

#### Lecture #16

## Quine-McCluskey



### Lecture #16: Quine-McCluskey

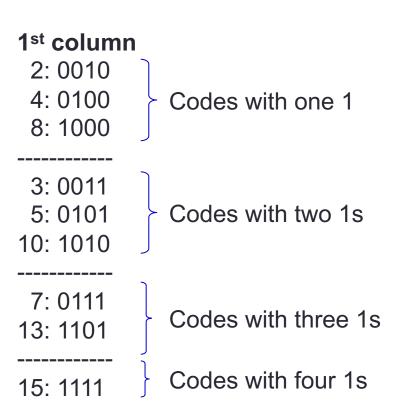
This topic is only for your own reading only.

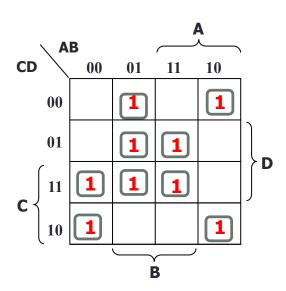
- A tabulation method similar in concept to K-map
- Applicable for functions with any number of variables
  - K-maps are useful for functions with at most 5 or 6 variables
- Tedious on paper, but can be automated (programmed)
- Non-examinable
  - But knowing it may enhance your understanding of K-maps

### Pls and EPls

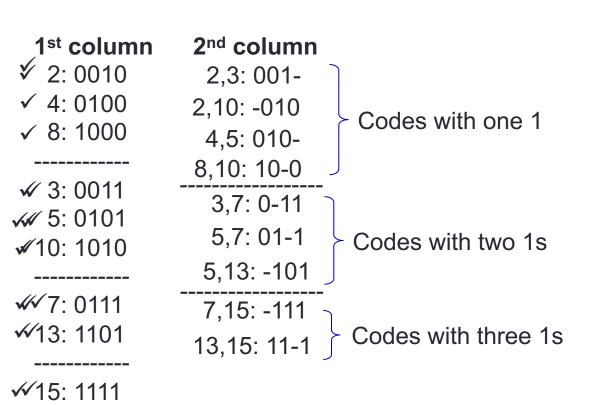
- To find the simplest SOP expression from a K-map, you need to obtain:
  - Minimum number of literals per product term; and
  - Minimum number of product terms.
- Achieved through K-map using
  - Biggest groupings of minterms (prime implicants) where possible; and
  - No redundant groupings (look for essential prime implicants)

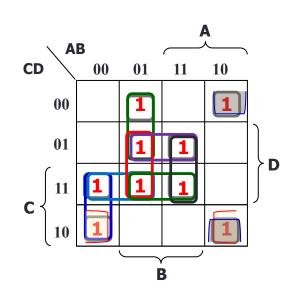
Step 1: List out all minterms in groups with same number of 1s in their binary codes.





Step 2: Combine codes that differ by 1 bit into bigger group, write the combined code in next column.





Step 3: Repeat step 2 – Combine codes that differ by 1 bit into bigger group, write the combined code in next column.

```
1st column
                  2<sup>nd</sup> column
✓ 2: 0010
                    2,3: 001-

√ 4: 0100

                   2,10: -010

√ 8: 1000

                    4,5: 010-
                   8,10: 10-0

√ 3: 0011

√ 5: 0101

                    3,7: 0-11
√10: 1010

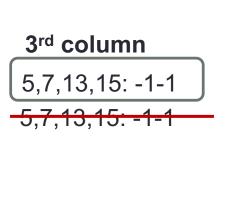
√ 5,7: 01-1

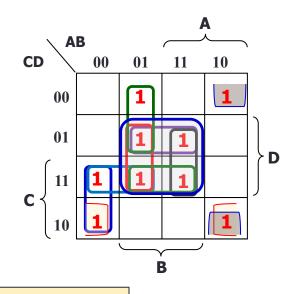
                 √ 5,13: -101

√ 7: 0111

√13: 1101
                 √ 7,15: -111
                 √13,15: 11-1
```

**√**15: 1111





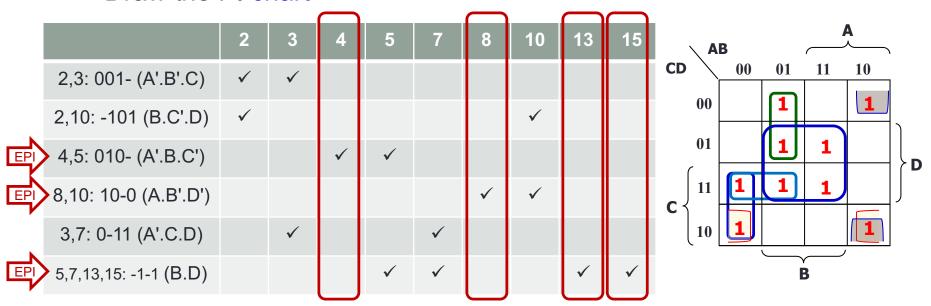
We have completed

Phase 1: Identifying all the

Prime Implicants (PIs)!

### Phase 2: Identify the Essential Prime Implicants (EPIs)

Draw the PI chart



Where are the EPIs? Look for columns containing a single tick.

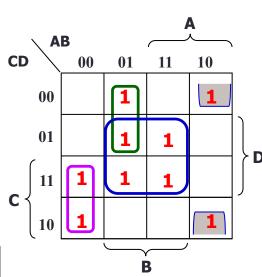
EPIs are: A'.B.C', A.B'.D', and B.D

But we are not done yet. There are still minterms not covered by the EPIs!

### Phase 2: After identifying the EPIs

Draw the reduced PI chart if there are minterms not covered





- 1. Find out what are the minterms covered by the EPIs.
- 2. Remove the EPIs and minterms they cover from the chart → reduced PI chart.

Answer: B.D + A'.B.C' + A.B'.D' + A'.B'.C

3. Find the minimum number of remaining PIs to cover the remaining minterms.

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