ST1131 Introduction to Statistics

Tutorial 11

- 12.32 t-score? A regression analysis is conducted with 25 observations.
 - a. What is the df value for inference about the slope β ?
 - **b.** Which two *t* test statistic values would give a P-value of 0.05 for testing H_0 : $\beta = 0$ against H_a : $\beta \neq 0$?
 - c. Which t-score would you multiply the standard error by in order to find the margin of error for a 95% confidence interval for β?
- **12.33 Predicting house prices** For the House Selling Prices FL data file on the text CD, MINITAB results of a regression analysis are shown for 100 homes relating y = selling price (in dollars) to x = the size of the house (in square feet).
 - a. Show all steps of a two-sided significance test of independence. Could the sample association between these two variables be explained by random variation?
 - b. Show that a 95% confidence interval for the population slope is (64, 90).
 - c. A builder had claimed that the selling price increases \$100, on average, for every extra square foot. Based on part b, what would you conclude about this claim?

House selling prices and size of home

Predictor	Coef	SE Coef	T	P
Constant	9161	10760	0.85	0.397
size	77.008	6.626	11.62	0.000

12.34 House prices in bad part of town Refer to the previous exercise. Of the 100 homes, 25 were in a part of town considered less desirable. For a regression analysis using y = selling price and x = size of house for these 25 homes,

- a. You plan to test H_0 : $\beta = 0$ against H_a : $\beta > 0$. Explain what H_0 means, and explain why a data analyst might choose a one-sided H_a for this test.
- **b.** For this one-sided alternative hypothesis, how large would the *t* test statistic need to be in order to get a P-value equal to (i) 0.05 and (ii) 0.01?

ST1131 Introduction to Statistics Tutorial 11

12.42 Student GPAs Refer to the Georgia Student Survey
data file on the text CD. Treat college GPA as the
response variable and high school GPA as the explanatory
variable, and suppose these students are a random sample
of all University of Georgia students.

- **a.** Can you conclude that these variables are associated in that population? Show all steps of the relevant significance test with significance level 0.05, and interpret.
- **b.** Find a 95% confidence interval for the population slope. Interpret the endpoints, and explain the correspondence with the result of the significance test in part a.

The regression equation is CGPA = 1.19 + 0.637 HSGPA

Predictor Coef SE Coef T P
Constant 1.1898 0.5496 2.16 0.035
HSGPA 0.6369 0.1442 4.42 0.000

12.54 Predicting GPA Refer to the Georgia Student Survey data file on the text CD. Regress y = college GPA on x = high school GPA.

- a. Stating the necessary assumptions, find a 95% confidence interval for the mean college GPA for all University of Georgia students who have high school GPA = 3.6.
- **b.** Find a 95% prediction interval for college GPA of a randomly chosen student having high school GPA = 3.6. Interpret.
- **c.** Explain the difference between the purposes of the intervals in part a and part b.

Predicted Values for New Observations
New
Obs Fit SE Fit 95% CI 95% PI
1 3.4828 0.0505 (3.3818, 3.5839)(2.8407, 4.1250)

Values of Predictors for New Observations New Obs HSGPA 1 3.60