## CS1231 Review 14

- 1. Let  $m \in \mathbb{N}$  and  $a \in \mathbb{Z}$ . An integer  $\overline{a}$  such that  $\underline{\mathbb{Q} \cdot \overline{a}} = \underline{\mathbb{Z}} \mod m$  is called an inverse of a modulo m.
- 2. Let  $m \in \mathbb{N}$  and  $a \in \mathbb{Z}$ . Then the inverse of a modulo m exists iff  $\underline{gcd(a,m)=1}$ .

  The inverse, if exists, is unique modulo m, i.e., if c, d are inverses, then  $\underline{d} = \underline{c} \quad \underline{modm}$ .
- 3. (Fermat's Little Theorem) If p is a prime and  $a \in \mathbb{Z}$  such that gcd(p, a) = 1, then  $\underline{ \alpha^{P-1} \equiv 1 \mod p}.$