

1. Solution:

(a) $\pi_{rname,pizza}(Sells) / \pi_{pizza}(\sigma_{cname='Maggie'}(Likes)) - \pi_{rname}(Sells \bowtie \sigma_{cname='Ralph'}(Likes))$

(b) Let $\pi_A(R) = Q \cup Q'$, where $Q = R/S$ and Q' are the remaining tuples in $\pi_A(R)$ that are not in quotient of R/S .

The expression $\pi_A(R) \times S$ computes all the combinations of $\pi_A(R)$ and S .

Thus, $Q' = \pi_A((\pi_A(R) \times S) - R)$.

Therefore, $Q = \pi_A(R) - Q' = \pi_A(R) - \pi_A((\pi_A(R) \times S) - R)$.

2. Solution:

```
drop table if exists Offices, Employees cascade;
```

```
create table Offices (
    office_id    integer,
    building     text not null,
    level        integer not null,
    room_number  integer not null,
    area         integer,
    primary key (office_id),
    unique (building, level, room_number)
);
```

```
create table Employees (
    emp_id       integer,
    name         text not null,
    office_id    integer not null,
    manager_id   integer,
    primary key (emp_id),
    foreign key (office_id) references Offices (office_id)
        on update cascade,
    foreign key (manager_id) references Employees (emp_id)
        on update cascade
);
```

Note that the constraint that each employee must be assigned to exactly one office and the constraint that each employee is managed by at most one manager are both enforced by the primary key constraint in **Employees** which ensures that there can't be two **Employees** records with the same primary key value and different values for `office_id` / `manager_id`.

3. Solution:

Each table in a database schema must have a primary key.

(a)

```
drop table if exists
    Books, Customers, Carts, Purchase, Purchased_Items cascade;

create table Books (
    isbn      text,
    title     text not null,
    authors   text not null,
    year      integer,
    edition   text not null
        check (edition in ('hardcopy', 'paperback', 'ebook')),
    publisher text,
    number_pages integer
        check (number_pages > 0),
    price     numeric not null
        check (price > 0),
    primary key (isbn)
);

create table Customers (
    cust_id integer,
    name     text not null,
    email    text,
    primary key (cust_id)
);

create table Carts (
    cust_id integer,
    isbn     text,
    primary key (cust_id, isbn),
    foreign key (cust_id) references Customers,
    foreign key (isbn) references Books
);

create table Purchase (
    pid integer,
    purchase_date date not null,
    cust_id integer not null,
    primary key (pid),
    foreign key (cust_id) references Customers
);

create table Purchased_Items (
    pid integer,
    isbn  text,
    primary key (pid, isbn),
    foreign key (pid) references Purchase,
```

```
foreign key (isbn) references Books
);
```

(b) (purchase_timestamp, cust_id) is a candidate key of Purchase.

```
create table Purchase (
    pid integer,
    purchase_timestamp timestamp not null,
    cust_id integer not null,
    primary key (pid),
    foreign key (cust_id) references Customers,
    unique (purchase_timestamp, cust_id)
);
```

(c) The constraint of the form “ $p \implies q$ ” is equivalent to “(not p) or q”.

1. This constraint can be expressed using a table constraint on Books:

```
check ((edition <> 'hardcover') or (price >= 30))
```

2. This constraint can't be expressed using the constructs learned so far.
3. This constraint can be expressed using a table constraint on Books:

```
check ((number_of_pages <= 1000) or (edition = 'ebook') or (price >=
100))
```

4. This constraint can be expressed using a table constraint on Books:

```
check ((publisher <> 'Acme') or (pub_year < 2010) or (edition =
'ebook'))
```

(d)

```
drop table if exists Books, Customers, Carts, Purchase,
Purchased_Items cascade;
```

```
create table Books (
    isbn      text,
    title     text not null,
    authors   text not null,
    year      integer,
    edition   text not null
        check (edition in ('hardcover', 'paperback', 'ebook')),
    publisher text,
    number_pages integer
        check (number_pages > 0),
    price     numeric
        check (price > 0),
    primary key (isbn)
```

```
);

create table Customers (
    cust_id integer,
    name      text not null,
    email     text,
    primary key (cust_id)
);

create table Carts (
    cust_id integer,
    isbn      text,
    primary key (cust_id, isbn),
    foreign key (cust_id) references Customers
        on delete cascade
        on update cascade,
    foreign key (isbn) references Books
        on delete cascade
        on update cascade
);

create table Purchase (
    pid integer,
    purchase_date date not null,
    cust_id integer not null,
    primary key (pid),
    foreign key (cust_id) references Customers
        on delete cascade
        on update cascade
);

create table Purchased_Items (
    pid integer,
    isbn      text default '0',
    primary key (pid, isbn),
    foreign key (pid) references Purchase
        on delete cascade
        on update cascade,
    foreign key (isbn) references Books
        on delete set default
        on update cascade
);
```

For the “on delete set default” action to work in `Purchased_items` when a referenced book in `Books` is deleted, there must exist a record in `Books` with `isbn = '0'`. If not, the deletion operation will be rejected.