RNA-Seq Differential Expression Analysis

Identify patterns that are biologically meaningful

Most common questions asked from RNA-Seq data?

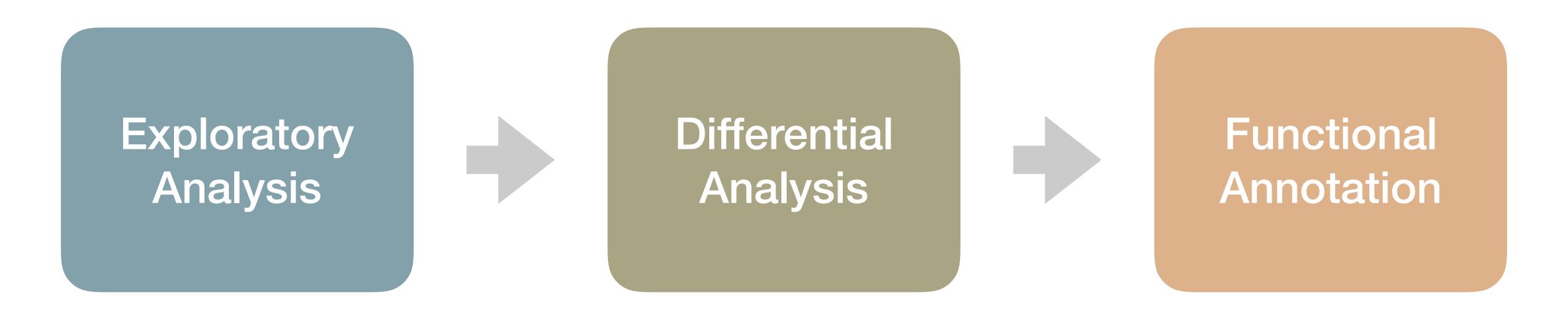
Is there biases affecting the results?

What samples are similar/different?

What genes are differentially over/under-expressed?

What are the functional pathways affected by these genes?

RNA-Seq Differential Expression Analysis Strategy



- Unsupervised analysis
- Do not test hypothesis
- Use to discover biases and unexpected variability

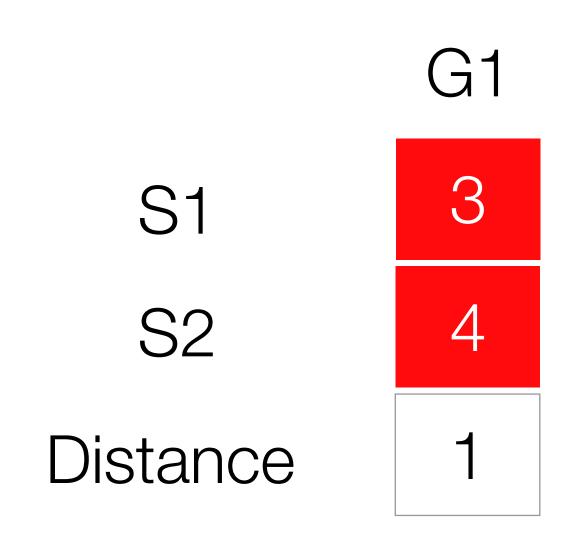
- Guided analysis
- Test experimental hypothesis
- Identify important
- features/genes

- Interpret the biology
- Find molecular functions or pathway affected by different conditions

Exploratory Analysis

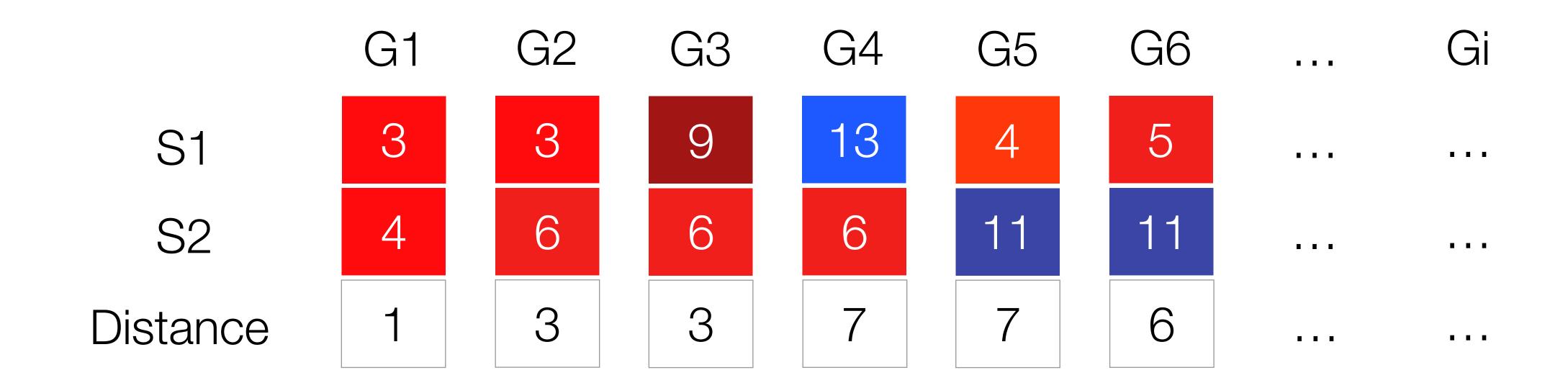
Discover sample groups from global gene expression pattern without prior knowledge

How similar are the samples?



How to quantitatively measure how similar are two samples?

How similar are the samples?



How to quantitatively measure how similar are two samples?

Distance between samples

Euclidean distance:

$$d(q, p) = \sqrt{\sum_{n=0}^{i} (q_i - p_i)^2}$$

Pearson's distance:

$$d(q,p) = 1 - \rho_{q,p}$$



 $d(p,q)^2 = (q_1 - p_1)^2 + (q_2 - p_2)^2$

Where $\rho_{q,p}$ is Pearson correlation coefficient between q, p

Distance between samples

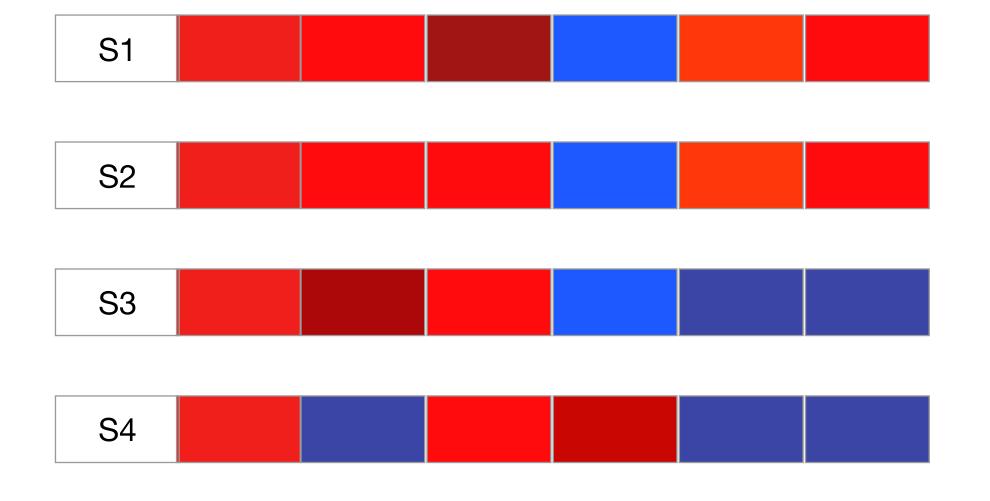


Euclidean distance:

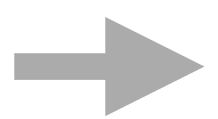
$$d(S1,S2) = \sqrt{\sum_{i=0}^{i} (S1_i - S2_i)^2} = \sqrt{1^2 + 3^2 + 3^2 + 7^2 + 7^2 + 6^2} = 76.5$$

Distance between samples

Gene Expression



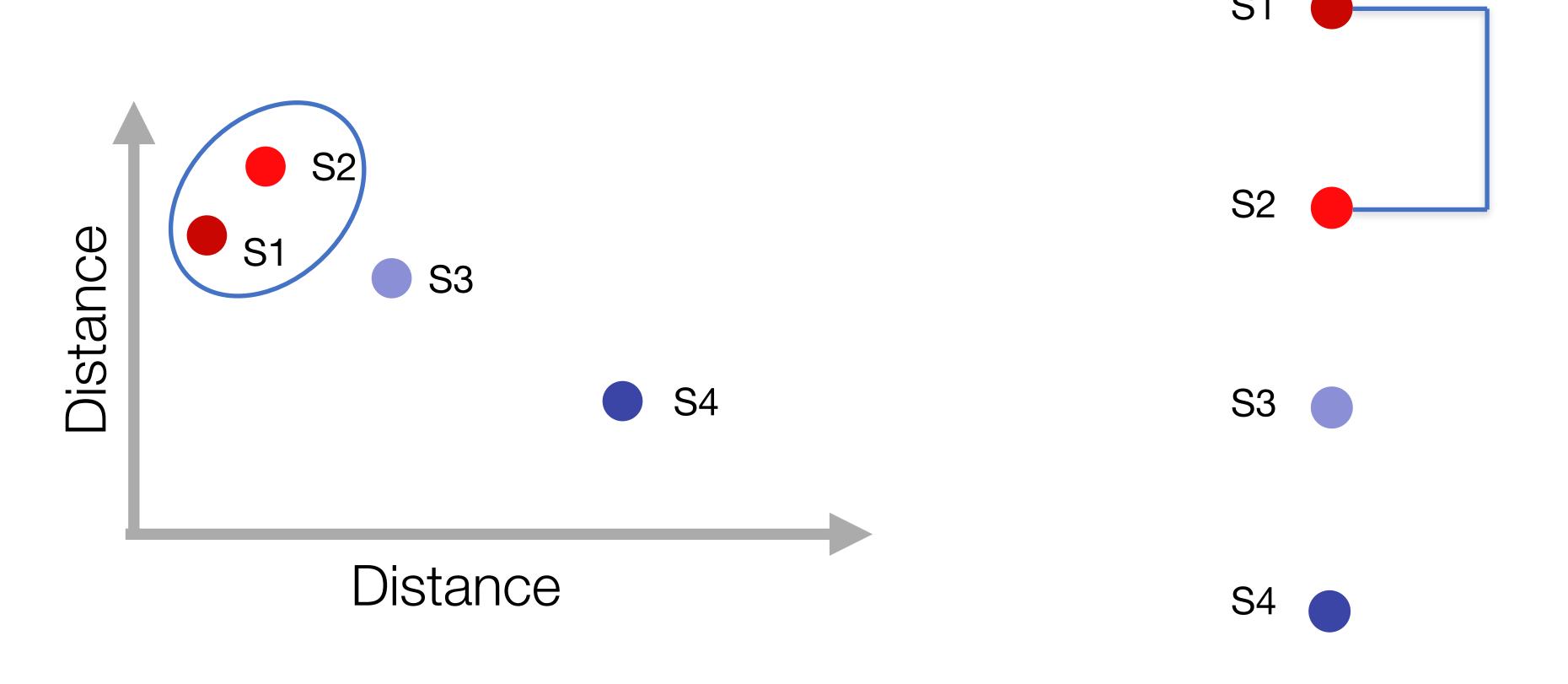
Compute pairwise distances

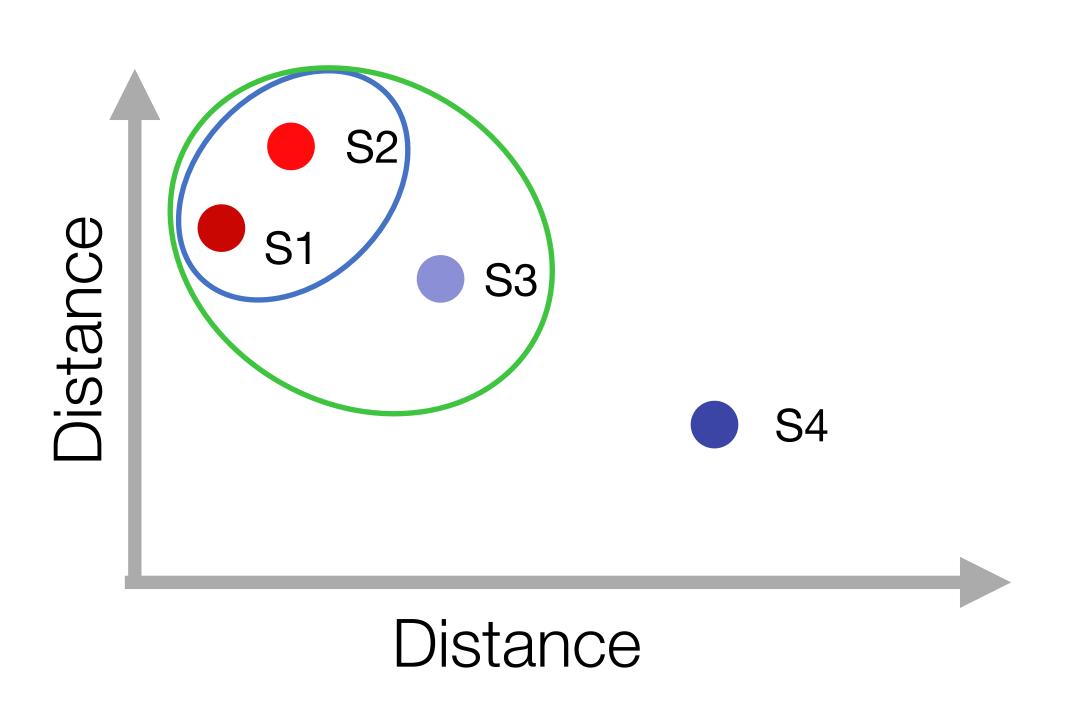


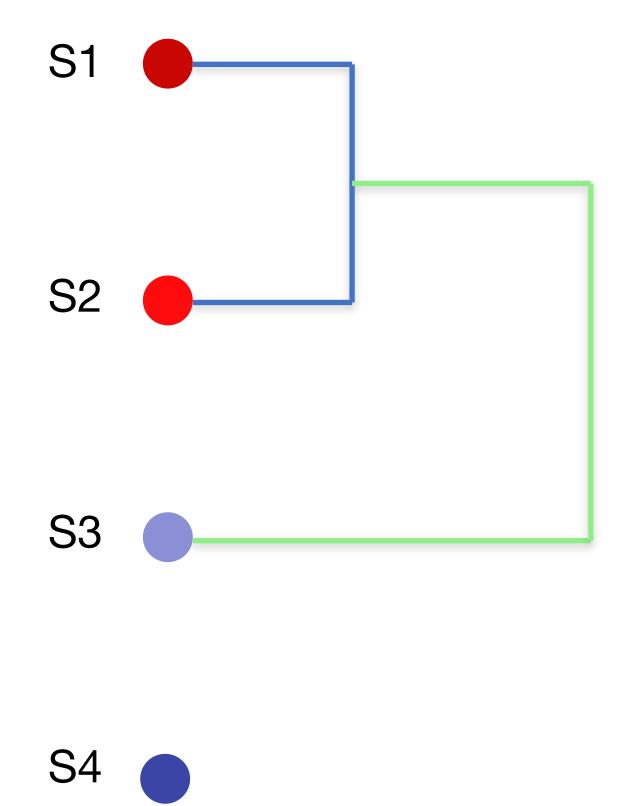
	S1	S2	S 3	S 4
S1	0	76	120	220
S2	76	0	96	198
S 3	120	96	0	132
S 4	220	198	132	0

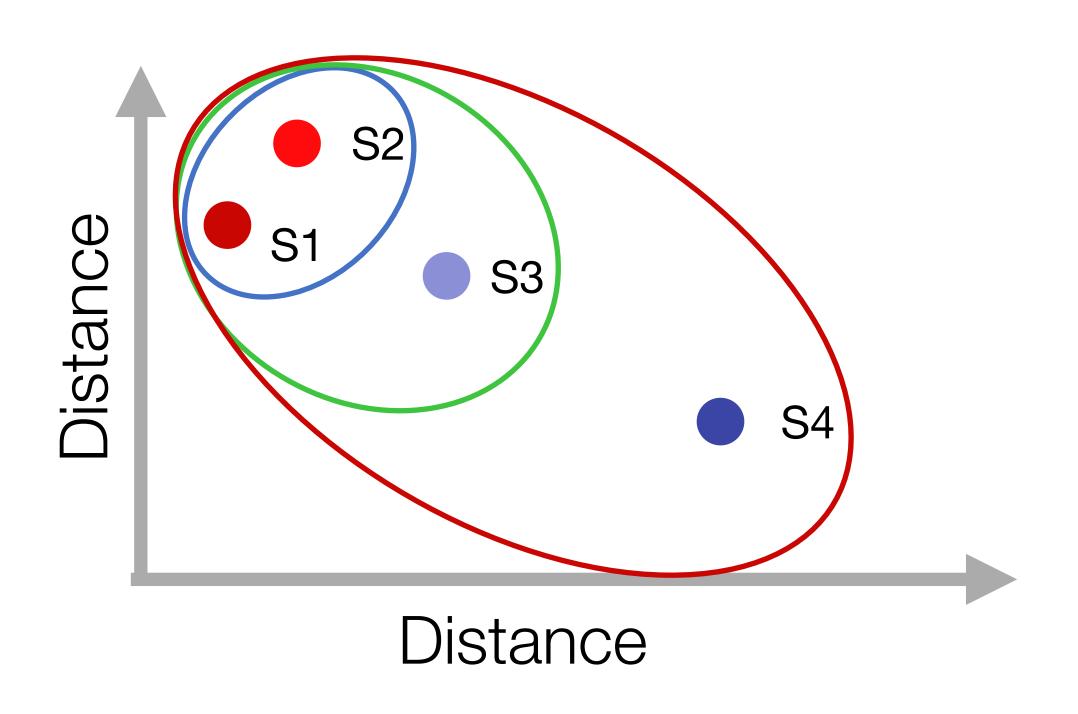
Similarity Distance Matrix

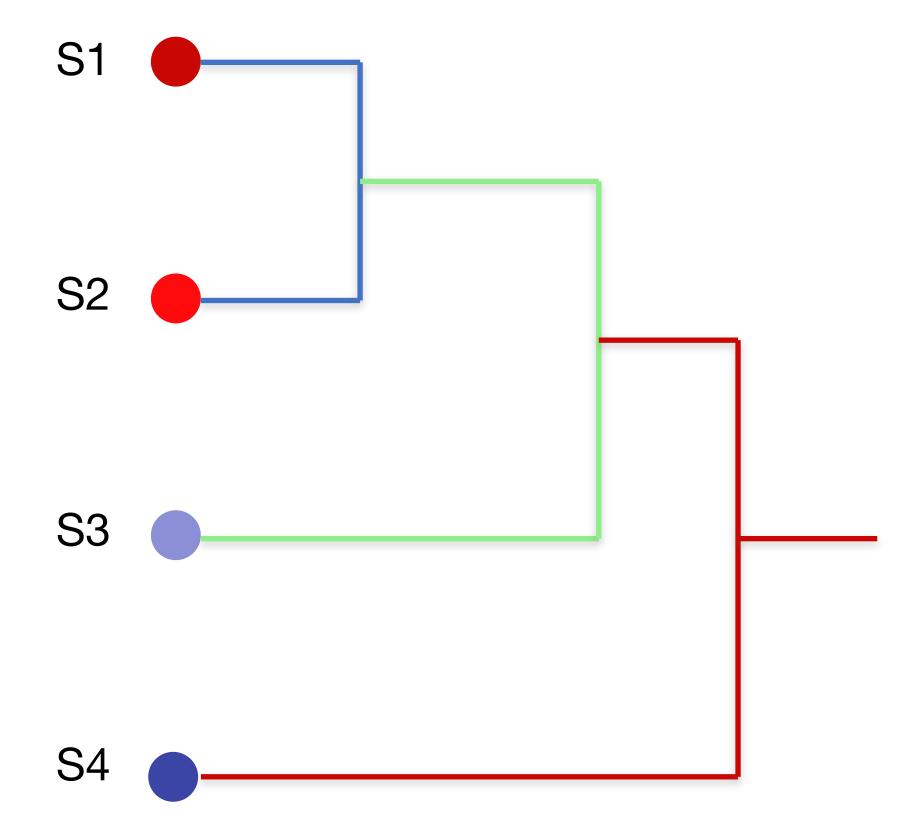




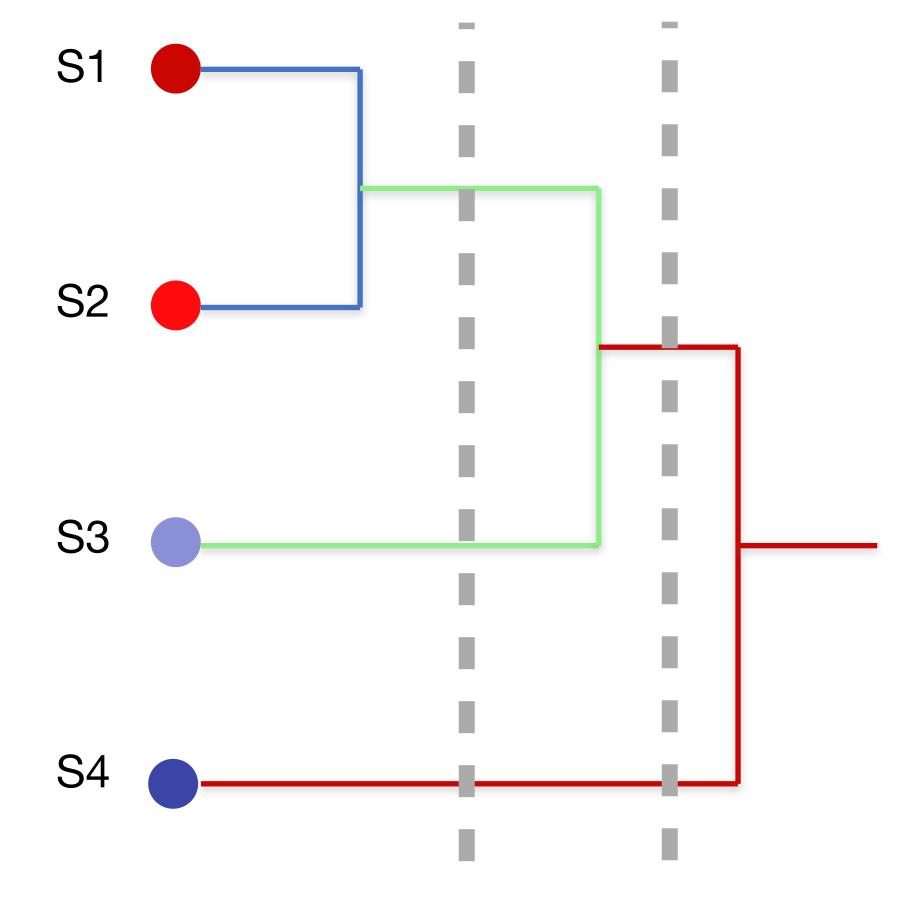






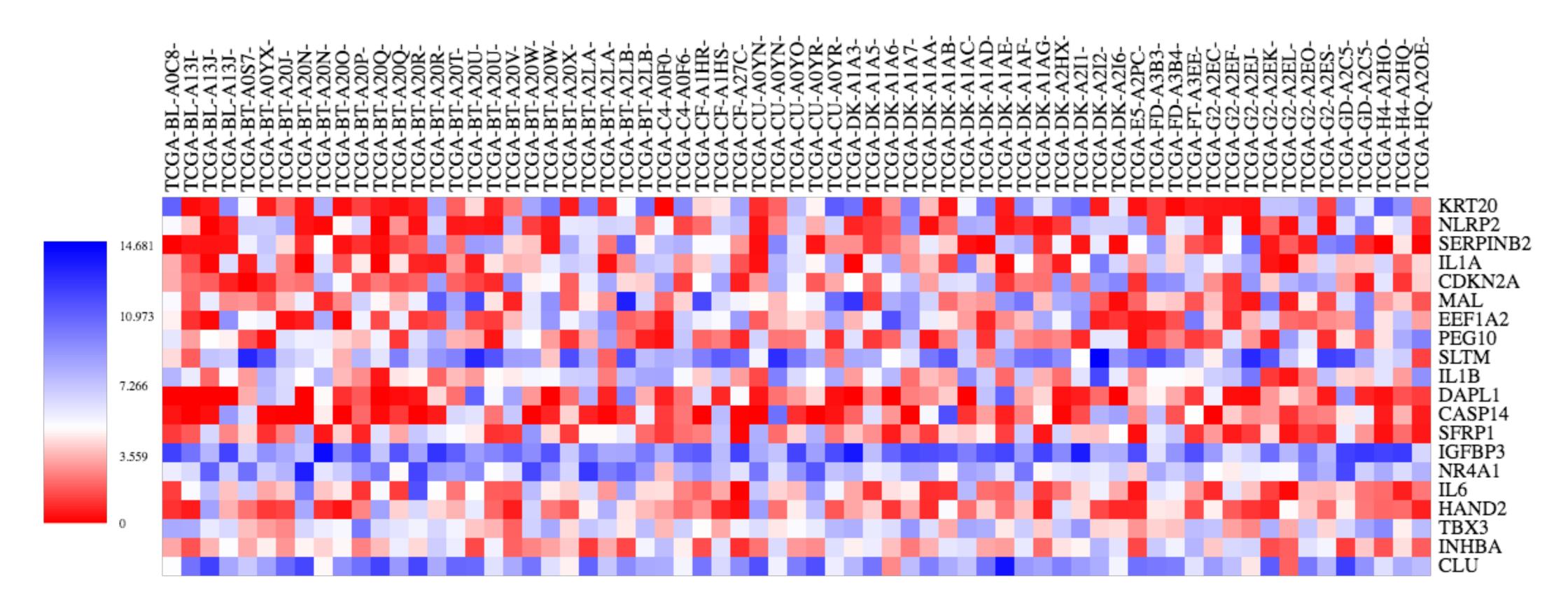


- Determine pairwise distance between all samples with each sample being its own cluster
- Connect closest pair of cluster until there is only one
- Cutting the dendrogram at a desired level to obtain desired number of clusters



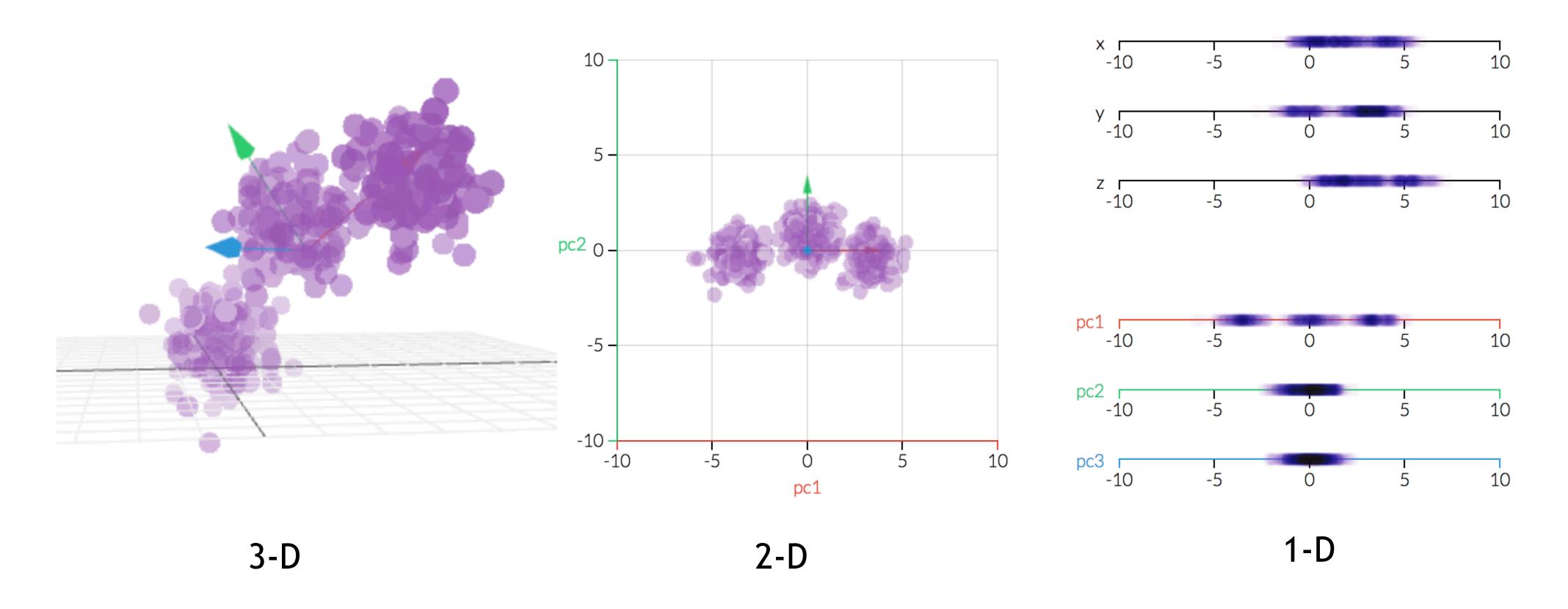
Feature Reduction Technique

Goal: Reduce the dataset to fewer dimensions yet approx. preserve the distance between the individual samples

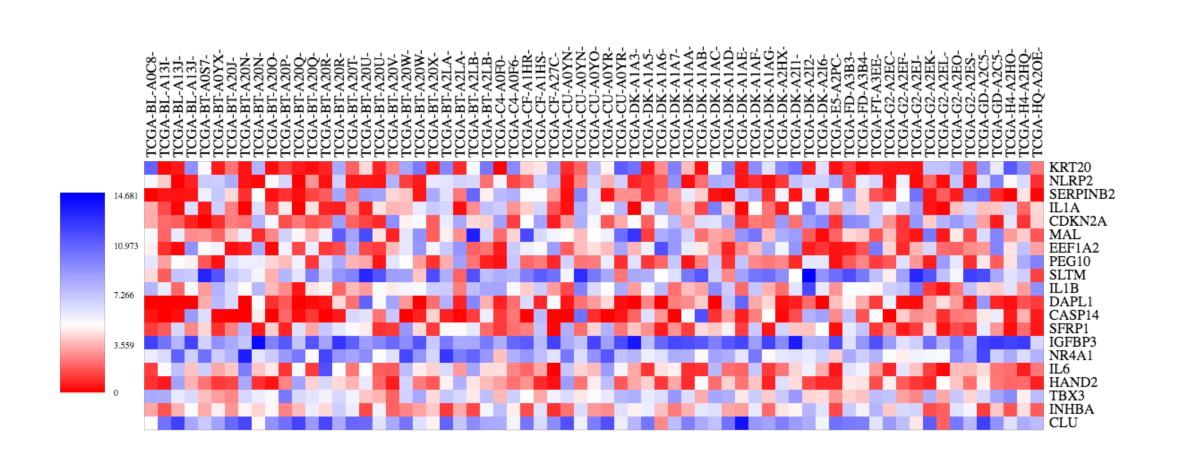


Feature Reduction Technique

Principle Component Analysis (PCA) convert a set of observations of possibly correlated variables into a set of linearly uncorrelated variables (Principle Component or PC's)



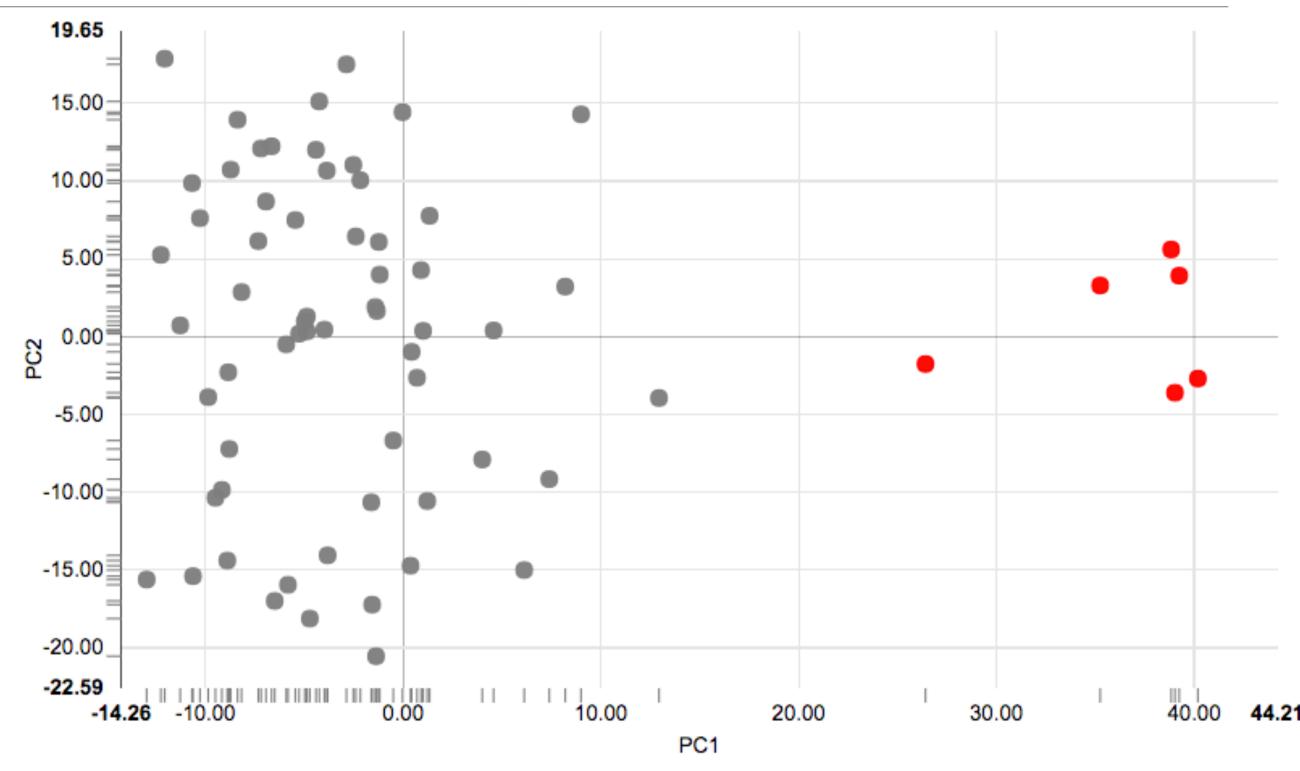
Principle Component Analysis and Visualization



starting point: matrix with expression values per gene and sample, e.g. 22,100 genes x 67 samples



- 22,100 Principle components x 67 Samples
- PC1-3 usually sufficient to capture the major trend

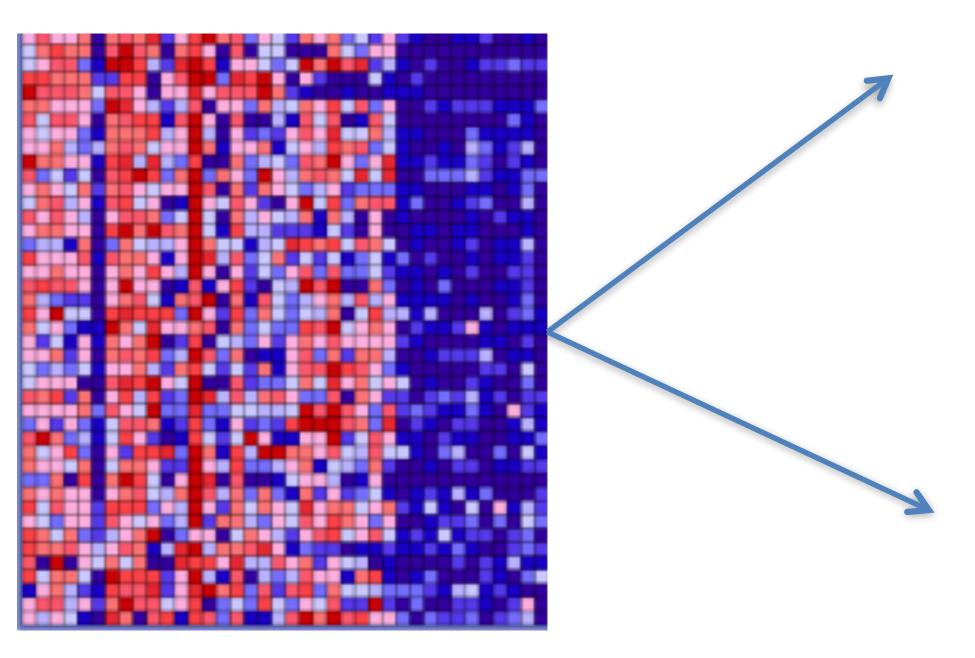


Selected	PC1	PC2
TCGA-BL-A13J-11A-13R-A10U-07	39.2507	3.9165
TCGA-BT-A20N-11A-11R-A14Y-07	40.1933	-2.6946
TCGA-BT-A20Q-11A-11R-A14Y-07	38.8414	5.5994
TCGA-BT-A20R-11A-11R-A16R-07	39.0328	-3.6043
TCGA-CU-A0YN-11A-11R-A10U-07	35.2515	3.2868
TCGA-CU-A0YR-11A-13R-A10U-07	26.4164	-1.7572

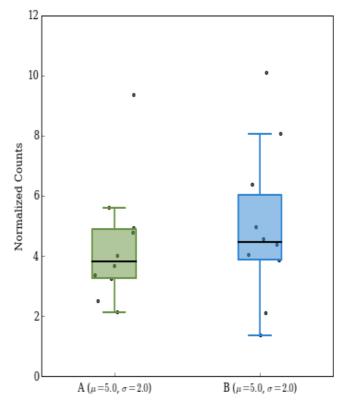
Differential gene expression analysis

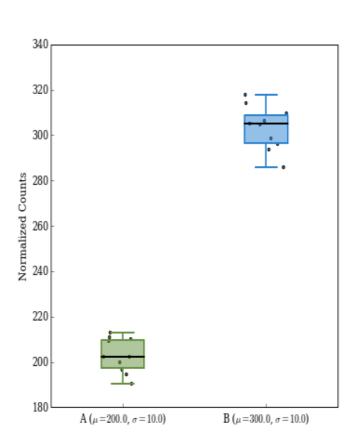
Identify genes with statistically significant expression differences between samples of different conditions

Modeling for Differential Gene Expression



1 test per gene!!!



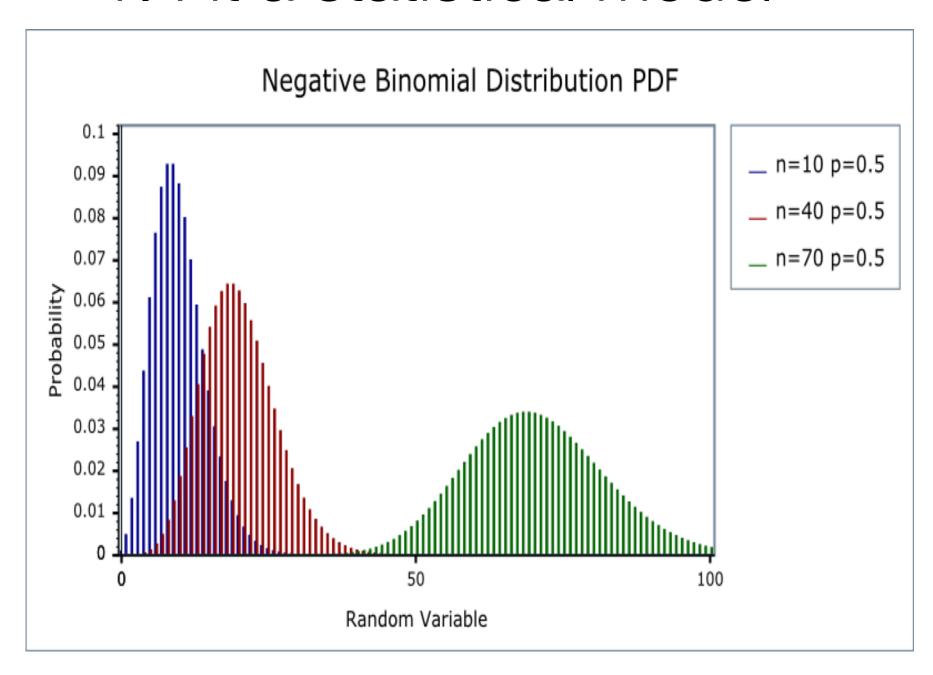


- 1. Estimate magnitude of DGE
 - Report as LogFC (log fold change)
- 2. Estimate the significance of
 - (adjusted) p-values that account for performing thousands of tests

H0: no difference in the read distribution between

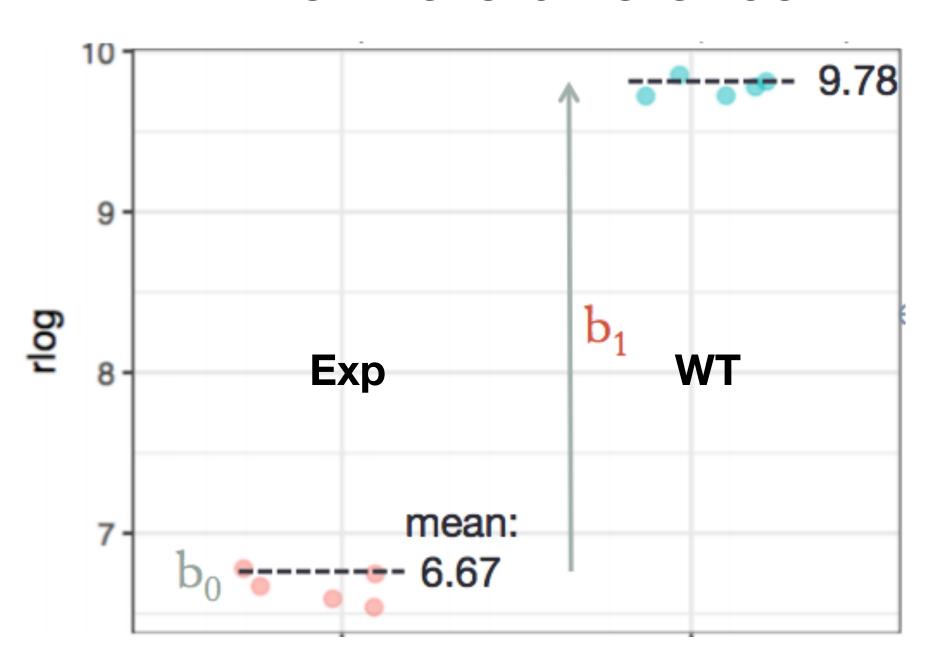
Modeling for Differential Gene Expression

1. Fit a statistical model



Empirically fit a distribution to estimate read count properties by negative binomial distribution

2. Estimate difference



Estimate the difference between groups using a linear model

$$Y = b_0 + b_1 * x + e$$

DGE Results

Gene	baseMean	baseMeanA	baseMeanB	foldChange	log2FC	pval	padj
FTL2	94.324	2.319	186.329	80.318	6.327	7.97E-44	2.89E-40
REC8	120.143	229.661	10.626	0.0462	-4.433	4.05E-38	9.32E-35
DLK2	626.928	1026.15	227.706	0.221	-2.171	1.18E-18	1.87E-15
• • •	• • •	• • •	• • •	• • •	• • •	• • •	• • •
PDE6b	430.808	301.37	560.239	1.858	0.894	0.328	0.765
LEPREL4	495.854	532.61	459.092	0.862	-0.214	0.328	0.765
NLRP12	4.009	5.466	2.535	0.463	-1.108	0.329	0.766

Commonly used methods DESeq2, edgeR, limma all produce results in similar format

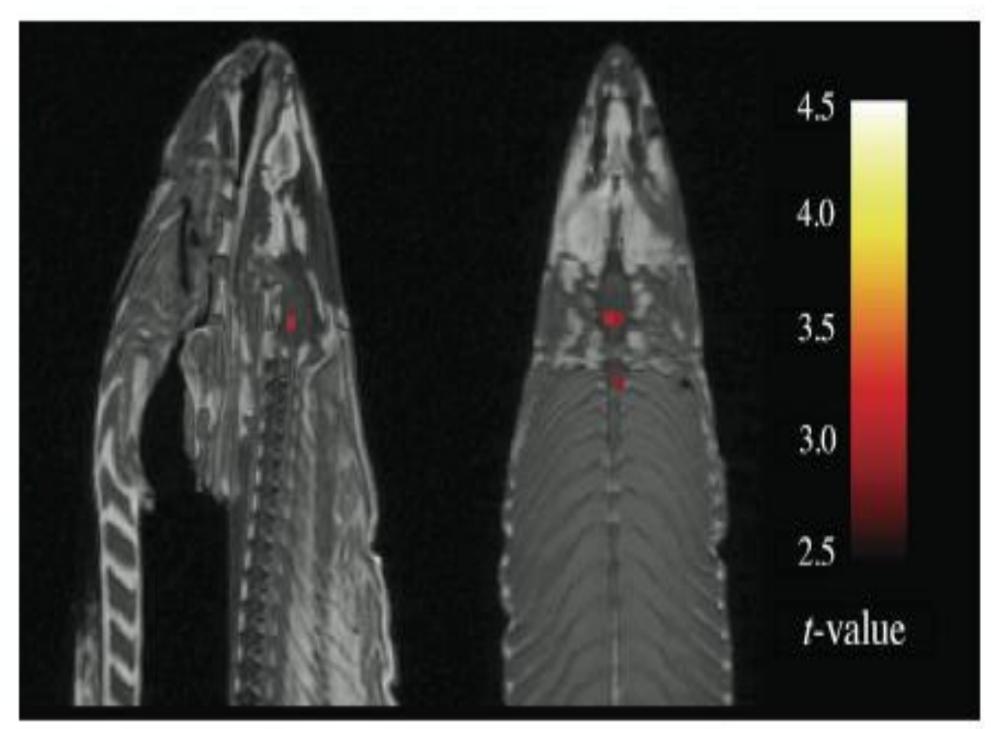
Controlling false-positives by multiple comparisons

- When the same question is asked thousands of times, some will show up as significant by random
- Most commonly used method for RNASeq is False Discovery Rate (FDR) by Benjamini-Hochberg

$$FDR = Q_e = E[V/(V+R)]$$

V = False Positives R = True Positives + False Positives

Ask a dead salmon a series of questions...



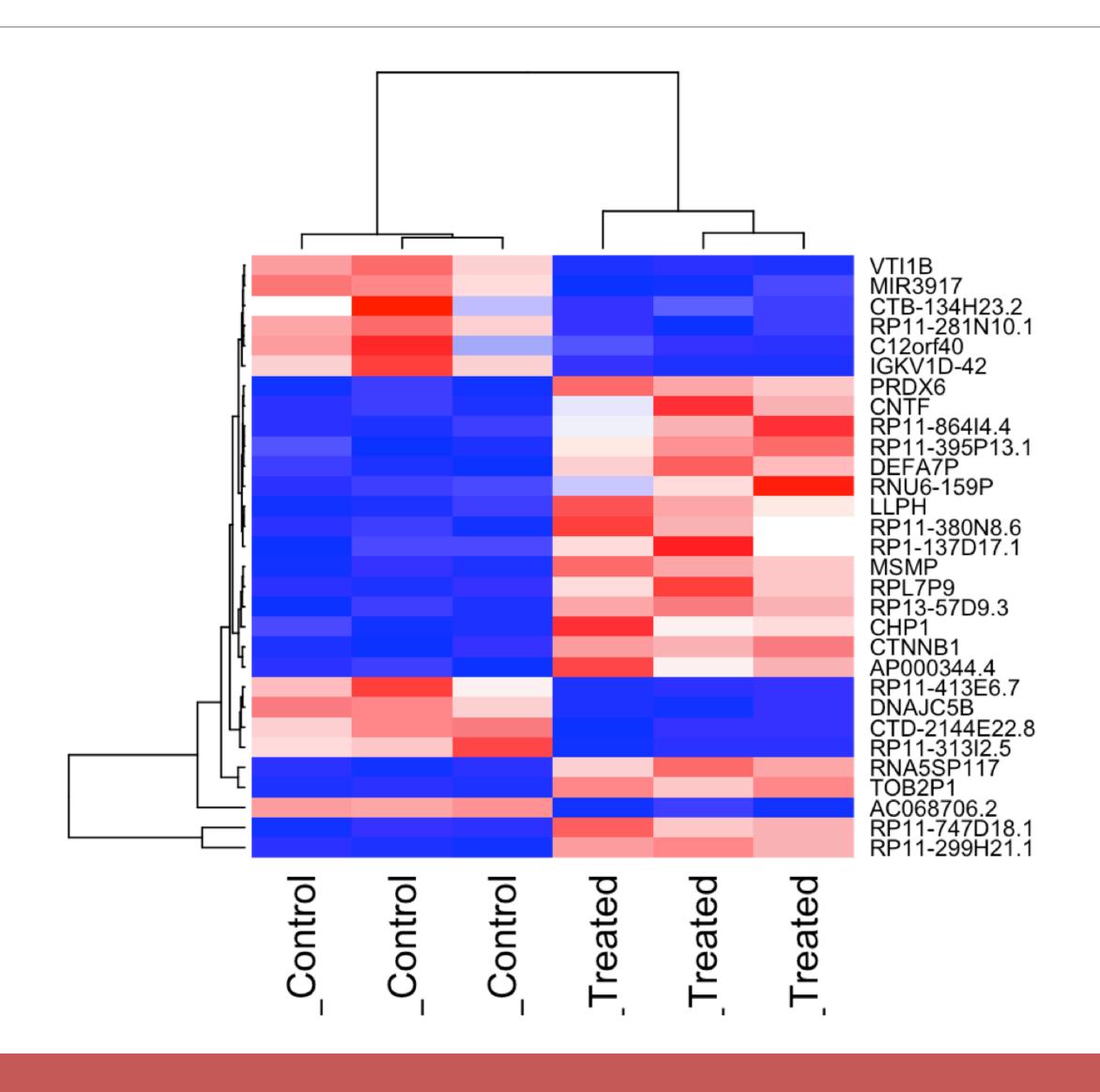
fMRI with many statistical tests performed (just like testing differential expression on many genes!)

DGE Results Examination

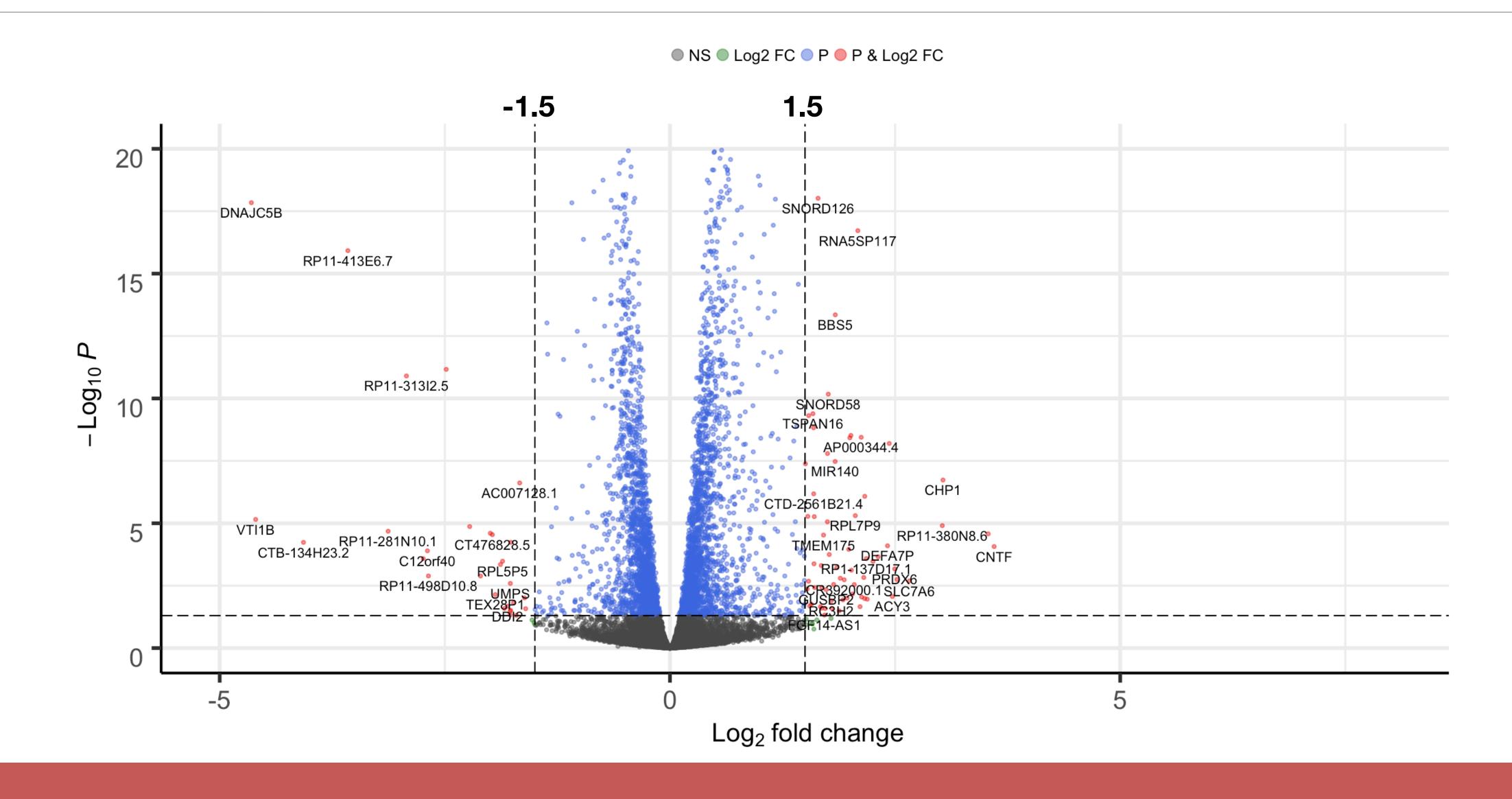
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Filter DGE result table by Log2FC (usually > 1.2) or adjusted P-value

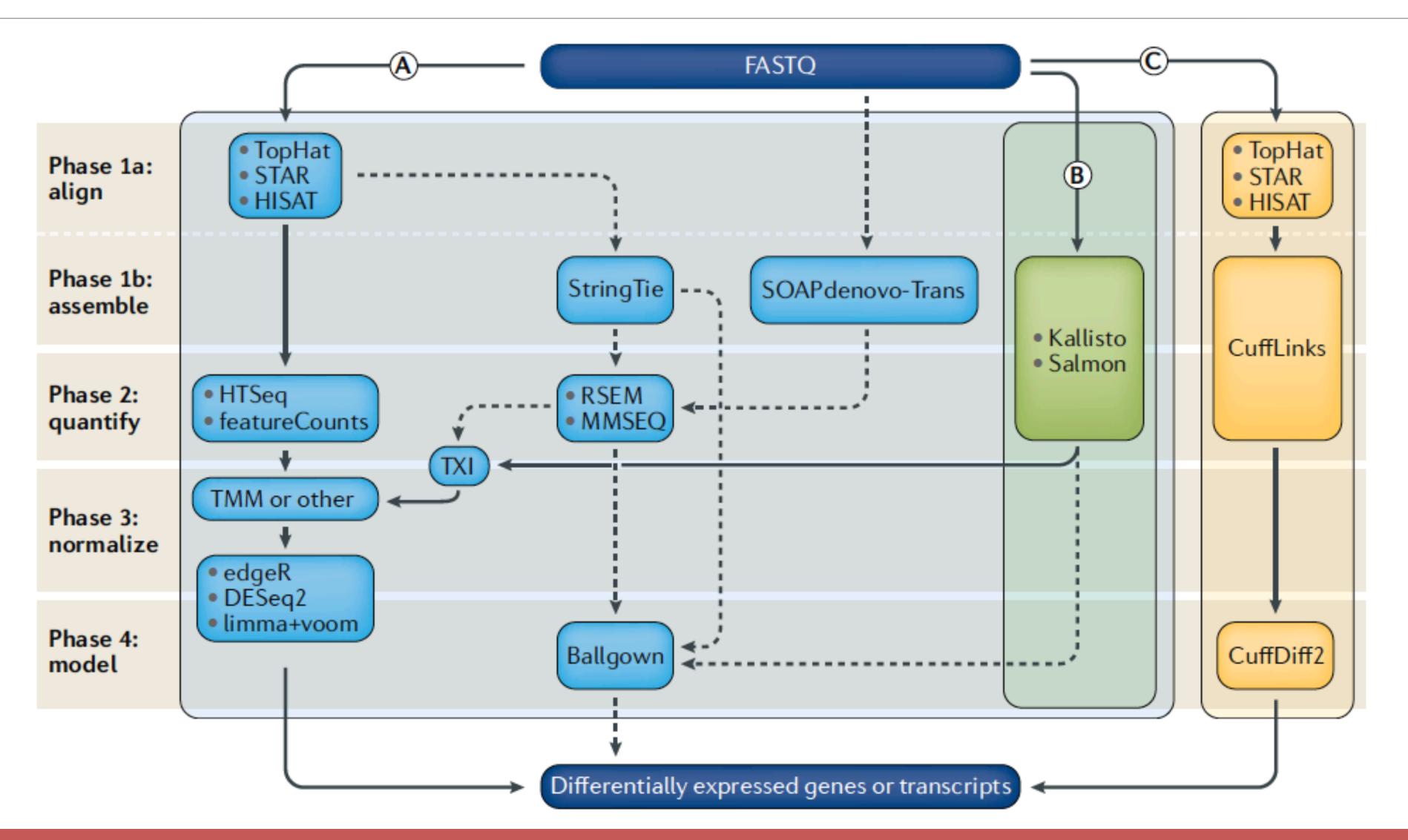
DGE Results: Heatmap



DGE Results - Volcano Plots

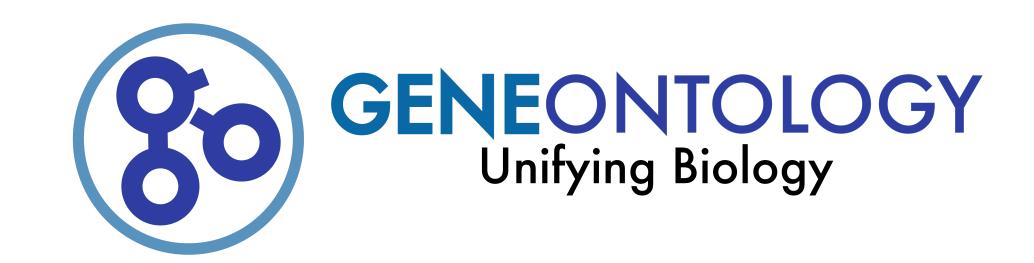


RNA-Seq Workflow Summary



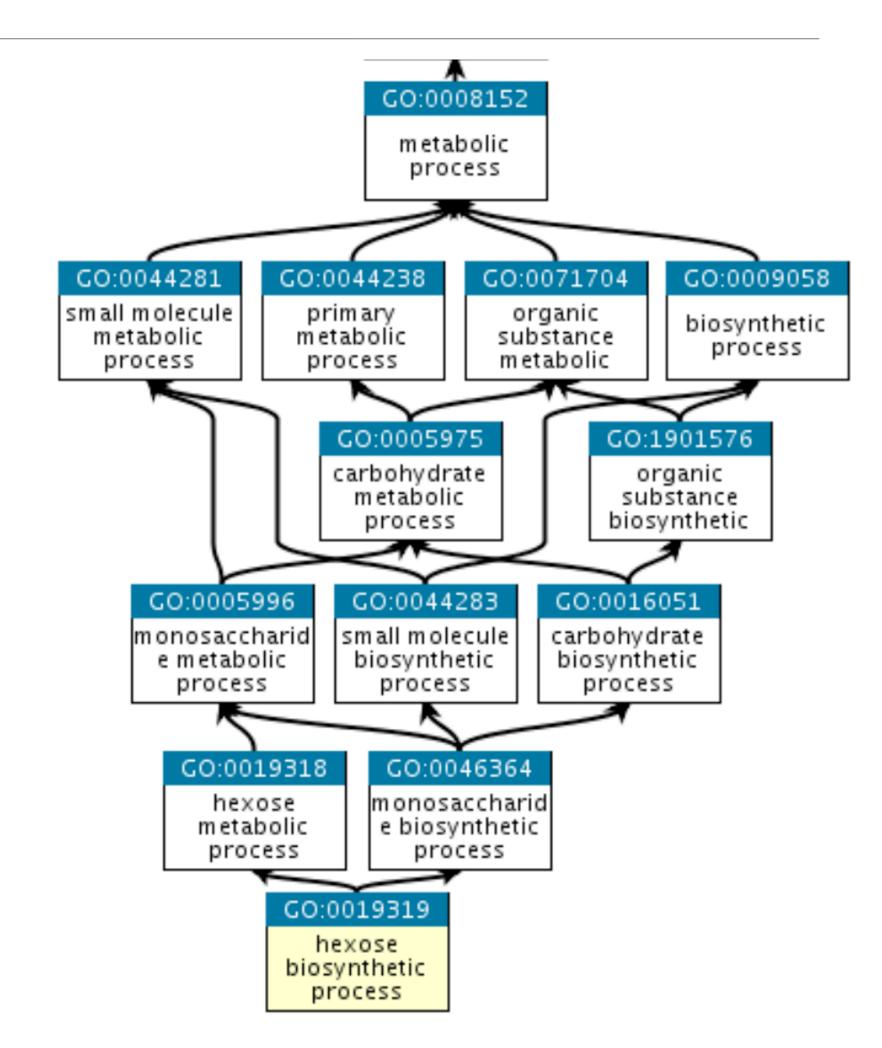
Functional Enrichment Analysis

Putting differential expressed genes into biological context using gene annotation databases



Gene Ontology Database (GO) - terms that group genes into sets of classes by their annotations

- 1. Molecular Function: Molecular-level activities performed by gene products, such as "catalysis" or "transport"
- 2. Cellular Component: The locations relative to cellular structures in which a gene product performs a function (e.g. "mitochondrion", "ribosome")
- 3. Biological Process: The larger processes, or 'biological programs' accomplished by multiple molecular activities (e.g. "DNA repair", "signal transduction")



Loosely hierarchical GO Term structure



The Molecular Signatures Database (MSigDB) is a collection of annotated gene sets

- Curated Gene Sets from literatures, such as functional pathway (KEGG), gene functional groups. Most commonly used gene set class
- · Contain domain specific gene sets (H, C6, C7)
- Human genome location (C1) Predicted gene sets (C2, C4)
- GO term (C5)



hallmark gene sets are coherently expressed signatures derived by aggregating many MSigDB gene sets to represent well-defined biological states or processes.

positional gene sets for each human chromosome and cytogenetic band.

curated gene sets from online pathway databases, publications in PubMed, and knowledge of domain experts.

motif gene sets based on conserved cis-regulatory motifs from a comparative analysis of the human, mouse, rat, and dog genomes.

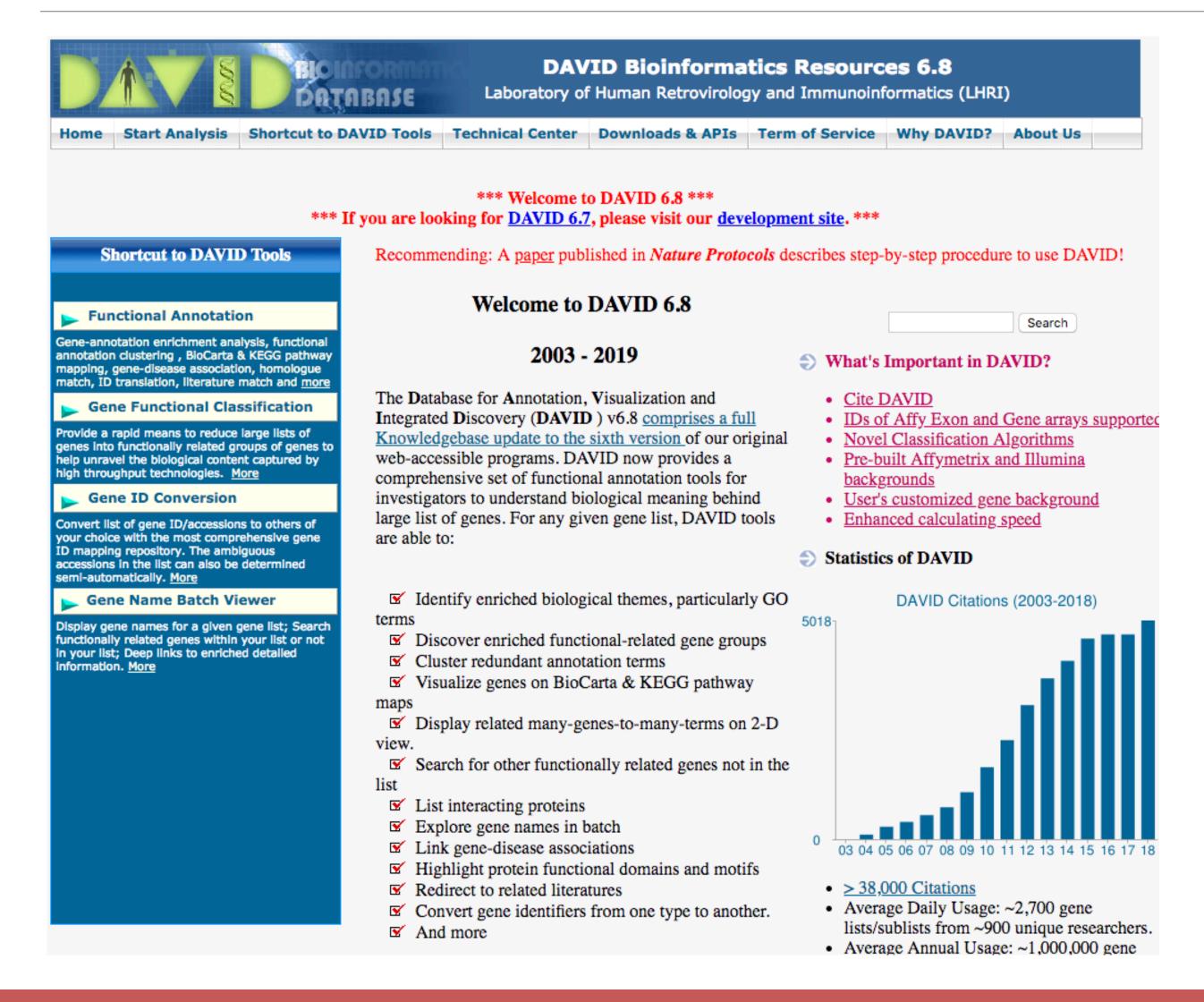
computational gene sets defined by mining large collections of cancer-oriented microarray data.

C5 GO gene sets consist of genes annotated by the same GO terms.

oncogenic gene sets defined directly from microarray gene expression data from cancer gene perturbations.

microarray gene expression data from immunologic studies.

Functional Enrichment Analysis with DAVID



Use a modified **Fisher Exact Test** to determine if there is enrichment

Confusion Matrix	Number of genes is DGE	Number of genes is not DGE		
Number of genes in pathway <i>y</i>	76	20		
Number of genes not in pathway <i>y</i>	2	29920		

p<0.0001!!!

Conclusion: Pathway y is differentially regulated



Detecting modest but coordinate changes

The goal of GSEA is to detect modest but coordinated changes in pre-specified sets of related genes by using all genes and their statistical variation values

Step 0: Sort Genes into a ranked gene list

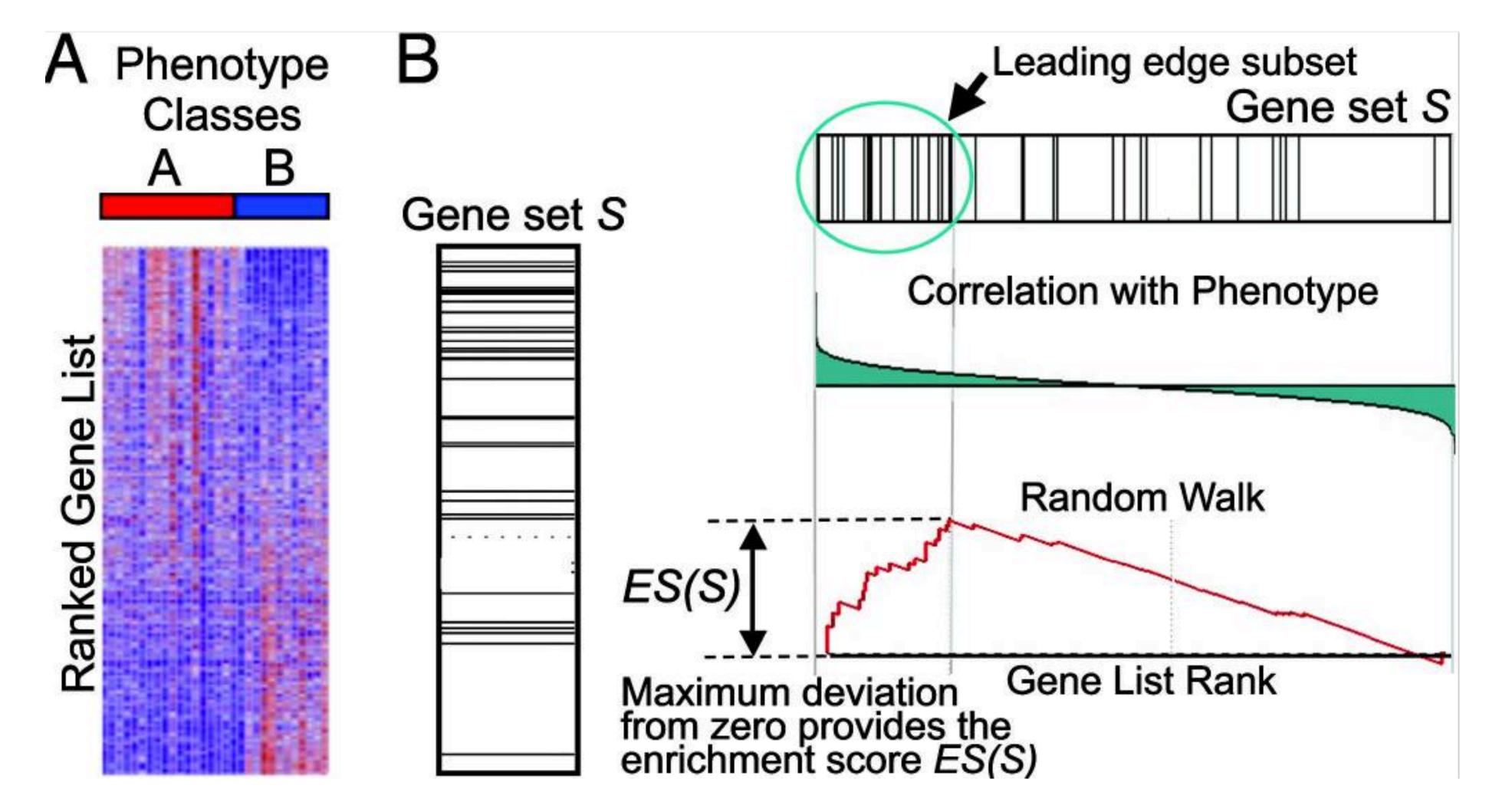
Step 1: Calculate Enrichment Score: Compute cumulative sum over ranked genes by summing statistics of gene in a set, and subtracting statistics of genes outside of the set

Step 2: Assess significance using Permutation Test: permute sample phenotype labels

Step 3: Adjust for multiple hypothesis testing: using FDR correction



Detecting modest but coordinate changes



RNA-Seq Analysis Road Map

