

CS4246 / CS5446

Tutorial Week 5

Muhammad **Rizki** Maulana
rizki@u.nus.edu

First

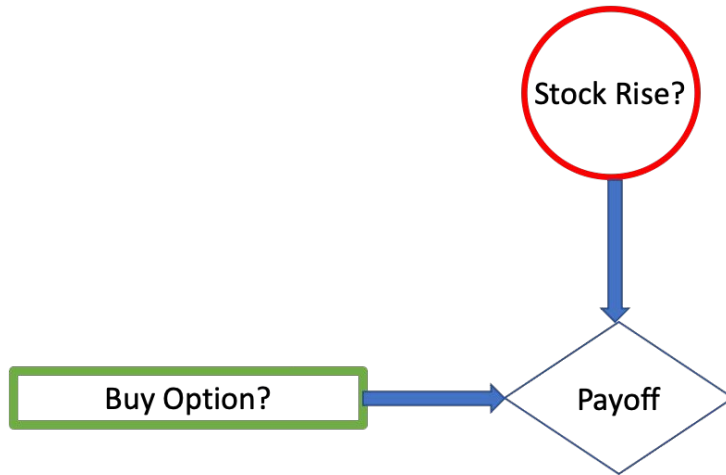
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- a) Draw an influence diagram to represent Mr. Bean's problem. Clearly indicate all the options/outcomes and numbers. Should he buy the options?

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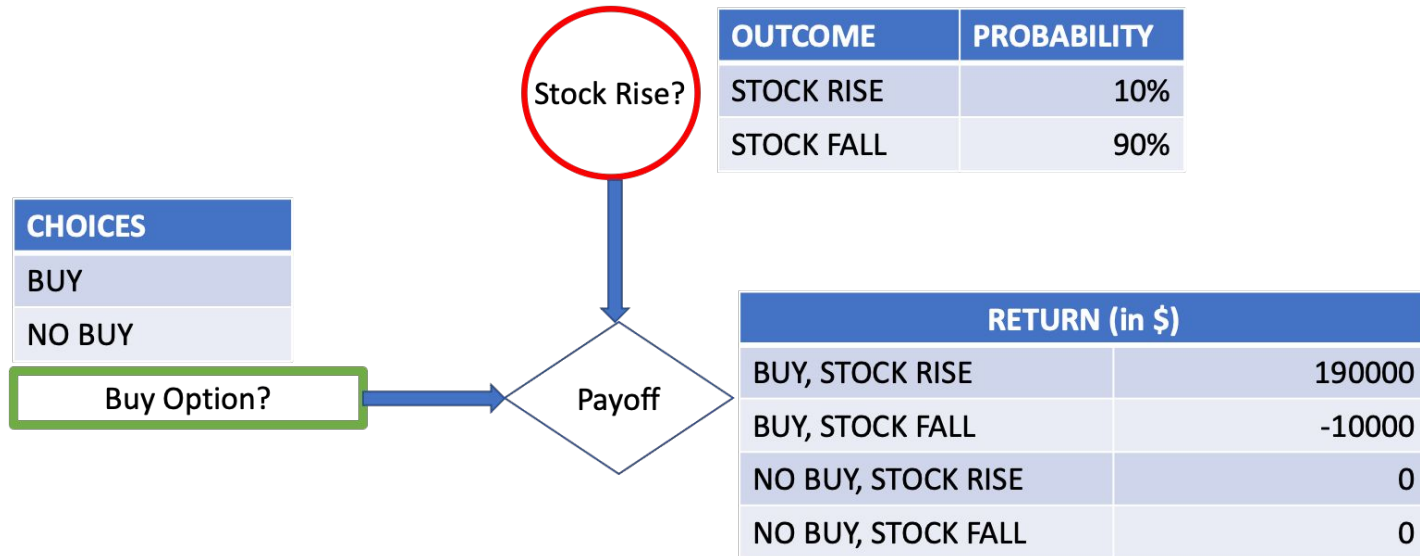
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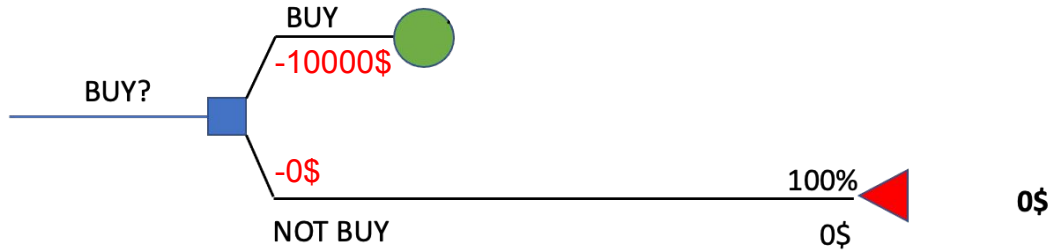
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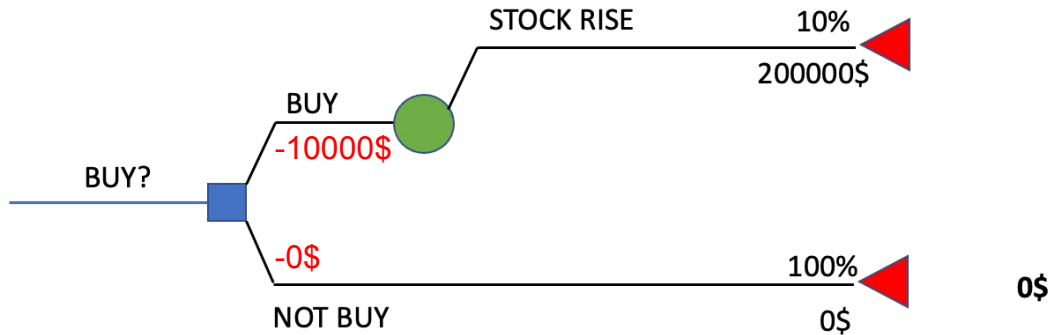
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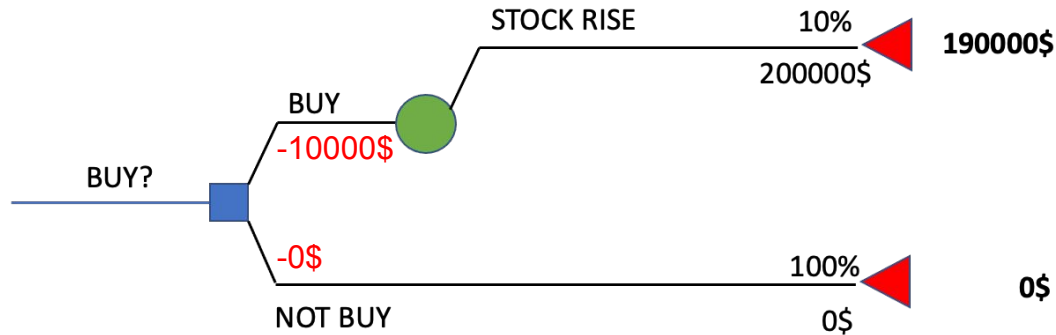
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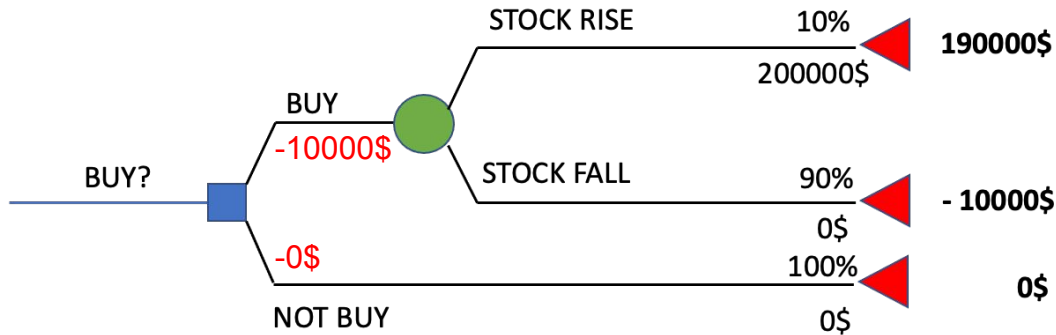
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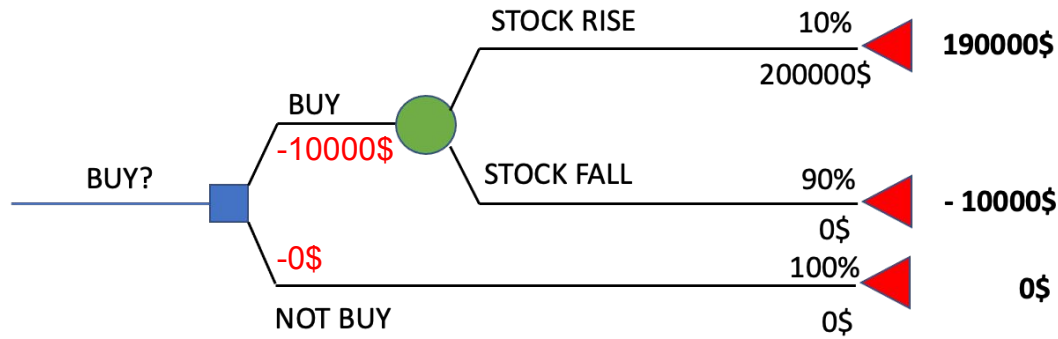
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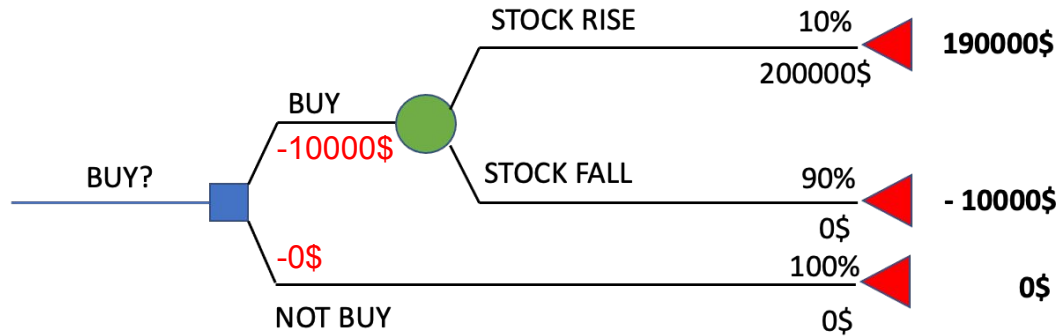
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$$\text{EMV (BUY)} = 190\text{K} \cdot 0.1 - 10\text{K} \cdot 0.9 = 10\text{K}$$

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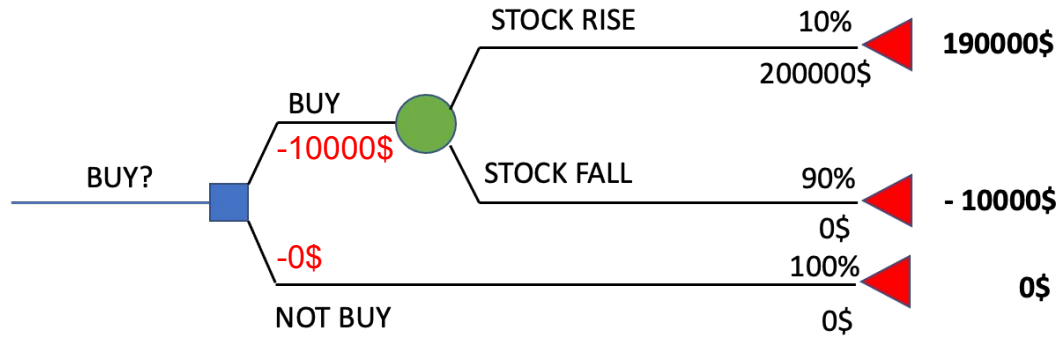


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$$\text{EMV (NOT BUY)} = 0$$

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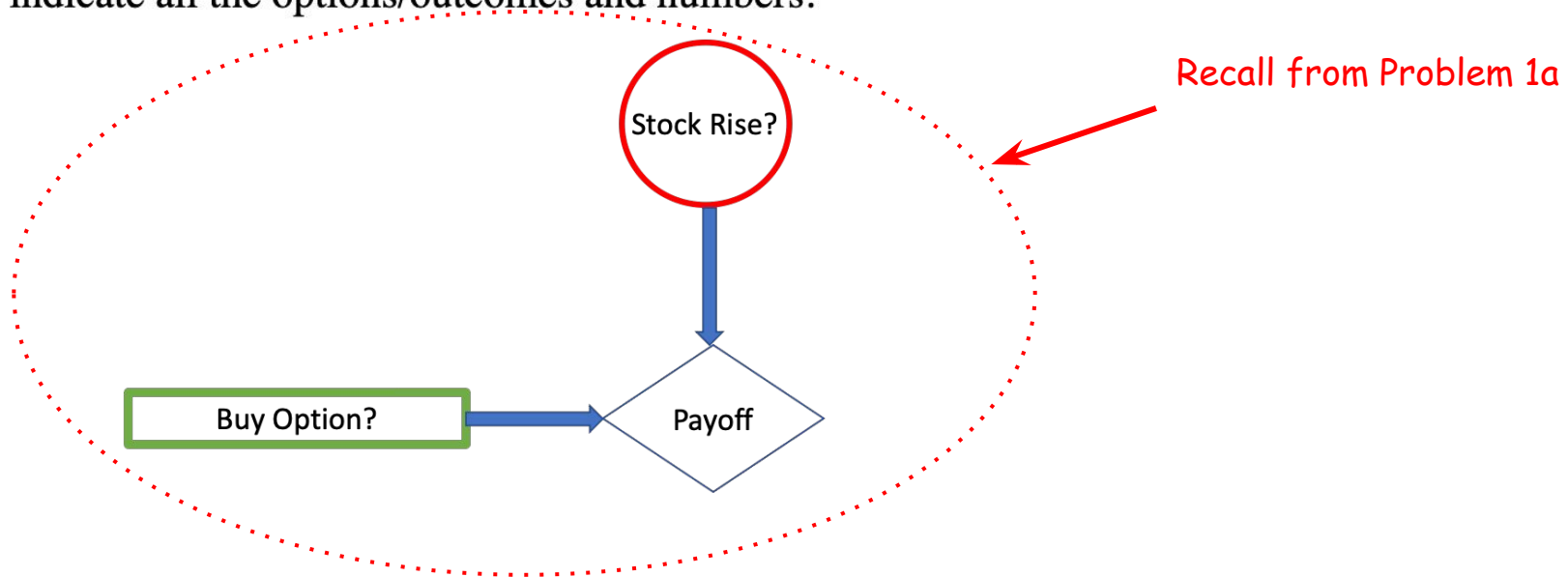
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- a) Represent the hypothetical situation where Mr. Bean will get perfect information before he makes the decision. How to represent this situation in an influence diagram? Clearly indicate all the options/outcomes and numbers.

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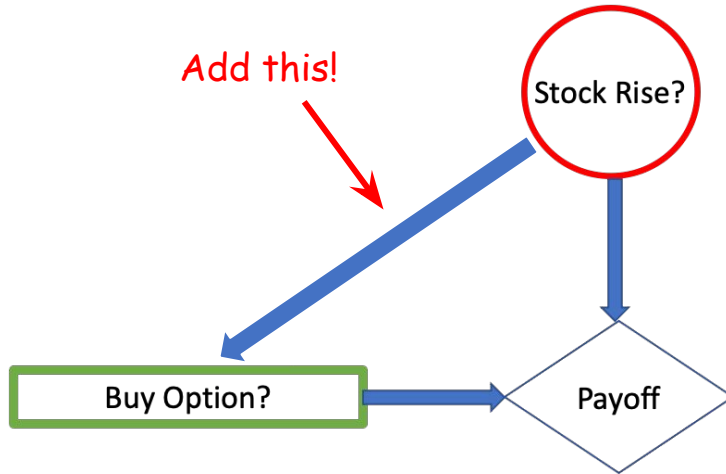
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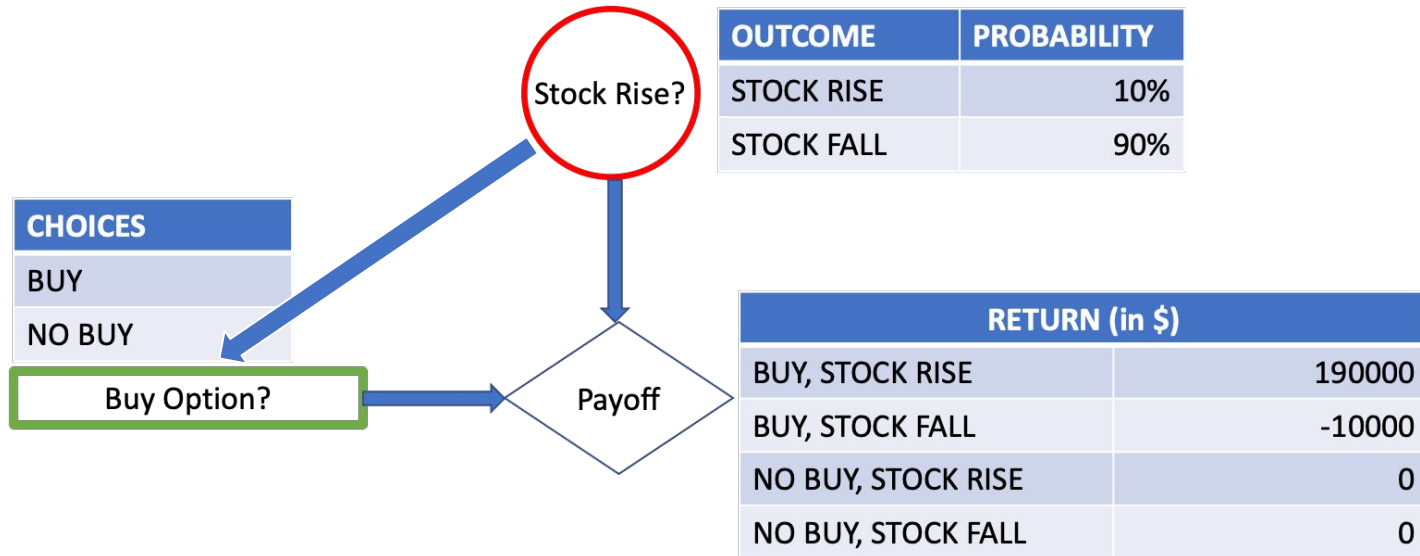
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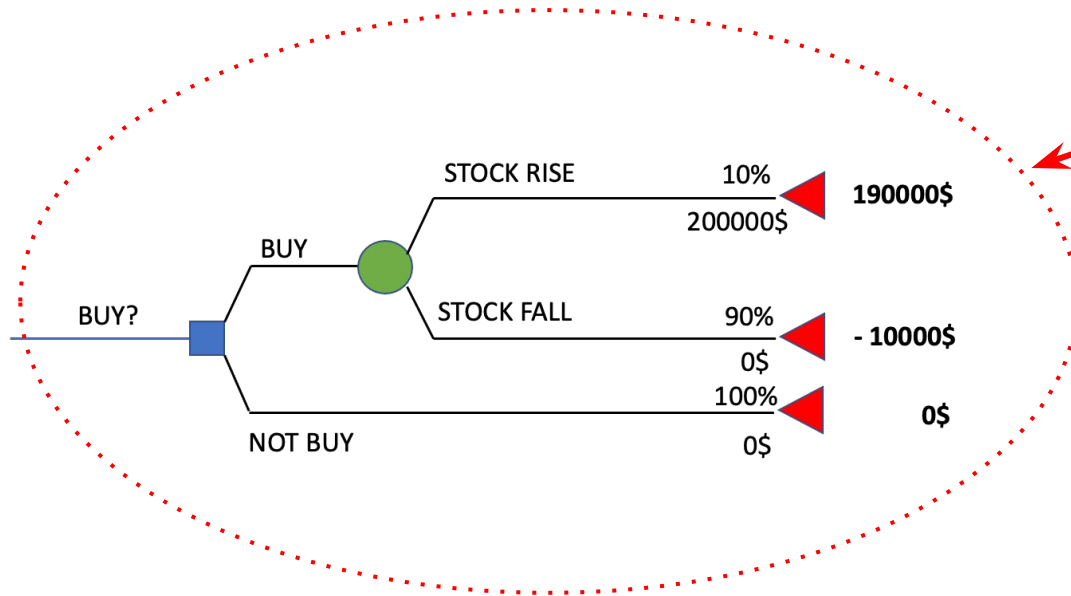
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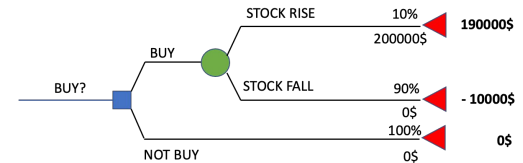
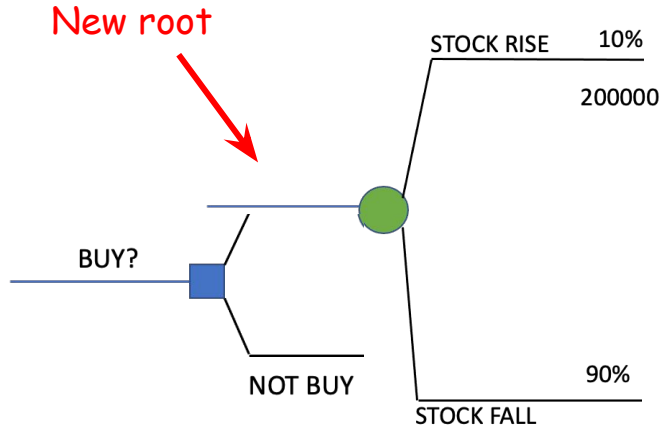
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Recall from Problem 1b

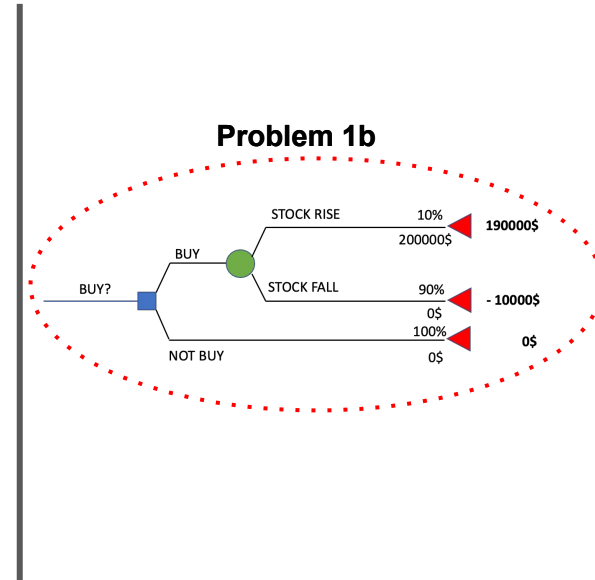
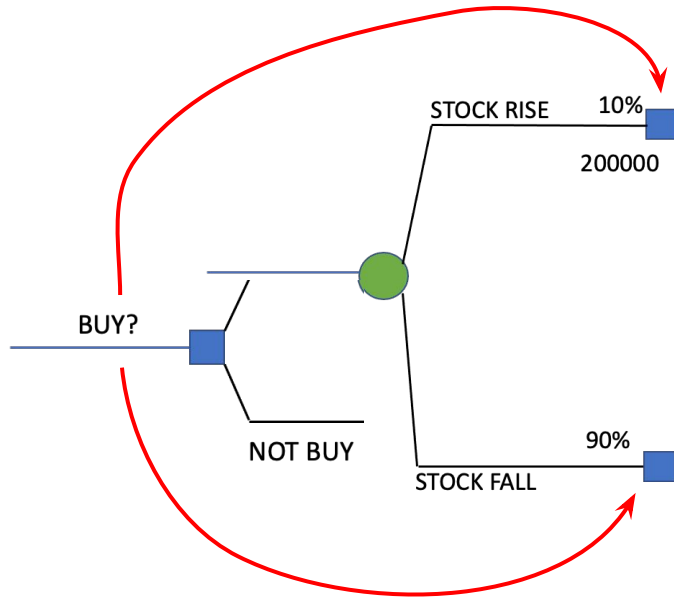
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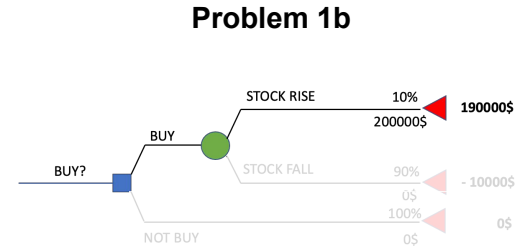
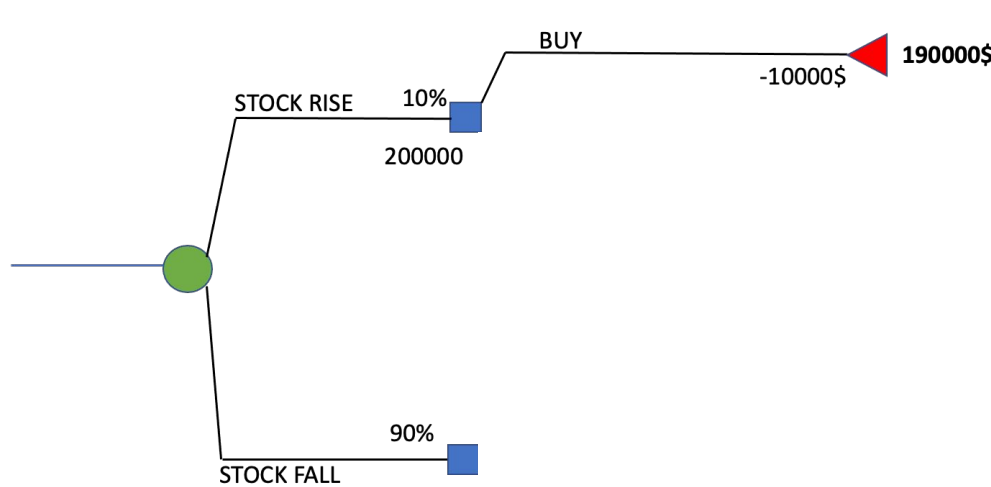
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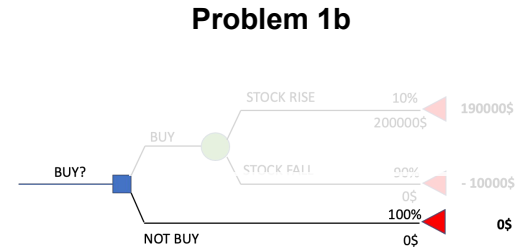
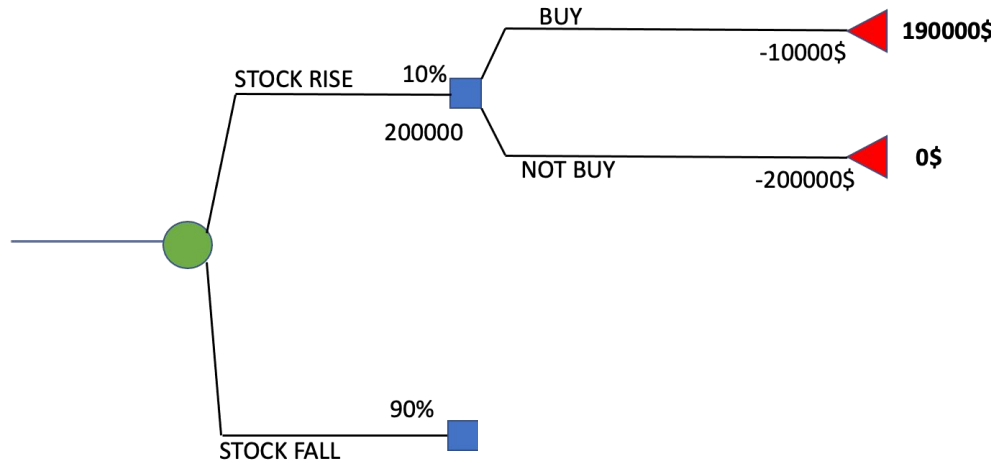
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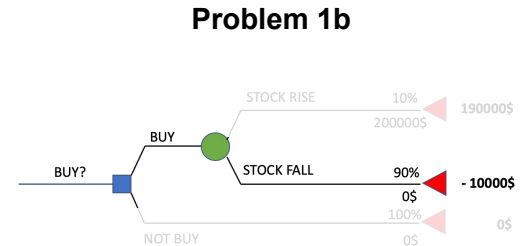
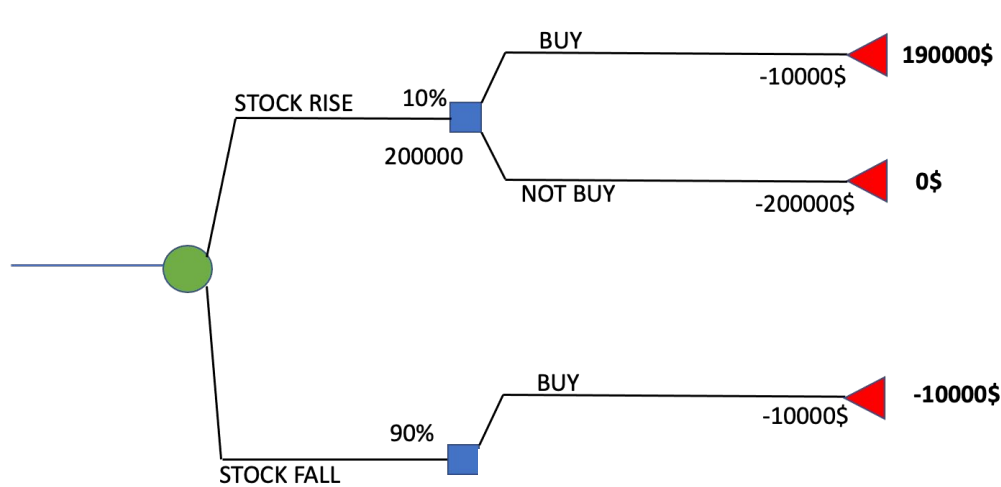
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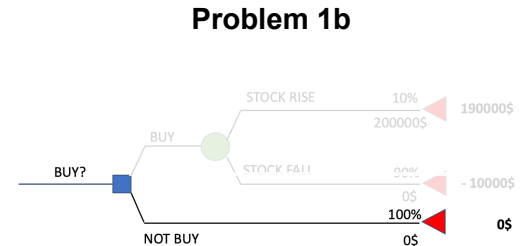
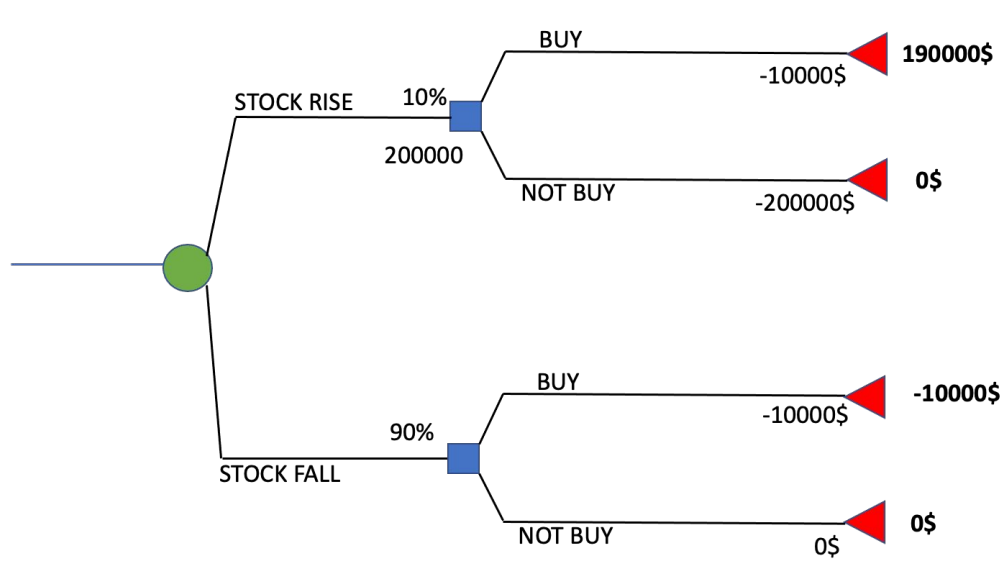
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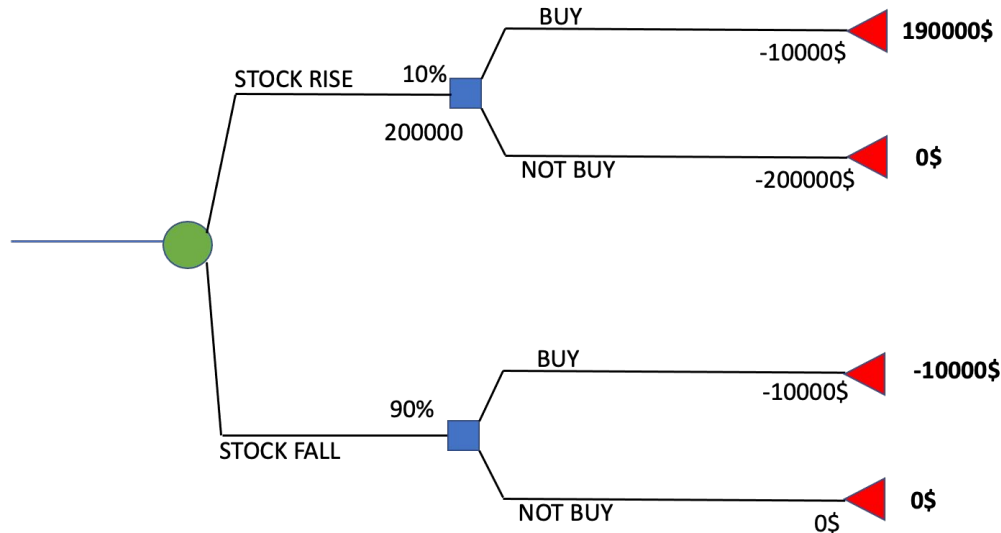
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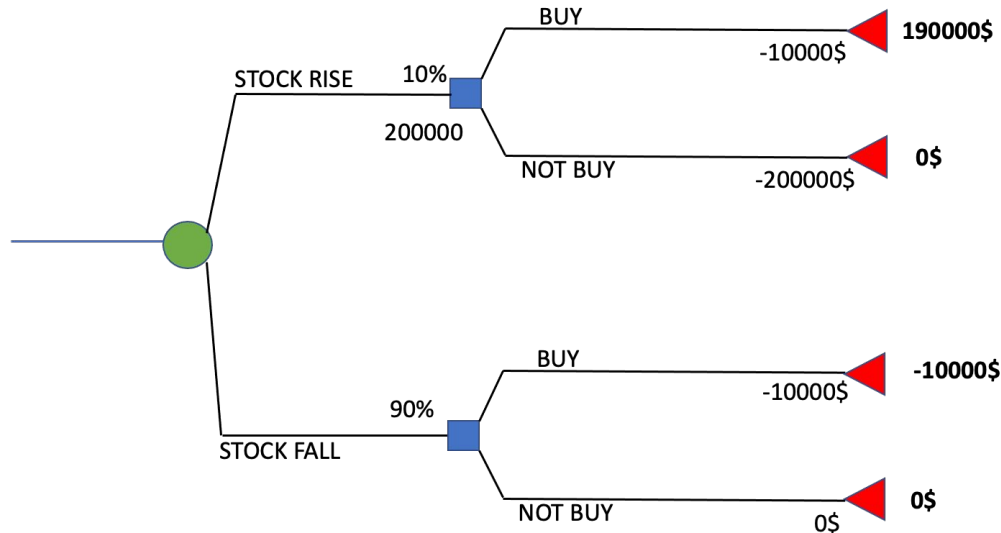
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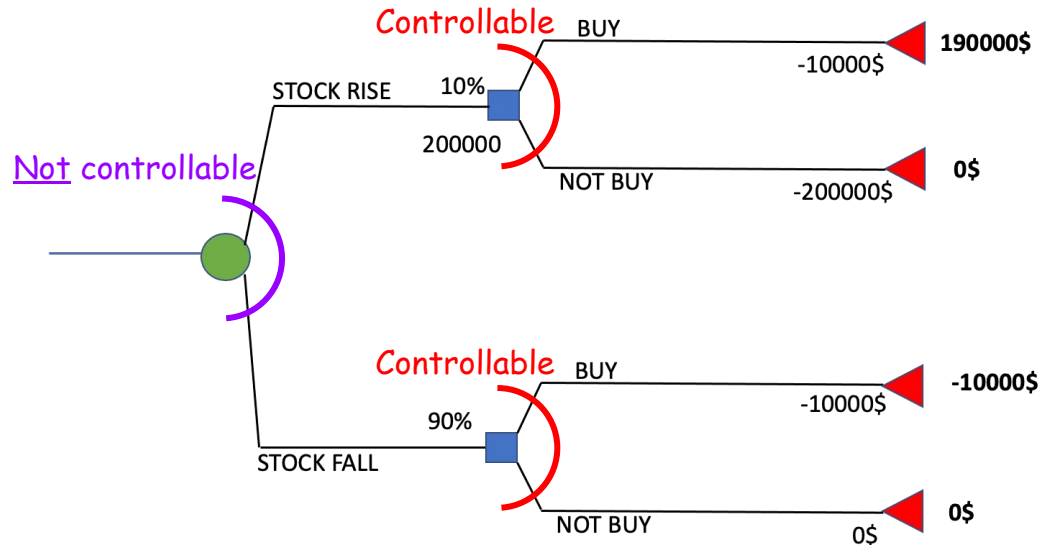
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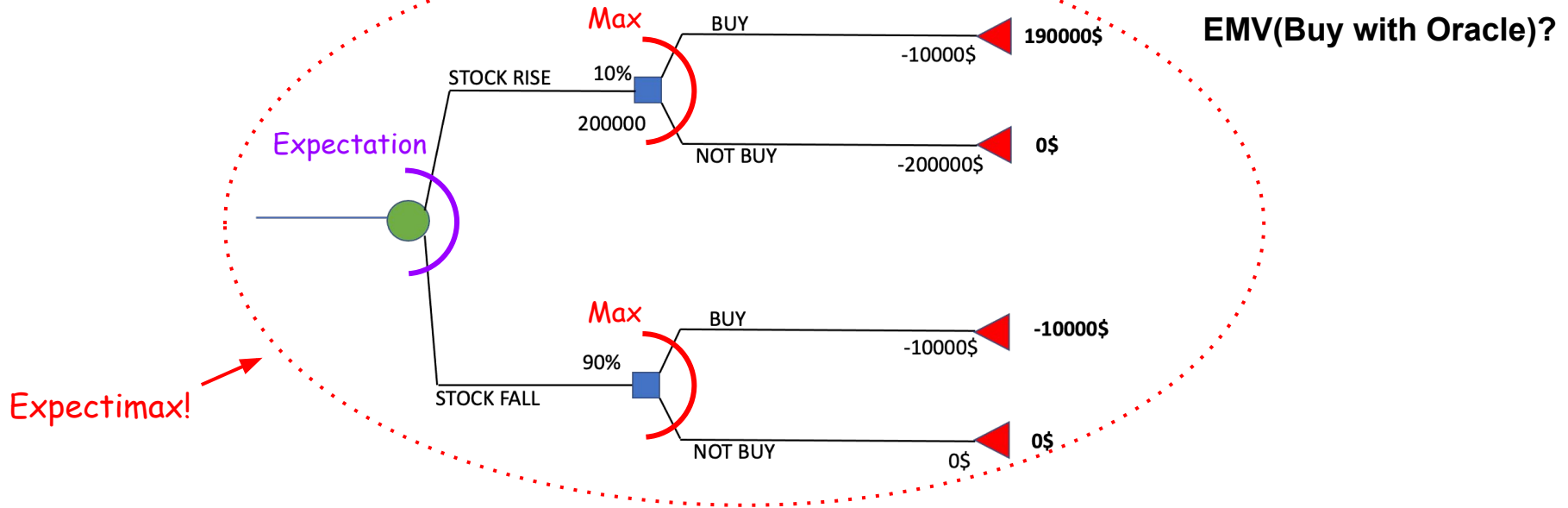
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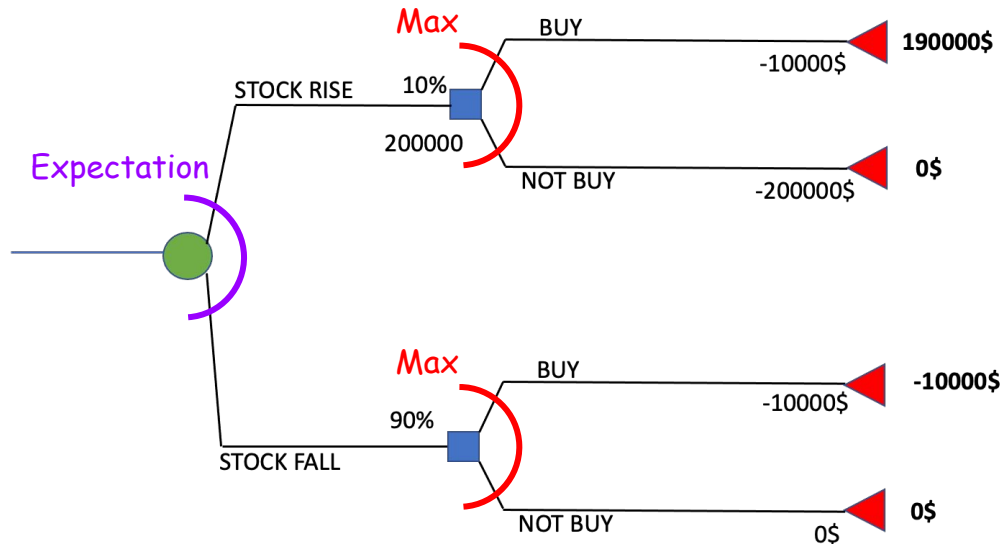
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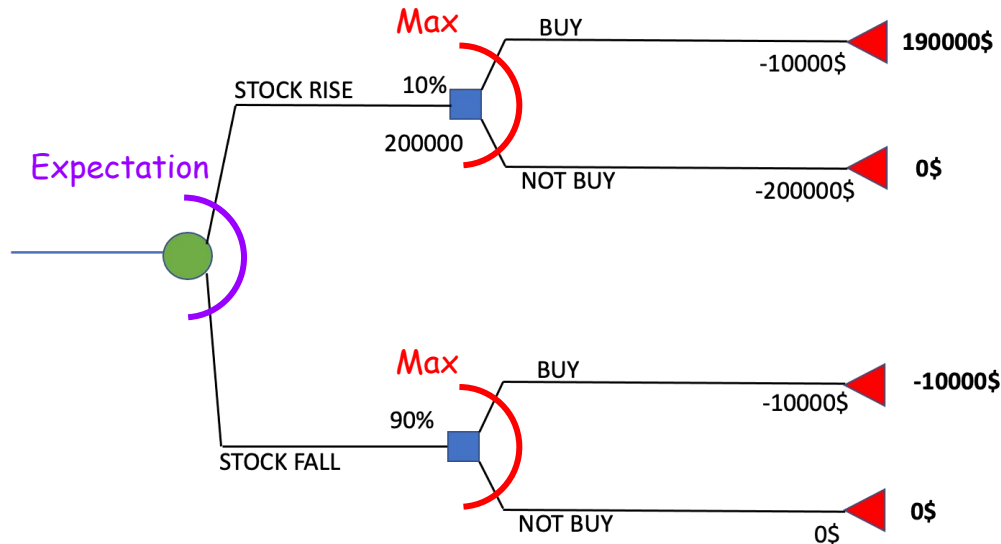
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EMV(Buy with Oracle)
 $= 190000 * 0.1 + 0 * 0.9$
 $= 19000$

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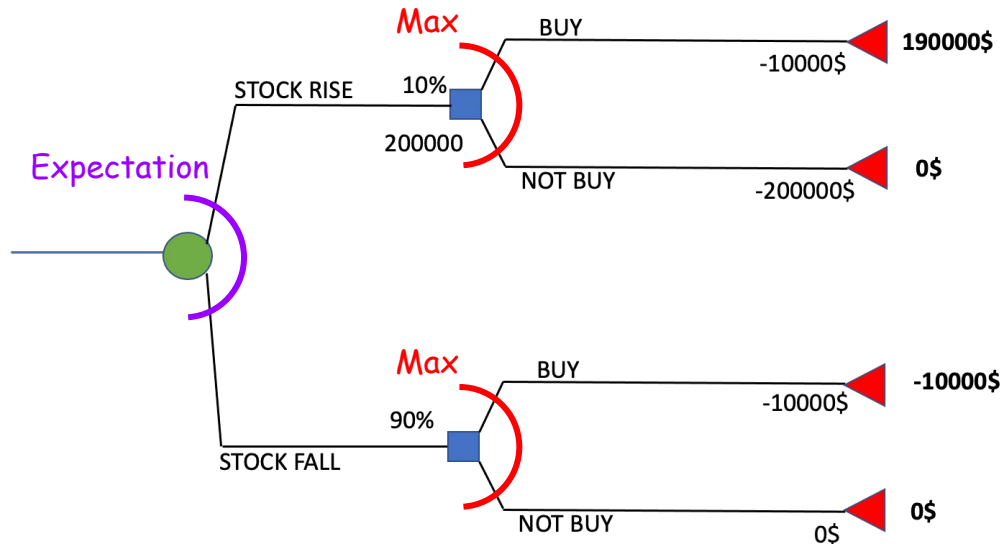


$$\begin{aligned} \text{EMV}(\text{Buy with Oracle}) &= 190000 * 0.1 + 0 * 0.9 \\ &= 19000 \end{aligned}$$

$$\begin{aligned} \text{Expected Value of Perfect Information} &= \text{EMV}(\text{Buy with Oracle}) - \text{EMV}(\text{Buy}) \end{aligned}$$

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$$\begin{aligned} \text{Expected Value of Perfect Information} &= \text{EMV}(\text{Buy with Oracle}) - \text{EMV}(\text{Buy}) \\ &= 19000 - 10000 = 9000 \end{aligned}$$

Third

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Consult financial guru (Dr. Nut):

- Diamond exists (stock rise) : 95% say "good"
- Diamond doesn't exists (stock fall) : 85% say "poor"

Draw the decision tree and calculate the expected value. Should Mr. Bean hire this guy (-\$7000)?

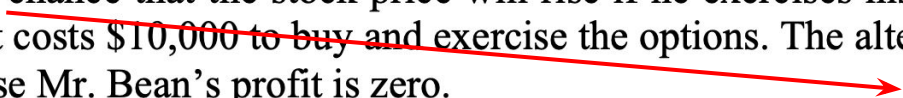
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$$\begin{aligned} P(\text{rise}) &= 0.1 \\ P(\text{fall}) &= 1.0 - 0.1 = 0.9 \end{aligned}$$

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- | | | | | |
|--|------------------|---|--------------------------------|--------|
| • Diamond exists (stock rise) | : 95% say "good" | → | $P(\text{"good"} \text{rise})$ | = 0.95 |
| • Diamond <u>doesn't</u> exists (stock fall) | : 85% say "poor" | → | $P(\text{"poor"} \text{fall})$ | = 0.85 |

$$P(\text{rise}) = 0.1$$

$$P(\text{fall}) = 0.9$$

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$$P(\text{"good"}) = P(\text{"good"}|\text{rise})P(\text{rise}) + P(\text{"good"}|\text{fall})P(\text{fall})$$

$P(\text{rise})$	$= 0.1$
$P(\text{fall})$	$= 0.9$
$P(\text{"good"} \text{rise})$	$= 0.95$
$P(\text{"poor"} \text{fall})$	$= 0.85$



Law of total probability

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$\begin{aligned}
 P(\text{"good"}) &= P(\text{"good"}|\text{rise})P(\text{rise}) + P(\text{"good"}|\text{fall})P(\text{fall}) \\
 &= 0.95 * 0.1 + 0.15 * 0.9
 \end{aligned}$$

P(rise)	= 0.1
P(fall)	= 0.9
P("good" rise)	= 0.95
P("poor" fall)	= 0.85

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$\begin{aligned} P(\text{"good"}) &= P(\text{"good"}|\text{rise})P(\text{rise}) + P(\text{"good"}|\text{fall})P(\text{fall}) \\ &= 0.95 * 0.1 + 0.15 * 0.9 \\ &= 0.23 \end{aligned}$$

$$\begin{aligned} P(\text{rise}) &= 0.1 \\ P(\text{fall}) &= 0.9 \\ P(\text{"good"}|\text{rise}) &= 0.95 \\ P(\text{"poor"}|\text{fall}) &= 0.85 \end{aligned}$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23$$

$P(\text{rise})$	$= 0.1$
$P(\text{fall})$	$= 0.9$
$P(\text{"good"} \text{rise})$	$= 0.95$
$P(\text{"poor"} \text{fall})$	$= 0.85$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23 \qquad P(\text{"poor"}) = 1.0 - P(\text{"good"}) = 0.77$$

$P(\text{rise})$	$= 0.1$
$P(\text{fall})$	$= 0.9$
$P(\text{"good"} \text{rise})$	$= 0.95$
$P(\text{"poor"} \text{fall})$	$= 0.85$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$

$$P(\text{rise}) = 0.1$$

$$P(\text{fall}) = 0.9$$

$$P(\text{"good"}|\text{rise}) = 0.95$$

$$P(\text{"poor"}|\text{fall}) = 0.85$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23 \quad P(\text{"poor"}) = 0.77$$

$$P(\text{rise}|\text{"good"}) = P(\text{"good"}|\text{rise})P(\text{rise}) / P(\text{"good"})$$

$P(\text{rise})$	$= 0.1$
$P(\text{fall})$	$= 0.9$
$P(\text{"good"} \text{rise})$	$= 0.95$
$P(\text{"poor"} \text{fall})$	$= 0.85$



Bayes rule

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$\begin{aligned}
 P(\text{"good"}) &= 0.23 & P(\text{"poor"}) &= 0.77 \\
 P(\text{rise}|\text{"good"}) &= P(\text{"good"}|\text{rise})P(\text{rise}) / P(\text{"good"}) \\
 &= 0.95 * 0.1 / 0.23
 \end{aligned}$$

$$\begin{aligned}
 P(\text{rise}) &= 0.1 \\
 P(\text{fall}) &= 0.9 \\
 P(\text{"good"}|\text{rise}) &= 0.95 \\
 P(\text{"poor"}|\text{fall}) &= 0.85
 \end{aligned}$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$\begin{aligned}
 P(\text{"good"}) &= 0.23 & P(\text{"poor"}) &= 0.77 \\
 P(\text{rise}|\text{"good"}) &= P(\text{"good"}|\text{rise})P(\text{rise}) / P(\text{"good"}) \\
 &= 0.95 * 0.1 / 0.23 \\
 &= 0.413
 \end{aligned}$$

$$\begin{aligned}
 P(\text{rise}) &= 0.1 \\
 P(\text{fall}) &= 0.9 \\
 P(\text{"good"}|\text{rise}) &= 0.95 \\
 P(\text{"poor"}|\text{fall}) &= 0.85
 \end{aligned}$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23 \qquad P(\text{"poor"}) = 0.77$$

$$P(\text{rise}|\text{"good"}) = 0.413$$

$$P(\text{rise}) = 0.1$$

$$P(\text{fall}) = 0.9$$

$$P(\text{"good"}|\text{rise}) = 0.95$$

$$P(\text{"poor"}|\text{fall}) = 0.85$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$

$$P(\text{rise}|\text{"good"}) = 0.413$$

$$P(\text{fall}|\text{"good"}) = 1.0 - P(\text{rise}|\text{"good"})$$

$$P(\text{rise}) = 0.1$$

$$P(\text{fall}) = 0.9$$

$$P(\text{"good"}|\text{rise}) = 0.95$$

$$P(\text{"poor"}|\text{fall}) = 0.85$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

$$\begin{aligned} P(\text{"good"}) &= 0.23 & P(\text{"poor"}) &= 0.77 \\ P(\text{rise}|\text{"good"}) &= 0.413 & P(\text{fall}|\text{"good"}) &= 0.587 \end{aligned}$$

$$\begin{aligned} P(\text{rise}) &= 0.1 \\ P(\text{fall}) &= 0.9 \\ P(\text{"good"}|\text{rise}) &= 0.95 \\ P(\text{"poor"}|\text{fall}) &= 0.85 \end{aligned}$$

Richie Bean is trying to strike it big in the stock market during the economic downturn. He is considering buying some options to a very risky stock on a diamond mine in Africa. There is only a 10% chance that the stock price will rise if he exercises his options, but the payoff is \$200,000. It costs \$10,000 to buy and exercise the options. The alternative is not to buy at all, in which case Mr. Bean's profit is zero.

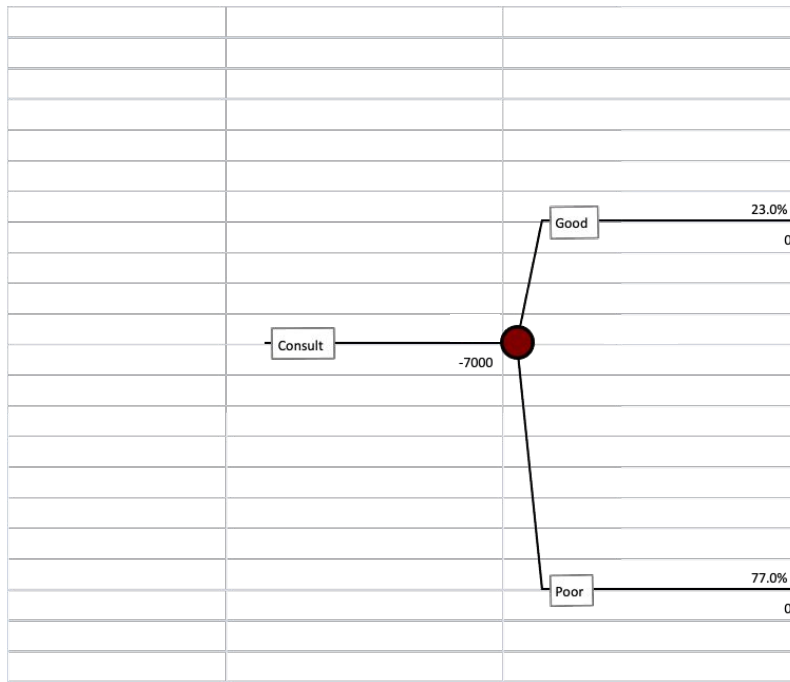
$$\begin{aligned} P(\text{"good"}) &= 0.23 & P(\text{"poor"}) &= 0.77 \\ P(\text{rise}|\text{"good"}) &= 0.413 & P(\text{fall}|\text{"good"}) &= 0.587 \\ P(\text{rise}|\text{"poor"}) &= 0.065 & P(\text{fall}|\text{"poor"}) &= 0.9935 \end{aligned}$$

$P(\text{rise})$	$= 0.1$
$P(\text{fall})$	$= 0.9$
$P(\text{"good"} \text{rise})$	$= 0.95$
$P(\text{"poor"} \text{fall})$	$= 0.85$



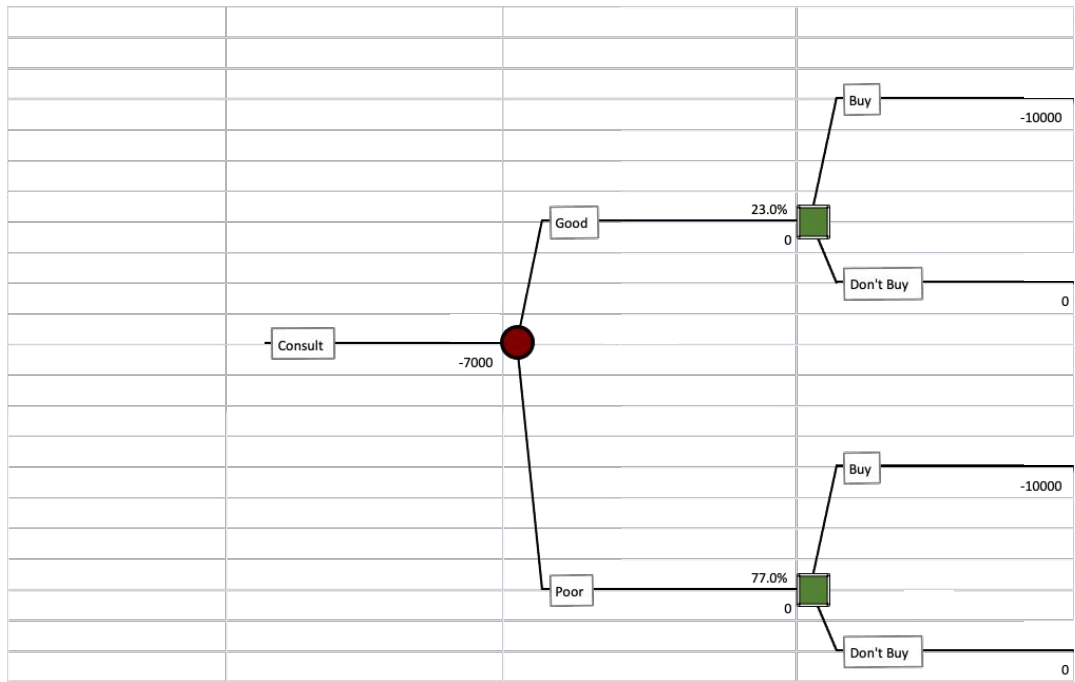
Similar things

Let's construct the tree!



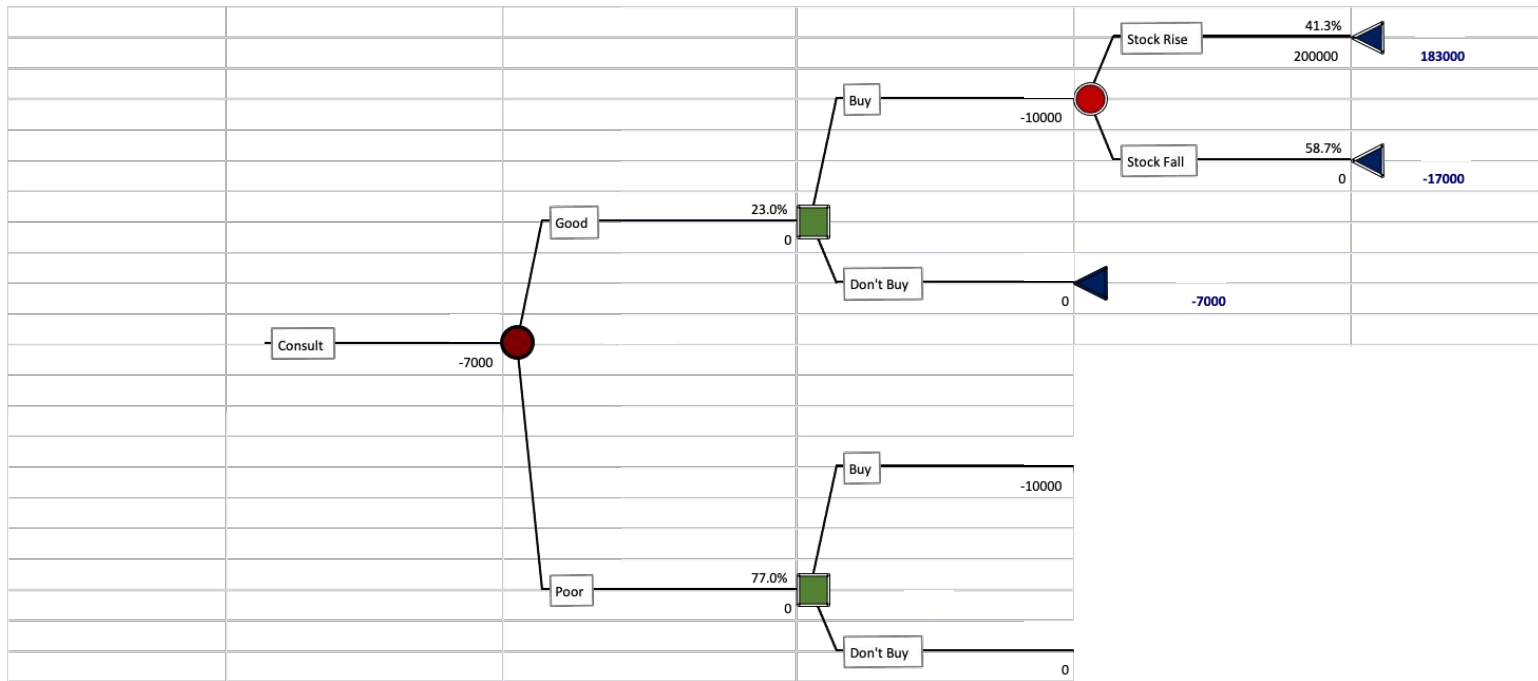
$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$



$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$

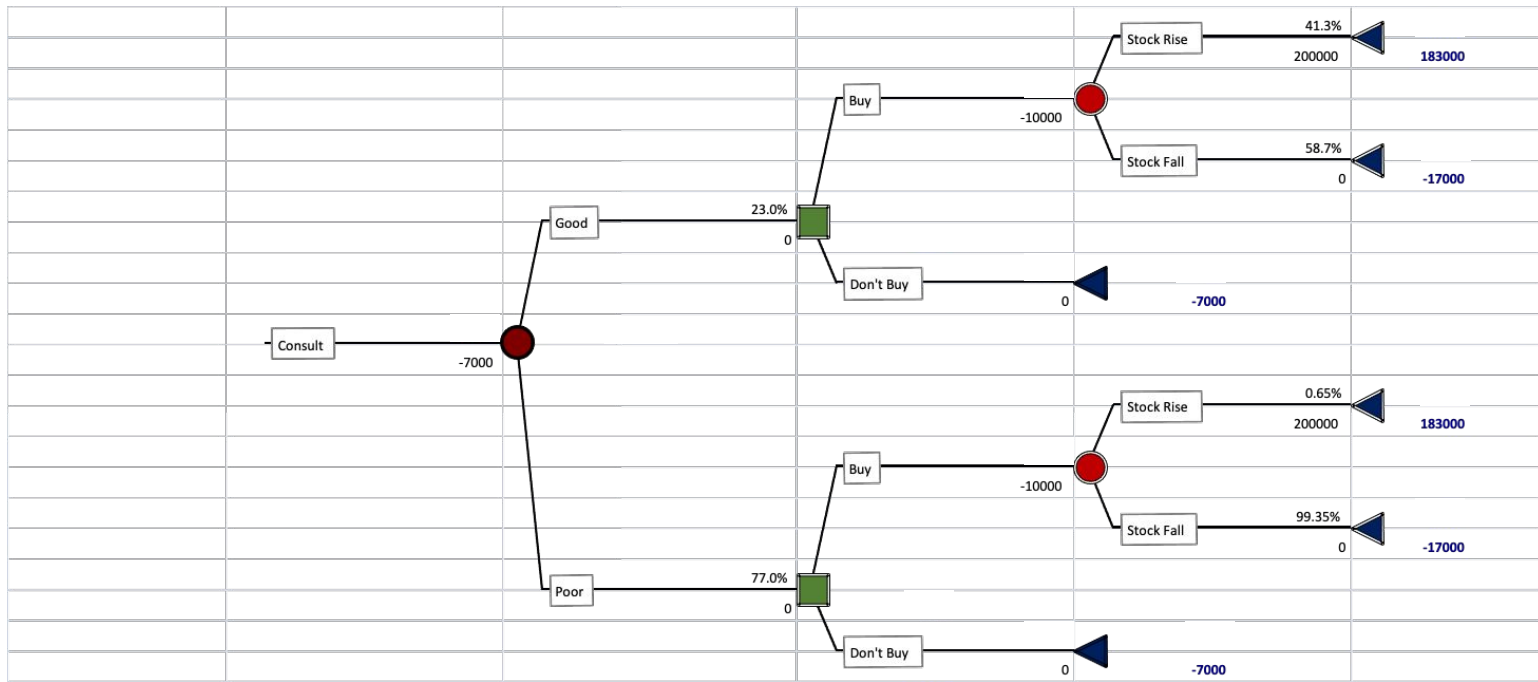


$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$

$$P(\text{rise}|\text{"good"}) = 0.413$$

$$P(\text{fall}|\text{"good"}) = 0.587$$



$$P(\text{"good"}) = 0.23$$

$$P(\text{"poor"}) = 0.77$$

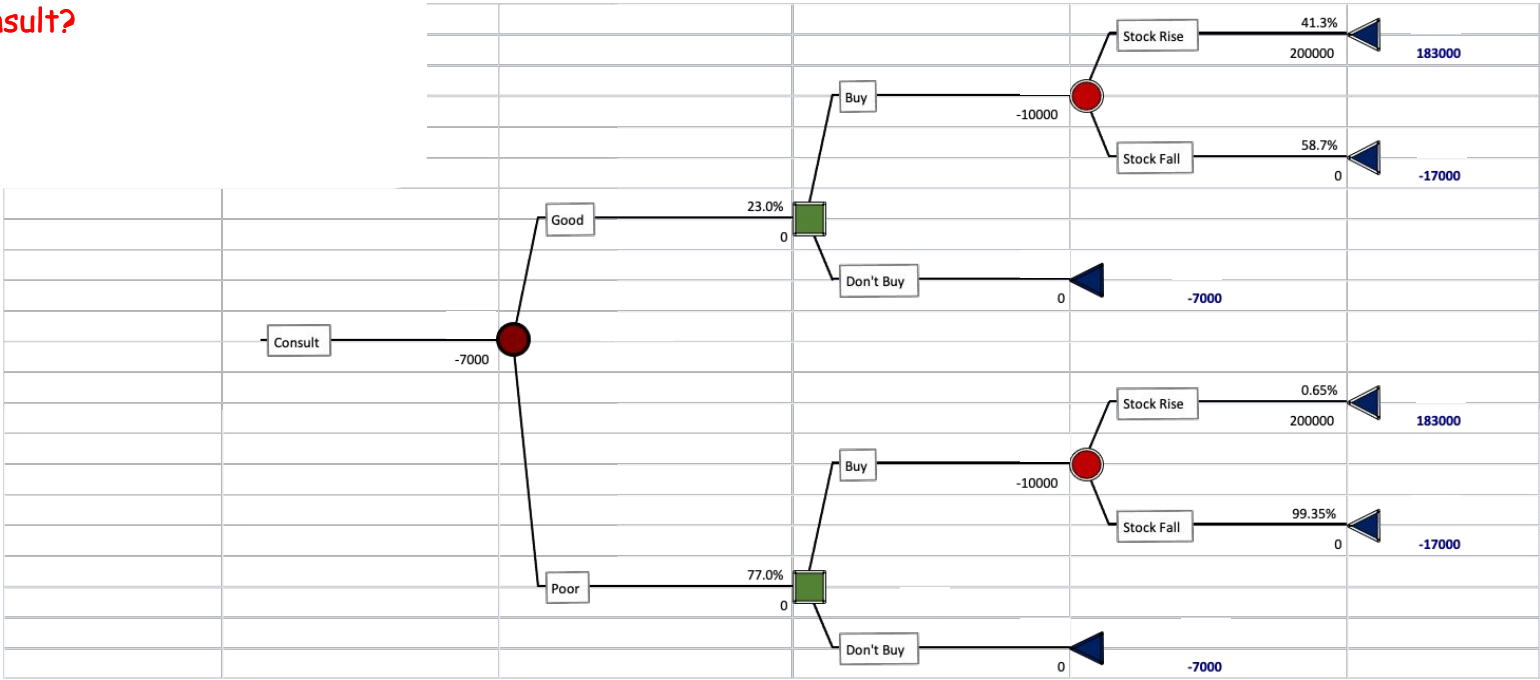
$$P(\text{rise}|\text{"good"}) = 0.413$$

$$P(\text{fall}|\text{"good"}) = 0.587$$

$$P(\text{rise}|\text{"poor"}) = 0.065$$

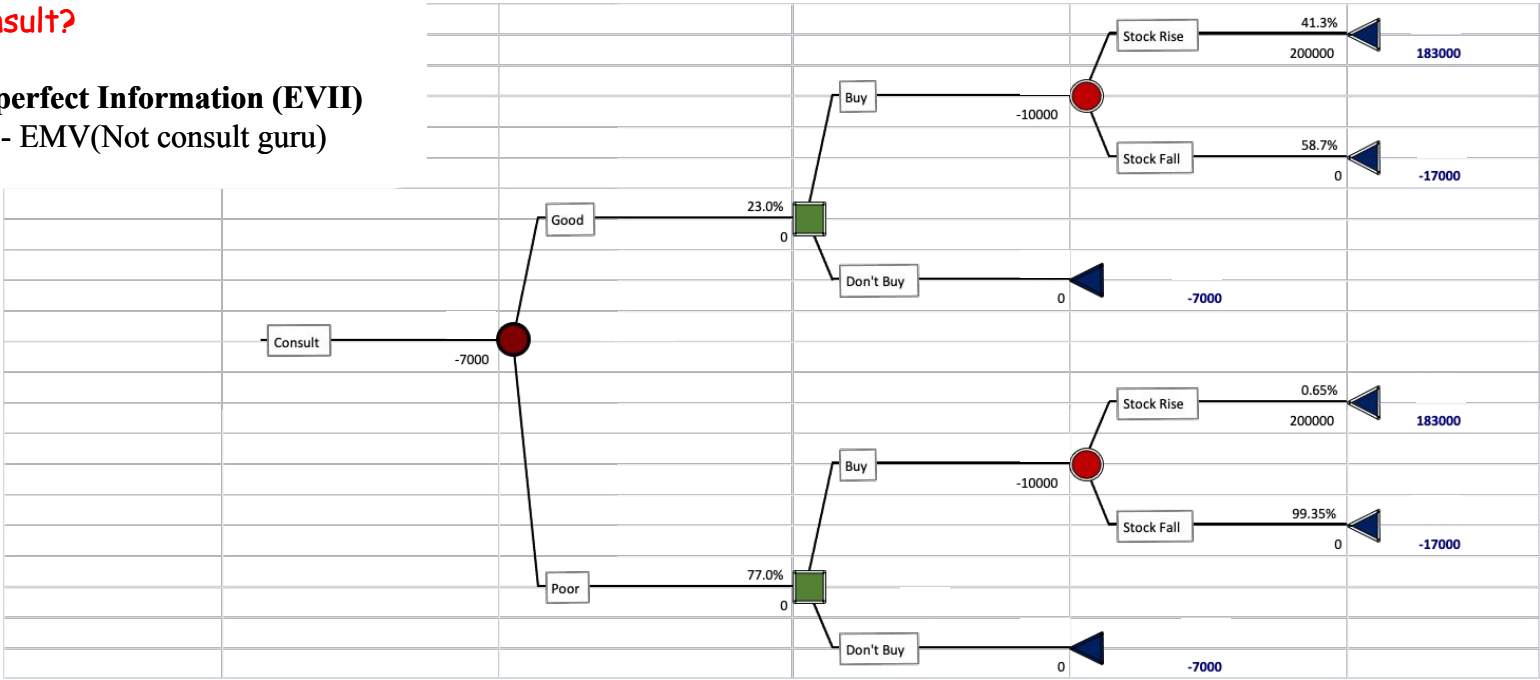
$$P(\text{fall}|\text{"poor"}) = 0.9935$$

Should Mr. Bean consult?



Should Mr. Bean consult?

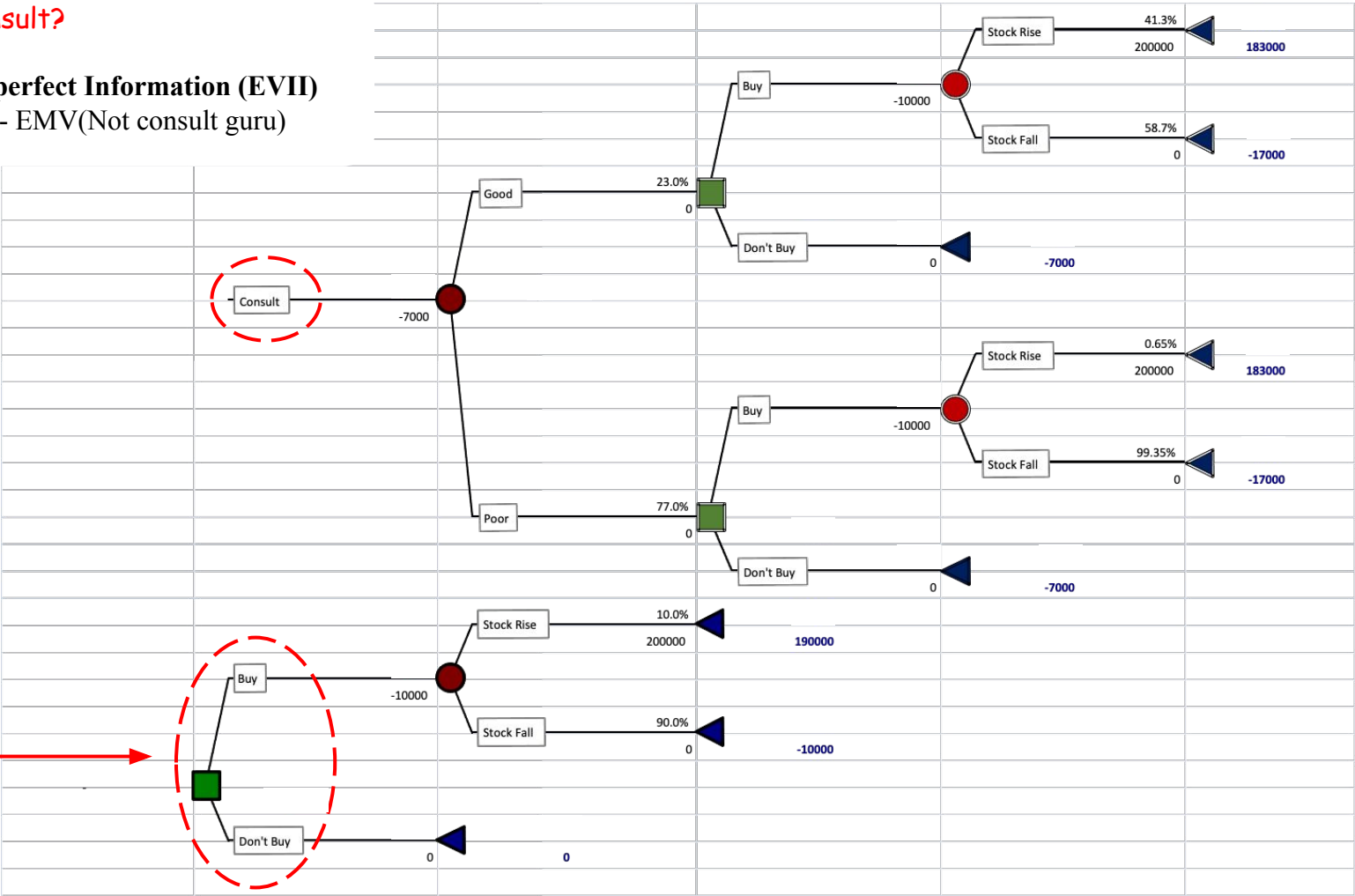
Expected Value of Imperfect Information (EVII)
= EMV(Consult Guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)
= EMV(Consult Guru) - EMV(Not consult guru)

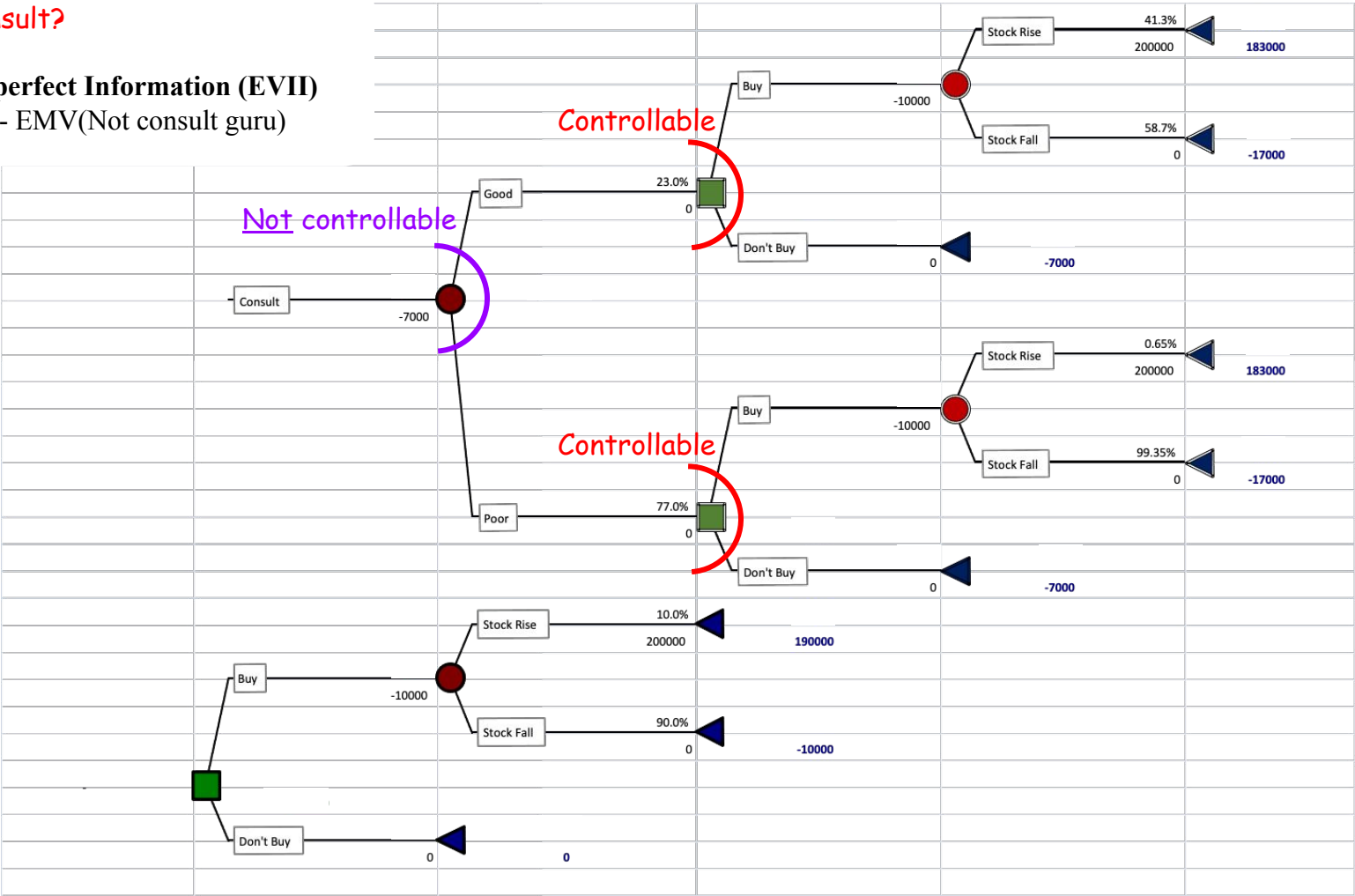
Problem 1 →



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

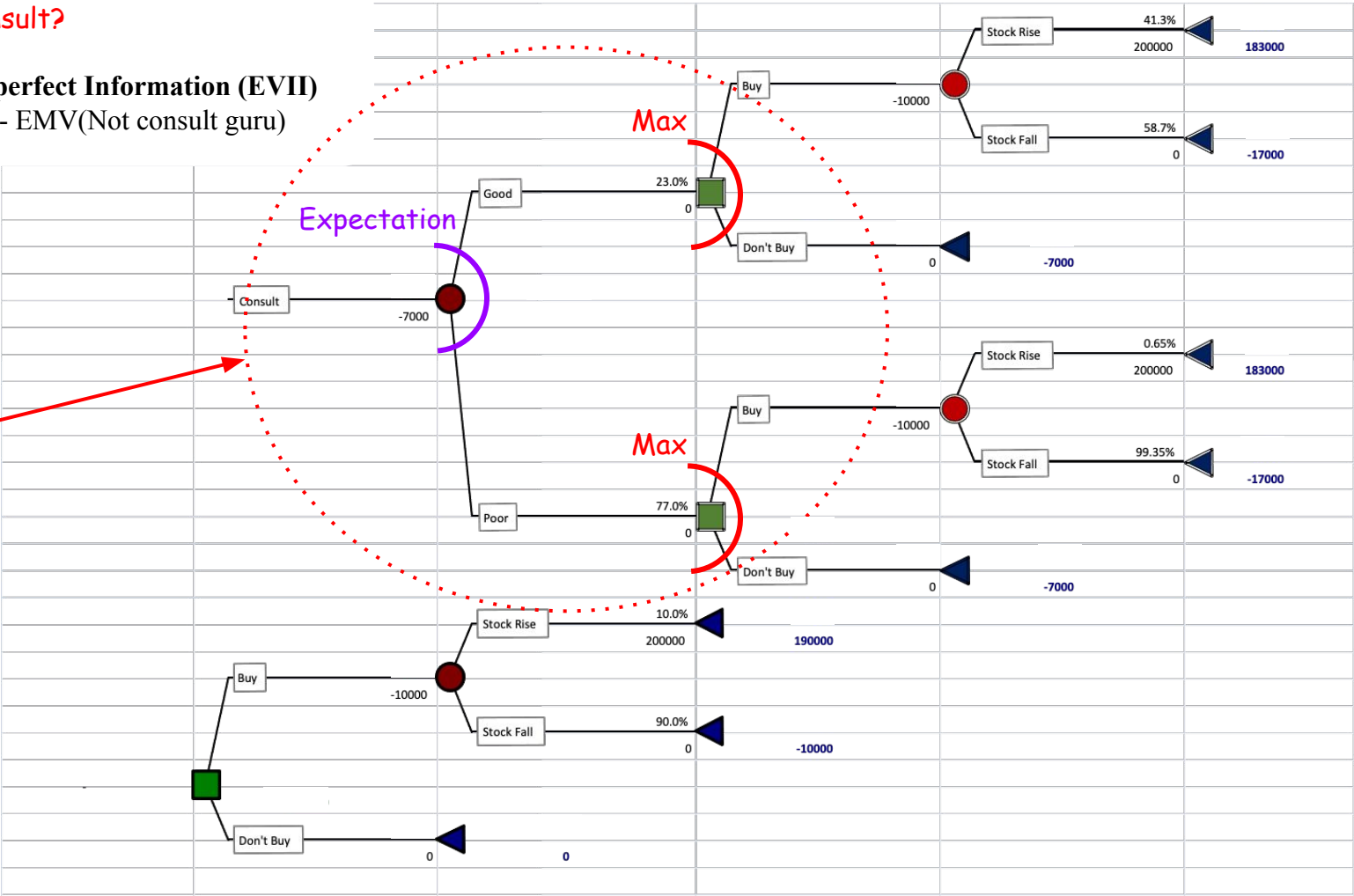
= EMV(Consult Guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)
= EMV(Consult Guru) - EMV(Not consult guru)

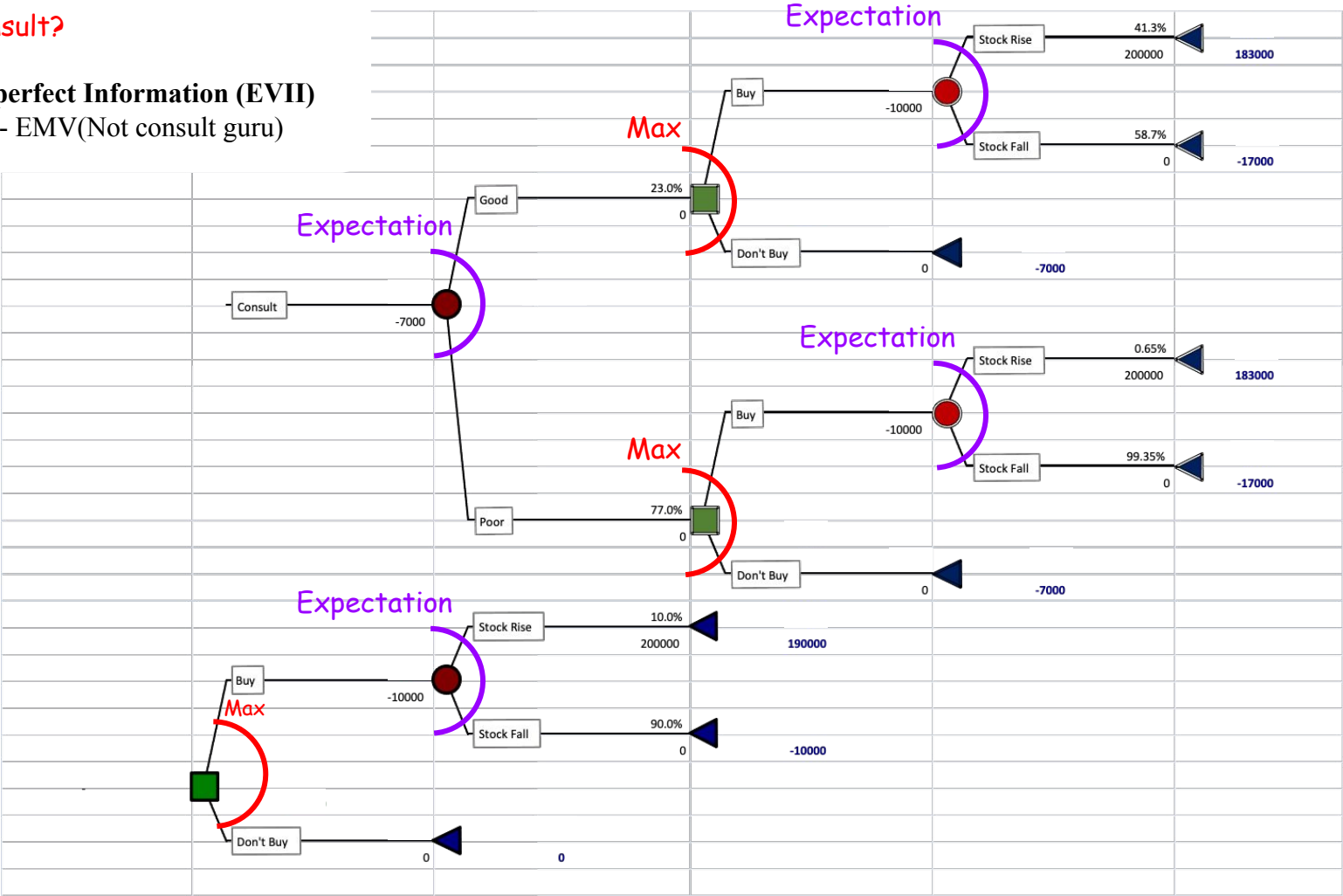
Expectimax!



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

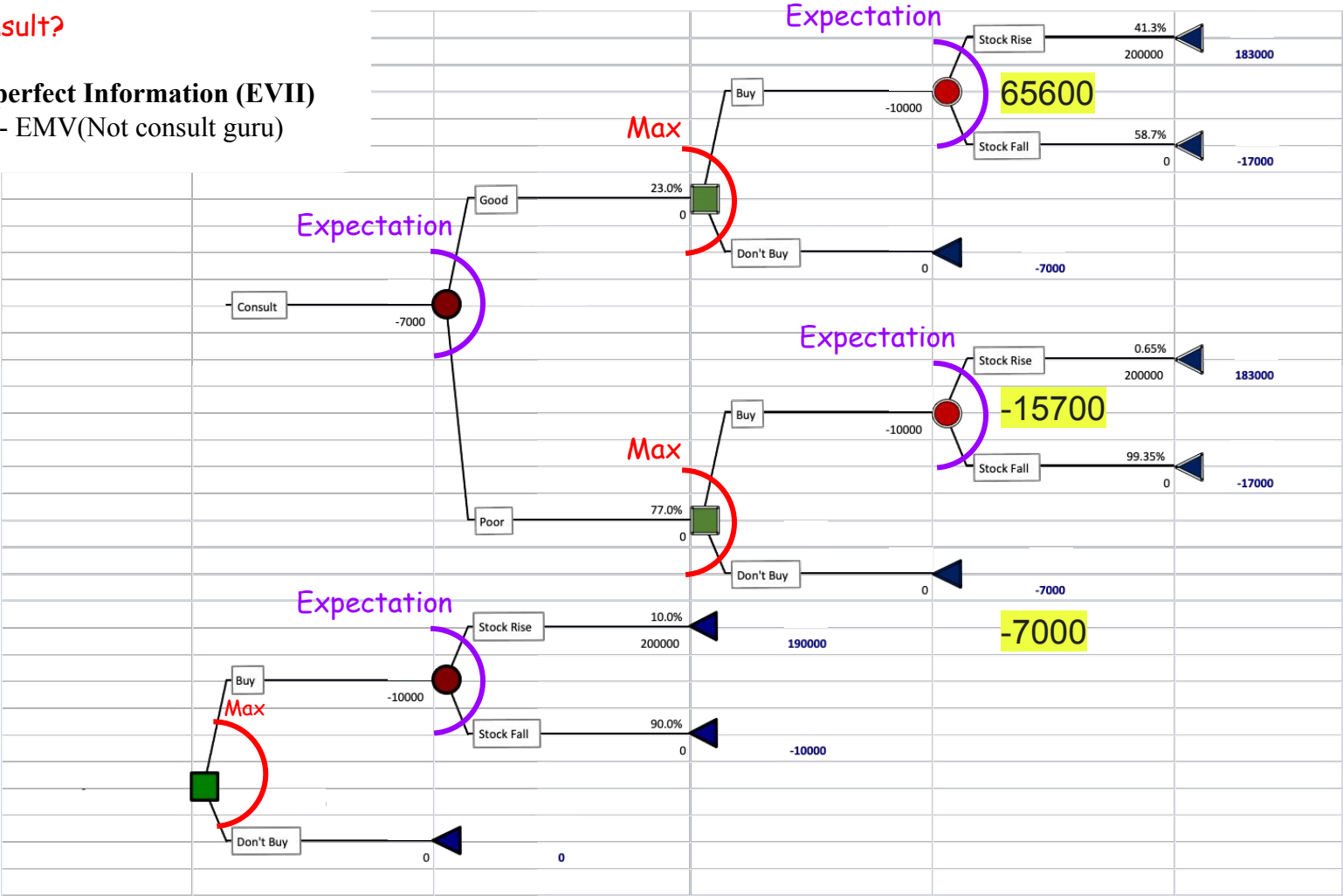
= EMV(Consult Guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

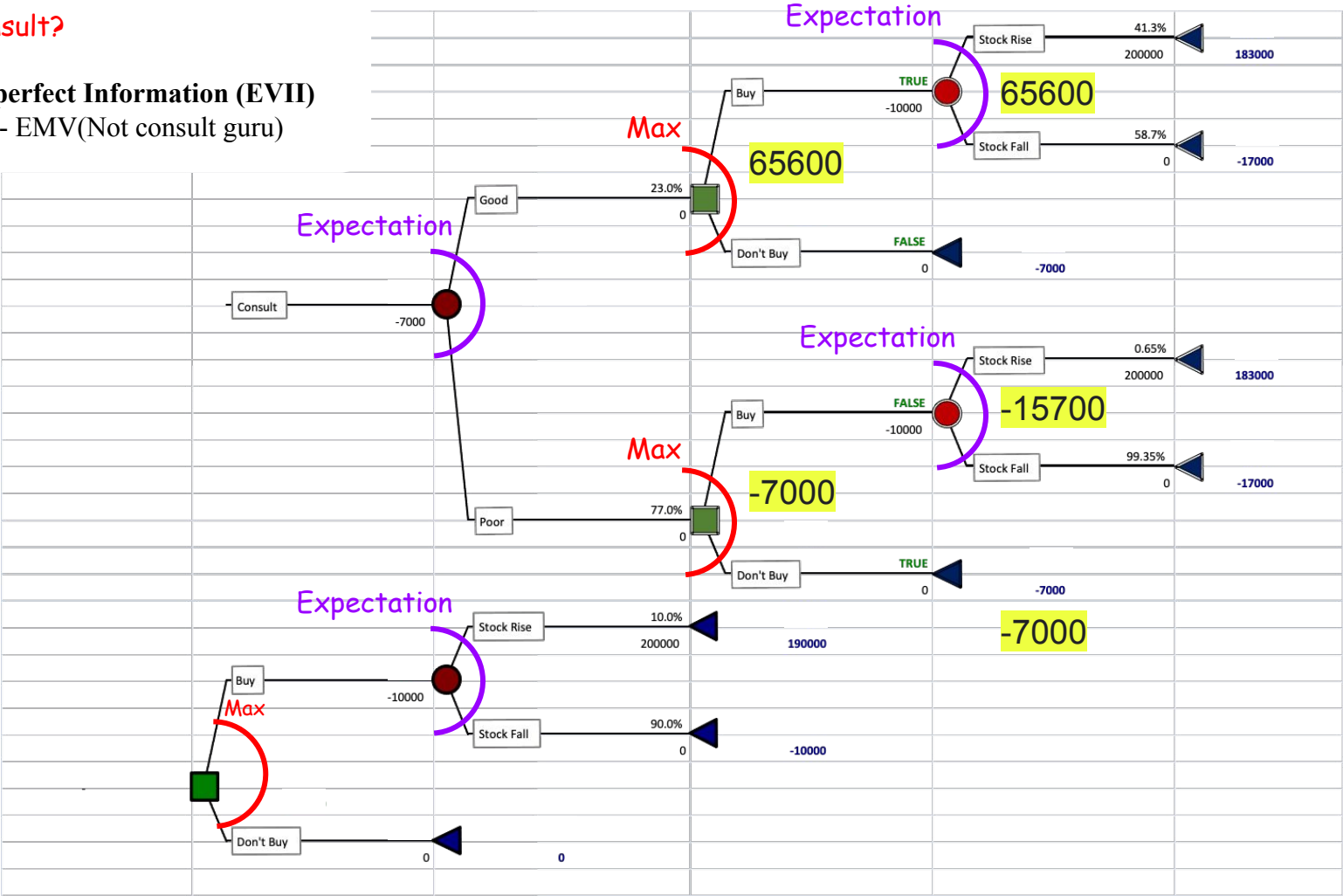
= EMV(Consult guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

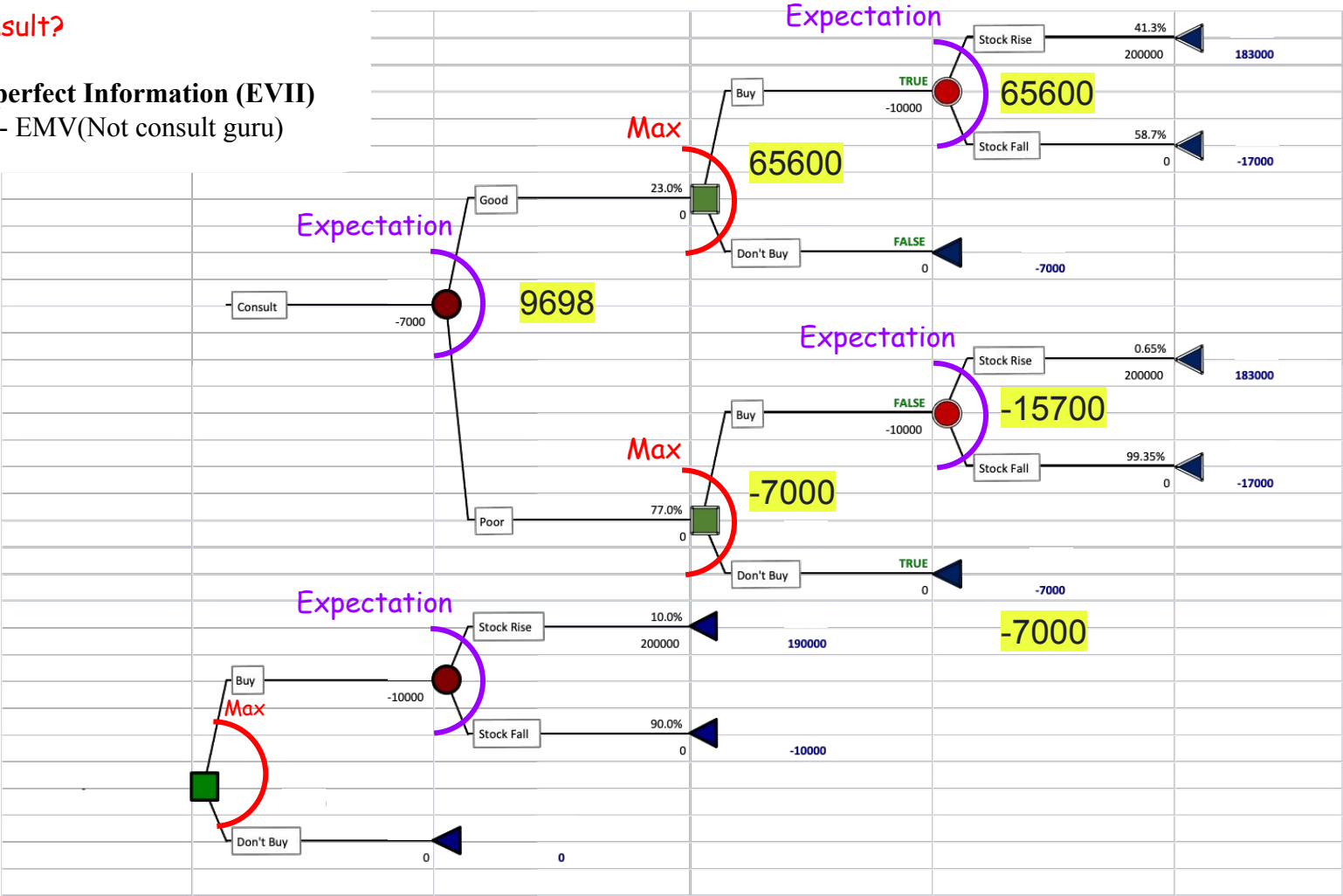
= EMV(Consult guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

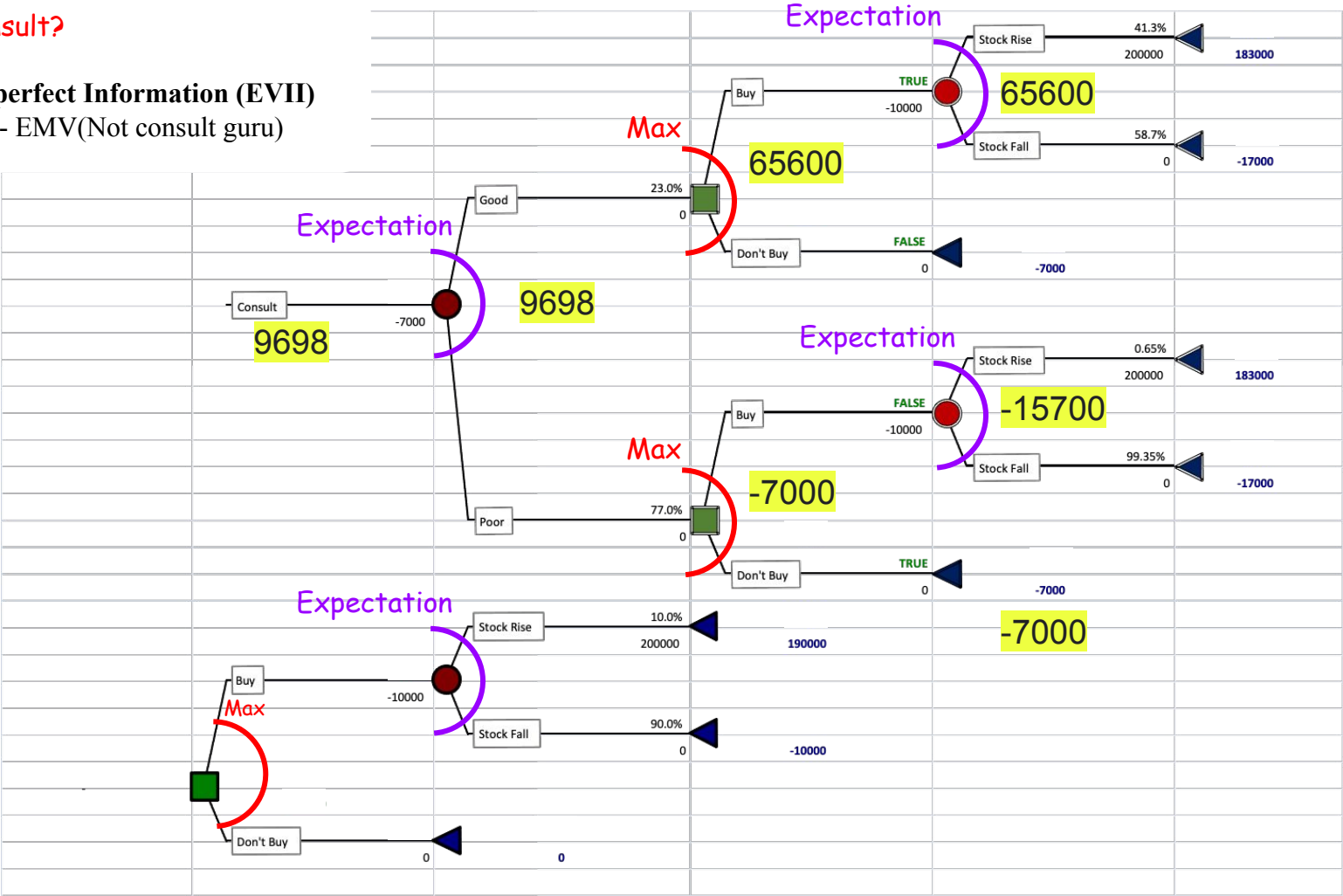
= EMV(Consult guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

= EMV(Consult guru) - EMV(Not consult guru)

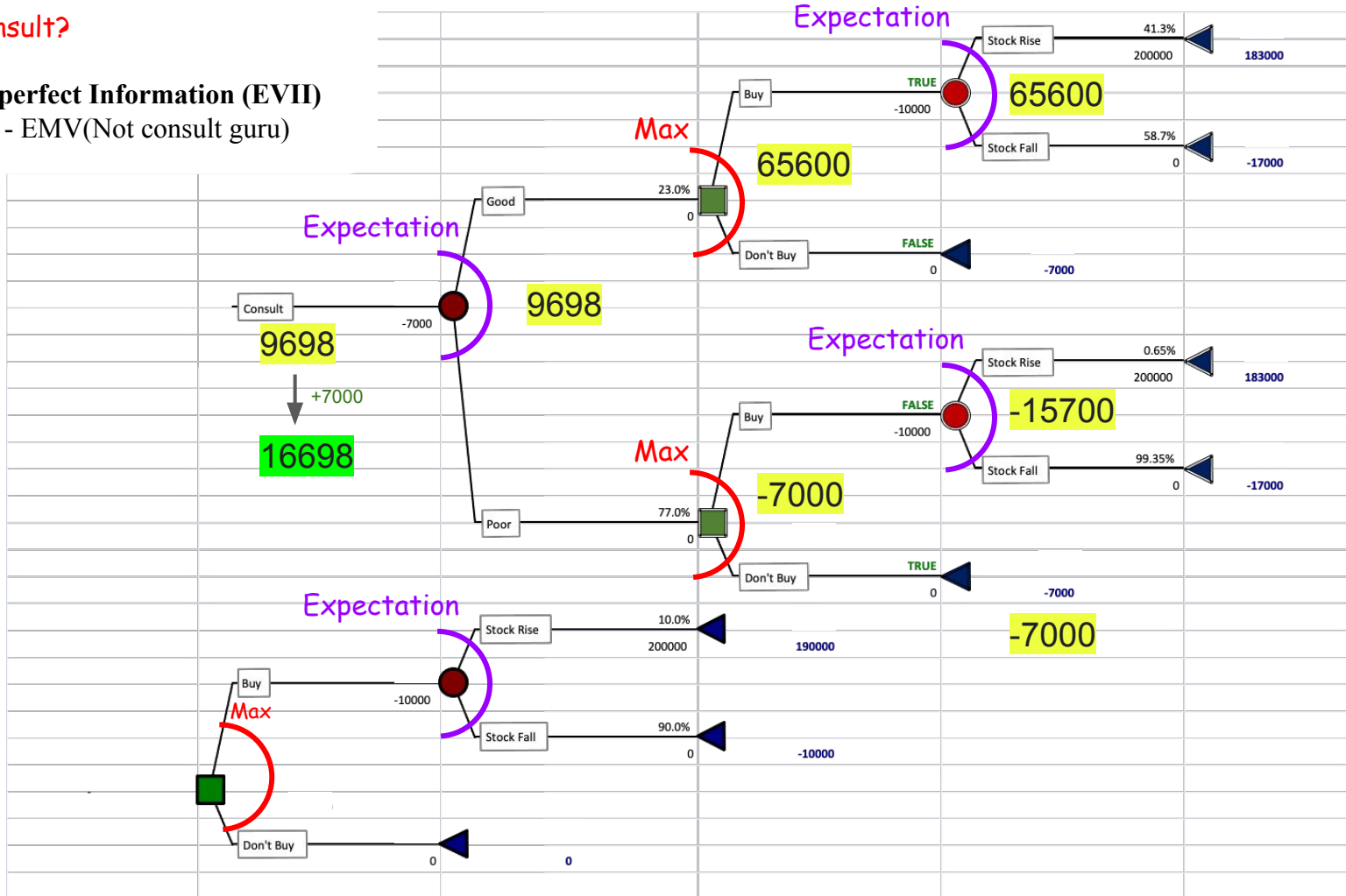


Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

$$= \text{EMV}(\text{Consult Guru}) - \text{EMV}(\text{Not consult guru})$$

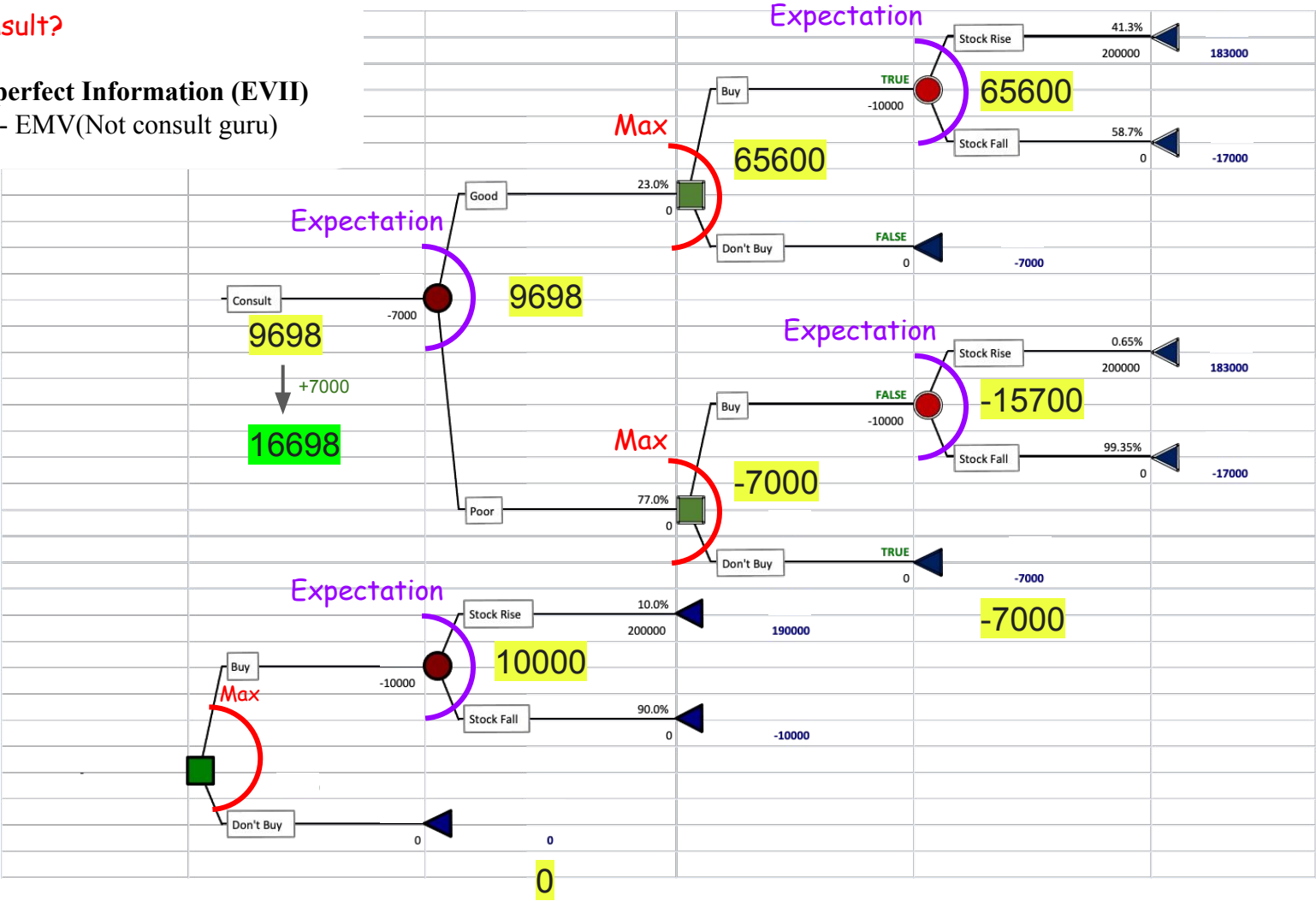
EVII is always calculated assuming the cost is zero, i.e., assuming the information is free.



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

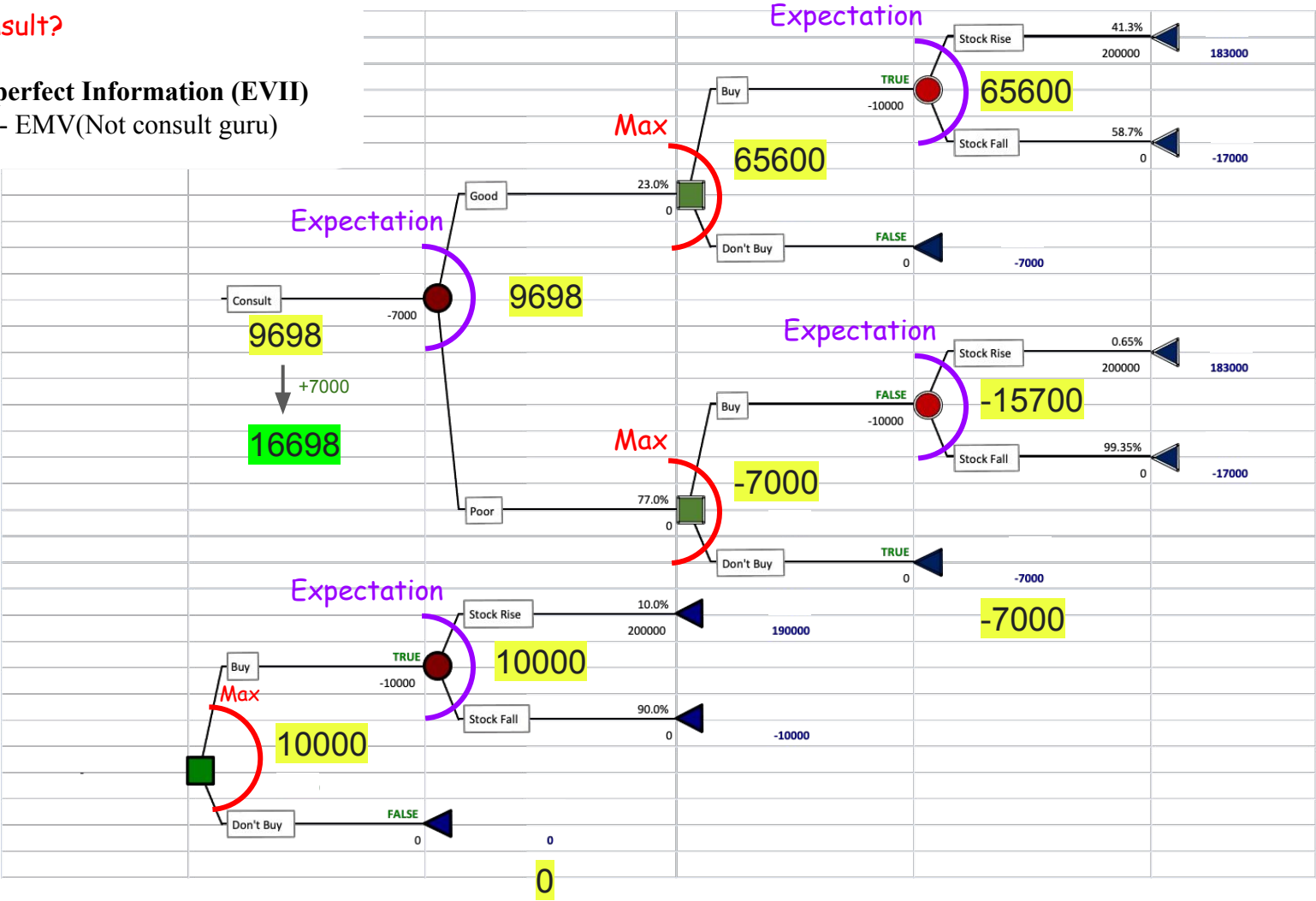
= EMV(Consult Guru) - EMV(Not consult guru)



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

= EMV(Consult Guru) - EMV(Not consult guru)



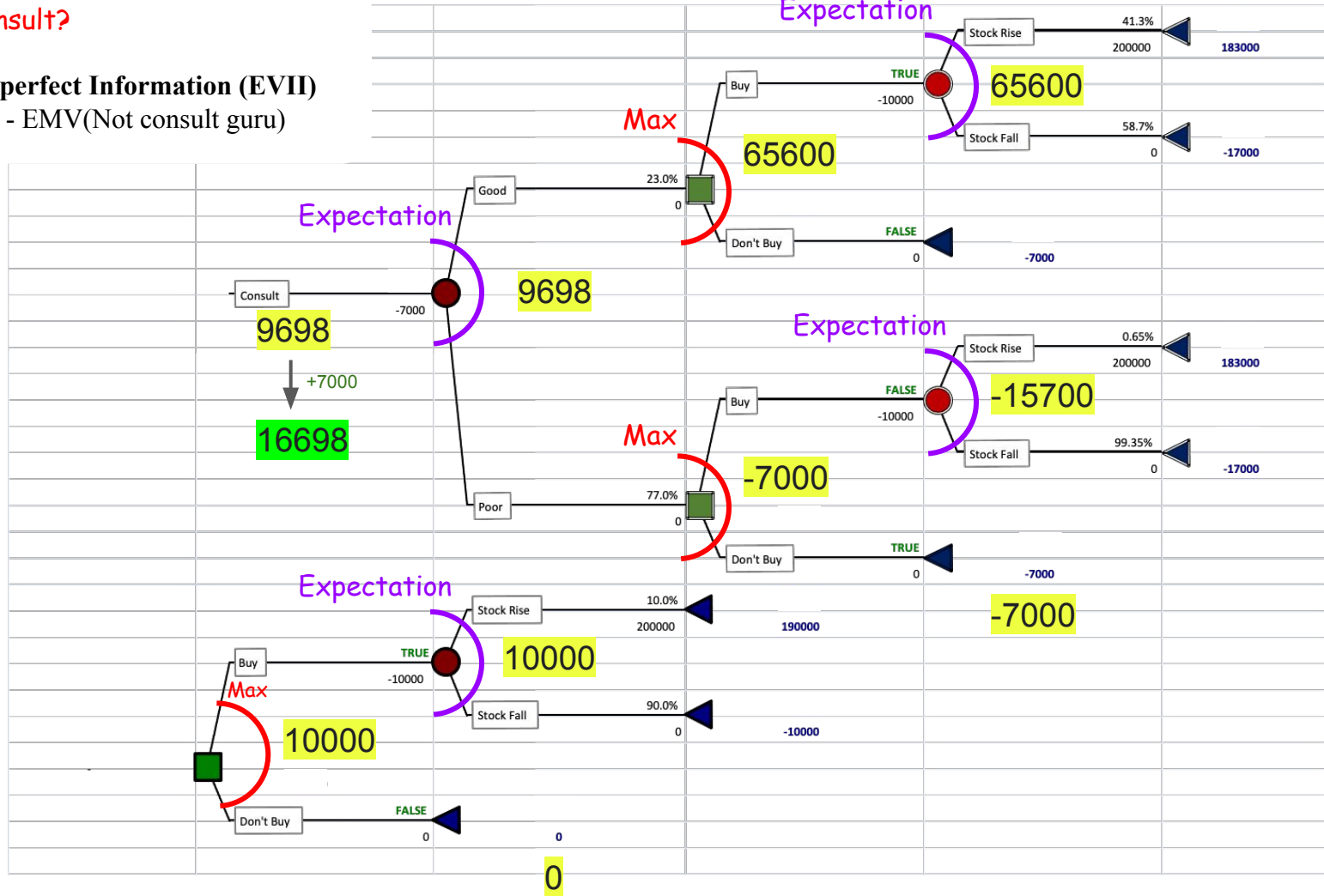
Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

= EMV(Consult Guru) - EMV(Not consult guru)

= 16698 - 10000

= **6698**



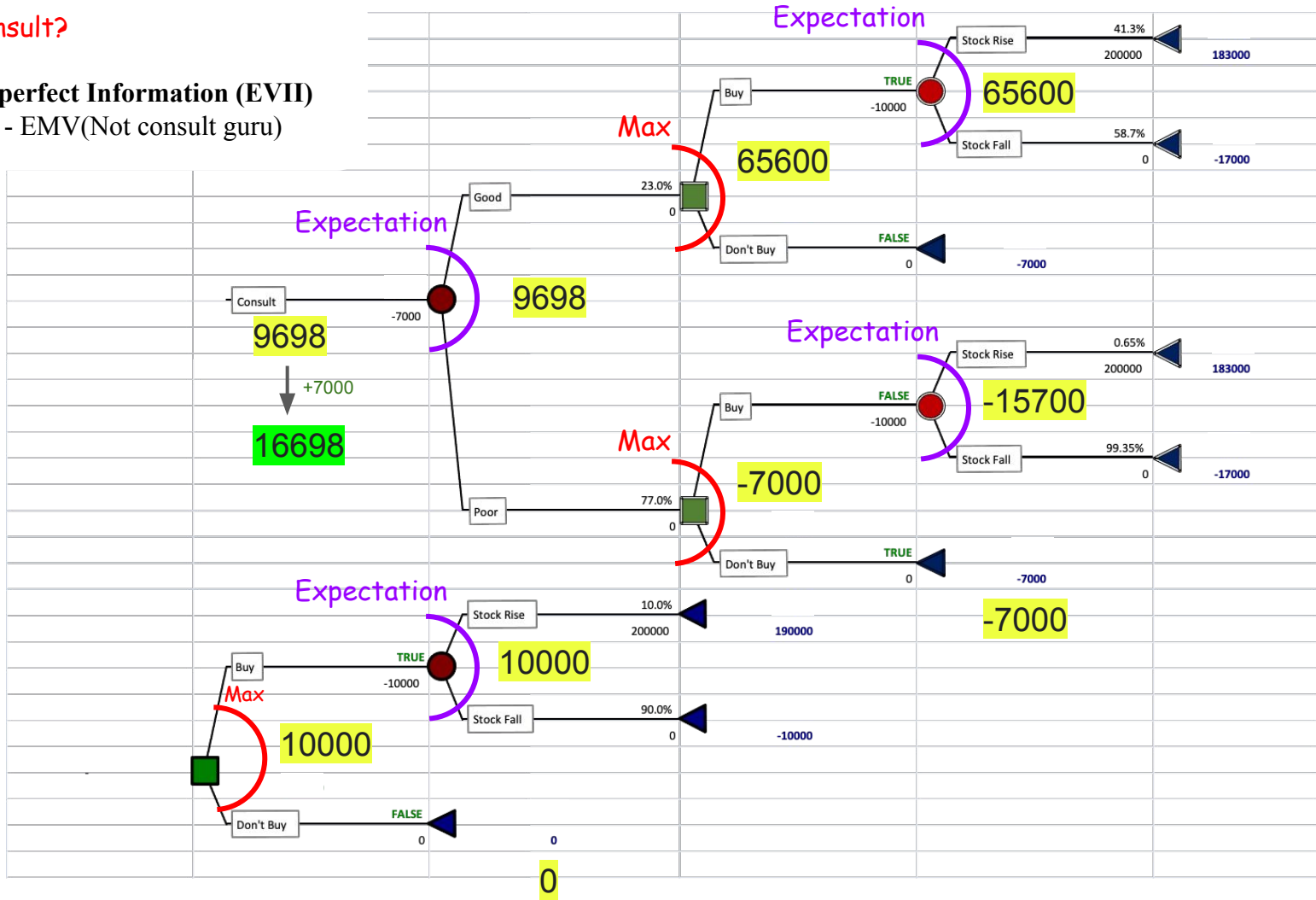
Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

$$= \text{EMV}(\text{Consult Guru}) - \text{EMV}(\text{Not consult guru})$$
$$= 16698 - 10000$$

= 6698 < 7000 (cost)

Not worth it!



Should Mr. Bean consult?

Expected Value of Imperfect Information (EVII)

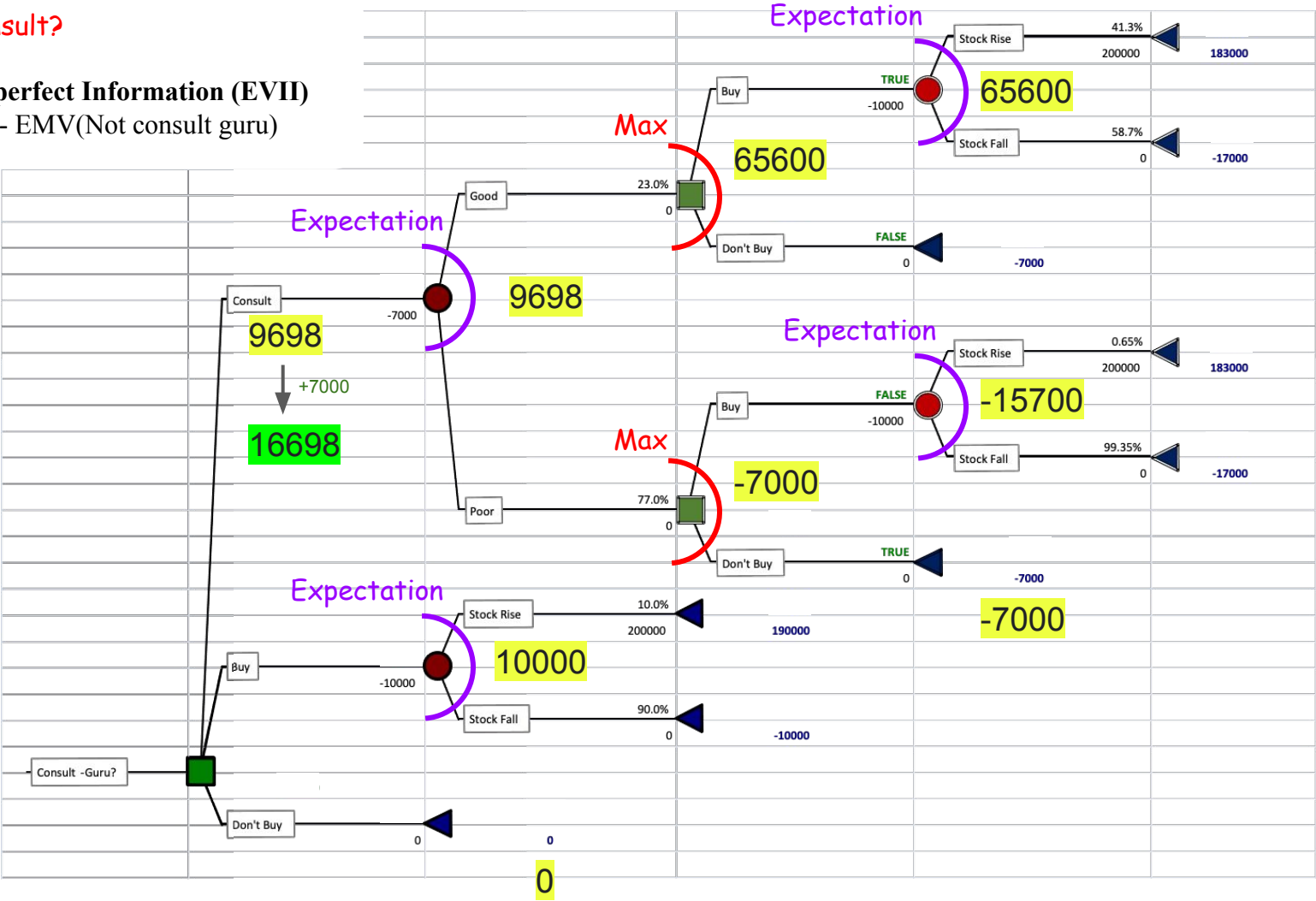
= EMV(Consult Guru) - EMV(Not consult guru)

= 16698 - 10000

= **6698** < 7000 (cost)

Not worth it!

Complete tree:



Should Mr. Bean consult?

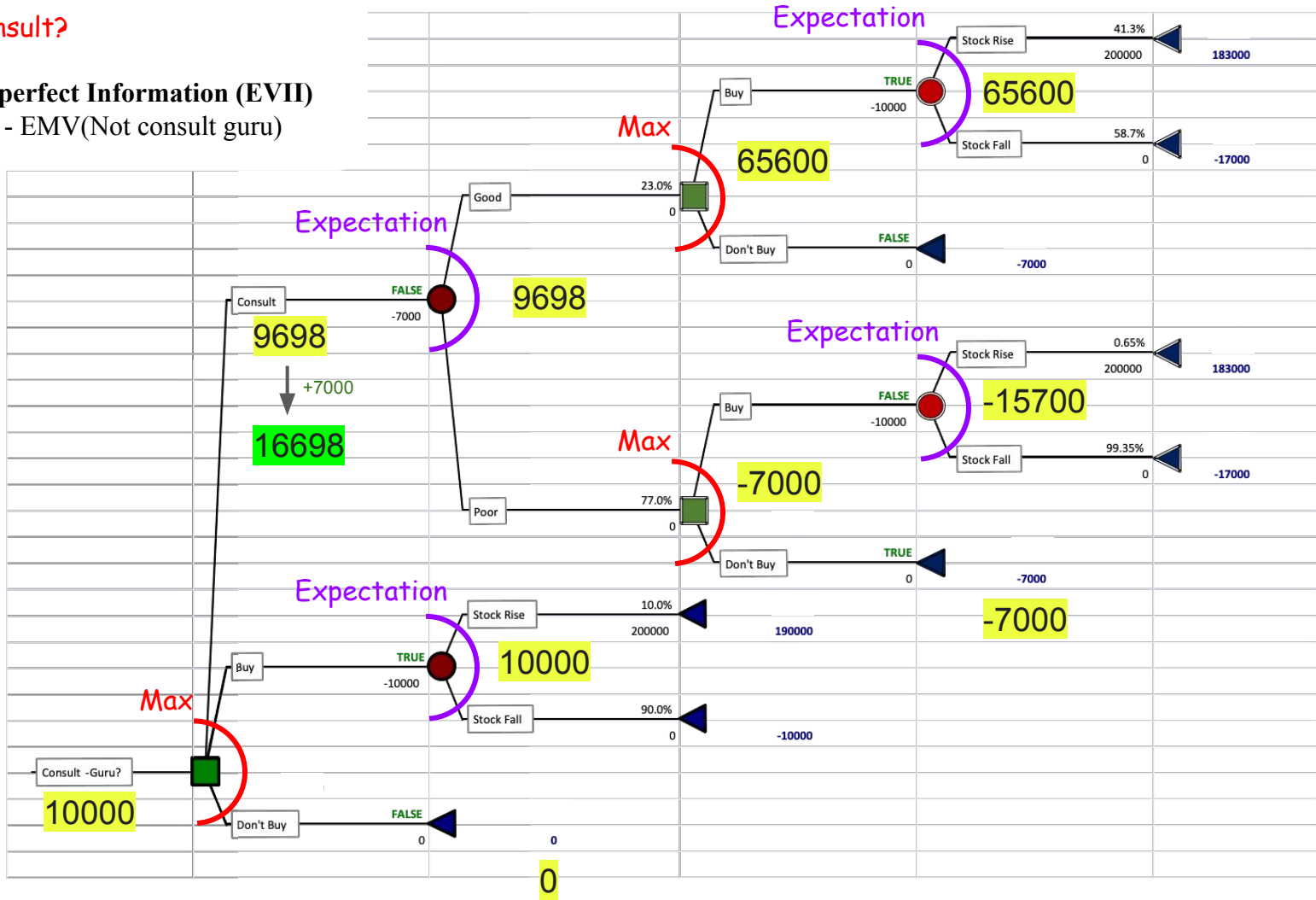
Expected Value of Imperfect Information (EVII)

$$= \text{EMV}(\text{Consult Guru}) - \text{EMV}(\text{Not consult guru})$$
$$= 16698 - 10000$$

= 6698 < 7000 (cost)

Not worth it!

Complete tree:



Question?

<EOF>

Credits

Decision tree and influence diagram images are adapted (with modifications) from the amazing works by **Abhinit** and **Evangelos**.