

# Capturing Spatial Dependencies with Deep Neural Networks I

Yao-Yi Chiang

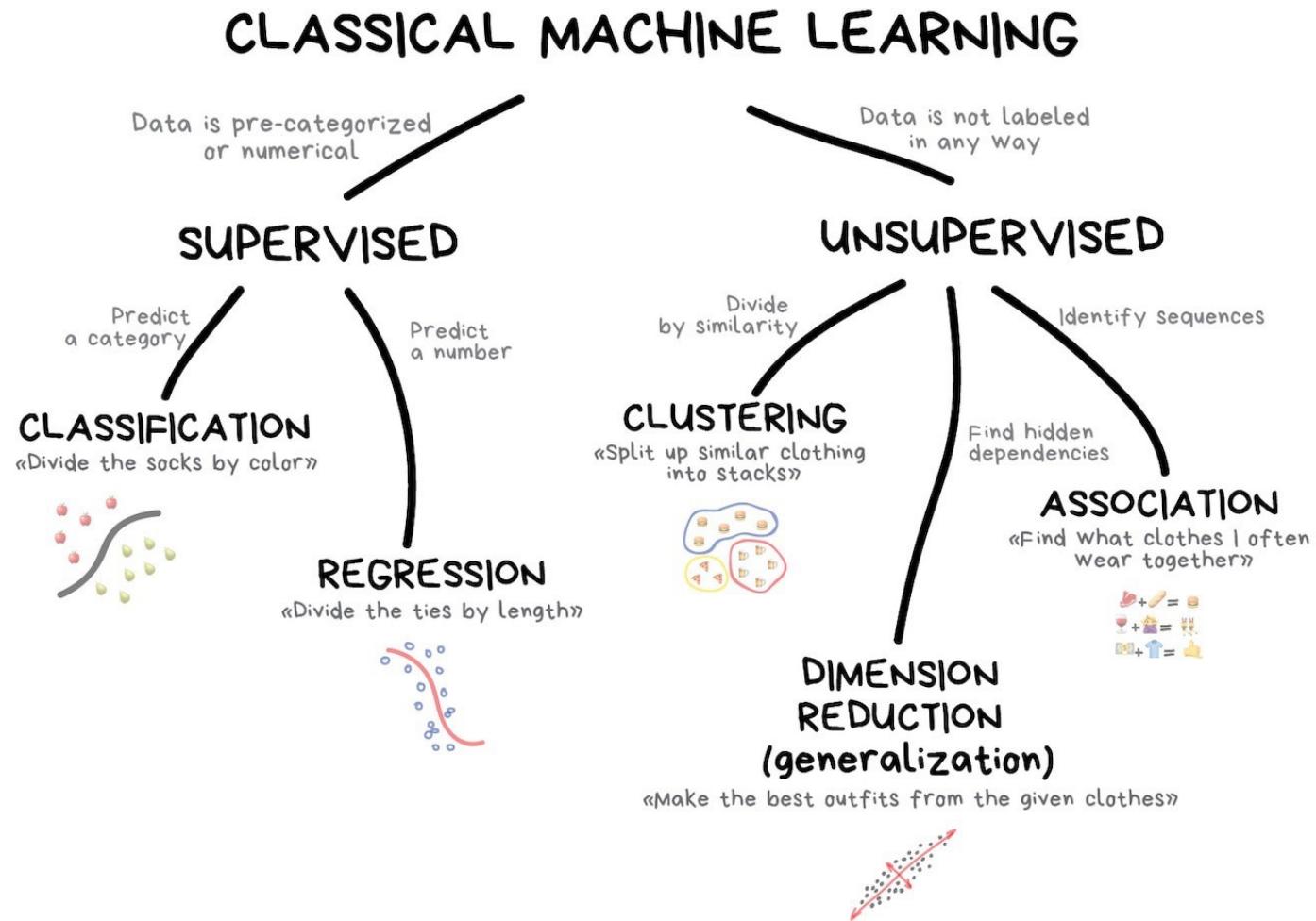
Computer Science and Engineering

University of Minnesota

[yaoyi@umn.edu](mailto:yaoyi@umn.edu)

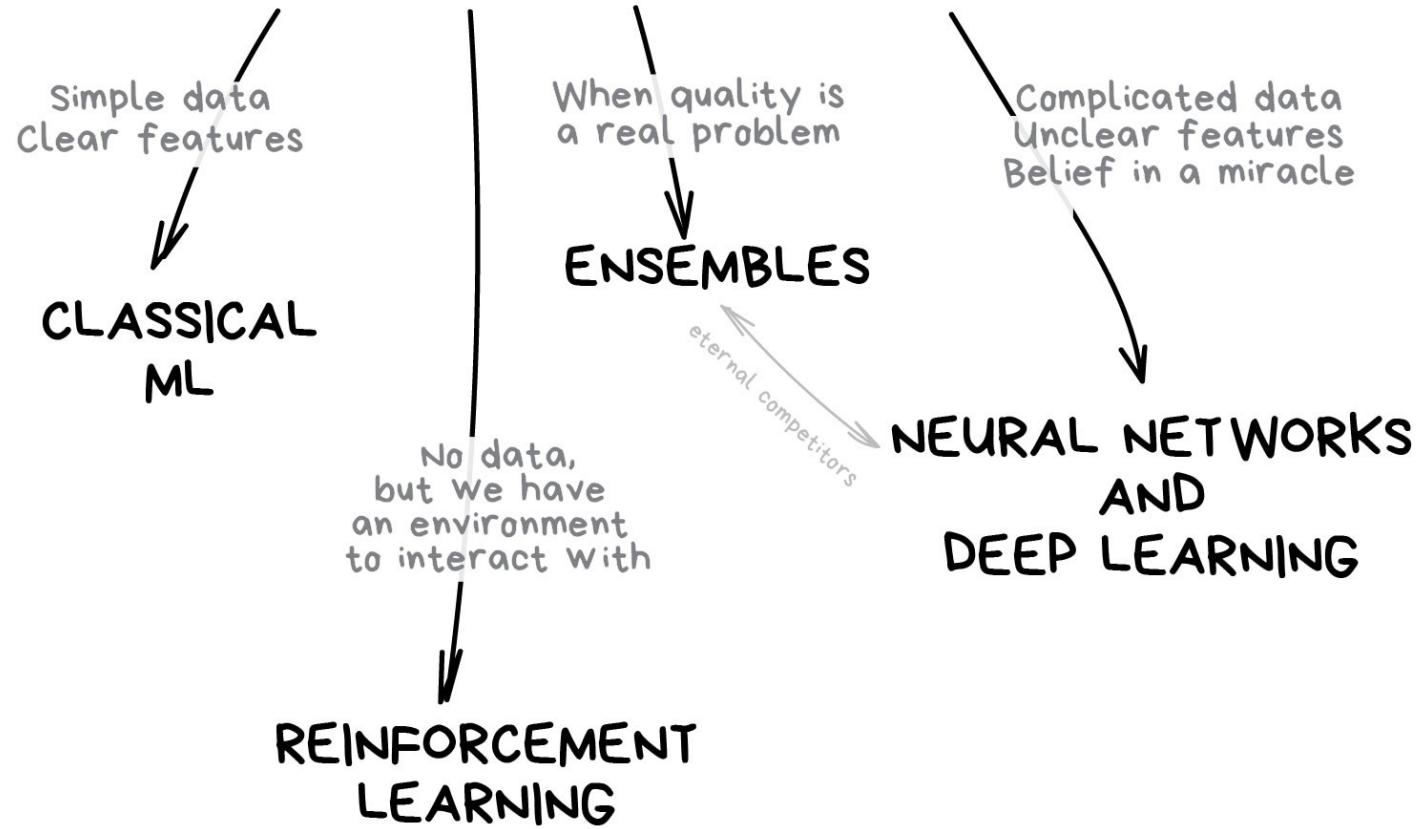
# What have we covered so far?

- Clustering
- Dimension Reduction
- Random Forest
  - Classification
  - Regression



What have we covered so far?

- Classical ML
- Ensembles



# Overhead Imagery Understanding Tasks

Image Recognition



Image Segmentation



Object Detection



Instance Segmentation



Airport

Runway

Building

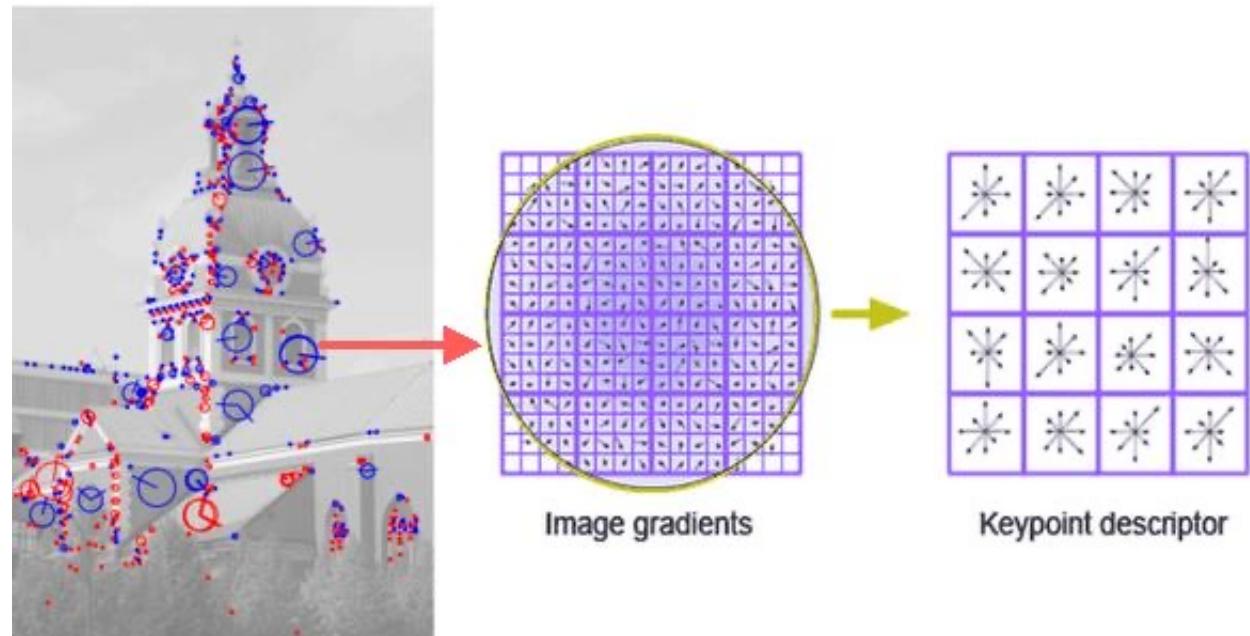
Vehicle

Plane

# Object Detection & Recognition in 1999

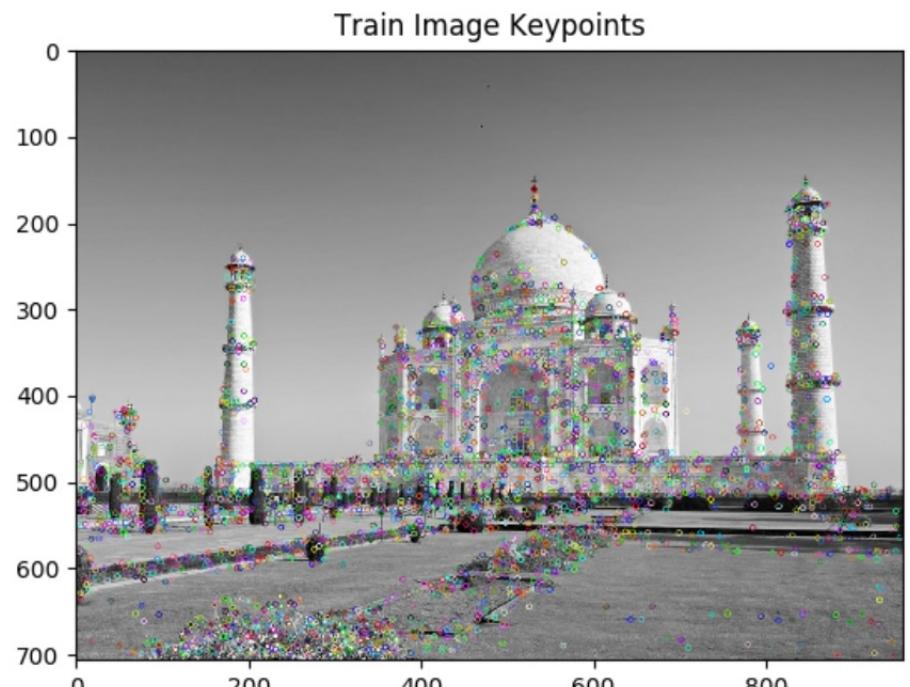
SIFT (Scale Invariant Feature Transform)

- SIFT is one of most popular **image feature extraction and description** algorithms
- SIFT extracts **feature points** and describe them with a **scale, illumination**, and **rotational** invariant descriptor



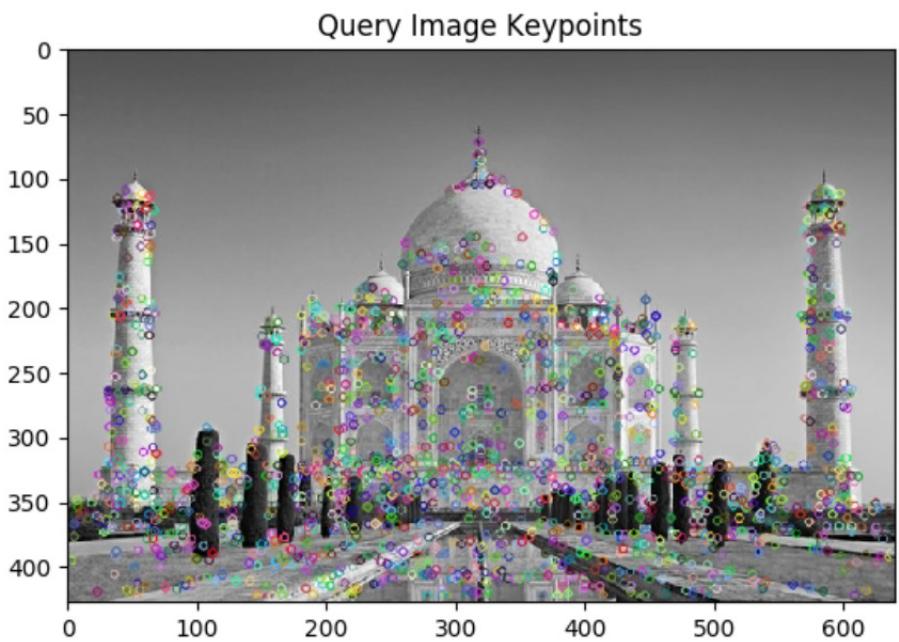
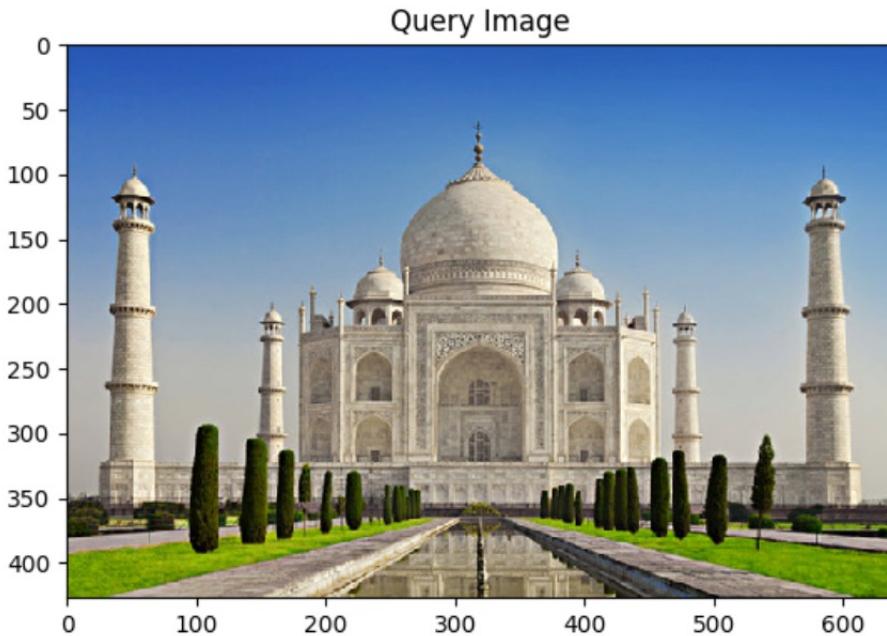
# Object Detection & Recognition in 1999

SIFT (Scale Invariant Feature Transform)



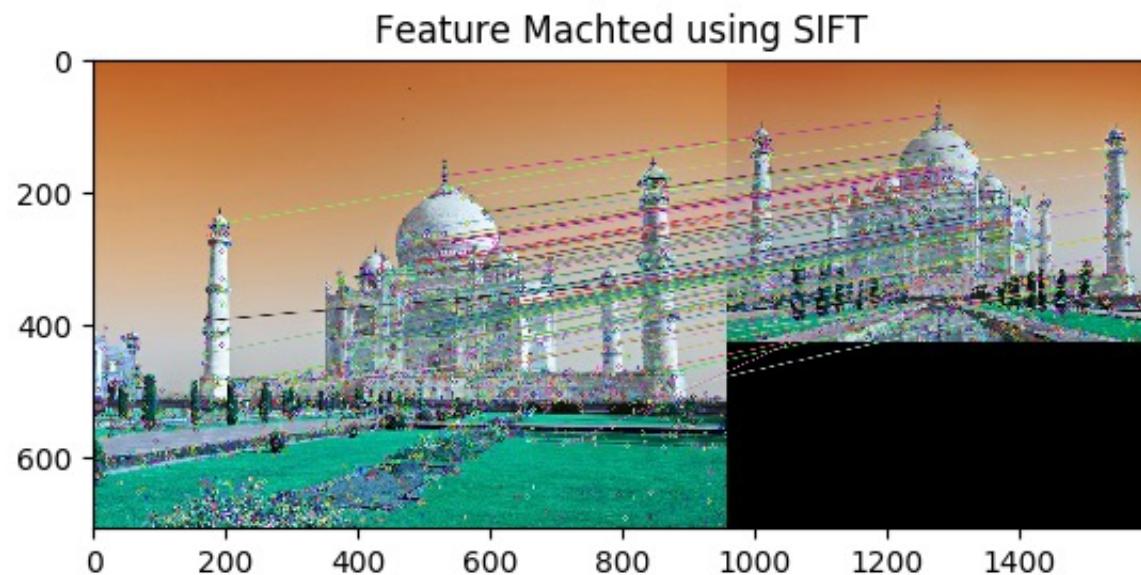
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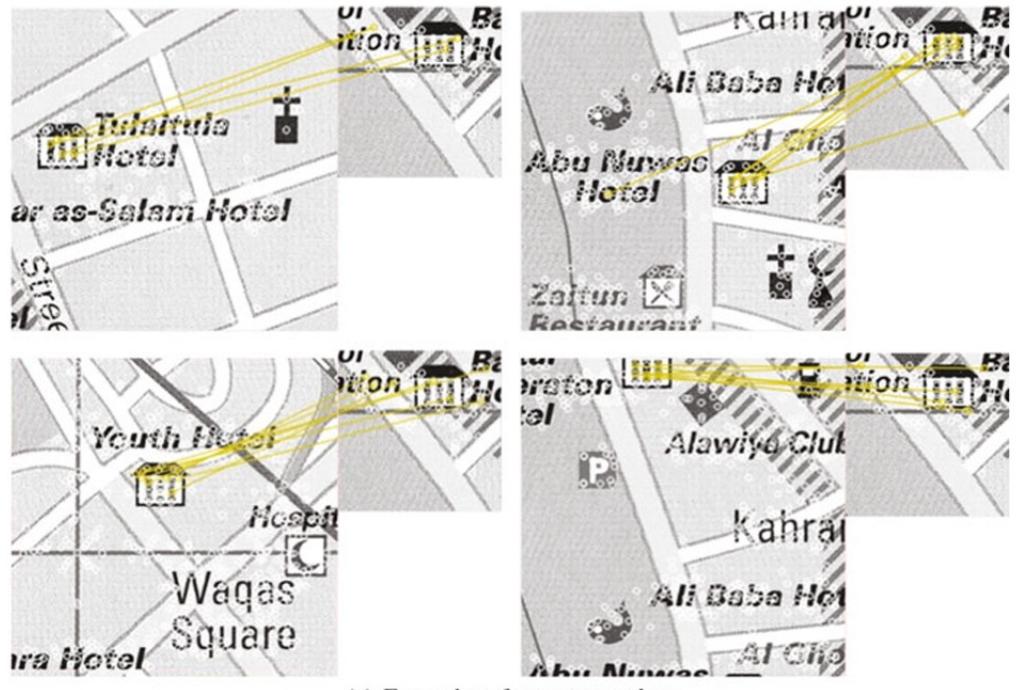
# Object Detection & Recognition in 1999

SIFT (Scale Invariant Feature Transform)



# Map Processing

- The small image on the right: hotel sample
- The small white circles on the maps: SURF descriptors
- The yellow lines connect **matches** between the SURF descriptors of the map area and the sample.



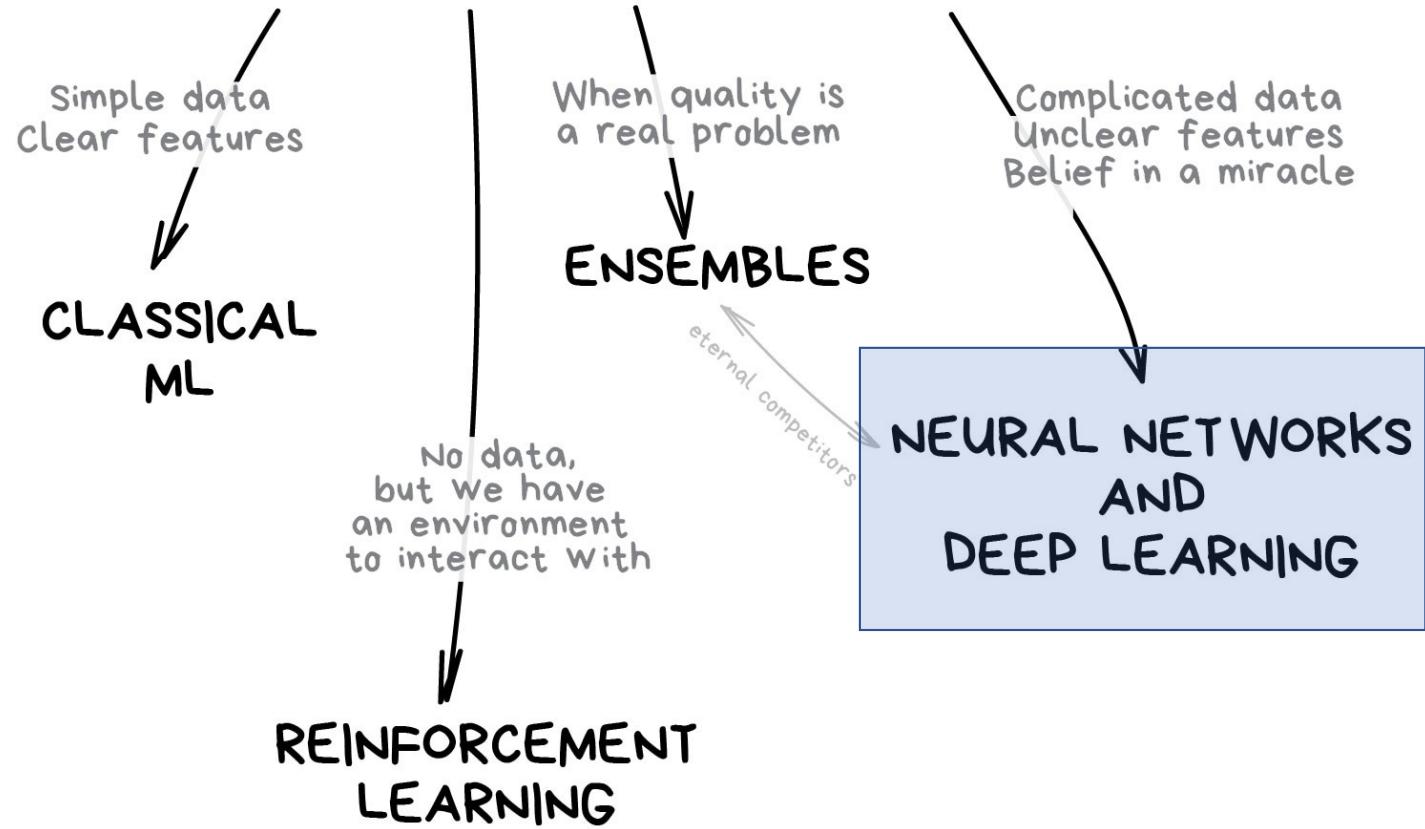
(a) Examples of correct matches

# Handcrafted Image Features

- Pros
  - Simple, easy to implement
  - Do not require significant computational power
  - Somehow explainable results
- Cons
  - Not very robust (e.g., objects need to be very similar for a match)
  - Limited computer vision applications

What have we covered so far?

- Classical ML
- Ensembles

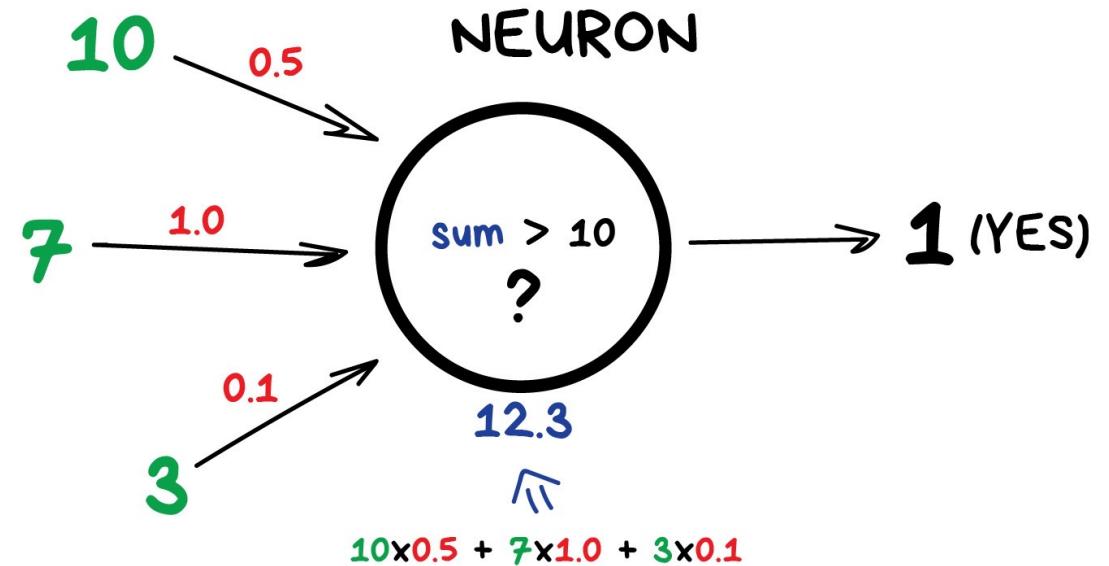


# Neural Networks and Deep Learning

A short introduction

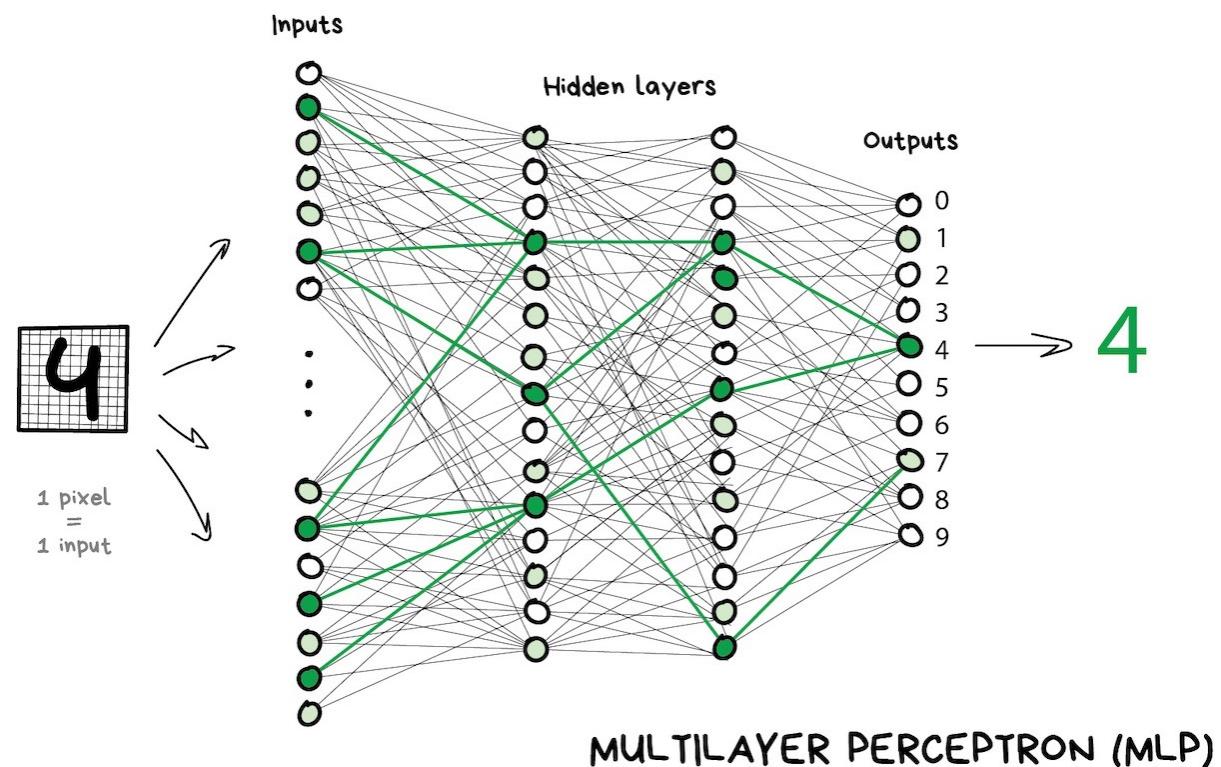
# Deep Neural Networks

- Neural networks with lots of “neurons” and layers



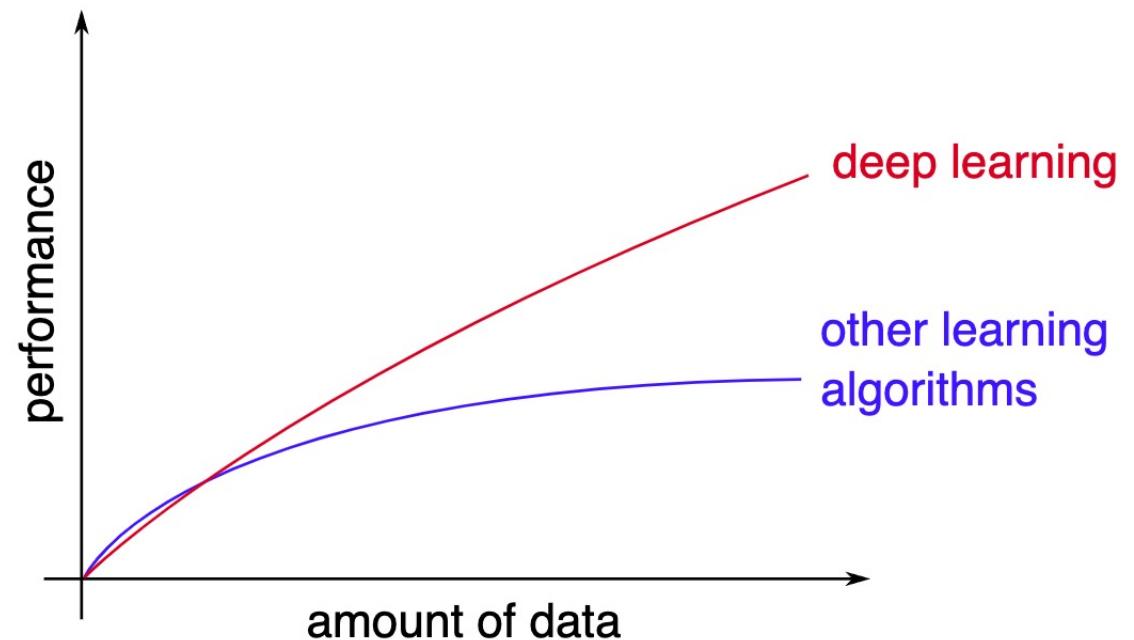
# Deep Neural Networks

- Neural networks with lots of “neurons” and layers
- Flexible network modules
- Can capture non-linear relationships in data



# Deep Neural Networks

- Neural networks with lots of “neurons” and layers
- Flexible network modules
- Can capture non-linear relationships in data
- Can take advantage of large amounts of training data



# Open Source Tools and Models



PYTORCH



Microsoft  
CNTK

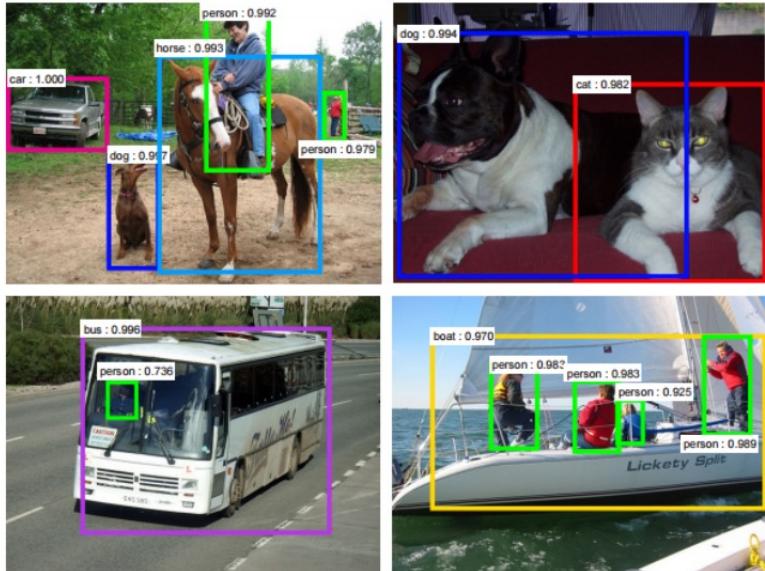
caffé2

dmlc  
**mxnet**

**gensim**    **spaCy**

theano

# DL for Computer Vision



[Faster R-CNN - Ren 2015]



[NVIDIA dev blog]

# DL for Natural Language Processing

Salit Kulla 11:29 AM \*\*\*  
to me

Hey, Wynton Marsalis is playing this weekend. Do  
you have a preference between Saturday and Sunday?

-S

I'm down for either.  
Let's do Saturday.  
I'm fine with whatever.

←  
Reply

→  
Forward

Translate

Italian Chinese French English - detected English Spanish French Translate

deep learning x l'apprentissage en profondeur ✓

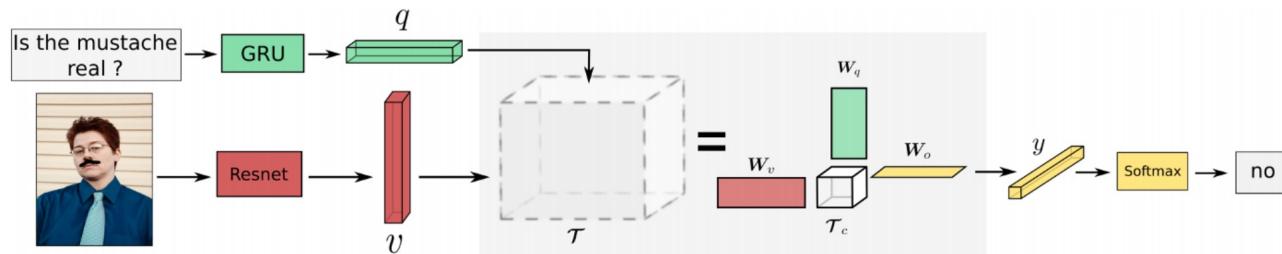
13/5000

☆ ⌂ ↶ ↷



[Google Inbox Smart Reply]

# DL for CV + NLP



[VQA - Mutan 2017]



"man in black shirt is playing guitar."



"construction worker in orange safety vest is working on road."



"two young girls are playing with lego toy."

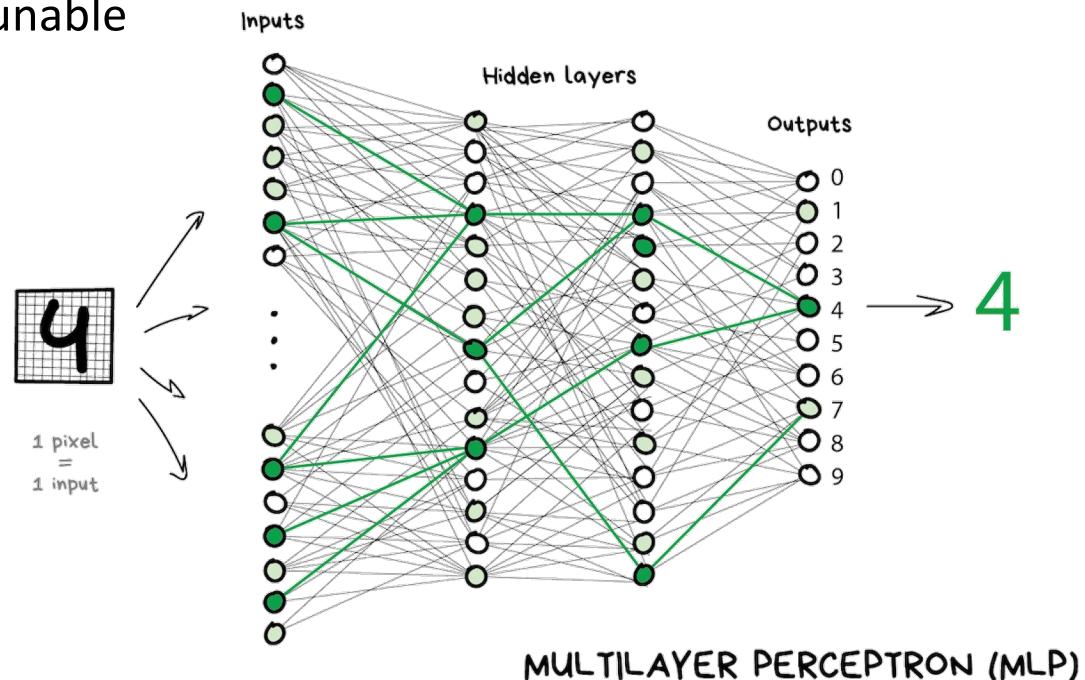


"boy is doing backflip on wakeboard."

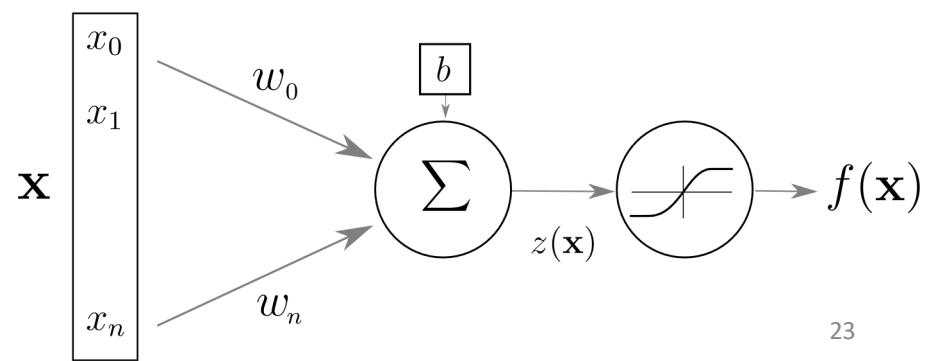
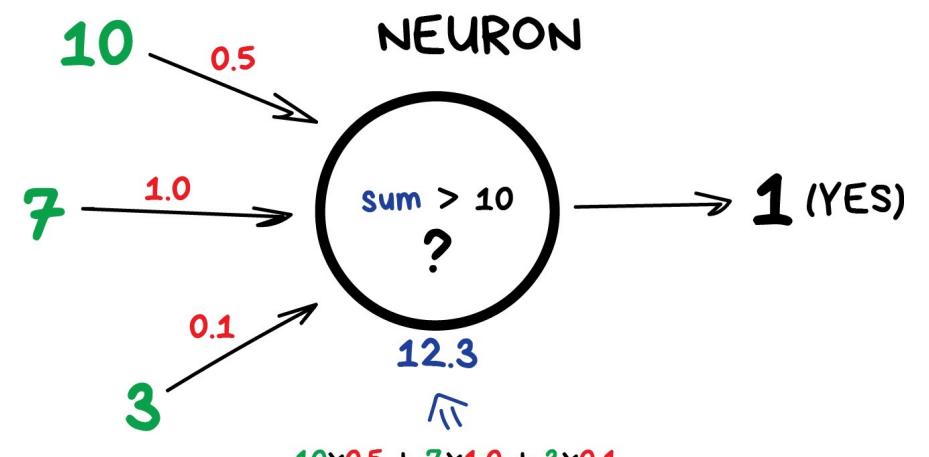
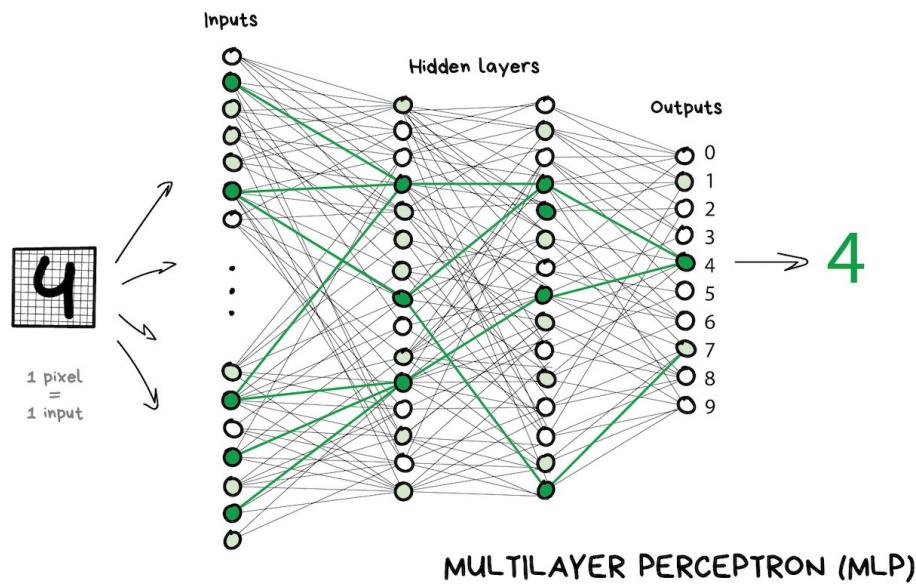
[Karpathy 2015]

# Neural Networks for Classification

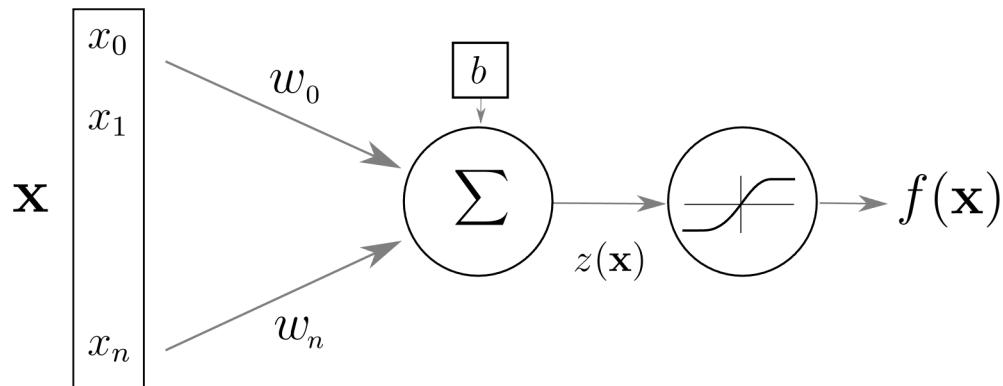
- Neural networks are functions with tunable parameters
  - Lots of parameters
- K-Class Classification
  - $f(\cdot; \theta): \mathbb{R}^N \rightarrow (0,1)^K$
- Sample  $s$  in dataset  $S$ :
  - $\mathbf{x}^s \in \mathbb{R}^N$
- Expected output:
  - $y^s \in [0, K - 1]$
- Output is a conditional probability distribution:
  - $f(\mathbf{x}^s; \theta)_c = P(Y = c | X = \mathbf{x}^s)$



# Artificial Neuron



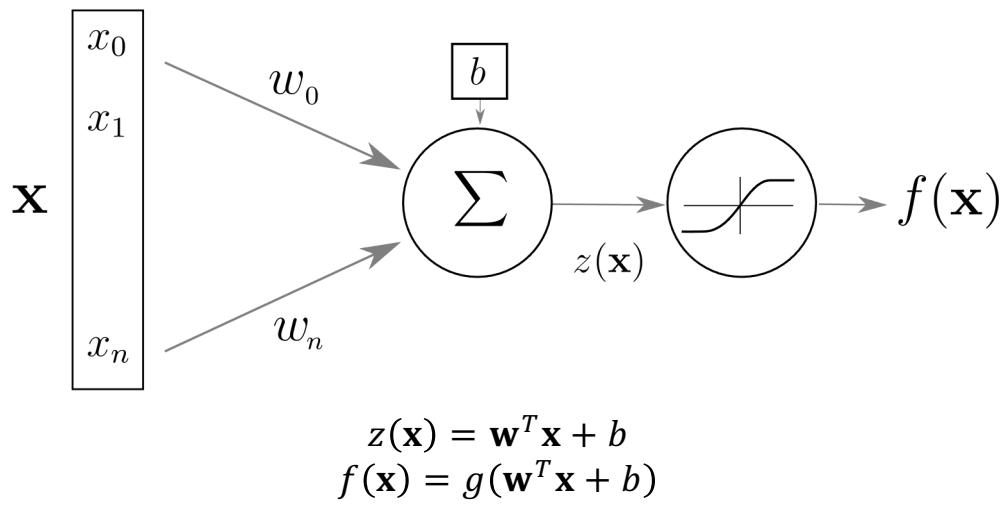
# Artificial Neuron



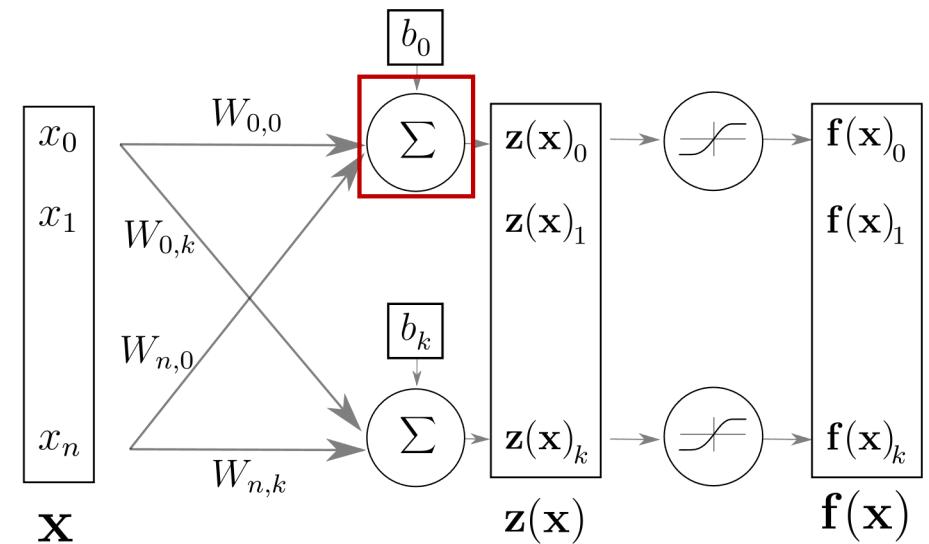
$$\begin{aligned} z(\mathbf{x}) &= \mathbf{w}^T \mathbf{x} + b && \text{e.g., } [0.01, 0.03, 0.04]^T \times [1, 2, 3] + 9 \\ f(\mathbf{x}) &= g(\mathbf{w}^T \mathbf{x} + b) \end{aligned}$$

$\mathbf{x}, f(\mathbf{x})$  input and output  
 $z(\mathbf{x})$  pre-activation (intermediate results)  
 $\mathbf{w}, b$  weights and bias  
 $g$  activation function

# Layer of Neurons

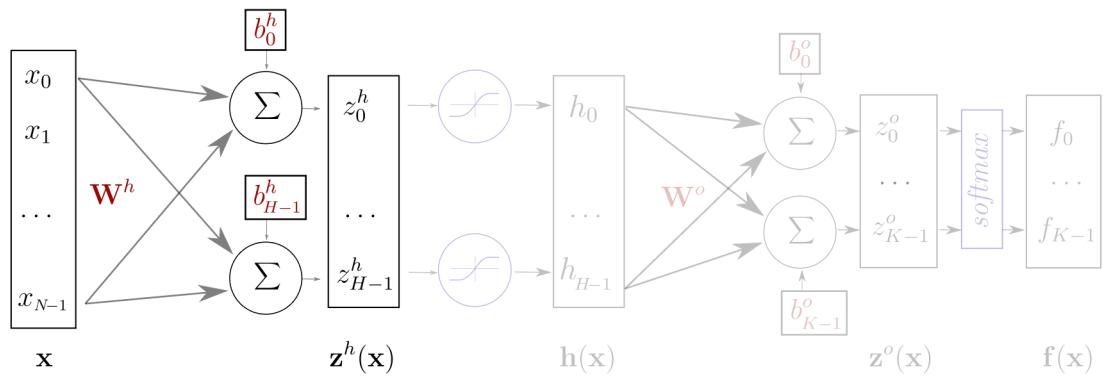


$\mathbf{x}, f(\mathbf{x})$  input and output  
 $z(\mathbf{x})$  pre-activation (intermediate results)  
 $\mathbf{w}, b$  weights (vector) and bias (scalar)  
 $g$  activation function



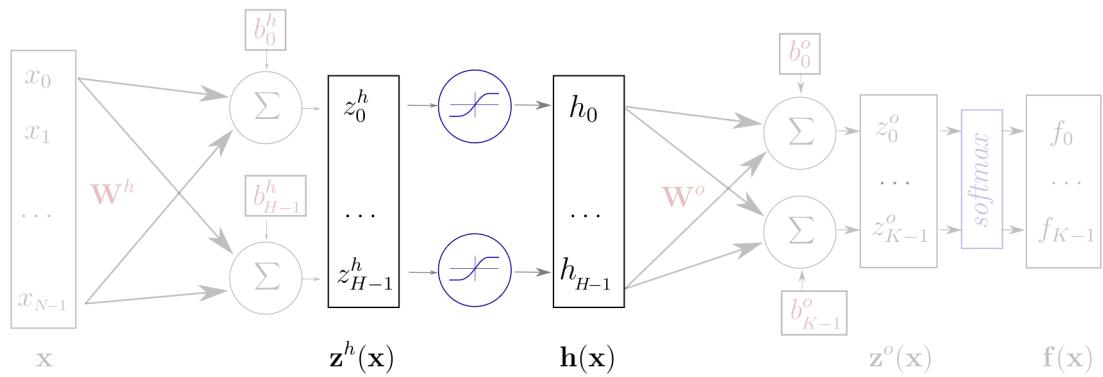
$\mathbf{f}(\mathbf{x}) = g(z(\mathbf{x})) = g(\mathbf{Wx} + \mathbf{b})$   
 $\mathbf{W}, \mathbf{b}$  now matrix and vector

# One Hidden Layer Network



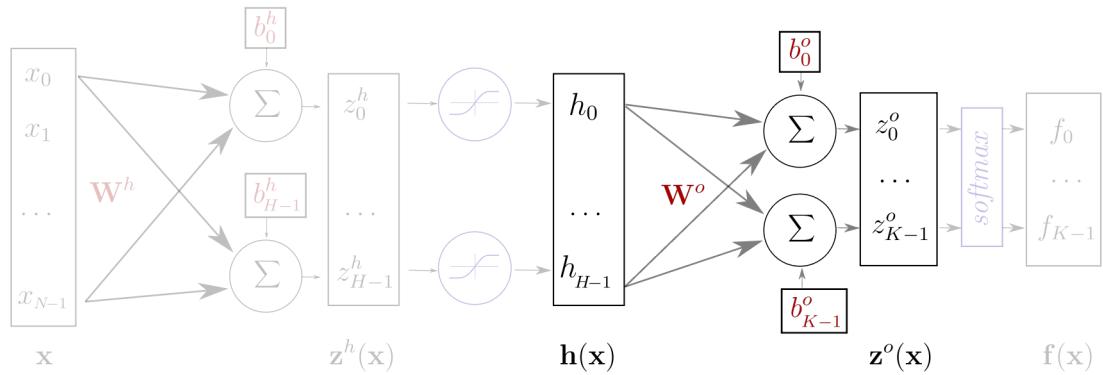
$$\mathbf{z}^h(\mathbf{x}) = \mathbf{W}^h \mathbf{x} + \mathbf{b}^h$$

# One Hidden Layer Network



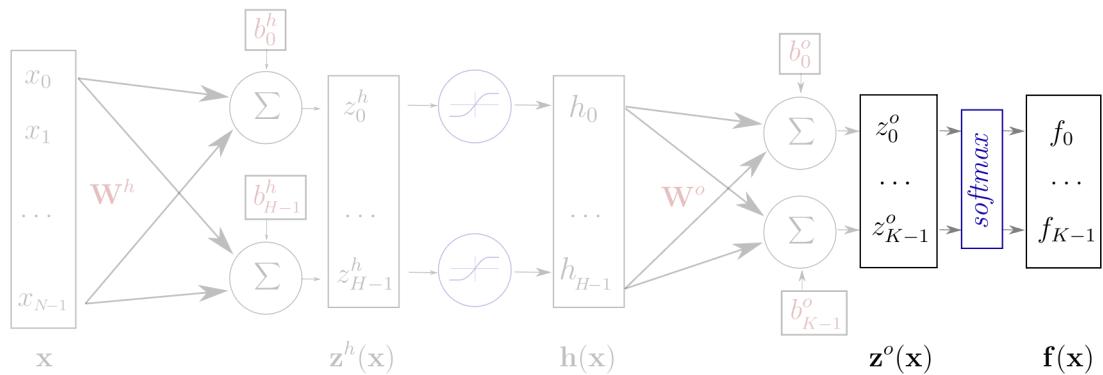
$$\begin{aligned}\mathbf{z}^h(\mathbf{x}) &= \mathbf{W}^h \mathbf{x} + \mathbf{b}^h \\ \mathbf{h}(\mathbf{x}) &= g\left(\mathbf{z}^h(\mathbf{x})\right) = g\left(\mathbf{W}^h \mathbf{x} + \mathbf{b}^h\right)\end{aligned}$$

# One Hidden Layer Network



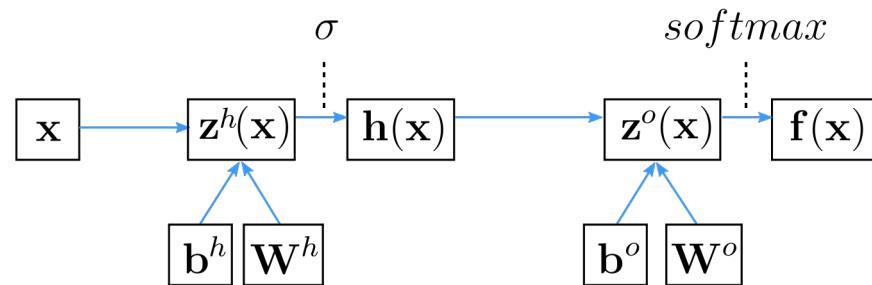
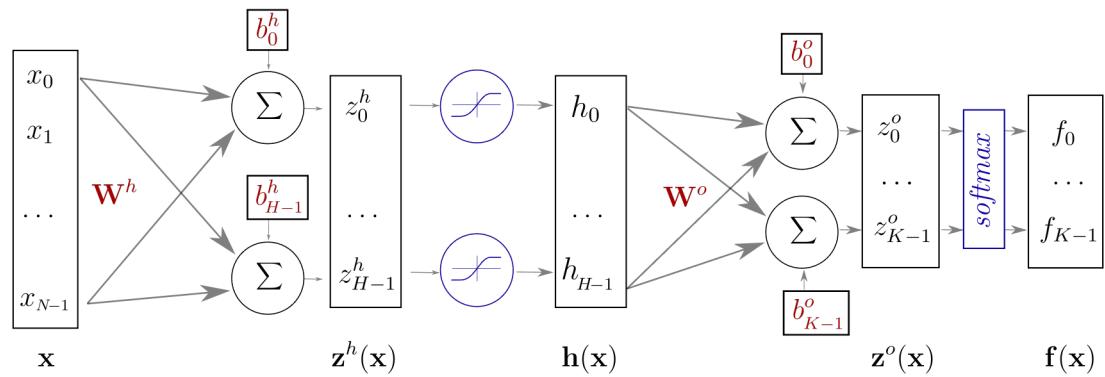
$$\begin{aligned}\mathbf{z}^h(\mathbf{x}) &= \mathbf{W}^h \mathbf{x} + \mathbf{b}^h \\ \mathbf{h}(\mathbf{x}) &= g\left(\mathbf{z}^h(\mathbf{x})\right) = g\left(\mathbf{W}^h \mathbf{x} + \mathbf{b}^h\right) \\ \mathbf{z}^o(\mathbf{x}) &= \mathbf{W}^o \mathbf{h}(\mathbf{x}) + \mathbf{b}^o\end{aligned}$$

# One Hidden Layer Network



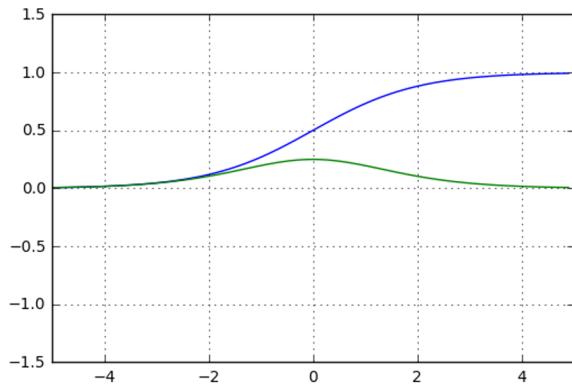
$$\begin{aligned}\mathbf{z}^h(\mathbf{x}) &= \mathbf{W}^h \mathbf{x} + \mathbf{b}^h \\ \mathbf{h}(\mathbf{x}) &= g(\mathbf{z}^h(\mathbf{x})) = g(\mathbf{W}^h \mathbf{x} + \mathbf{b}^h) \\ \mathbf{z}^o(\mathbf{x}) &= \mathbf{W}^o \mathbf{h}(\mathbf{x}) + \mathbf{b}^o \\ \mathbf{f}(\mathbf{x}) &= softmax(\mathbf{z}^o(\mathbf{x})) = softmax(\mathbf{W}^o \mathbf{h}(\mathbf{x}) + \mathbf{b}^o)\end{aligned}$$

# One Hidden Layer Network



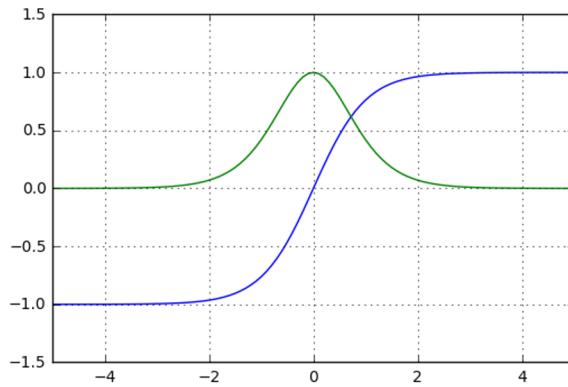
Computational Graph

# Element-wise activation functions



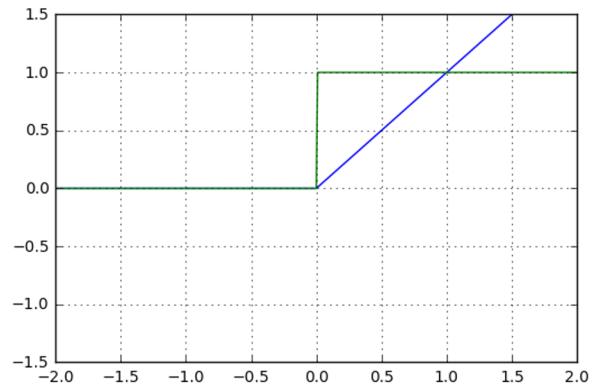
$$\text{sigm}(x) = \frac{1}{1 + e^{-x}}$$

$$\text{sigm}'(x) = \text{sigm}(x)(1 - \text{sigm}(x))$$



$$\tanh(x) = \frac{e^{2x} - 1}{e^{2x} + 1}$$

$$\tanh'(x) = 1 - \tanh(x)^2$$

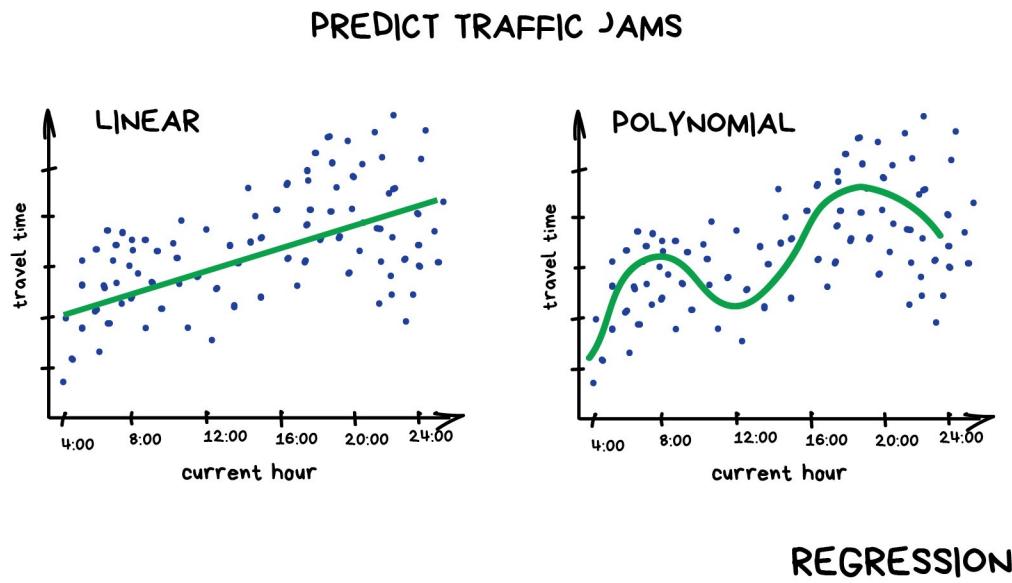


$$\text{relu}(x) = \max(0, x)$$

$$\text{relu}'(x) = 1_{x>0}$$

blue: activation function  
green: derivative

# Activation Functions



What if polynomial regression still could not find a good fit?

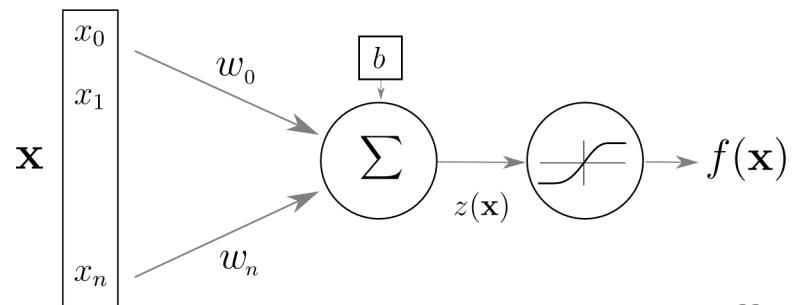
- Activation functions introduce **non-linearities**

- Linear

$$z(\mathbf{x}) = \mathbf{w}^T \mathbf{x} + b$$

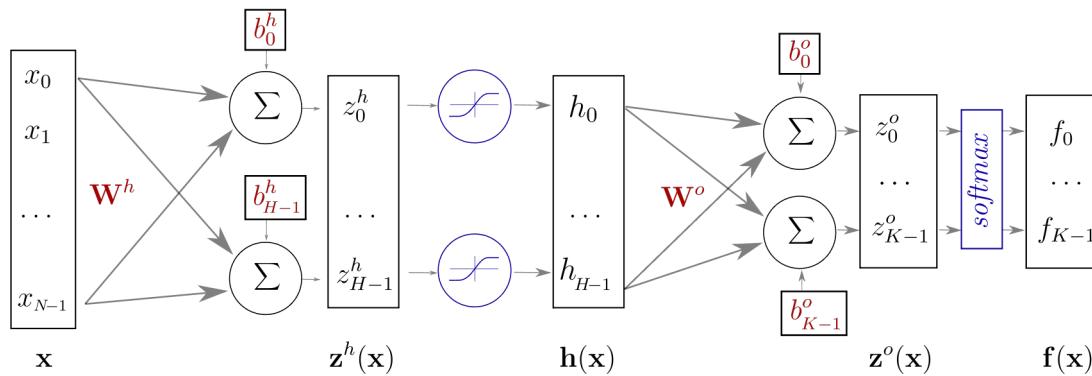
- Non-linear

$$f(\mathbf{x}) = g(\mathbf{w}^T \mathbf{x} + b)$$



# Softmax function

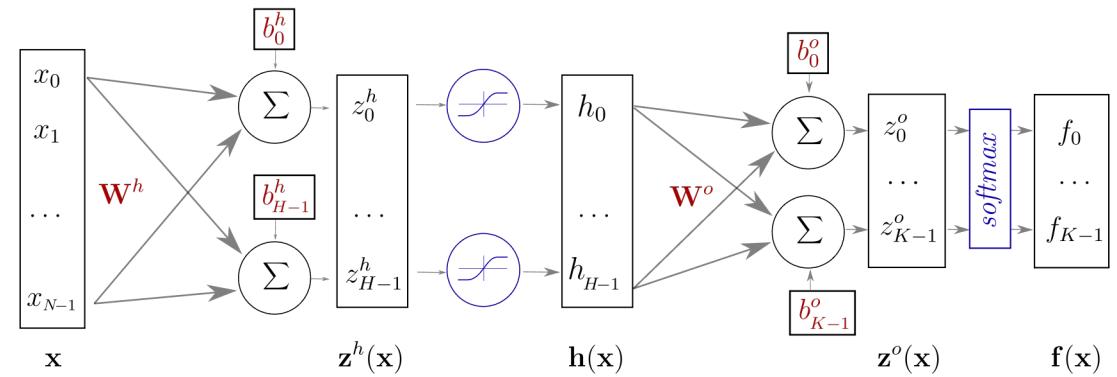
- “Any time we wish to represent **a probability distribution over a discrete variable with  $n$  possible values**, we may use the softmax function. This can be seen as a generalization of the sigmoid function which was used to represent a probability distribution over a binary variable.” Deep Learning



$$\text{softmax}(\mathbf{x}) = \frac{1}{\sum_{i=1}^n e^{x_i}} \cdot \begin{bmatrix} e^{x_1} \\ e^{x_2} \\ \vdots \\ e^{x_n} \end{bmatrix}$$

# Softmax Example

- Class 0: [1, 0, 0]
- Class 1: [0, 1, 0]
- Class 2: [0, 0, 1]
- True  $y$  for an input  $x$ 
  - [0, 1, 0]
- Softmax results scale to probabilities and **sum up to 1.0**
  - [0.09003057 0.66524096 0.24472847]
  - $p(Y = c|X = \mathbf{x}) = \text{softmax}(\mathbf{z}(\mathbf{x}))_c$
  - Might use **argmax()** to return [0, 1, 0] -> Class 1

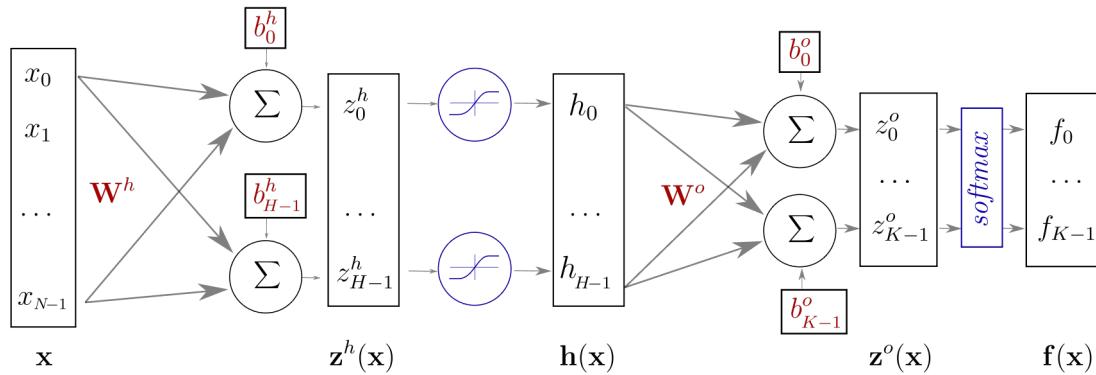


$$\text{softmax}(\mathbf{x}) = \frac{1}{\sum_{i=1}^n e^{x_i}} \cdot \begin{bmatrix} e^{x_1} \\ e^{x_2} \\ \vdots \\ e^{x_n} \end{bmatrix}$$

<https://machinelearningmastery.com/softmax-activation-function-with-python/#:~:text=The%20softmax%20function%20is%20used%20as%20the%20activation%20function%20in,more%20than%20two%20class%20labels.>

# Training the network

- From  $\mathbf{x} = [x_0 \dots x_{n-1}]$ , the network generates  $[0.09003057 \ 0.66524096 \ 0.24472847]$ 
  - What if the true label is  $[1, 0, 0]$ ?
- Adjust  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$  so that hopefully the next prediction will be closer to the true label



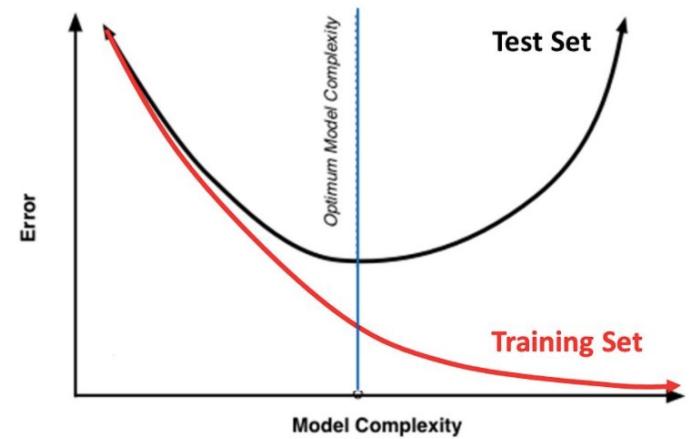
# Training the network

- Using the training data, find  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$  that **minimize** some **loss function** w.r.t the quality of the prediction
  - $l(\mathbf{f}(\mathbf{x}^s; \theta), y^s)$
- We need some way to **quantitatively compare the two probability distributions**: [0.09003057 0.66524096 0.24472847] and [1, 0, 0]
  - e.g., using **cross entropy** to measure the difference between the predicted distribution to the ground truth label
- The comparison results will **give the network some directions** to generate a prediction closer to [1, 0, 0]
  - by **updating**  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$

# Avoid Overfitting

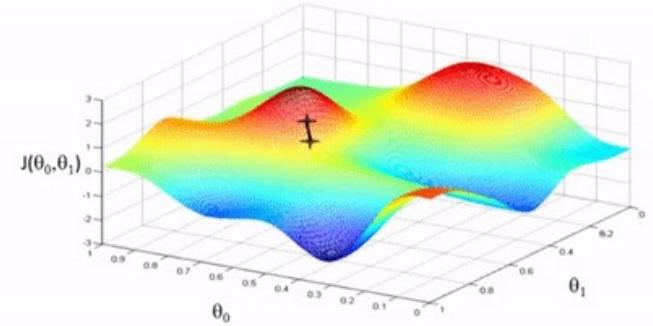
- Typically, minimizing  $l(\mathbf{f}(\mathbf{x}^s; \theta), y^s)$  is not enough
  - Especially with complex models (lots of parameters)
- Regularization
  - We might want to also add a regularization term
    - e.g., L2:  $\lambda\Omega(\theta) = \lambda(||W^h||^2 + ||W^o||^2)$
    - Recall:  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$
- Dropout
- Early stopping

Training Vs. Test Set Error



# Gradient Descent

- Initialize  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$  randomly
- For  $E$  epochs perform:
  - For all samples ( $s \subset S$ )
    - Compute gradients from all samples:  $\Delta = \nabla_{\theta} L_s(\theta)$
    - Update parameters:  $\theta \leftarrow \theta - \eta \Delta$
    - $\eta > 0$  is called the learning rate
  - Repeat until the epoch is completed (all of  $S$  is covered)
  - Stop when reaching criterion:
    - e.g., error stops decreasing when computed on validation set

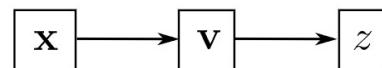


Andrew Ng

# Computing Gradients

- Output Weights:  $\frac{\partial l(\mathbf{f}(\mathbf{x}), y)}{\partial W_{i,j}^o}$
- Hidden Weights:  $\frac{\partial l(\mathbf{f}(\mathbf{x}), y)}{\partial W_{i,j}^h}$
- The network is **a composition of differentiable modules**
- Instead of computing the gradients for each layer individually, we can apply the “chain rule”
- Easy to calculate with complex network and loss functions

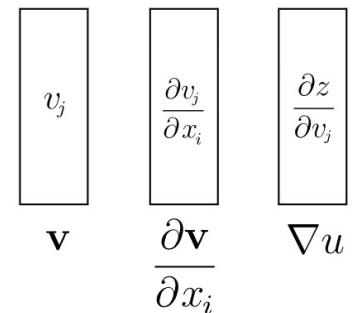
- Output bias:  $\frac{\partial l(\mathbf{f}(\mathbf{x}), y)}{\partial b_i^o}$
- Hidden bias:  $\frac{\partial l(\mathbf{f}(\mathbf{x}), y)}{\partial b_i^h}$



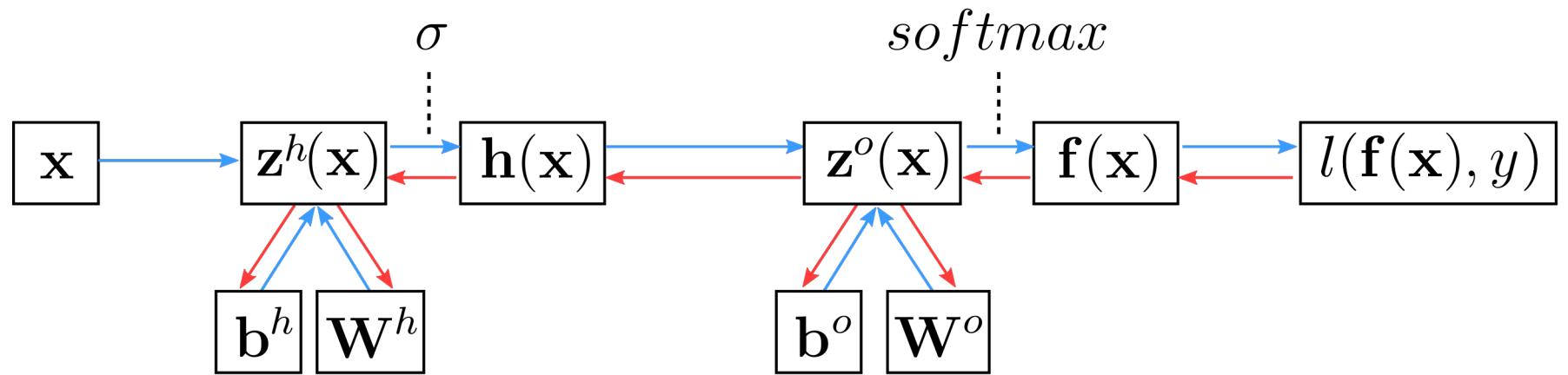
$$z = u(\mathbf{v}(\mathbf{x}))$$

**chain-rule**

$$\frac{\partial z}{\partial x_i} = \sum_j \frac{\partial z}{\partial v_j} \frac{\partial v_j}{\partial x_i} = \nabla u \cdot \frac{\partial \mathbf{v}}{\partial x_i}$$

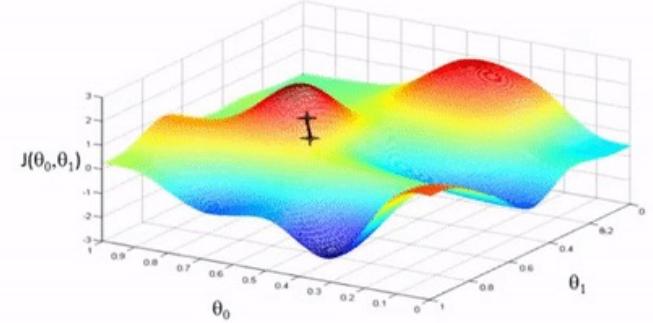


# Backpropagation



# Stochastic Gradient Descent with Mini Batch

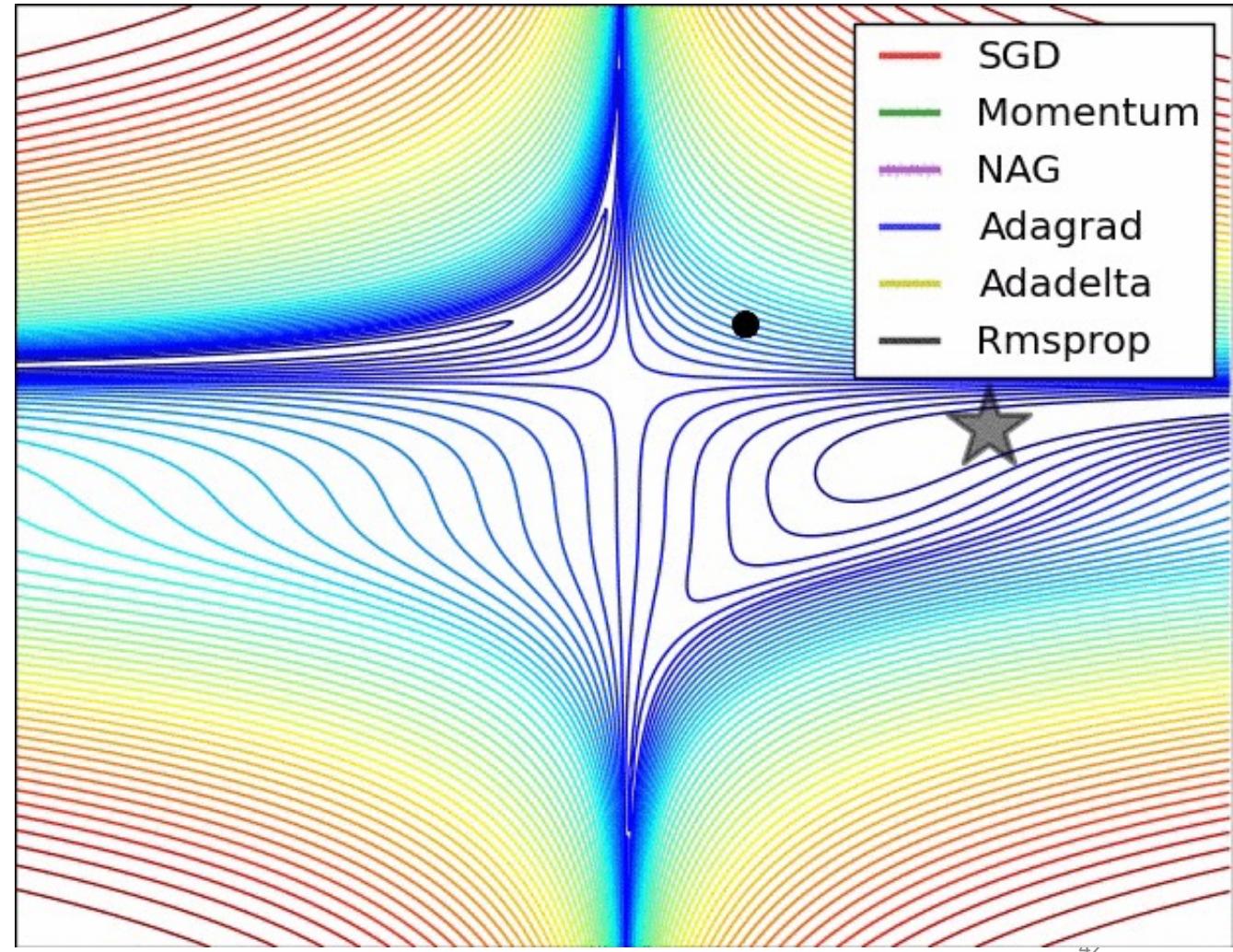
- Initialize  $\theta = (\mathbf{W}^h; \mathbf{b}^h; \mathbf{W}^o; \mathbf{b}^o)$  randomly
- For  $E$  epochs perform:
  - Randomly select a small batch (mini-batch) of samples ( $B \subset S$ )
    - Compute gradients:  $\Delta = \nabla_{\theta} L_B(\theta)$
    - Update parameters:  $\theta \leftarrow \theta - \eta \Delta$
    - $\eta > 0$  is called the learning rate
  - Repeat until the epoch is completed (all of  $S$  is covered)
  - Stop when reaching criterion:
    - e.g., error stops decreasing when computed on validation set



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# Initialization and Learning

- Normalize your input
- Initialize weights with random numbers (bias to 0)
- Adjust SGD learning rate
- Momentum
  - Accumulate gradients across successive updates
- Other optimizers

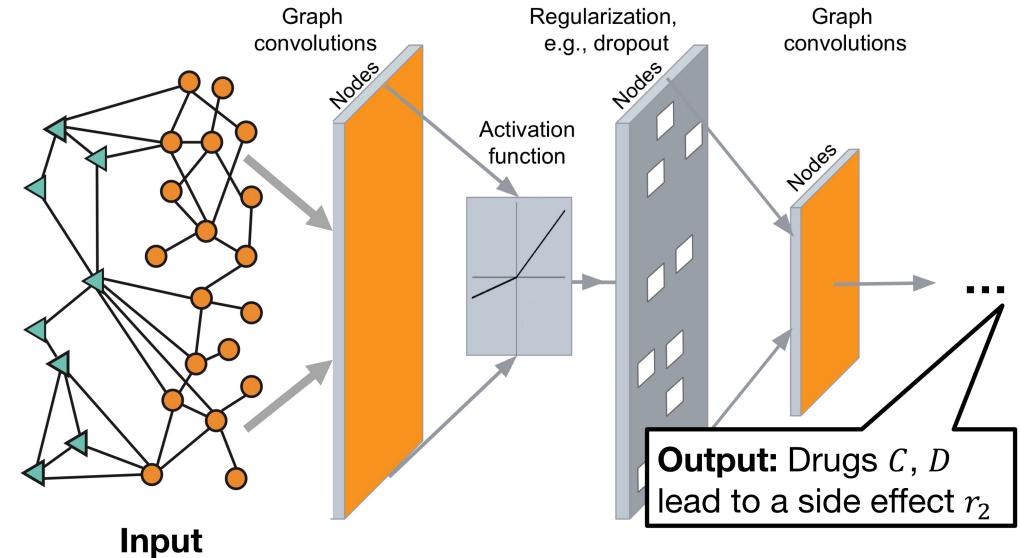
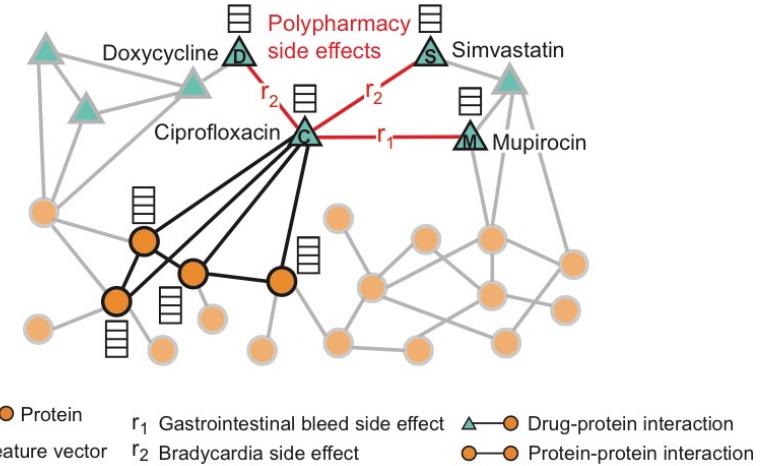
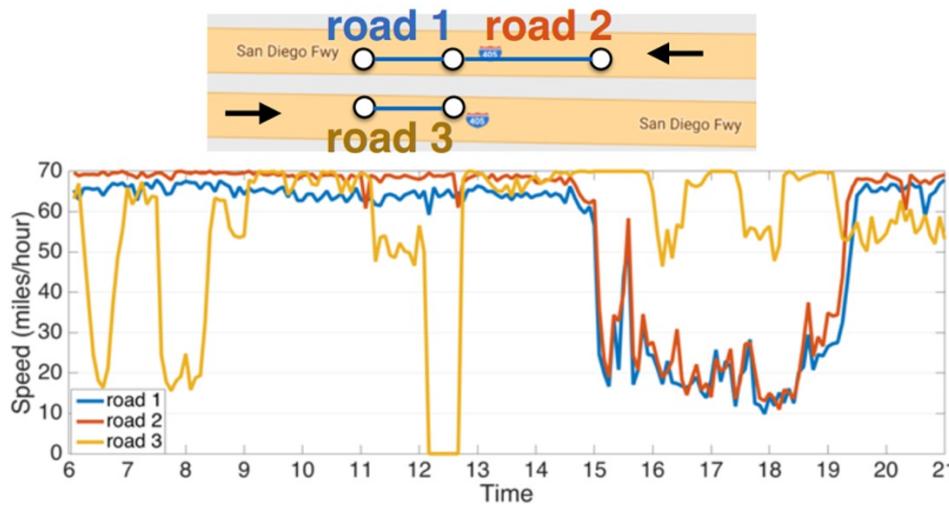


Credits: Alec Radford

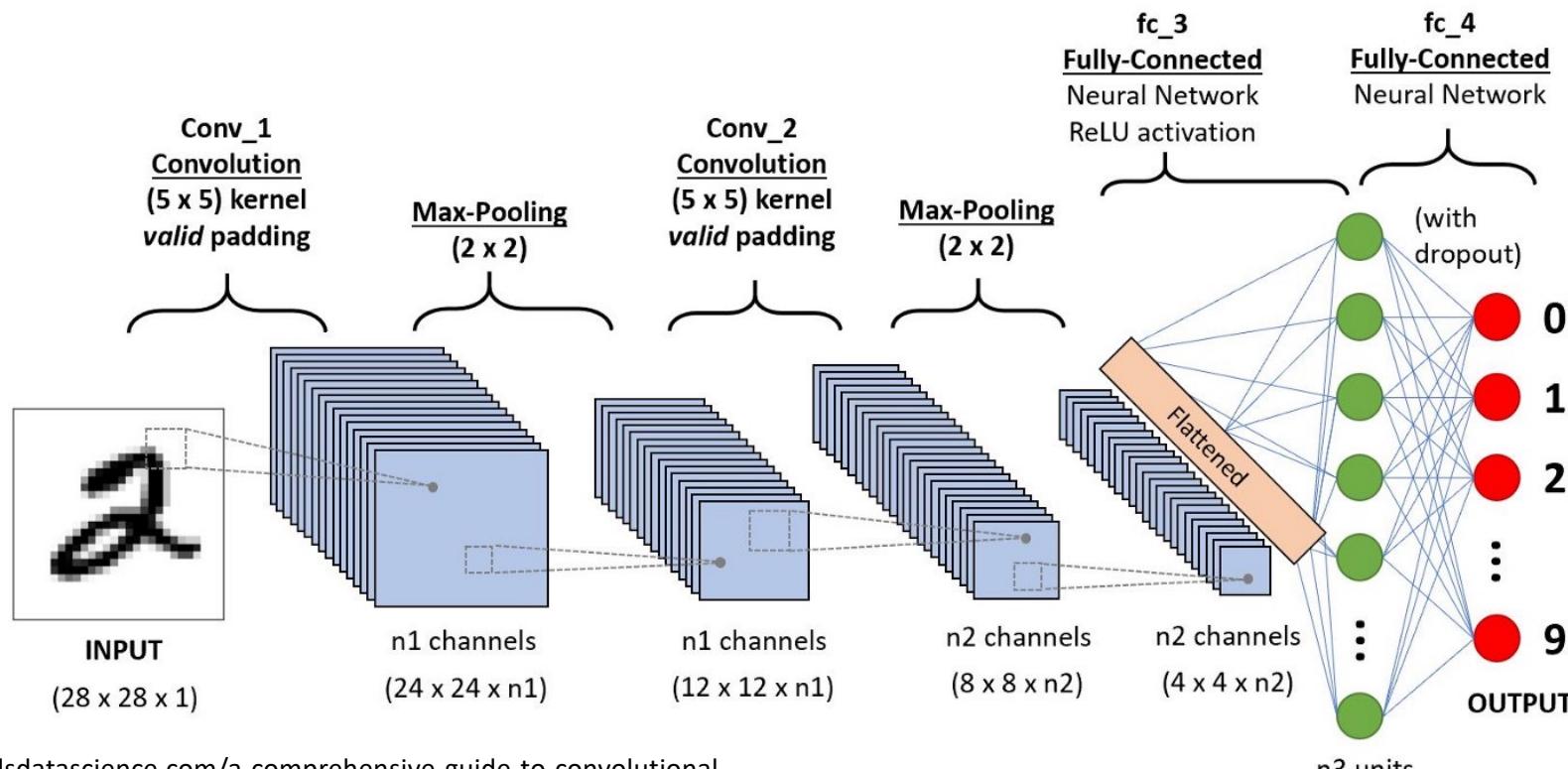
# Many Types of Neural Network Architectures

- Graph Neural Networks
- Convolutional Neural Networks
- Recurrent Neural Networks
- Transformer
- We can also mix them!

# Graph Neural Networks

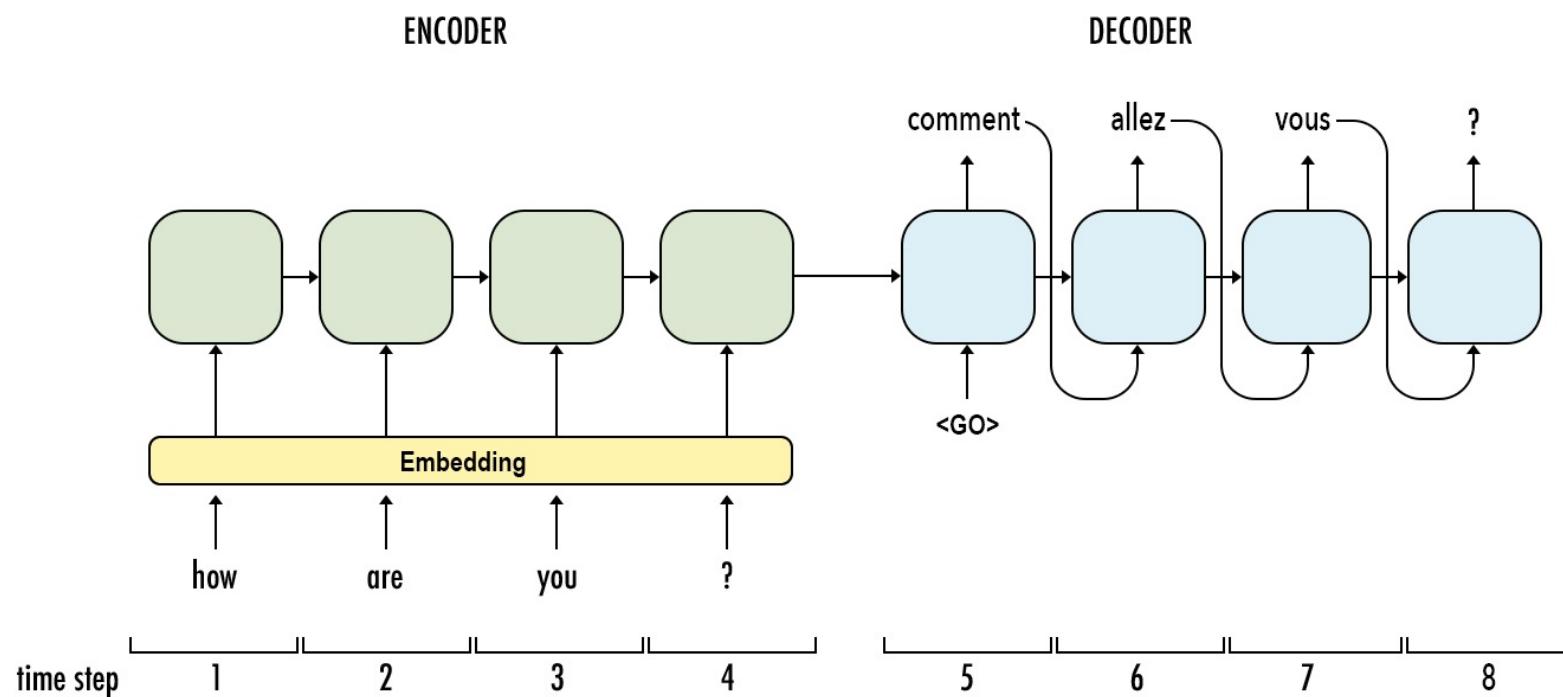


# Convolutional Neural Networks

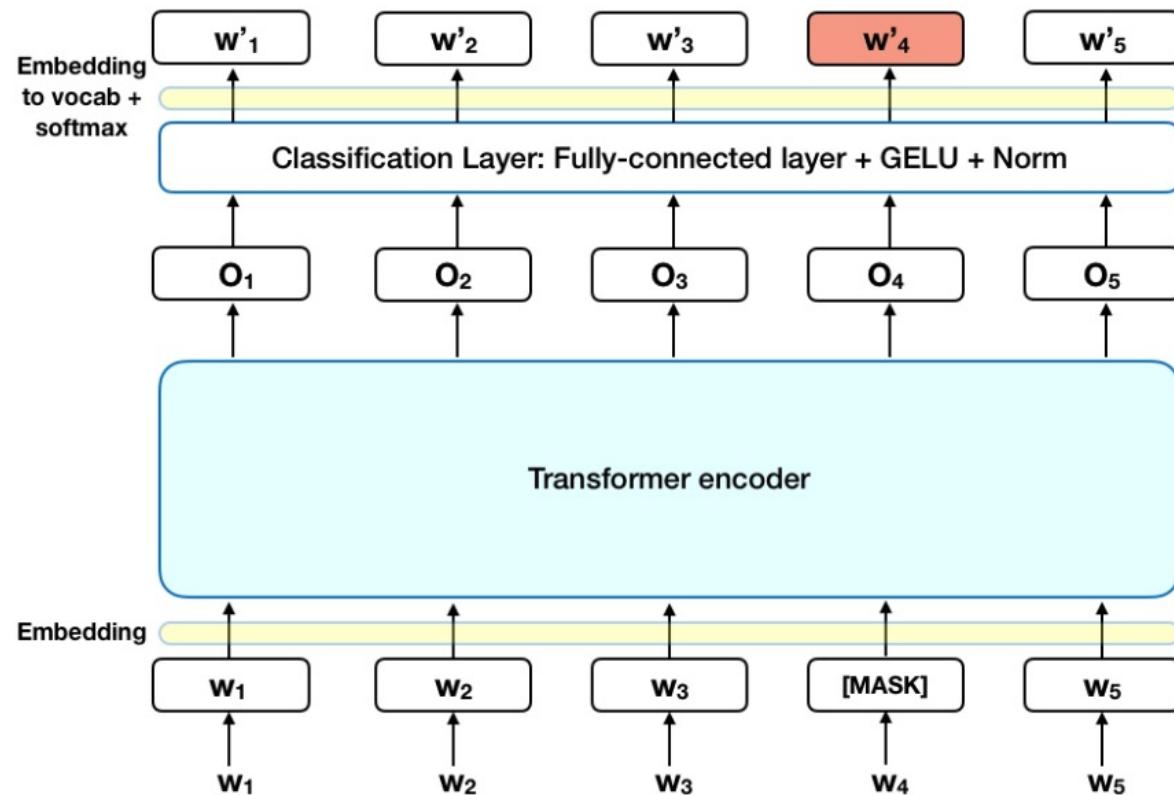


<https://towardsdatascience.com/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53>

# Recurrent Neural Networks



# Transformer



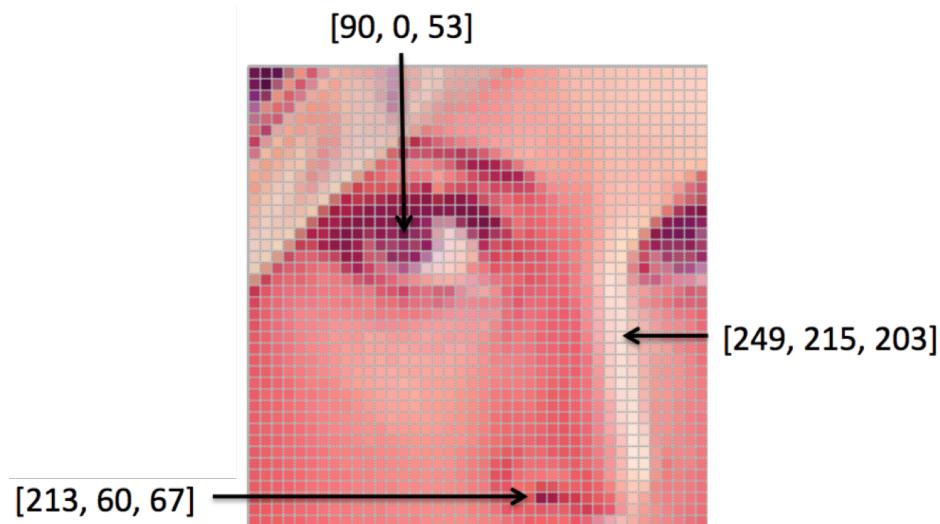
# Neural Networks & DL Summary

- DL is very versatile and can capture non-linear relationships
- DL can take advantage of large amounts of training data
- Design a DL network include the decisions of network architectures, loss functions, and regularizer
- Training a DL network concerns initialization (including data normalization), learning rate, learning algorithms, and batch sizes (SGD)
- Many open-source tools, books, and tutorials are available online

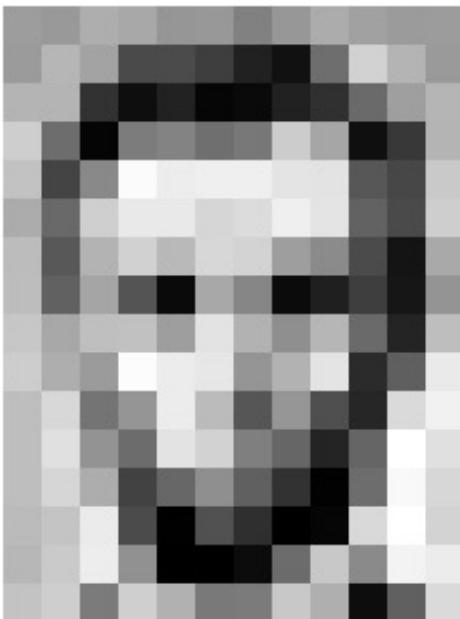
# Convolutional Neural Networks

A short introduction

# Image as Functions



# Image as Functions

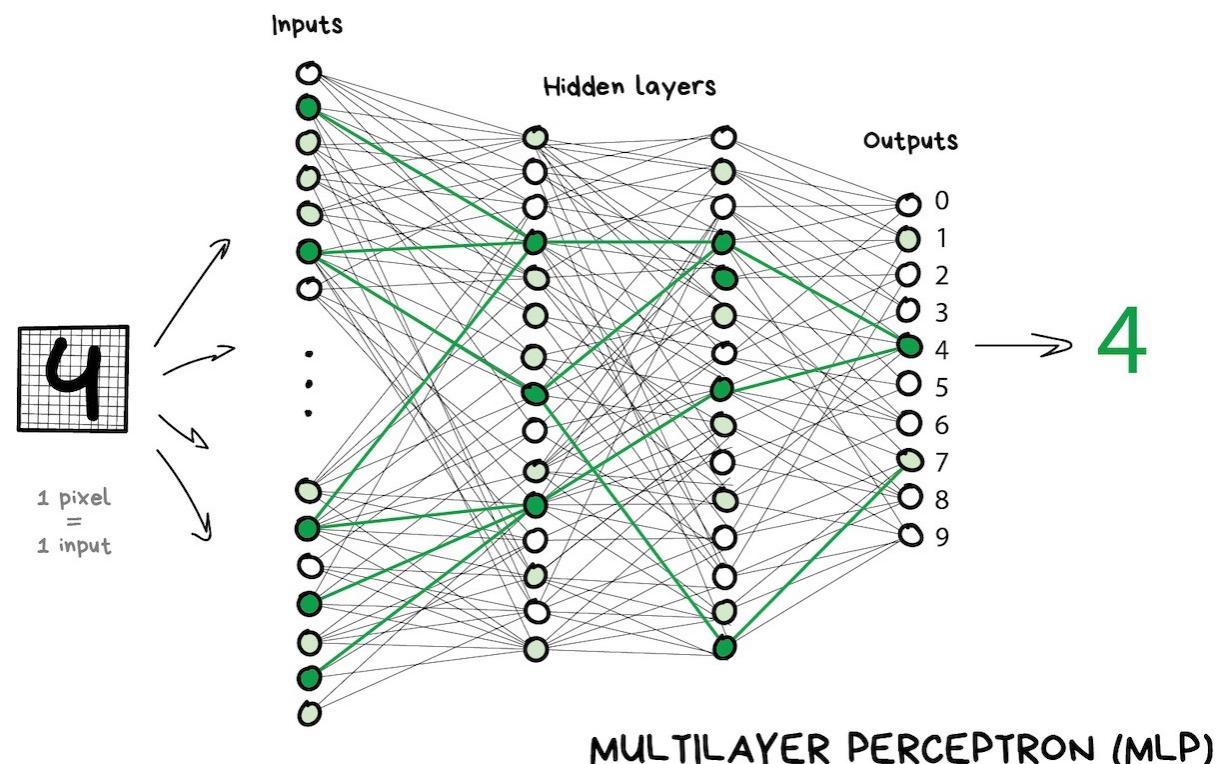


157	153	174	168	150	152	129	151	172	161	155	156
155	182	163	74	75	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	105	159	181
206	109	5	124	131	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	105	207	233	233	214	220	239	228	98	74	206
188	88	179	209	185	215	211	158	139	75	20	169
189	97	165	84	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	105	36	190
205	174	155	252	236	231	149	178	228	43	95	234
190	216	116	149	236	187	85	150	79	38	218	241
190	224	147	108	227	210	127	102	36	101	255	224
190	214	173	56	103	143	95	50	2	109	249	215
187	196	235	75	1	81	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
195	206	123	207	177	121	123	209	175	13	96	218

157	153	174	168	150	152	129	151	172	161	155	156
155	182	163	74	75	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	105	159	181
206	109	5	124	131	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	105	207	233	233	214	220	239	228	98	74	206
188	88	179	209	185	215	211	158	139	75	20	169
189	97	165	84	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	105	36	190
205	174	155	252	236	231	149	178	228	43	95	234
190	216	116	149	236	187	85	150	79	38	218	241
190	224	147	108	227	210	127	102	36	101	255	224
190	214	173	56	103	143	95	50	2	109	249	215
187	196	235	75	1	81	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
195	206	123	207	177	121	123	209	175	13	96	218

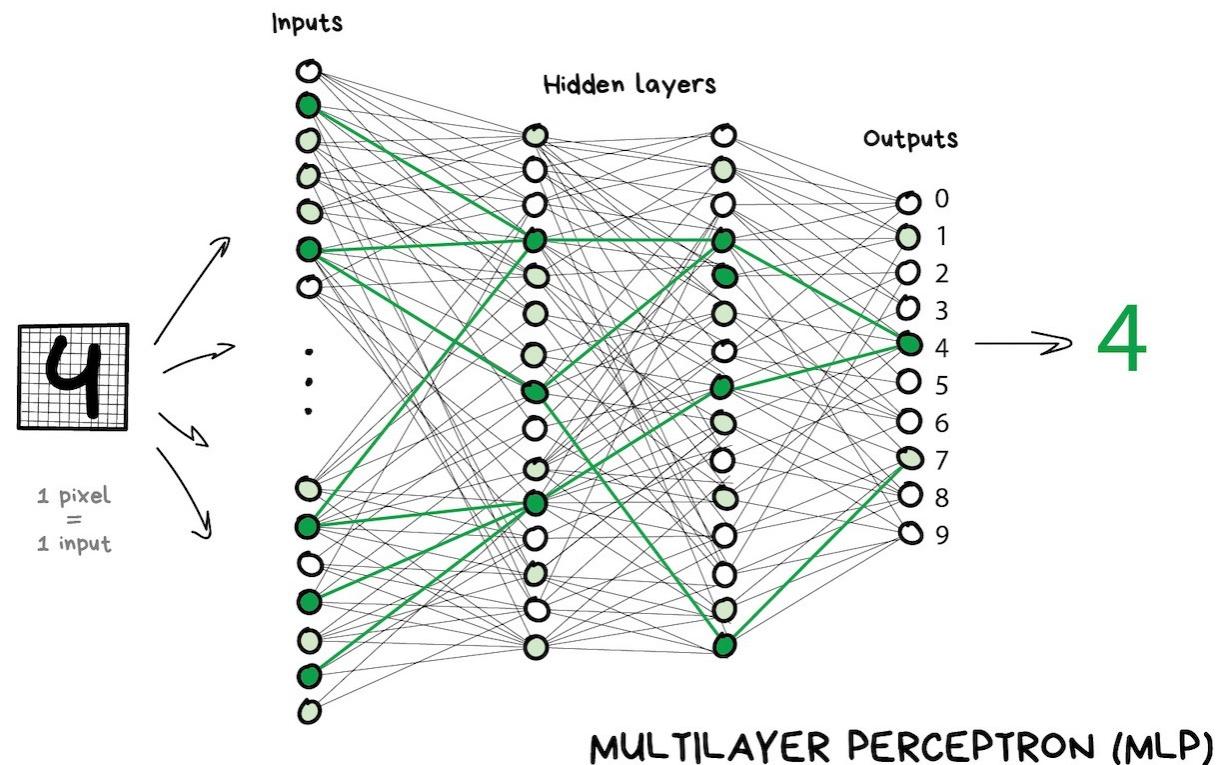
# Image Classification with Dense Layers

- How many parameters do we need?
  - Two hidden layers
  - Fully connected
  - Assuming a  $28 \times 28$  image, 3 channels (RGB), 2 layers, 1,000 neuron each
    - $28 \times 28 \times 3 \times 2 \times 1000 + 2 \times 1000 = 4.7M!$

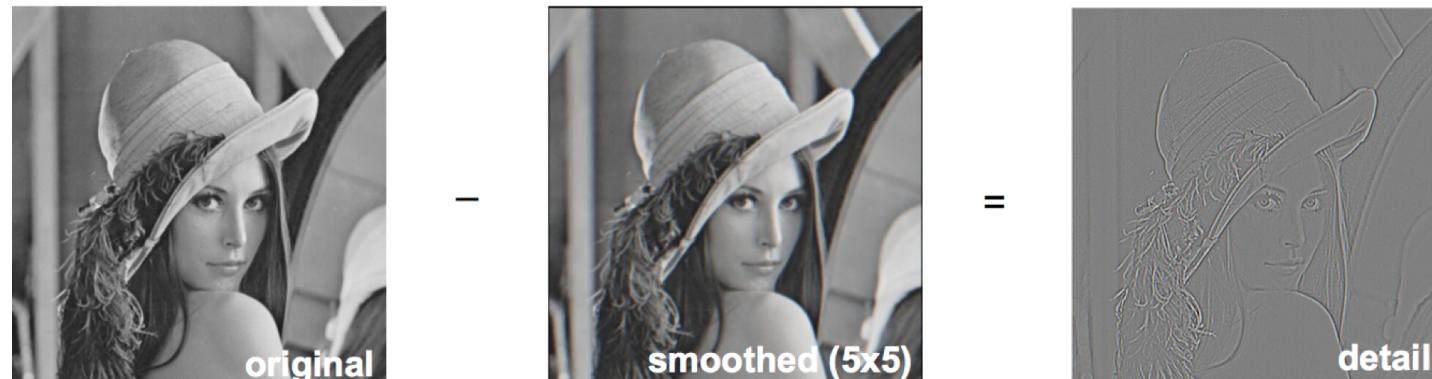


# Image Classification with Dense Layers

- Spatial structure is not used
  - Spatial relations between pixel values
- The input image is “flattened”
  - From 2D pixels to 1D inputs

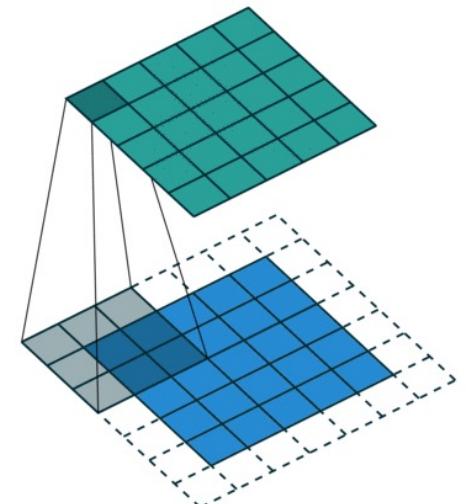


# Image Filters, Convolution, Kernel

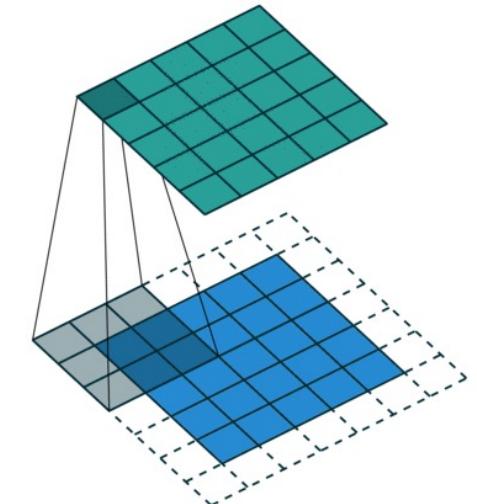


$$\begin{matrix} \bullet 0 & \bullet 0 & \bullet 0 \\ \bullet 0 & \bullet 1 & \bullet 0 \\ \bullet 0 & \bullet 0 & \bullet 0 \end{matrix}$$

$$-\frac{1}{9} \begin{matrix} \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \end{matrix}$$



# Image Filters, Convolution, Kernel



$$\begin{bmatrix} \bullet 0 & \bullet 0 & \bullet 0 \\ \bullet 0 & \bullet 1 & \bullet 0 \\ \bullet 0 & \bullet 0 & \bullet 0 \end{bmatrix}$$

+

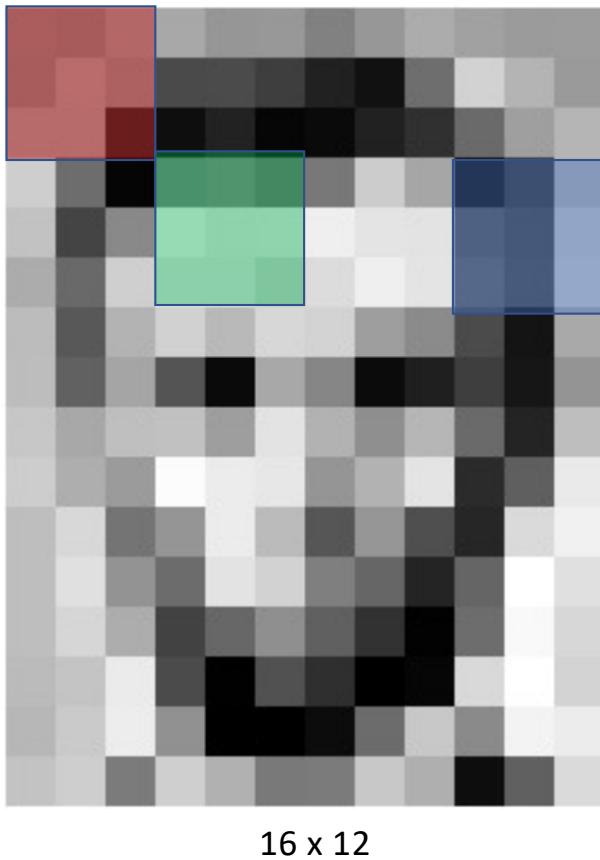
$$\begin{bmatrix} \bullet 0 & \bullet 0 & \bullet 0 \\ \bullet 0 & \bullet 1 & \bullet 0 \\ \bullet 0 & \bullet 0 & \bullet 0 \end{bmatrix}$$

$$- \frac{1}{9} \begin{bmatrix} \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \end{bmatrix}$$

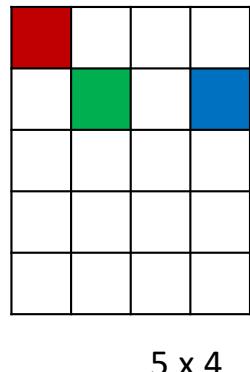
$$\begin{bmatrix} \bullet 0 & \bullet 0 & \bullet 0 \\ \bullet 0 & \bullet 2 & \bullet 0 \\ \bullet 0 & \bullet 0 & \bullet 0 \end{bmatrix}$$

$$- \frac{1}{9} \begin{bmatrix} \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \\ \bullet 1 & \bullet 1 & \bullet 1 \end{bmatrix}$$

# Image Filters, Convolution, Kernel



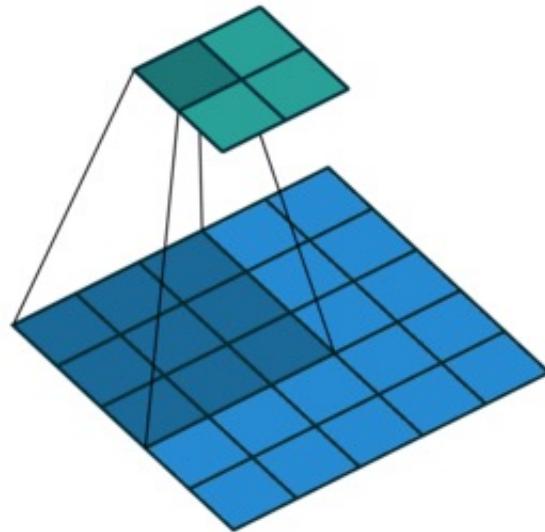
- Apply a convolution kernel on the image to generate another image
- The output image can have **a different size** from the input image, depending on the kernel sizes/types, stride sizes, and padding methods



- Each cell in the output image summarizes a  $3 \times 3$  area in the original image
- The same summarization operation for every cell, e.g., use the average intensity

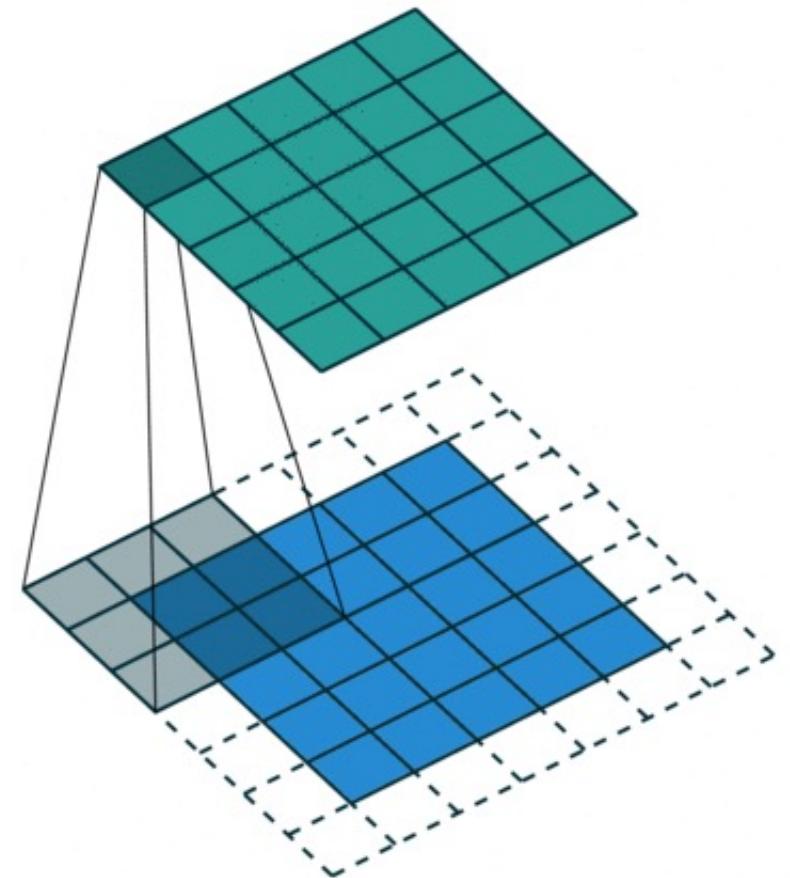
# Strides

- Strides: increment step size for the convolution operator
- Reduces the size of the output map
- A stride of 2:



# Padding

- Padding: artificially fill borders of image
- Useful to keep spatial dimension constant across filters
- Useful with strides and large receptive fields
- Usually: fill with 0s



# Padding

0 <sub>0</sub>	0 <sub>1</sub>	0 <sub>2</sub>	0	0	0	0	0
0 <sub>2</sub>	3 <sub>2</sub>	3 <sub>0</sub>	2	1	0	0	0
0 <sub>0</sub>	0 <sub>1</sub>	0 <sub>2</sub>	1	3	1	1	0
0	3	1	2	2	3	0	0
0	2	0	0	2	2	0	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

0	0	0 <sub>0</sub>	0 <sub>1</sub>	0 <sub>2</sub>	0	0	0
0	3	3 <sub>2</sub>	2 <sub>2</sub>	1 <sub>0</sub>	0	0	0
0	0	0 <sub>0</sub>	1 <sub>1</sub>	3 <sub>2</sub>	1	0	0
0	3	1	2	2	3	0	0
0	2	0	0	2	2	0	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

0	0	0	0	0 <sub>0</sub>	0 <sub>1</sub>	0 <sub>2</sub>	0
0	3	3	2	1 <sub>2</sub>	0 <sub>2</sub>	0 <sub>0</sub>	0
0	0	0	1	3 <sub>0</sub>	1 <sub>1</sub>	0 <sub>2</sub>	0
0	3	1	2	2	3	0	0
0	2	0	0	2	2	0	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

0	0	0	0	0	0	0	0
0	3	3	2	1	0	0	0
0 <sub>0</sub>	0 <sub>1</sub>	0 <sub>2</sub>	1	3	1	1	0
0 <sub>2</sub>	3 <sub>2</sub>	1 <sub>0</sub>	2	2	3	0	0
0 <sub>0</sub>	2 <sub>1</sub>	0 <sub>2</sub>	0	2	2	0	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

0	0	0	0	0	0	0	0
0	3	3	2	1	0	0	0
0	0	0 <sub>0</sub>	1 <sub>1</sub>	3 <sub>2</sub>	1	0	0
0	3	1 <sub>2</sub>	2 <sub>2</sub>	2 <sub>0</sub>	3	0	0
0	2	0 <sub>0</sub>	0 <sub>1</sub>	2 <sub>2</sub>	2	0	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

0	0	0	0	0	0	0	0
0	3	3	2	1	0	0	0
0	0	0	1	3 <sub>0</sub>	1 <sub>1</sub>	0 <sub>2</sub>	0
0	3	1	2	2 <sub>2</sub>	3 <sub>2</sub>	0 <sub>0</sub>	0
0	2	0	0	2 <sub>0</sub>	2 <sub>1</sub>	0 <sub>2</sub>	0
0	2	0	0	0	0	1	0
0	0	0	0	0	0	0	0

6.0	17.0	3.0
8.0	17.0	13.0
6.0	4.0	4.0

# Sizes and Dimensions

- Assuming square input, dimension  $i \times i$
- Padding size =  $p$
- Stride size = 1
- Kernel size =  $k$
- Output dimension =  $o \times o$ 
$$o = (i - k) + 2 \times p + 1$$
- Read <https://arxiv.org/abs/1603.07285>

# Sizes and Dimensions

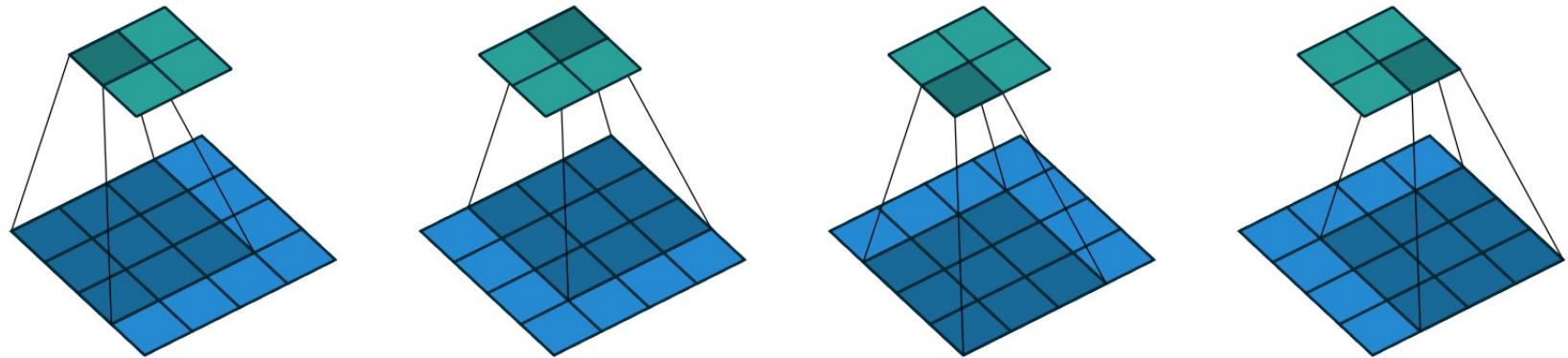


Figure 2.1: (No padding, unit strides) Convolving a  $3 \times 3$  kernel over a  $4 \times 4$  input using unit strides (i.e.,  $i = 4$ ,  $k = 3$ ,  $s = 1$  and  $p = 0$ ).

$$o = (i - k) + 2 \times p + 1$$

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# Sizes and Dimensions

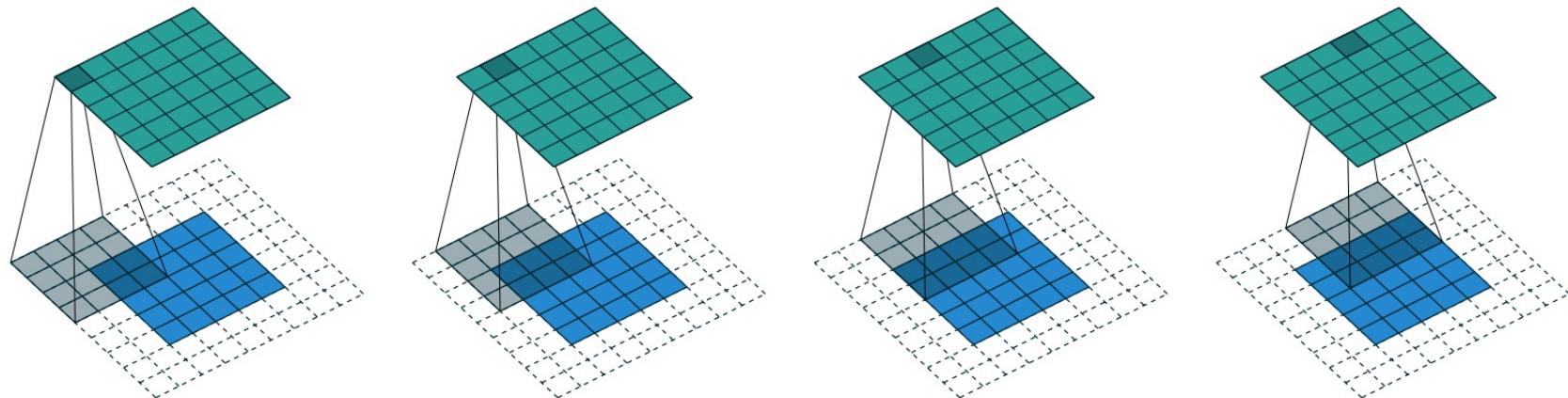


Figure 2.2: (Arbitrary padding, unit strides) Convolving a  $4 \times 4$  kernel over a  $5 \times 5$  input padded with a  $2 \times 2$  border of zeros using unit strides (i.e.,  $i = 5$ ,  $k = 4$ ,  $s = 1$  and  $p = 2$ ).

$$o = (i - k) + 2 \times p + 1$$

62

# Sizes and Dimensions

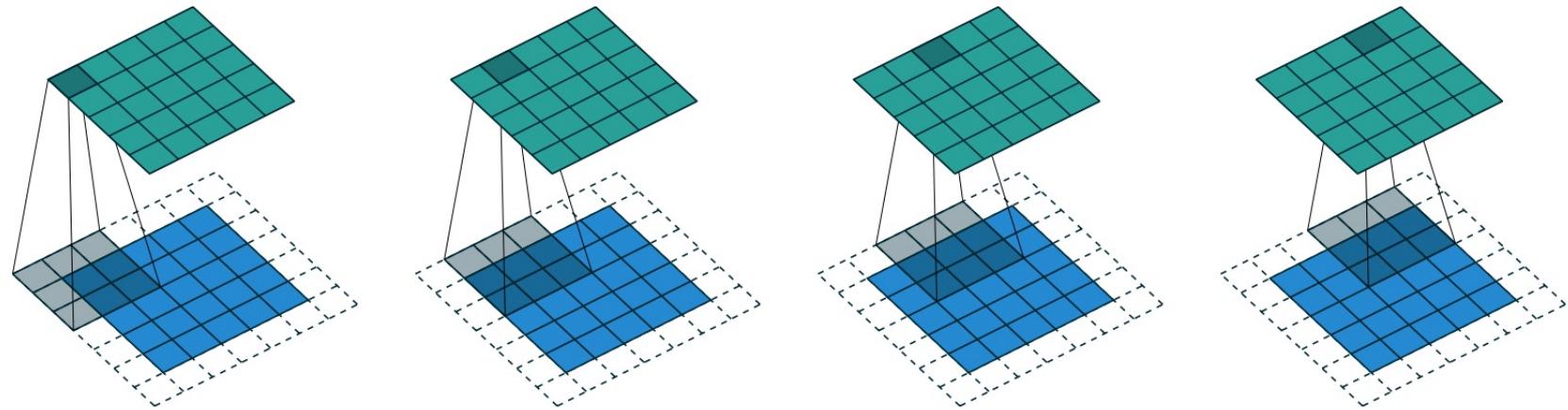


Figure 2.3: (Half padding, unit strides) Convolving a  $3 \times 3$  kernel over a  $5 \times 5$  input using half padding and unit strides (i.e.,  $i = 5$ ,  $k = 3$ ,  $s = 1$  and  $p = 1$ ).

$$o = (i - k) + 2 \times p + 1; k = 2 \times p + 1$$

63

# Sizes and Dimensions

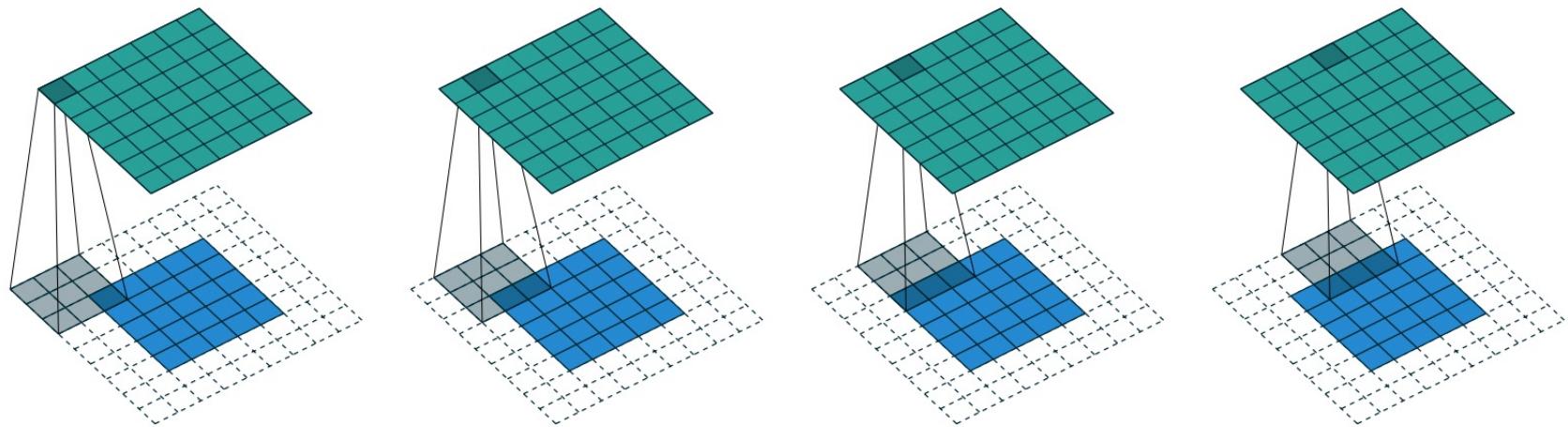


Figure 2.4: (Full padding, unit strides) Convolving a  $3 \times 3$  kernel over a  $5 \times 5$  input using full padding and unit strides (i.e.,  $i = 5$ ,  $k = 3$ ,  $s = 1$  and  $p = 2$ ).

$$o = (i - k) + 2 \times p + 1; p = k - 1$$

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# Convolution in Neural Networks

- $x$  is a  $3 \times 3$  chunk (dark area) of the image (blue array)
- Kernel is the subscripts in the dark area
- A neuron is parameterized with the kernel
  - $3 \times 3$  weight matrix  $w$

Image:  $im$ , dimensions  $5 \times 5$

Kernel:  $k$ , dimensions  $3 \times 3$

3 <sub>0</sub>	3 <sub>1</sub>	2 <sub>2</sub>	1	0
0 <sub>2</sub>	0 <sub>2</sub>	1 <sub>0</sub>	3	1
3 <sub>0</sub>	1 <sub>1</sub>	2 <sub>2</sub>	2	3
2	0	0	2	2
2	0	0	0	1

12.0	12.0	17.0
10.0	17.0	19.0
9.0	6.0	14.0

$$(k \star im)(x, y) = \sum_{n=0}^2 \sum_{m=0}^2 k(n, m) \cdot im(x + n - 1, y + m - 1)$$

# Convolution in Neural Networks

- $x$  is a  $3 \times 3$  chunk (dark area) of the image (blue array)
- Kernel is the subscripts in the dark area
- A neuron is parameterized with the kernel
  - $3 \times 3$  weight matrix  $\mathbf{w}$
- The activation obtained by sliding the kernel window to compute:

$$z(x) = \text{relu}(\mathbf{w}^T x + b)$$

Image:  $im$ , dimensions  $5 \times 5$

Kernel:  $k$ , dimensions  $3 \times 3$

3 <sub>0</sub>	3 <sub>1</sub>	2 <sub>2</sub>	1	0
0 <sub>2</sub>	0 <sub>2</sub>	1 <sub>0</sub>	3	1
3 <sub>0</sub>	1 <sub>1</sub>	2 <sub>2</sub>	2	3
2	0	0	2	2
2	0	0	0	1

12.0	12.0	17.0
10.0	17.0	19.0
9.0	6.0	14.0

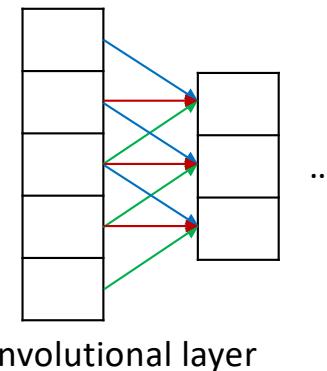
$$\begin{aligned} & (k * im)(x, y) && \mathbf{w}^T x \\ &= \sum_{n=0}^2 \sum_{m=0}^2 k(n, m) \cdot im(x + n - 1, y + m - 1) \end{aligned}$$

# Motivations

- Local connectivity
  - A neuron depends only on **a few local** input neurons
  - Translation invariance
- Comparison to Fully connected
  - Parameter sharing, reduce overfitting
  - Make use of spatial structure: **strong prior** for vision!

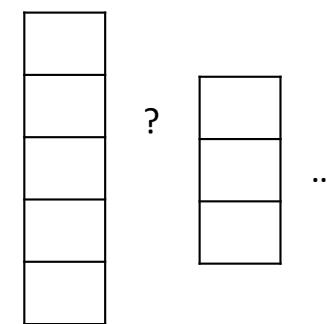
1D Convolution View:  
How many parameters  
do we need?

Kernel dimensions + 1



Convolutional layer

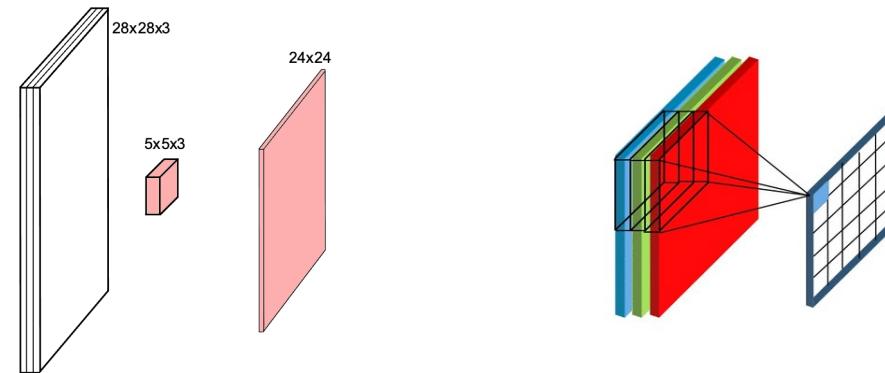
#current layer neurons x #previous layer neurons + #current layer neurons



Fully connected (dense layer)

# Multiple Channels

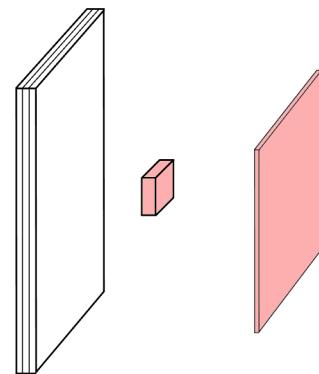
- Colored image = tensor of shape (height, width, channels)
- Convolutions are usually **computed for each channel separately and summed**:



$$(k * im^{color}) = \sum_{c=0}^2 k^c * im^c$$

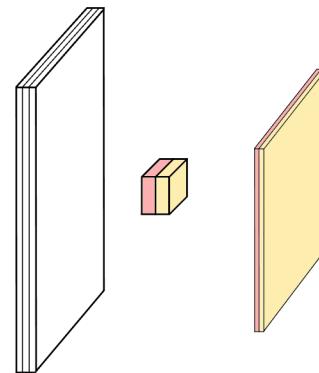
# Multiple Convolutions

- Multiple kernel sizes aka receptive fields (usually 1, 3, 5, 7, 11)



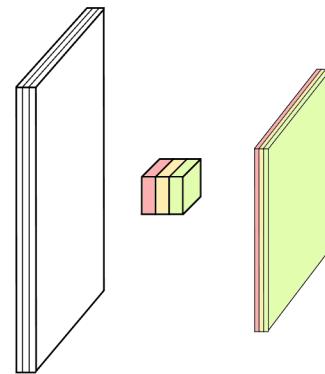
# Multiple Convolutions

- Multiple kernel sizes aka receptive fields (usually 1, 3, 5, 7, 11)



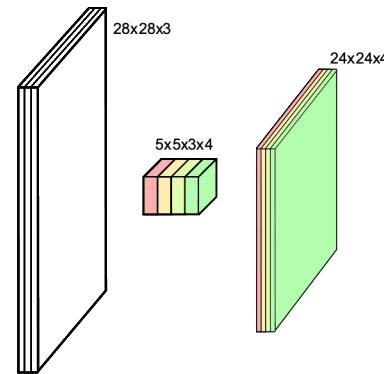
# Multiple Convolutions

- Multiple kernel sizes aka receptive fields (usually 1, 3, 5, 7, 11)



# Multiple Convolutions

- Multiple kernel sizes aka receptive fields (usually 1, 3, 5, 7, 11)



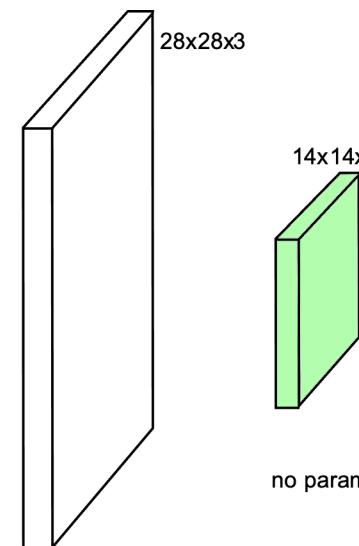
# Pooling

- Spatial dimension reduction
- Local invariance
- No parameters: max or average of 2x2 units

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

max pool with 2x2 filters  
and stride 2

6	8
3	4



no parameters!

# Put it all together

Input

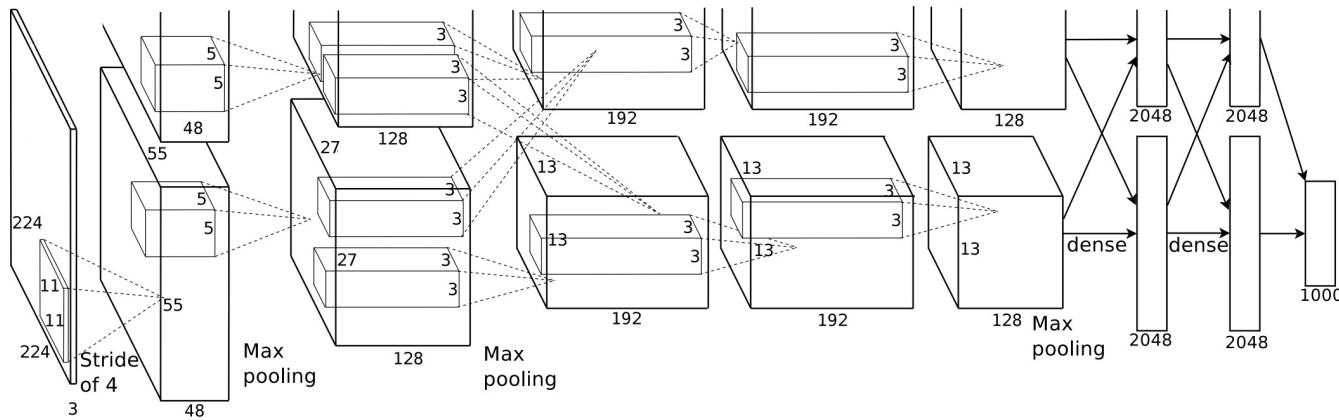
Conv blocks

- Convolution + activation (relu)
- Convolution + activation (relu)
- ...
- Maxpooling 2x2

Output

- Fully connected layers
- Softmax

# AlexNet



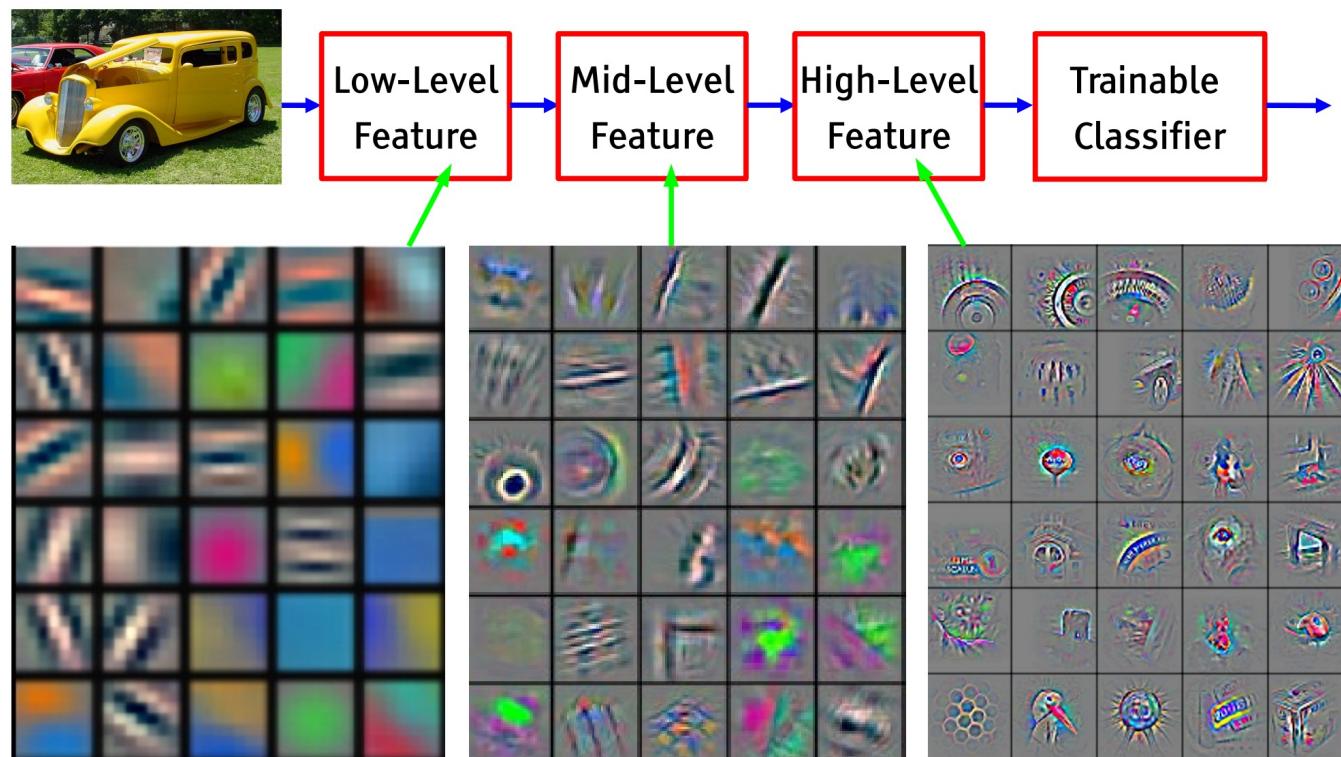
- First conv layer: kernel 11x11x3x96 stride 4
  - Kernel shape: (11,11,3,96)
  - Output shape: (55,55,96)
  - Number of parameters: 34,944
  - Equivalent MLP parameters:  $43.7 \times 1e9$

INPUT:	[227x227x3]			
CONV1:	[55x55x96]	96	11x11 filters at stride 4, pad 0	
MAX POOL1:	[27x27x96]	3x3	filters at stride 2	
CONV2:	[27x27x256]	256	5x5 filters at stride 1, pad 2	
MAX POOL2:	[13x13x256]	3x3	filters at stride 2	
CONV3:	[13x13x384]	384	3x3 filters at stride 1, pad 1	
CONV4:	[13x13x384]	384	3x3 filters at stride 1, pad 1	
CONV5:	[13x13x256]	256	3x3 filters at stride 1, pad 1	
MAX POOL3:	[6x6x256]	3x3	filters at stride 2	
FC6:	[4096]	4096	neurons	
FC7:	[4096]	4096	neurons	
FC8:	[1000]	1000	neurons (softmax logits)	

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Simplified version of Krizhevsky, Alex, Sutskever, and Hinton. "Imagenet classification with deep convolutional neural networks." NIPS 2012

# Hierarchical Representation



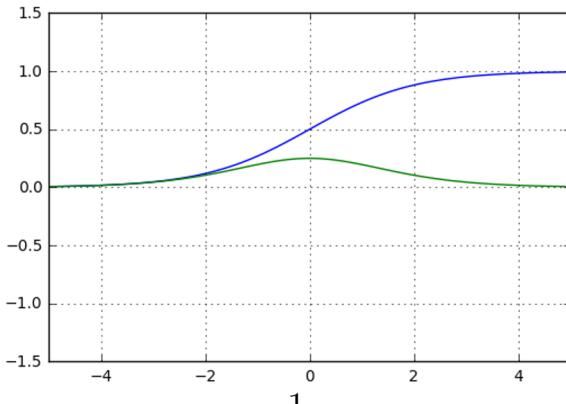
Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

# AlexNet

- One of the first deep convolutional networks to achieve considerable accuracy on the 2012 ImageNet LSVRC-2012 challenge
  - 84.7% vs 73.8% (second best)
- Data augmentation and dropout layers to reduce overfitting
- Use ReLu to avoid the vanishing gradient problem

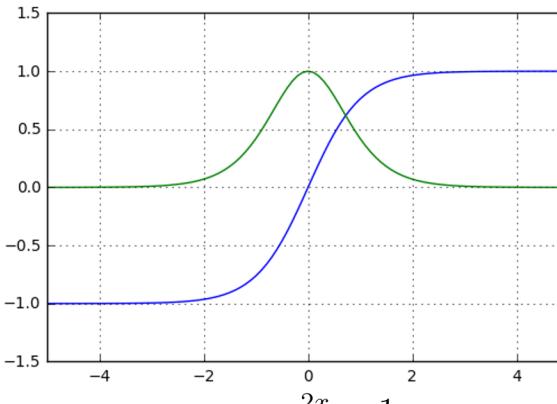
# Vanishing gradient problem

- Recall that the optimization process is based on backpropagation of gradient computed with the loss function
- When the gradients are already small, the chain rule makes the gradients of the earlier layers even smaller (e.g., decreases exponentially the number of layers)
- Earlier layers are difficult to train – weights do not change due to the small gradients



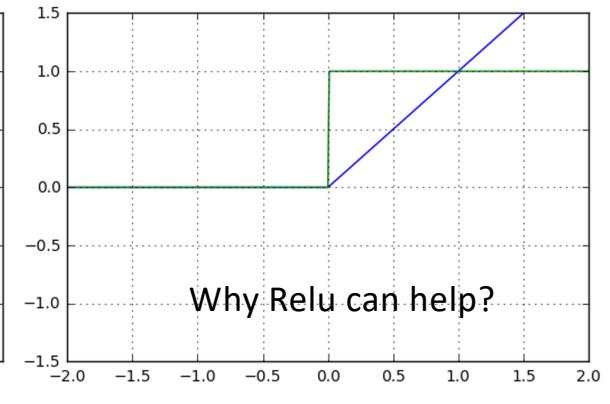
$$\text{sigm}(x) = \frac{1}{1 + e^{-x}}$$

$$\text{sigm}'(x) = \text{sigm}(x)(1 - \text{sigm}(x))$$



$$\tanh(x) = \frac{e^{2x} - 1}{e^{2x} + 1}$$

$$\tanh'(x) = 1 - \tanh(x)^2$$



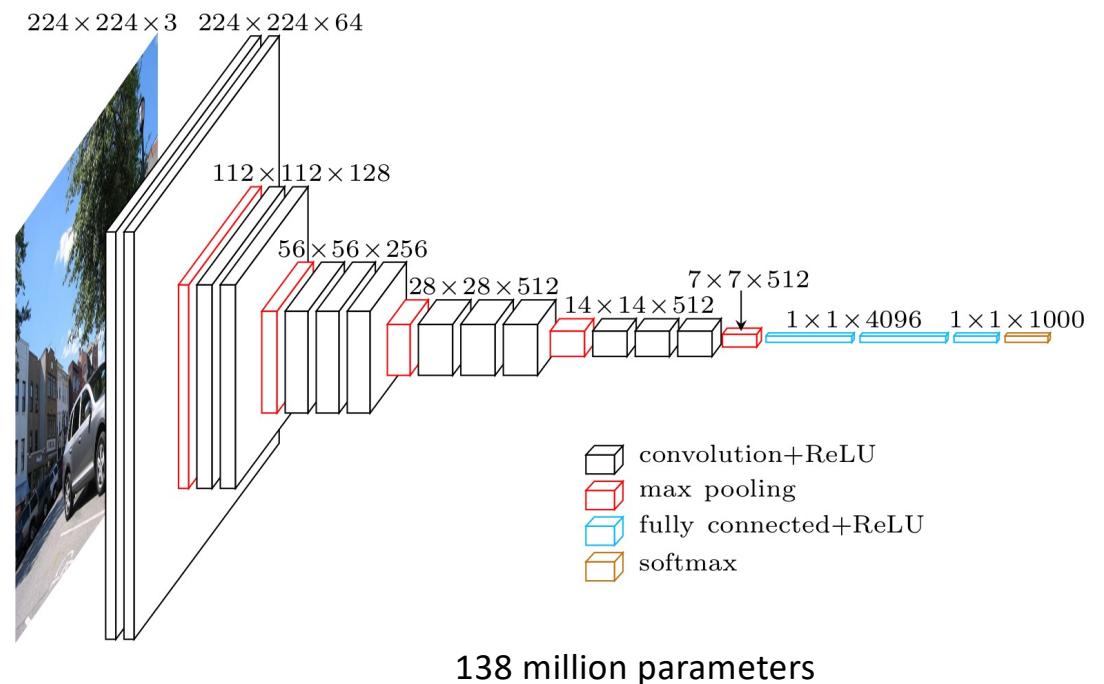
$$\text{relu}(x) = \max(0, x)$$

$$\text{relu}'(x) = 1_{x>0}$$

Why Relu can help?

# Let's go deeper: VGG-16

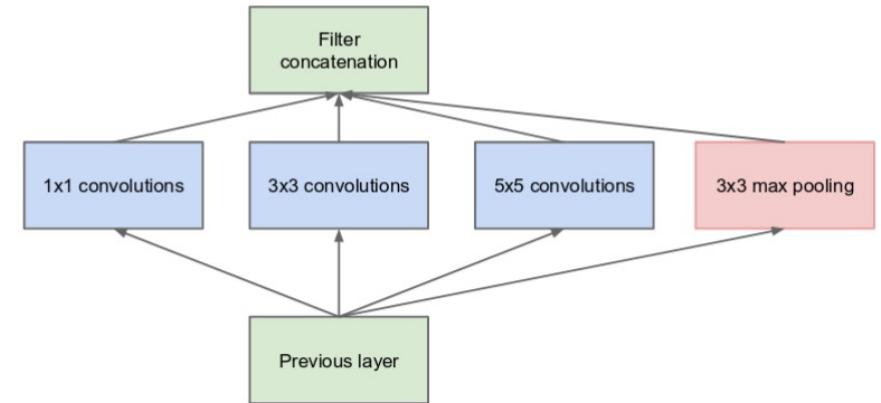
- More layers than AlexNet
  - 138m vs 62m parameters
- Effectively use **fixed size, small kernels** to replace larger, variable size kernels
- Building blocks:
  - Conv, Conv, Max Pooling or
  - Conv, Conv, Conv, Max Pooling



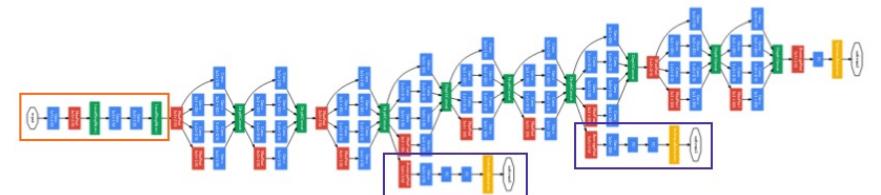
Simonyan, Karen, and Zisserman. "Very deep convolutional networks for large-scale image recognition." (2014)

# Let's go wider: GoogleNet Inception

- Capture **global (semantic) information** with **larger kernel**
- Capture **local (spatial) information** with **smaller kernel**
- Use multiple variable size kernels in the same layer
  - Fewer layers, easier to train
  - Still capture both global and local information

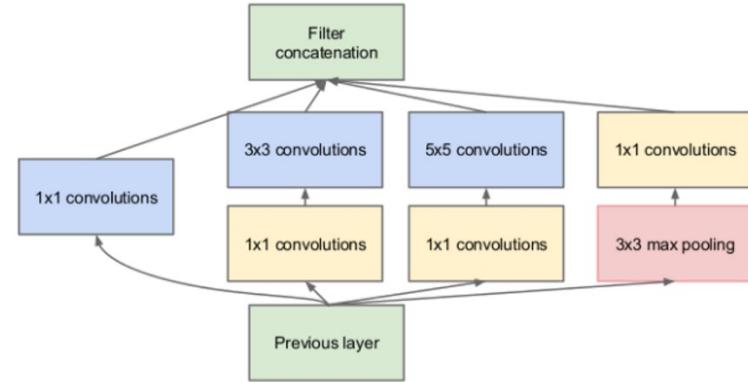


(a) Inception module, naïve version



# 1D convolution in GoogleNet

- Reduce the number of channels
  - Summed
- Selectively squeeze information from multiple channels in the previous layer to 1 channel
  - Like dimension reductions
  - Allow efficient use of multiple kernels



# Can we go deeper again?

## ResNet

- More layers, deeper models
  - 34, 50, 101, 152 layers
- Skipped connections pass information across layers
  - Mitigate (but not solve) the vanishing gradient problem

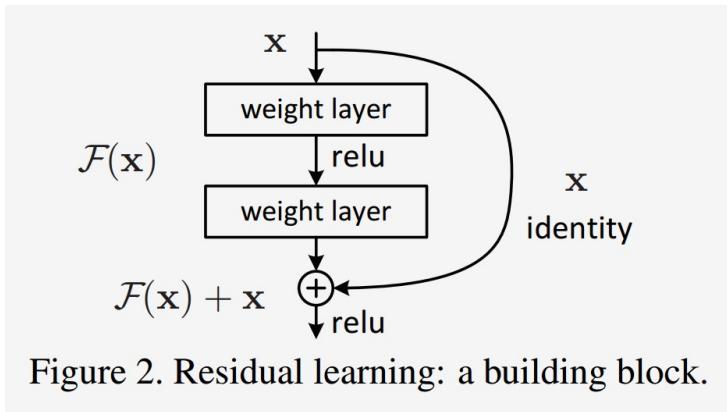
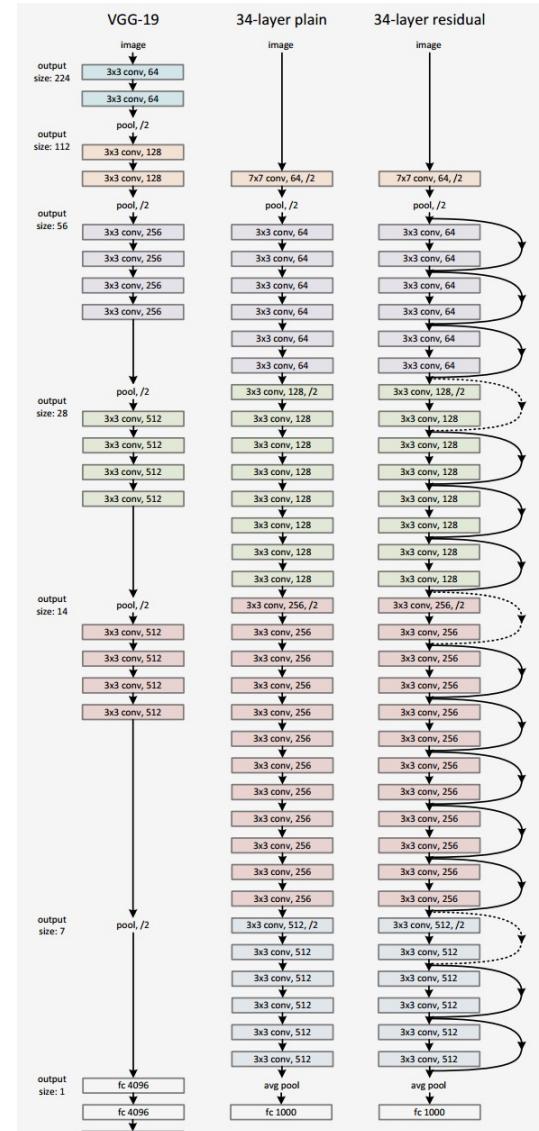


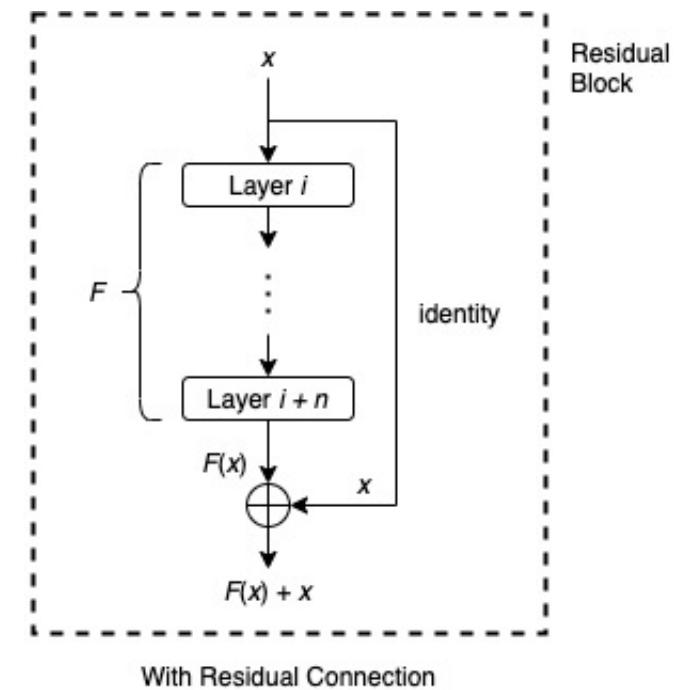
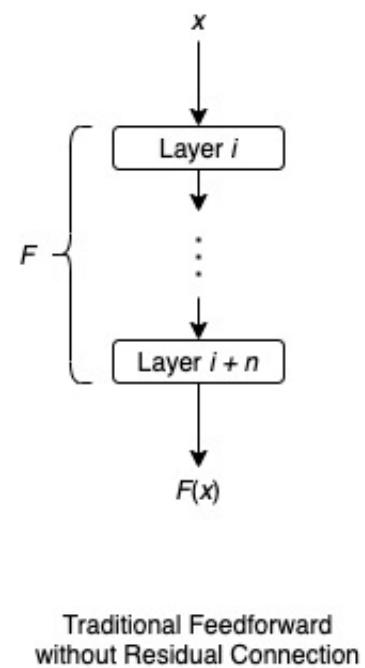
Figure 2. Residual learning: a building block.

He, Kaiming, et al. "Deep residual learning for image recognition." CVPR. 2016.



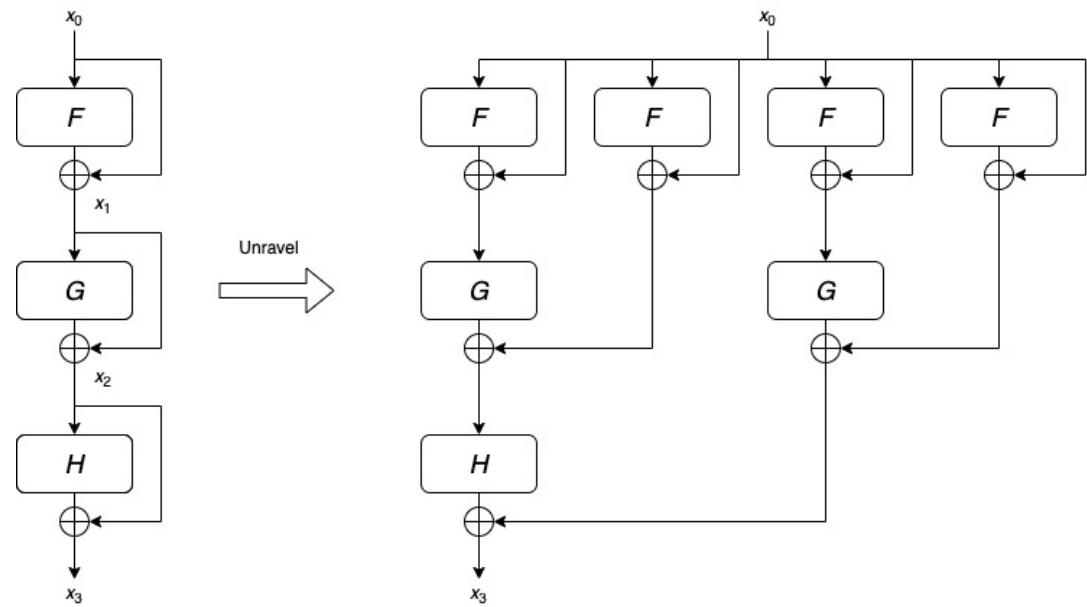
# Residual Connections

- Also called the skipped or skip connections
- Used in many different types of neural networks to facilitate training (e.g., mitigate the vanish gradient problem)



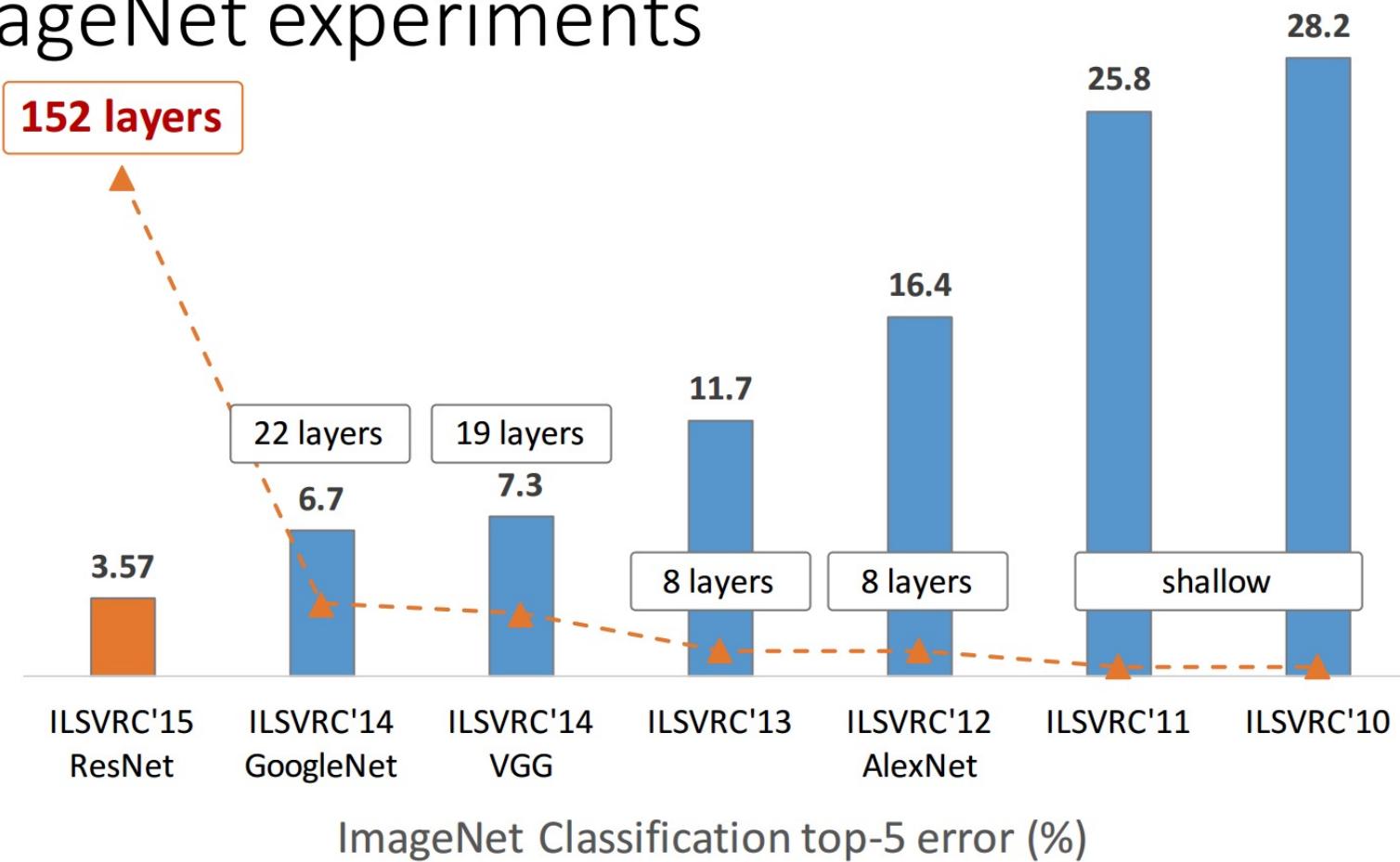
# Residual Connections

- As ensembles of shallow neural networks
- Empirically, residual connections often help generate better models and results, e.g., see DenseNet



$$\begin{aligned}x_3 &= H(x_2) + x_2 \\&= H(G(x_1) + x_1) + G(x_1) + x_1 \\&= H(G(F(x_0) + x_0) + F(x_0) + x_0) + G(F(x_0) + x_0) + F(x_0) + x_0\end{aligned}$$

# ImageNet experiments



from Kaiming He slides "Deep residual learning for image recognition." ICML. 2016.

# AlexNet, VGG, Inception, ResNet

- FLOP = floating point operations (required for a forward pass)
  - e.g., training AlexNet would take similar time as training Inception

Comparison					
Network	Year	Salient Feature	top5 accuracy	Parameters	FLOP
AlexNet	2012	Deeper	84.70%	62M	1.5B
VGGNet	2014	Fixed-size kernels	92.30%	138M	19.6B
Inception	2014	Wider - Parallel kernels	93.30%	6.4M	2B
ResNet-152	2015	Shortcut connections	95.51%	60.3M	11B

# State of the Art

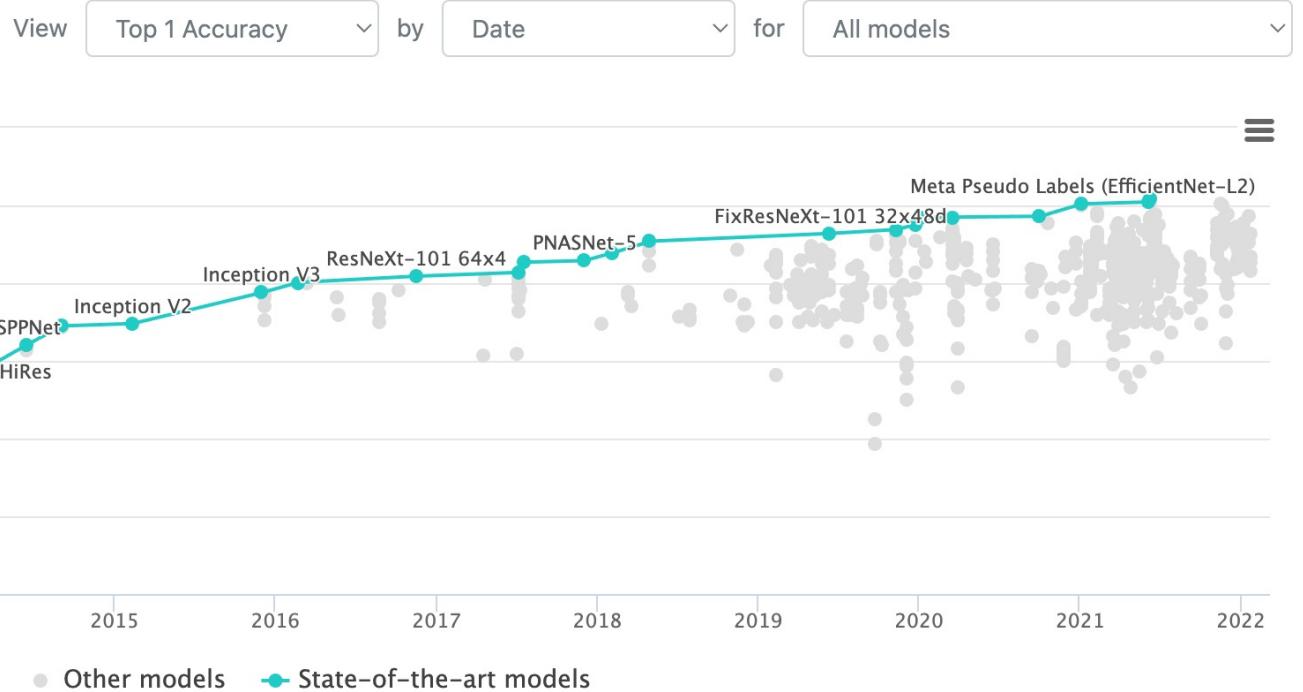
Meta Pseudo Labels, Hieu Pham et al.  
(Jan 2021)

Method	# Params	Extra Data	ImageNet		ImageNet-ReAL [6]
			Top-1	Top-5	Precision@1
ResNet-50 [24]	26M	—	76.0	93.0	82.94
ResNet-152 [24]	60M	—	77.8	93.8	84.79
DenseNet-264 [28]	34M	—	77.9	93.9	—
Inception-v3 [62]	24M	—	78.8	94.4	83.58
Xception [11]	23M	—	79.0	94.5	—
Inception-v4 [61]	48M	—	80.0	95.0	—
Inception-resnet-v2 [61]	56M	—	80.1	95.1	—
ResNeXt-101 [78]	84M	—	80.9	95.6	85.18
PolyNet [87]	92M	—	81.3	95.8	—
SENet [27]	146M	—	82.7	96.2	—
NASNet-A [90]	89M	—	82.7	96.2	82.56
AmoebaNet-A [52]	87M	—	82.8	96.1	—
PNASNet [39]	86M	—	82.9	96.2	—
AmoebaNet-C + AutoAugment [12]	155M	—	83.5	96.5	—
GPipe [29]	557M	—	84.3	97.0	—
EfficientNet-B7 [63]	66M	—	85.0	97.2	—
EfficientNet-B7 + FixRes [70]	66M	—	85.3	97.4	—
EfficientNet-L2 [63]	480M	—	85.5	97.5	—
ResNet-50 Billion-scale SSL [79]	26M	3.5B labeled Instagram	81.2	96.0	—
ResNeXt-101 Billion-scale SSL [79]	193M	3.5B labeled Instagram	84.8	—	—
ResNeXt-101 WSL [42]	829M	3.5B labeled Instagram	85.4	97.6	88.19
FixRes ResNeXt-101 WSL [69]	829M	3.5B labeled Instagram	86.4	98.0	89.73
Big Transfer (BiT-L) [33]	928M	300M labeled JFT	87.5	98.5	90.54
Noisy Student (EfficientNet-L2) [77]	480M	300M unlabeled JFT	88.4	98.7	90.55
Noisy Student + FixRes [70]	480M	300M unlabeled JFT	88.5	98.7	—
Vision Transformer (ViT-H) [14]	632M	300M labeled JFT	88.55	—	90.72
EfficientNet-L2-NoisyStudent + SAM [16]	480M	300M unlabeled JFT	88.6	98.6	—
Meta Pseudo Labels (EfficientNet-B6-Wide)	390M	300M unlabeled JFT	90.0	98.7	<b>91.12</b>
Meta Pseudo Labels (EfficientNet-L2)	480M	300M unlabeled JFT	<b>90.2</b>	<b>98.8</b>	91.02

# Image Classification on ImageNet

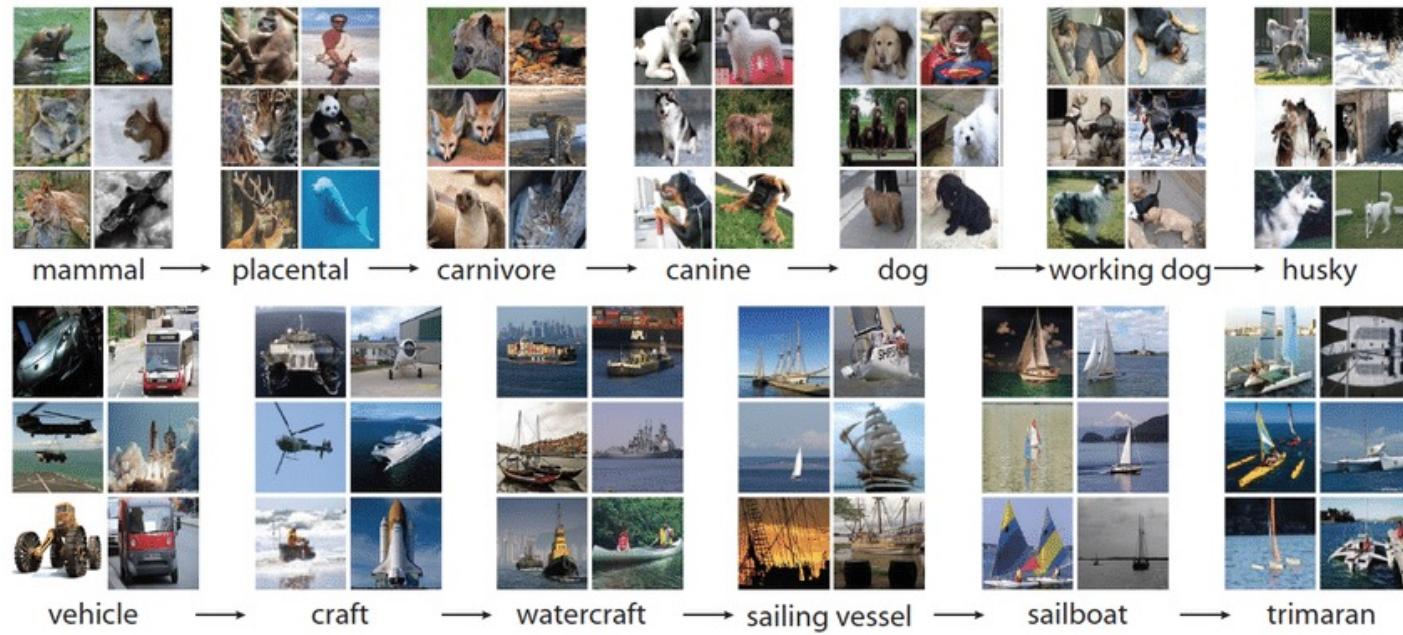
Leaderboard

Dataset



# Pre-trained Models

- Training a model on ImageNet (14m+ annotated images) from scratch takes **days or weeks**.
- Many models trained on ImageNet and their weights are publicly available



# ImageNet & Pre-trained Models

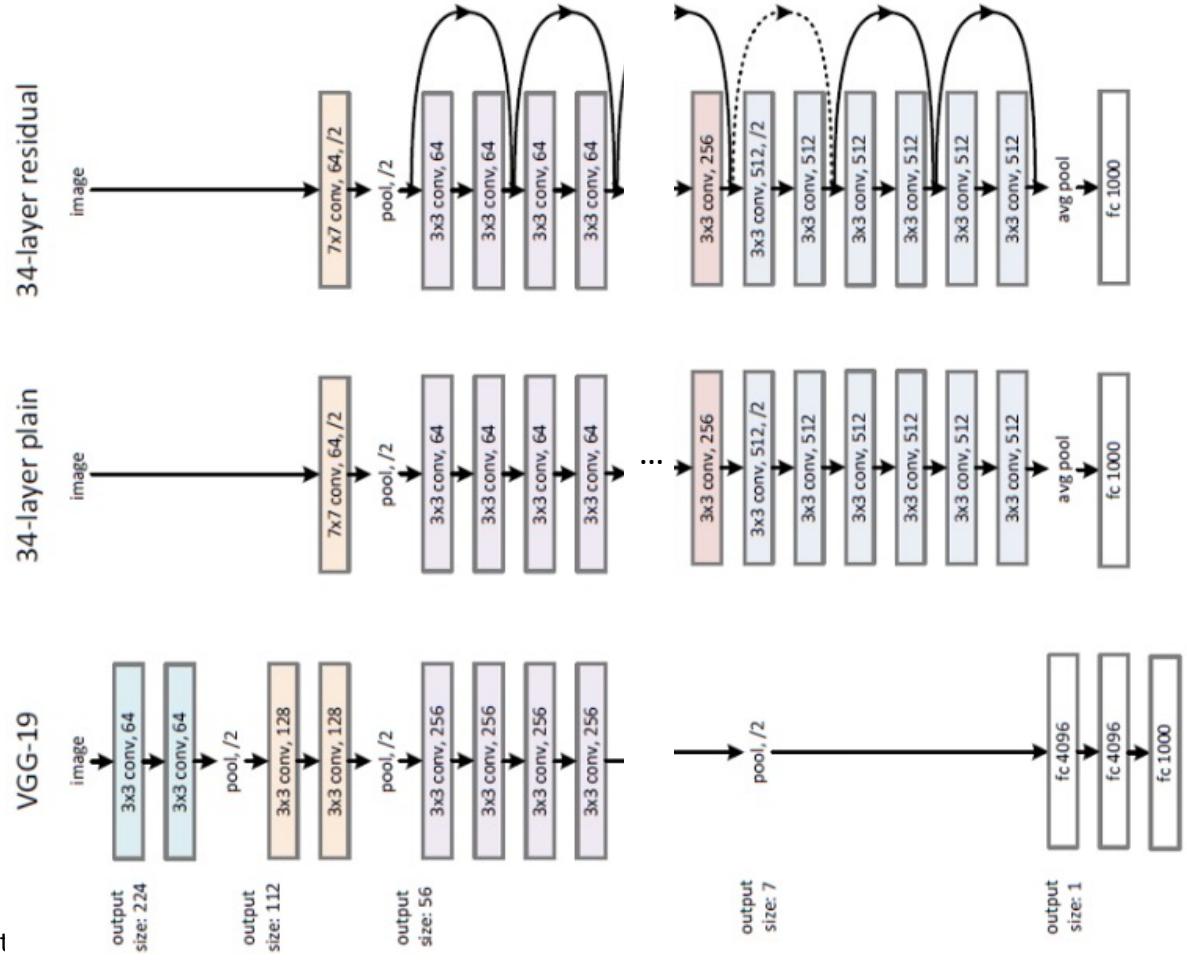
- Many models trained on ImageNet and their weights are publicly available
- Transfer learning
  - Use pre-trained weights, **remove last layers** to compute representations of images
  - Train a classification model from these features **on a new classification task**
  - The network is used as a **generic feature extractor**
  - Better than handcrafted feature extraction on natural images

# Fine-tuning Pre-trained Models

- Fine-tuning
  - Retraining the **(some) parameters of the network** (given enough data)
  - Truncate the last layer(s) of the pre-trained network
  - Freeze the remaining layers weights
  - Add a (linear) classifier on top and train it for a few epochs
  - Then fine-tune the whole network or the few deepest layers
  - **Use a smaller learning rate when fine tuning**

# PyTorch Tutorial

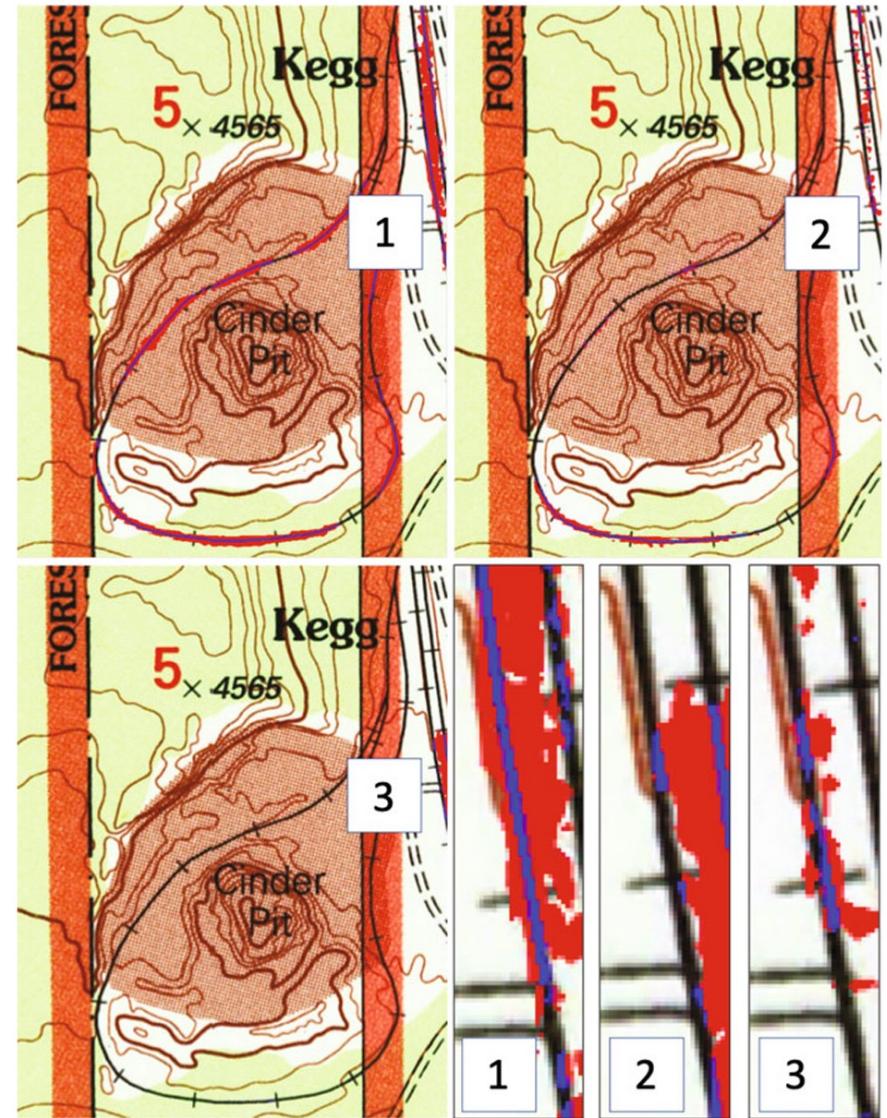
- **Finetuning the convnet:** initialize the network with a pretrained network. Rest of the training looks as usual.
- **ConvNet as fixed feature extractor:** freeze the weights for all of the network **except that of the final fully connected layer.** This last fully connected layer is replaced with a new one with random weights and only this layer is trained.



[https://pytorch.org/tutorials/beginner/transfer\\_learning\\_tutorial.html](https://pytorch.org/tutorials/beginner/transfer_learning_tutorial.html)  
<https://towardsdatascience.com/review-resnet-winner-of-ilsvrc-2015-image-classification-localization-detection-e39402bfa5d8>

# Fine-tuning Example

- Semantic segmentation results (overlaying with the test map) using pre-trained PSPNet with large size training data and trained from the shallow (top left), middle (top right), and deep layers (bottom left) (FP in red and TP in blue)



# Bias and Ethical Concerns

- Neural networks are great approximators
  - You get what you trained with
- Training data can have bias
- Model can have bias
- Applications can discriminate against certain populations
  - “In July 2020, the National Institute of Standards and Technology (NIST) conducted independent assessments to confirm these results. It reported that facial recognition technologies for 189 algorithms showed racial bias toward women of color. NIST also concluded that even the best facial recognition algorithms studied couldn’t correctly identify a mask-wearing person nearly 50% of the time.”

# CNN Summary

- A powerful neural network architecture for many tasks, especially computer vision
- Reduce the number of parameters (parameter sharing)
- Capture spatial interactions in a neighborhood (i.e., kernel size)
- Capture consistent spatial interactions across the input space (e.g., the input image) – could be a limitation
- Many types of CNN architectures and pretrained models are available
- Models can have bias and ethical concerns should be addressed

# Acknowledgements

- Deep learning slides adapted from <https://m2dsupsdiclass.github.io/lectures-labs/> by Olivier Grisel and Charles Ollion (CC-By 4.0 license)
- Gil, Yolanda (Ed.) Introduction to Computational Thinking and Data Science. Available from <http://www.datascience4all.org>



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