standardize the data
      scaler = StandardScaler()
      X train = scaler.fit transform(X train)
      X_val = scaler.transform(X_val)
      X test = scaler.transform(X test)
      # Initialize and train the Support Vector Classifier
      svm_clf = LinearSVC(dual = False)
      svm_clf.fit(X_train, y_train)
      # Report accuracy on train, val and test
      y_train_pred = svm_clf.predict(X_train)
      y_val_pred = svm_clf.predict(X_val)
      y_test_pred = svm_clf.predict(X_test)
      train_accuracy = accuracy_score(y_train, y_train_pred)
      val_accuracy = accuracy_score(y_val, y_val_pred)
      test_accuracy = accuracy_score(y_test, y_test_pred)
      print(f"Training Accuracy: {train accuracy}")
      print(f"Validation Accuracy: {val_accuracy}")
      print(f"Test Accuracy: {test_accuracy}")
```

Training Accuracy: 0.8005464480874317 Validation Accuracy: 0.7950819672131147 Test Accuracy: 0.8536585365853658

0.3.11 Train Dual SVM

2.3.2 Train a dual SVM (with default parameters) on the loan dataset. Make predictions and report the accuracy on the training, validation, and test sets.

```
[73]: ### Code here
svm_clf = LinearSVC(dual = True, max_iter = 10000)

# Initialize and train the Support Vector Classifier
svm_clf.fit(X_train, y_train)
y_train_pred = svm_clf.predict(X_train)

# Report accuracy on train, val and test
y_val_pred = svm_clf.predict(X_val)
y_test_pred = svm_clf.predict(X_test)
train_accuracy = accuracy_score(y_train, y_train_pred)
val_accuracy = accuracy_score(y_val, y_val_pred)
test_accuracy = accuracy_score(y_test, y_test_pred)
print(f"Training Accuracy: {train_accuracy}")
print(f"Validation Accuracy: {val_accuracy}")
print(f"Test Accuracy: {test_accuracy}")
```

Training Accuracy: 0.8005464480874317
Validation Accuracy: 0.7950819672131147

Test Accuracy: 0.8536585365853658

[]: