

# SLICING

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We've used slicing in this course before, but now it's time to dive deeper into slicing

Slicing relies on indexing → only works with **sequence types**

**Mutable Sequence Types**

extract data

**assign** data

**Immutable Sequence Types**

extract data

**Example**

```
l = [1, 2, 3, 4, 5]
```

```
l[0:2] → [1, 2]
```

```
l[0:2] = ('a', 'b', 'c')
```

```
l[0:2] → ['a', 'b', 'c', 3, 4, 5]
```



## The Slice Type

Although we usually slice sequences using the more conventional notation:

```
my_list[i:j]
```

slice definitions are actually **objects** → of type **slice**

```
s = slice(0, 2)
```

```
type(s) → slice
```

```
s.start → 0
```

```
s.end → 2
```

```
l = [1, 2, 3, 4, 5]
```

```
l[s] → [1, 2]
```

This can be useful because we can **name** slices and use symbols instead of a literal subsequently

Similar to how you can name ranges in Excel...



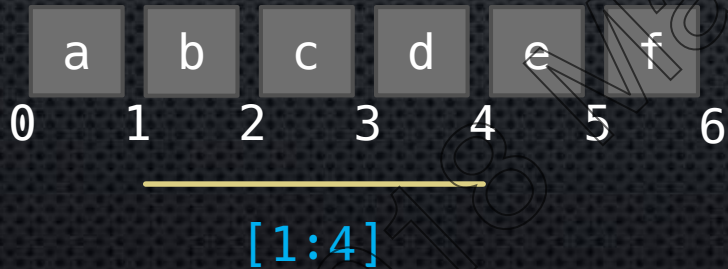
## Slice Start and Stop Bounds

`[i:j]` start at `i` (including `i`) stop at `j` (excluding `j`)

all integers `k` where `i <= k < j`

also remember that indexing is zero-based

It can be convenient to think of slice bounds this way





## Effective Start and Stop Bounds

Interestingly the following works:

```
l = ['a', 'b', 'c', 'd', 'e', 'f']
```

```
l[3:100] → ['d', 'e', 'f']
```

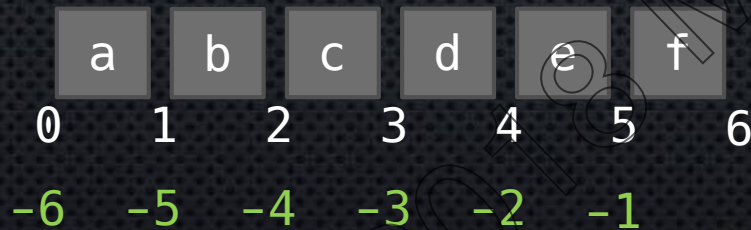
 No error!

we can specify slices that are "out of bounds"

In fact, negative indices work too:

```
l[-1] → 'f'
```

```
l[-3:-1] → ['d', 'e']
```





## Step Value

Slices also support a third argument – the **step** value

`[i:j:k]`

(a.k.a stride)

`slice(i, j, k)`

When not specified, the step value defaults to **1**

```
l = ['a', 'b', 'c', 'd', 'e', 'f']
    0  1  2  3  4  5
   -6 -5 -4 -3 -2 -1
```

`l[0:6:2]`      `0, 2, 4`       $\rightarrow$  `['a', 'c', 'e']`

`l[1:6:3]`      `1, 4`       $\rightarrow$  `['b', 'e']`

`l[1:15:3]`      `1, 4`       $\rightarrow$  `['b', 'e']`

`l[-1:-4:-1]`      `-1, -2, -3`       $\rightarrow$  `['f', 'e', 'd']`



## Range Equivalence

Any slice essentially defines a sequence of indices that is used to select elements for another sequence

In fact, any indices defined by a slice can also be defined using a **range**

The difference is that slices are defined **independently** of the sequence being sliced

The **equivalent range** is only **calculated** once the **length** of the sequence being sliced is known

### Example

<code>[0:100]</code>	↳ sequence of length 10	→ <code>range(0, 10)</code>
	↳ sequence of length 6	→ <code>range(0, 6)</code>



## Transformations `[i:j]`

The effective indices "generated" by a slice are actually dependent on the length of the sequence being sliced

Python does this by reducing the slice using the following rules:

`seq[i:j]`

`l = ['a', 'b', 'c', 'd', 'e', 'f']`  
0 1 2 3 4 5  
-6 -5 -4 -3 -2 -1

length = 6

if `i > len(seq)` → `len(seq)`

`[0:100]` → `range(0, 6)`

if `j > len(seq)` → `len(seq)`

if `i < 0` → `max(0, len(seq) + i)`

`[-10:3]` → `range(0, 3)`

if `j < 0` → `max(0, len(seq) + j)`

`[-5:3]` → `range(1, 3)`

`i` omitted or `None` → `0`

`[:100]` → `range(0, 6)`

`j` omitted or `None` → `len(seq)`

`[3:]` → `range(3, 6)`

`[:]` → `range(0, 6)`



## Transformations $[i:j:k]$ , $k > 0$

With extended slicing things change depending on whether  $k$  is negative or positive

$$[i:j:k] = \{x = i + n * k \mid 0 \leq n < (j-i)/k\}$$

$k > 0$  the indices are:  $i, i+k, i+2k, i+3k, \dots, < j$  stopping when  $j$  is reached or exceeded, but never including  $j$  itself

$l = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ ['a', & 'b', & 'c', & 'd', & 'e', & 'f'] \\ -6 & -5 & -4 & -3 & -2 & -1 \end{matrix}$

length = 6

if  $i, j > \text{len}(\text{seq}) \rightarrow \text{len}(\text{seq})$

$[0:100:2] \rightarrow \text{range}(0, 6, 2)$

if  $i, j < 0 \rightarrow \max(0, \text{len}(\text{seq}) + i/j)$

$[-10:100:2] \rightarrow \text{range}(0, 6, 2)$

$[-5:100:2] \rightarrow \text{range}(1, 6, 2)$

$i$  omitted or `None`  $\rightarrow 0$

$[ :6:2 ] \rightarrow \text{range}(0, 6, 2)$

$j$  omitted or `None`  $\rightarrow \text{len}(\text{seq})$

$[1::2] \rightarrow \text{range}(1, 6, 2)$

$[::2] \rightarrow \text{range}(0, 6, 2)$

so same rules as  $[i:j]$  – makes sense, since that would be the same as  $[i:j:1]$



Transformations  $[i:j:k]$ ,  $k < 0$

$[i:j:k] = \{x = i + n * k \mid 0 \leq n < (j-i)/k\}$

$k < 0$  the indices are:  $i, i+k, i+2k, i+3k, \dots, > j$

$l = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ ['a', & 'b', & 'c', & 'd', & 'e', & 'f'] \\ -6 & -5 & -4 & -3 & -2 & -1 \end{matrix}$

length = 6

if  $i, j > \text{len}(\text{seq}) \rightarrow \text{len}(\text{seq}) - 1$

$[5:2:-1] \rightarrow \text{range}(5, 2, -1)$

$[10:2:-1] \rightarrow \text{range}(5, 2, -1)$

if  $i, j < 0 \rightarrow \max(-1, \text{len}(\text{seq}) + i/j)$

$[5:-2:-1] \rightarrow \text{range}(5, 4, -1)$

$[-2:-5:-1] \rightarrow \text{range}(4, 1, -1)$

$[-2:-10:-1] \rightarrow \text{range}(4, -1, -1)$

$i$  omitted or `None`  $\rightarrow \text{len}(\text{seq}) - 1$

$[:-2:-1] \rightarrow \text{range}(5, 4, -1)$

$j$  omitted or `None`  $\rightarrow -1$

$[5::-1] \rightarrow \text{range}(5, -1, -1)$

$:::-1] \rightarrow \text{range}(5, -1, -1)$



## Summary

`[i:j]`    `[i:j:k]`     $k > 0$

`[i:j:k]`     $k < 0$

$i > \text{len}(\text{seq})$

$\text{len}(\text{seq})$

$\text{len}(\text{seq})-1$

$j > \text{len}(\text{seq})$

$\text{len}(\text{seq})$

$\text{len}(\text{seq})-1$

$i < 0$

$\max(0, \text{len}(\text{seq})+i)$

$\max(-1, \text{len}(\text{seq})+i)$

$j < 0$

$\max(0, \text{len}(\text{seq})+j)$

$\max(-1, \text{len}(\text{seq})+j)$

$i$  omitted / `None`

0

$\text{len}(\text{seq})-1$

$j$  omitted / `None`

$\text{len}(\text{seq})$

-1



## Examples

```
l = ['a', 'b', 'c', 'd', 'e', 'f']  
    0   1   2   3   4   5  
   -6  -5  -4  -3  -2  -1
```

length = 6

```
[-10:10:1]  -10 → 0  
             10 → 6  
             → range(0, 6)
```

```
[10:-10:-1] 10 → 5  
             -10 → max(-1, 6-10) → max(-1, -4) → -1  
             → range(5, -1, -1)
```

We can of course easily define empty slices!

```
[3:-1:-1]   3 → 3  
            -1 → max(-1, 6-1) → 5  
            → range(3, 5, -1)
```



## Example

`seq` = sequence of length 6

`seq[::-1]`

`i` is omitted  $\rightarrow \text{len}(\text{seq}) - 1 \rightarrow 5$

`j` is omitted  $\rightarrow -1$

$\rightarrow \text{range}(5, -1, -1) \rightarrow 5, 4, 3, 2, 1, 0$

`seq = 'python'`

`seq[::-1]  $\rightarrow$  'nohtyp'`



If you get confused...

The `slice` object has a method, `indices`, that returns the equivalent range start/stop/step for any slice given the length of the sequence being sliced:

```
slice(start, stop, step).indices(length) → (start, stop, step)
```

the values in this tuple can be used to generate a list of indices using the `range` function

```
slice(10, -5, -1) with a sequence of length 6
```

```
i=10 > 6 → 6-1 → 5
```

```
j=-5 < 0 → max(-1, 6+-5) → max(-1, 1) → 1 → range(5, 1, -1)  
→ 5, 4, 3, 2
```

```
slice(10, -5, -1).indices(6) → (5, 1, -1)
```

```
list(range(*slice(10,-5,-1).indices(6))) → [5, 4, 3, 2]
```



# Code Exercises

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