ST1131 Introduction to Statistics

- 5.2 Testing a coin Your friend decides to flip a coin repeatedly to analyze whether the probability of a head on each flip is 1/2. He flips the coin 10 times and observes a head 7 times. He concludes that the probability of a head for this coin is 7/10 = 0.70.
 - a. Your friend claims that the coin is not balanced, since the probability is not 0.50. What's wrong with your friend's claim? its not a long run
 - b. If the probability of flipping a head is actually 1/2, what would you have to do to ensure that the cumulative proportion of heads falls very close to 1/2?

flip many times

- 5.6 Random digits Consider a random number generator designed for equally likely outcomes. Which of the following is not correct, and why?
 - a. For each random digit generated, each integer between 0 and 9 has probability 0.10 of being selected.
 - **b.** If you generate 10 random digits, each integer between 0 and 9 must occur exactly once.
 - c. If you generated a very large number of random digits, then each integer between 0 and 9 would occur close to 10% of the time. false, false,true,true
 - d. The cumulative proportion of times that a 0 is generated tends to get closer to 0.10 as the number of random digits generated gets larger and larger.

subjective, used judgement as no data

- 5.8 Heart transplant Before the first human heart transplant, Dr. Christiaan Barnard of South Africa was asked to assess the probability that the operation would be successful. Did he need to rely on the relative frequency definition or the subjective definition of probability? Explain.
- 5.16 More true-false questions Your teacher gives a true-false pop quiz with 10 questions. 2^10
 - a. Show that the number of possible outcomes for the sample space of possible sequences of 10 answers is 1024.
 - b. What is the complement of the event of getting at least one of the questions wrong?getting all correct
 - c. With random guessing, show that the probability of getting at least one question wrong is 0.999.1-1/1024
- 5.20 Wrong sample space A couple plans on having four children. The father notes that the sample space for the number of girls the couple can have is 0, 1, 2, 3, and 4. He goes on to say that since there are five outcomes in the sample space, and since each child is equally likely to be a boy or girl, all five outcomes must be equally likely. Therefore, the probability of all four children being girls is 1/5. Explain the flaw in his reasoning.
- x = 1, 2, 3, 4, 5 diff probabilit, cannot compare or use binomial distribution to calc each probability

P(AB) = P(AIB)xP(B)

if independent, P(A)P(B)

Tutorial 5

- 5.24 Protecting the environment When the General Social Survey most recently asked subjects whether they are a member of an environmental group (variable GRNGROUP) and whether they would be very willing to pay higher prices to protect the environment (variable GRNPRICE), the results were as shown in the table. For 5, 504/795 randomly selected American adult:
 - a. Estimate the probability of being (i) a member of an environmental group and (ii) willing to pay higher prices to protect the environment.
 - **b.** Estimate the probability of being both a member of an environmental group and very willing to pay higher prices to protect the environment.
 - c. Given the probabilities in part a, show that the probability in part b is larger than it would be if the variables were independent Interprote / 795
 - **d.** Estimate the probability that a person is a member of an environmental group or very willing to pay higher prices to protect the environment. Do this (i) directly using the 15 ants 435 (45) and (ii) by applying the appropriate probability rule to the estimated probabilities found in parts a and b.

(0	7 7 304 (69)/795 Pay Higher Prices (GRNPRICE)		
		Yes	No	Total
Environmental	Yes	69	15	84
Group Member (GRNGROUP)	No	435	276	711
	Total	504	291	795

- 5.32 Cancer deaths Current estimates are that about 25% of all deaths are due to cancer, and of the deaths that are due to cancer, 30% are attributed to tobacco, 40% to diet, and 30% to other causes.
 - a. Define events, and identify which of these four probabilities refer to conditional probabilities.
 - **b.** Find the probability that a death is due to cancer and tobacco. .25 x .3

sensitivity P(PIC), specifity P(not P I not C)

- 5.58 More screening for breast cancer Refer to the previous exercise. For young women, the prevalence of breast cancer is lower. Suppose the sensitivity is 0.86 and the specificity is 0.88, but the prevalence is only 0.001.
 - a. Given that a test comes out positive, find the probability that the woman truly has breast cancer. P= event of
 - **b.** Show how to use a tree diagram with frequencies for a typical sample of 1000 women to explain to someone who has not studied statistics why the probability found in part a is so low.
 - c. Of the cases that are positive, explain why the proportion in error is likely to be larger for a young population than for an older population.

P(P) = P(C) + xP(PIC) + P(not C)

P(not C IP) is the probability of false positive

 $P(A \text{ or } (B) = 1 - P(\text{not } A \text{ or not } B) = P(A) + P(B) - {}_{2}P(AB)$

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Tutorial 5

5.74 Independent on coffee? Students in a geography class are asked whether they've visited Europe in the past 12 months and whether they've flown on a plane in the past 12 months.

dependant

- a. For a randomly selected student, would you expect these events to be independent or dependent? Explain.
- b. How would you explain to someone who has never studied statistics what it means for these events to be either independent or dependent?
- c. Students in a different class were asked whether they've visited Italy in the past 12 months and whether they've visited France in the past 12 months. For a randomly selected student, would you expect these events to be independent or dependent? Explain.
- d. Students in yet another class were asked whether they've been to a zoo in the past 12 months and whether they drink coffee. For a randomly selected student, would you expect these events to be independent or dependent? Explain. independent
- e. If you had to rank the pairs of events in parts a, c, and d in terms of the strength of any dependence, which pair of events is most dependent? Least dependent?

a most dependent, b least dependent

probability = drug availability ,condition = clubs

- Addiction and Substance Abuse (CASA) at Columbia
 University reported results of a survey of 1297 teenagers
 about their views on the use of illegal substances. Twenty
 percent of the teens surveyed reported going to clubs for
 music or dancing at least once a month. Of them, 26%
 said drugs were usually available at these club events.
 Which of these percentages estimates a conditional
 probability? For each that does, identify the event conditioned on and the event to which the probability refers.
- 5.88 Screening for heart attacks Biochemical markers are used by emergency room physicians to aid in diagnosing patients who have suffered acute myocardial infarction (AMI), or what's commonly referred to as a heart attack. One type of biochemical marker used is creatine kinase (CK). Based on a review of published studies on the effectiveness of these markers (by E. M. Balk et al., Annals of Emergency Medicine, vol. 37, pp. 478–494, 2001), CK had an estimated sensitivity of 37% and specificity of 87%. Consider a population having a prevalence rate of 25%.
 - a. Explain in context what is meant by the sensitivity equaling 37%. True positive
 - **b.** Explain in context what is meant by the specificity equaling 87%. True negative
 - c. Construct a tree diagram for this diagnostic test. Label the branches with the appropriate probabilities.