

Tool: Test of Normality: test if pop. distn is normal using a random sample from that pop.  $x'$

$H_0$ : pop is normal

$H_1$ : pop is NOT normal

$\Rightarrow$  p-value = large  $\Rightarrow$  pop is normal  
small  $\Rightarrow$  NOT normal.

Recap: to examine if a sample is from a pop that is normal:

- $\ominus$  hist + normal density curve
- $\ominus$  qq plot
- $\ominus$  Normality test  $\rightarrow$  Shapiro Wilk test  
in R: `shapiro.test(x)`

Weight of males & Females (gender affects weight)

$\mu_1 \longleftrightarrow \mu_2$   $\mu = 3.3$  X

Males: 100 pp  $\Rightarrow \bar{Y}$   $\bar{X} \rightarrow \mu_2$

Females: 100 pp  $\Rightarrow \bar{X}$   $\bar{Y} \rightarrow \mu_1$

$\mu_1$  vs  $\mu_2$ :  $H_0$ :  $\mu_1 - \mu_2$  = 0

$H_1$ :  $\mu_1 - \mu_2 \neq 0 \leftarrow$   
 $< 0 \leftarrow$   
 $> 0 \leftarrow$

group 1 from pop 1  $\Rightarrow \sigma_1^2$   
 group 2 from pop 2  $\Rightarrow \sigma_2^2$

$\Rightarrow$  sample variance:  $S_1^2$   
 $S_2^2$

9 9.5 ?  
 9 18

Tool Test of equal variance:  $H_0$ : 2 variances are equal  
 $H_1$ : \_\_\_\_\_ NOT equal

$\rightarrow$  p-value?

in R: var.test(x, y)

Bartlett  $\Rightarrow$  when samples are  $\approx$  normal

Levene  $\Rightarrow$  \_\_\_\_\_ NOT normal

one sample:  $T = \frac{\bar{X} - 3.3}{SE(\bar{X})} \sim t_{n-1}$   $H_0: \mu = 3.3$

two sample:  $H_0: (\mu_1 - \mu_2) = 0$   
 $T = \frac{(\bar{X} - \bar{Y}) - 0}{SE(\bar{X} - \bar{Y})}$

paired samples: 1  $X_1 \rightarrow Y_1 \rightarrow D_1$   $Y - X$  or  $X - Y$

$\vdots$   $\vdots$   $\vdots$   
 $n$   $X_n \rightarrow Y_n \rightarrow D_n$   
 $\mu_X$  vs  $\mu_Y$   
 $\mu_D$  vs 0  
 $\mu_D = 0$

Bartlett test : test if variances of groups are the same.

⇒ used if the groups are normal.

H<sub>0</sub> : the variances are the same.

Levene test : → similar to Bartlett test but for groups → non normal.