

CS1231 Review 18

1. The number of r -permutations of a set of n distinct elements (**no repetition allowed**) is $P(n, r) = \frac{n!}{(n-r)!} = \underbrace{n \cdot (n-1) \cdots (n-r+1)}_r$.
2. The number of r -permutations of a set of n distinct elements **with repetition allowed** is $n^r = \underbrace{n \cdot n \cdots n}_r$.
3. The number of r -combinations of a set of n distinct elements (**no repetition allowed**) is $\binom{n}{r} = \frac{n!}{r!(n-r)!}$.
4. The number of r -combinations of a set of n distinct elements **with repetition allowed** is $\binom{n+r-1}{r}$.
5. The number of **nonnegative** integer solutions of the equation

$$x_1 + x_2 + \cdots + x_n = r$$

is $\frac{\binom{n+r-1}{r}}{r}.$

6. The number of **positive** integer solutions of the equation

is $\binom{r-1}{n-1}$.

$$x_1 + x_2 + \cdots + x_n = r$$

$n-1$
 > 0

7. A **graph** $G = (V, E)$ consists of V , a nonempty finite set of vertices and E , a set of edges.

8. Each edge is associated with either one or two vertices called its end point(s)

9. An edge with one endpoint is called a loop.



10. If more than one edge are associated with a pair of vertices, such edges are called multiple edges



11. A graph with no loops or multiple edges is simple graph.

12. A graph with no loops but admits multiple edges is called a multigraph.

13. A **Digraph** $G = (V, E)$ consists of V , a nonempty finite set of vertices and E , a set of directed edges.



14. The directed edge associated with the ordered pair (u, v) is said to start from u and end at v and is denoted as $\overrightarrow{u, v}$.