# A Note On Two Sample Tests

### What we want to test

Given two populations,

Population 1  $\mu_1, \sigma_1^2$ 

Population 2  $\mu_2, \sigma_2^2$ 

Is  $\mu_1 = \mu_2$ ?

Obviously,  $\mu_1$  and  $\mu_2$  are not known to us. Typically,  $\sigma_1^2$  and  $\sigma_2^2$  are not known to us as well.

# What we have

Sample 1 drawn from population 1, and sample 2 drawn from population 2.

Sample 1 of size  $n_1$ 

 $\overline{x}, s_1^2$ 

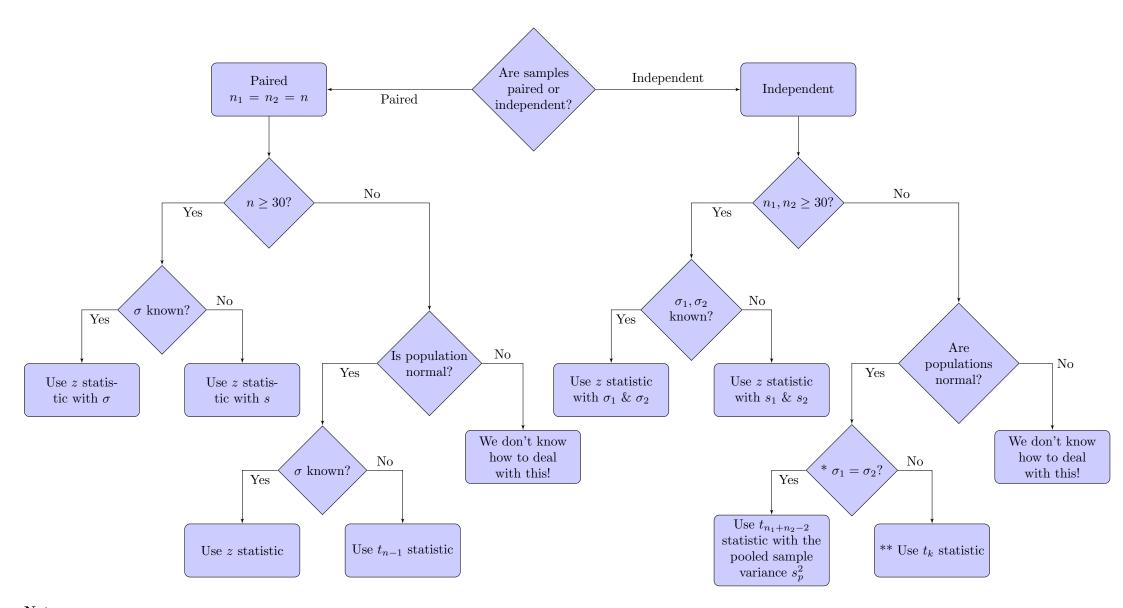
Sample 2 of size  $n_2$ 

 $\overline{y}, s_2^2$ 

By comparing  $\overline{x}$  with  $\overline{y}$ , check if  $\mu_1 = \mu_2$ , say.

## What we do

Use one of the two sample tests depicted in the following flow chart.



#### Notes

- \* In practice, to check if  $\sigma_1^2 = \sigma_2^2$ , we use the F-test as outlined in Section 7.6.
- \*\* This is not covered in this course. We use a t-statistic with degree of freedom k estimated by the integer part of  $\frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\frac{(s_1^2/n_1)^2}{n_1 1} + \frac{(s_2^2/n_2)^2}{n_2 1}}$