

Trees

CS4248 Natural Language Processing

Week 09

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Recap of Week 08

Recurrent Neural Networks: Modeling sequences, NN style

Conditional Language Models: LMs with inputs

Encoder-Decoder: When Conditional LMs are implemented NN style

Solving the encoding bottleneck: Attention Mechanism

Searching more effectively: Beam Search Decoding



Week 09 Agenda

Context-Free Grammar (CFG)
Chomsky Normal Form (CNF)

Syntactic Parsing
Statistical Parsing



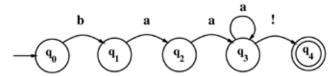
Context Free Grammars (CFG)

Recap: Regular and Context Free Languages

From Week 02: Equivalence among Regex, Regular Languages

and Finite State Automata (FSA).

A regex is an equivalent to an FSA.



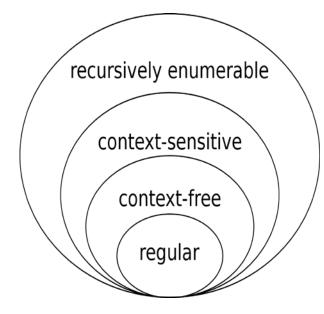
RE: /baa+!/

baa! baaa! baaaa! baaaaa!

•••

	Input		
State	b	а	!
0	1	0	0
1	0	2	Ø
2	0	3	Ø
3	0	3	4
4:	0	Ø	Ø

statetransition table



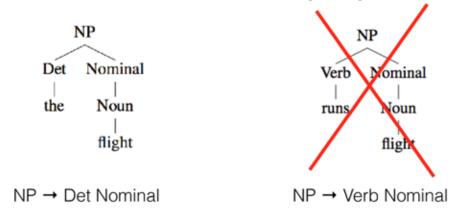
Slides adapted from Hwee Tou Ng (NUS). Picture from Wikipedia.



Context Free Grammar

A CFG gives a formal way to define what meaningful constituents are and exactly how a constituent is formed out of other constituents (or words).

It defines the valid structures in a language.





Definition of CFG

A context-free grammar defines how symbols in a language combine to form valid structures

NP	→	Det Nominal
NP	→	ProperNoun
Nominal	\rightarrow	Noun Nominal Noun
Det	→	a the
Noun	\rightarrow	flight







Definition of CFG

N	Finite set of non-terminal symbols	NP, VP, S
Σ	Finite alphabet of terminal symbols	the, dog, a
R	Set of production rules, each $A \rightarrow \beta$ $\beta \in (\Sigma, N)$	S → NP VP Noun → dog
S	Start symbol	

What part of this specification makes this context-free?

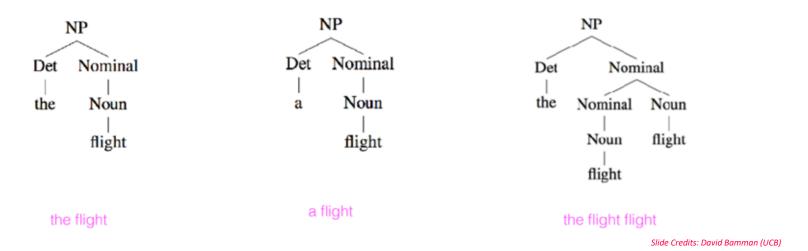
Infinite strings from finite productions

- This is the house
- This is the house that Jack built
- This is the cat that lives in the house that Jack built
- This is the dog that chased the cat that lives in the house that Jack built
- This is the flea that bit the dog that chased the cat that lives in the house the Jack built
- This is the virus that infected the flea that bit the dog that chased the cat that lives in the house that Jack built



Definition of Derivation

Given a CFG, a derivation is the sequence of productions used to generate a string of words (e.g., a sentence), often visualized as a parse tree.





Constituents

Constituents are group of words that behave as a single unit.

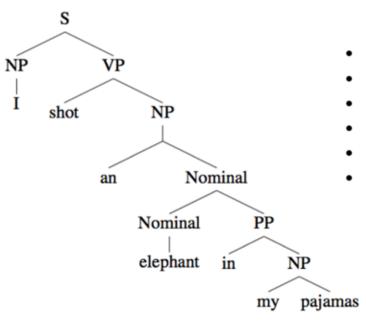
Linguists characterize constituents in a number of ways, including:

- where they occur (e.g., "NPs can occur before verbs")
- where they can move in variations of a sentence
 - On March 19th, I'd like to fly from Atlanta to Denver
 - I'd like to fly on March 19th from Atlanta to Denver
 - I'd like to fly from Atlanta to Denver on March 19th
- what parts can move and what parts can't
 - X On March I'd like to fly 19th from Atlanta to Denver
- what they can be conjoined with
 - I'd like to fly from Atlanta to Denver on March 17th and in the morning

Adapted from Dan Jurafsky (Stanford)



Definition of Constituents



Every internal node is a phrase

- my pajamas
- in my pajamas
- · elephant in my pajamas
- an elephant in my pajamas
- shot an elephant in my pajamas
- I shot an elephant in my pajamas

Each phrase could be replaced by another of the same type of constituent

NUS National University of Singapore School of Computing

Ambiguity, Revisited



Why is ambiguity a problem in NLP?

Picture Credits: https://examples.yourdictionary.com/reference/examples/examples-of-ambiguity.html



Ambiguity

There are multiple ways to interpret a sentence

Structural Ambiguity: When a grammar can assign more than one parse to a sentence.



Ambiguity

There are multiple ways to interpret a sentence

Structural Ambiguity: When a grammar can assign more than one parse to a sentence.

Why would this become a problem?



Structural Ambiguity

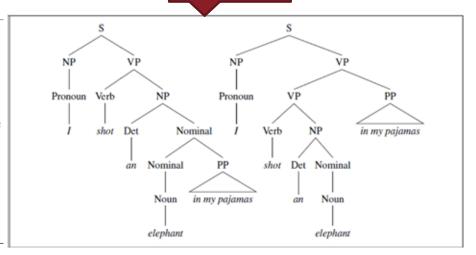
Which one is correct?

Lexicon Grammar $S \rightarrow NPVP$ Det → that | this | the | a $S \rightarrow Aux NP VP$ Noun → book | flight | meal | money $Verb \rightarrow book \mid include \mid prefer$ $S \rightarrow VP$ NP → Pronoun Pronoun $\rightarrow I \mid she \mid me$ NP → Proper-Noun Proper-Noun → Houston | NWA $NP \rightarrow Det Nominal$ $Aux \rightarrow does$ Nominal → Noun Preposition \rightarrow from | to | on | near | through Nominal → Nominal Noun $Nominal \rightarrow Nominal PP$ $VP \rightarrow Verb$ $VP \rightarrow Verb NP$

VP → Verb NP PP

PP → Preposition NP

 $VP \rightarrow Verb PP$ $VP \rightarrow VP PP$





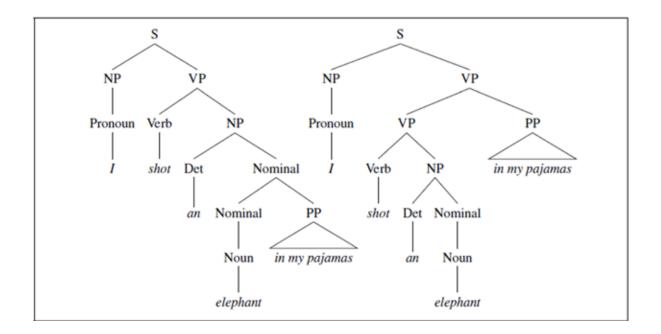
Structural Ambiguity

Two common kinds of structural ambiguity

- 1. Attachment Ambiguity
 - a particular constituent can be attached to the parse tree at more than one place
- 2. Coordination Ambiguity
 - phrases can be conjoined by a conjunction like "and"

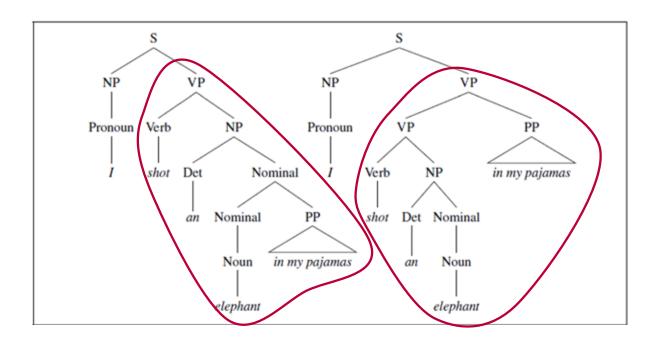


Attachment Ambiguity





Attachment Ambiguity Cont.



Relating "in my pajamas" to "an elephant" or modifying "shot"



How many interpretations?

"the best roti prata and laksa"



Coordination Ambiguity

"the best roti prata and laksa"

- [the best [[roti prata] and [laksa]]
- 2. [[the best [roti prata]] and [laksa]]



Solving Ambiguity

The fact that there are many grammatically correct parses but which are unreasonable semantically becomes a problem.

How can we solve this problem?



Solving Ambiguity

The fact that there are many grammatically correct parses but which are unreasonable semantically becomes a problem.

How can we solve this problem?

- 1. Syntactic Parsing: Extract all possible parses for a sentence
- Syntactic Disambiguation: Score all parses and return the best parse



How do we evaluate parses?

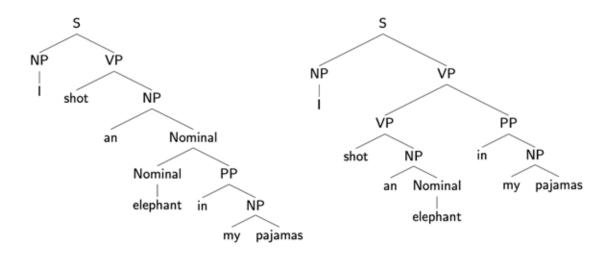
Represent a parse tree as a collection of tuples $\langle \langle l_1, i_1, j_1 \rangle$, $\langle l_2, i_2, j_2 \rangle$, . . . , $\langle l_n, i_n, j_n \rangle$, where

- l_k is the non-terminal labeling the k^{th} phrase
- i_k is the index of the first word in the k^{th} phrase
- j_k is the index of the last word in the k^{th} phrase

Convert gold-standard tree and system hypothesized tree into this representation, then estimate precision, recall, and F1.



Evaluation Example



$$\underbrace{\left\langle \begin{array}{c} \langle \mathsf{NP}, 3, 7 \rangle, \\ \langle \mathsf{Nominal}, 4, 7 \rangle \end{array} \right\rangle \left\langle \begin{array}{c} \langle \mathsf{S}, 1, 7 \rangle, \langle \mathsf{VP}, 2, 7 \rangle, \\ \langle \mathsf{PP}, 5, 7 \rangle, \langle \mathsf{NP}, 6, 7 \rangle \\ \langle \mathsf{Nominal}, 4, 4 \rangle \end{array} \right\rangle}_{\mathsf{only in left tree}} \underbrace{\left\langle \begin{array}{c} \langle \mathsf{VP}, 2, 4 \rangle, \\ \langle \mathsf{NP}, 3, 4 \rangle \end{array} \right\rangle}_{\mathsf{only in right tree}} \underbrace{\left\langle \begin{array}{c} \langle \mathsf{VP}, 2, 4 \rangle, \\ \langle \mathsf{NP}, 3, 4 \rangle \end{array} \right\rangle}_{\mathsf{only in right tree}}$$



Chomsky Normal Form

Normalizing Context-Free Grammars



Context Free Grammar

N	Finite set of non-terminal symbols	NP, VP, S
Σ	Finite alphabet of terminal symbols	the, dog, a
R	Set of production rules, each $A \rightarrow \beta \\ \beta \in (\Sigma, N)$	NP → DT JJ NN Noun → dog
S	Start symbol	



Chomsky Normal Form

N	Finite set of non-terminal symbols	NP, VP, S
Σ	Finite alphabet of terminal symbols	the, dog, a
R	Set of production rules, each $A \rightarrow \beta$ $\beta = \text{single terminal (from } \Sigma) \text{ or two } \text{non-terminals (from } N)$	S → NP VP Noun → dog
S	Start symbol	



CNF and CFG

Any CFG can be converted into a weakly equivalent CNF grammar (recognizing the same set of sentences as in the original grammar but differing in their derivation).

NP

NN



$$NP \rightarrow X NN$$

$$X \rightarrow DT JJ$$



CFG to CNF: CFG

\rightarrow	NP VP
\rightarrow	VBD NP
\rightarrow	VP PP
\rightarrow	Nominal PP
\rightarrow	NN
\rightarrow	NNS
\rightarrow	PRP
\rightarrow	IN NP
\rightarrow	DT NN
\rightarrow	Nominal
\rightarrow	PRP\$ Nominal

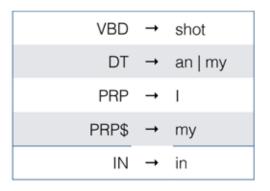
VBD	→	shot
DT	→	an my
NN	→	elephant
NNS	→	pajamas
PRP	\rightarrow	I
PRP\$	\rightarrow	my
IN	\rightarrow	in

I shot an elephant in my pajamas



CFG to CNF: CNF

S	\rightarrow	NP VP
VP	\rightarrow	VBD NP
VP	\rightarrow	VP PP
Nominal	\rightarrow	Nominal PP
Nominal	→	pajamas elephant I
PP	\rightarrow	IN NP
NP	\rightarrow	DT NN
NP	→	pajamas elephant I
NP	→	PRP\$ Nominal



I shot an elephant in my pajamas



Syntactic Parsing

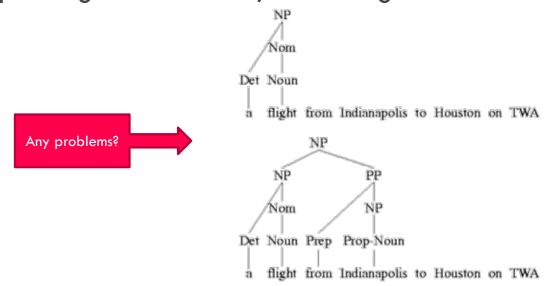
Cocke—Younger—Kasami (CYK) Chart Parsing a.k.a.

Dynamic Programming, 3rd encounter



Parsing

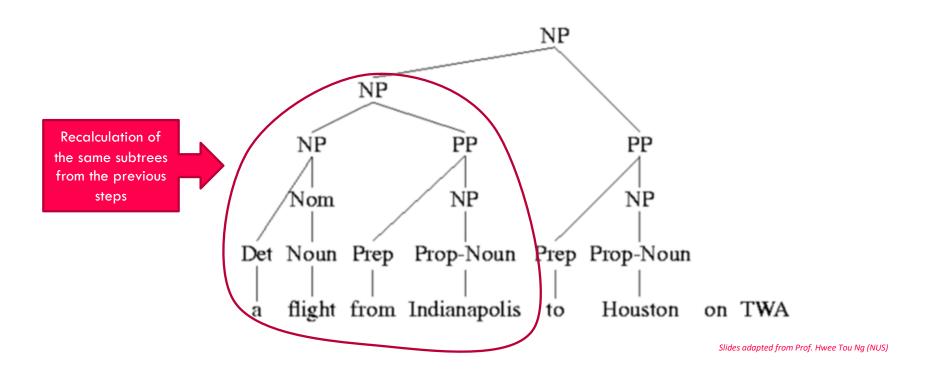
One means to extract a sentential parse tree is by repeatedly parsing the sentence, left to right.



Slides adapted from Prof. Hwee Tou Ng (NUS)



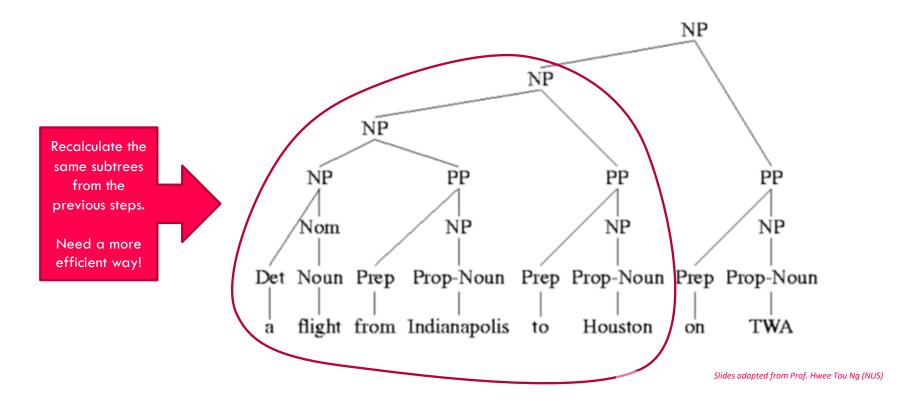
Parsing of subtrees



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Parsing of subtrees





CYK Parsing

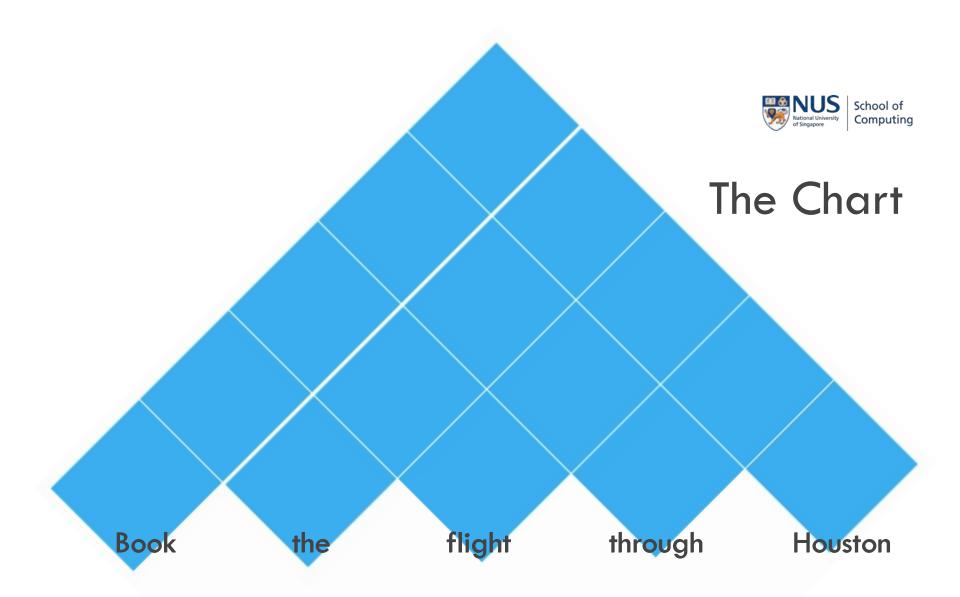
Stands for its 3 inventors: Cocke-Younger-Kasami (CYK)

Bottom-Up Dynamic Programming approach to handling redundancy when computing the parse trees.

It requires the CFG to be in CNF:

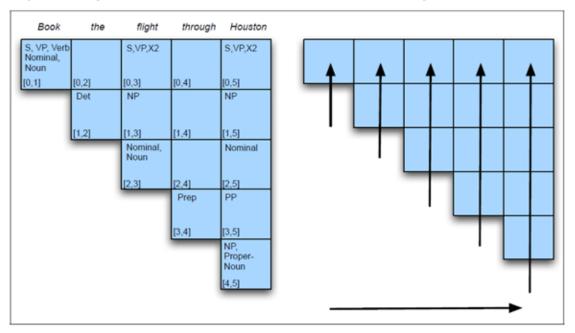
- The grammar is ε (epsilon)-free
- Either 2 non-terminal symbols or 1 terminal symbol on the RHS

Slides adapted from Prof. Hwee Tou Ng (NUS)



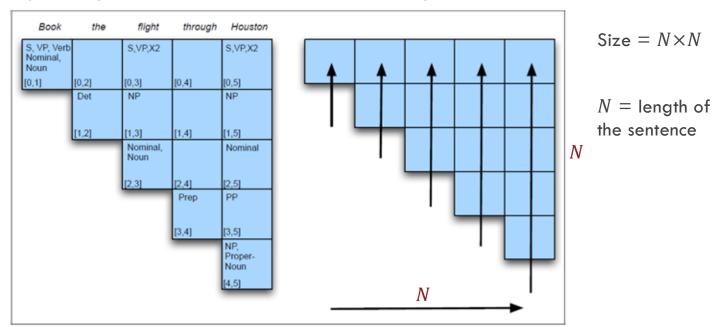


Completing the parse table in a bottom up manner



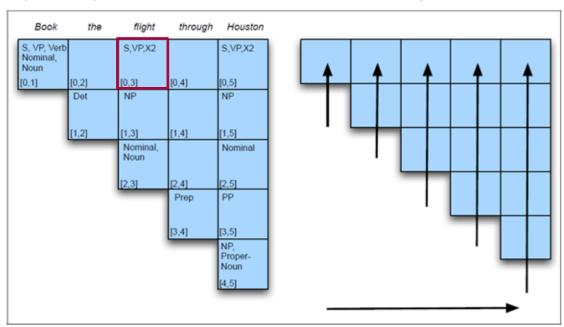


Completing the parse table in a bottom up manner





Completing the parse table in a bottom up manner

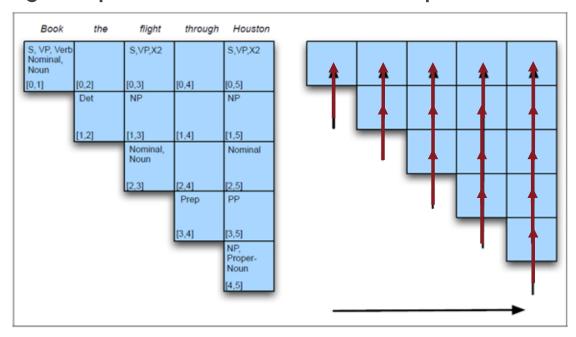


Each cell represent all the possible parses for span [i, j) (using a 0 index).

E.g. [0,3] = all the possible parses for span [0, 3) "book the flight"



Completing the parse table in a bottom up manner

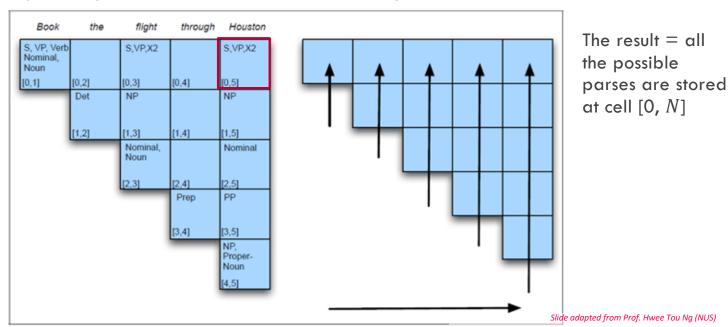


CYK fills the table from the bottom to top, from left to right.

Starts from [4,5], then followed by [3, 4], [3, 5] until [0,5]



Completing the parse table in bottom up-manner.





CYK Algorithm

```
\textbf{function} \ \mathsf{CKY}\text{-}\mathsf{PARSE}(words, \mathit{grammar}) \ \textbf{returns} \ \mathit{table}
```

```
for j \leftarrow from 1 to LENGTH(words) do

for all \{A \mid A \rightarrow words[j] \in grammar\}

table[j-1,j] \leftarrow table[j-1,j] \cup A

for i \leftarrow from j-2 down to 0 do

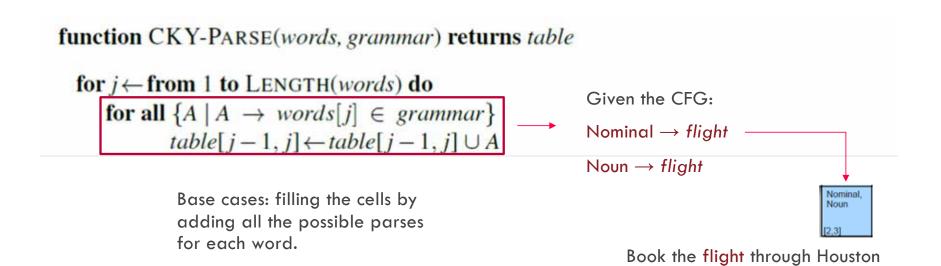
for k \leftarrow i+1 to j-1 do

for all \{A \mid A \rightarrow BC \in grammar \text{ and } B \in table[i,k] \text{ and } C \in table[k,j]\}

table[i,j] \leftarrow table[i,j] \cup A
```



CYK Algorithm Cont.





CYK Algorithm Cont.

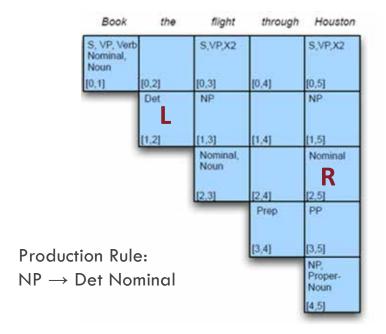
Recursive cases: fill all the other cells by adding all the possible combinations of 2 subtrees.

for $i \leftarrow$ from j - 2 down to 0 do

for $k \leftarrow i+1$ to j-1 do for all $\{A \mid A \rightarrow BC \in grammar \text{ and } B \in table[i,k] \text{ and } C \in table[k,j]\}$ $table[i,j] \leftarrow table[i,j] \cup A$



CYK Algorithm (Filling [1,5], Try 1)



Combine "the" with "flight through Houston"

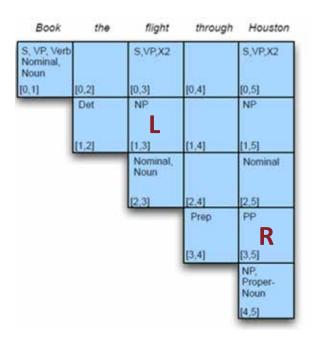
$$[1,2] = [Det]$$

$$[2,5] = [Nominal]$$

$$= [NP]$$

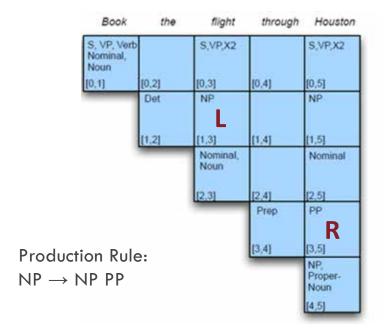


CYK Algorithm (Filling [1,5], Try 2)





CYK Algorithm (Filling [1,5], Try 2)



[1,5] = "the flight through Houston"

Combine "the flight" with "through Houston"

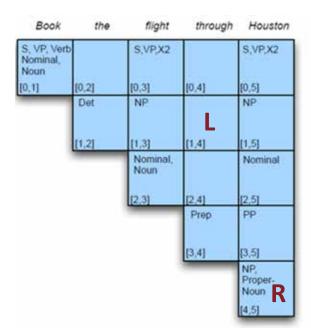
$$[1,3] = [NP]$$

$$[3,5] = [PP]$$

$$= [NP]$$

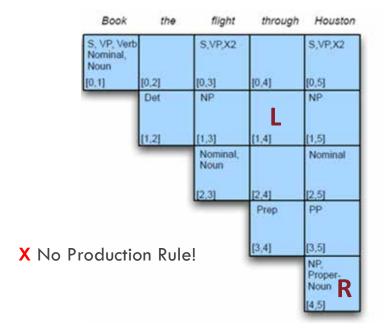


CYK Algorithm (Filling [1,5], Try 3)





CYK Algorithm (Filling [1,5], Try 3)



Combine "the flight through" with "Houston"



CYK Summary

Another encounter with dynamic programming to reuse computations.

Cell [0,N] contains all the possible parses for a given input

While resultant parses are grammatical, some are unlikely

We want to know how to get the most reasonable parses



Statistical Parsing

Upgrading CKY to account for probable parses



Statistical Parsing

Resolve structural ambiguity by choosing the most probable parse



Definition of PCFG

Probabilistic context-free grammar: each production is also associated with a probability.

for a given parse tree T for sentence S comprised of n rules from R (each $A \rightarrow \beta$):

$$P(T,S) = \prod_{i}^{n} P(\beta|A)$$



Definition of PCFG

N	Finite set of non-terminal symbols	NP, VP, S
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R	Set of production rules, each $A \rightarrow \beta [p]$ $p = P(\beta \mid A)$	S → NP VP Noun → dog
S	Start symbol	



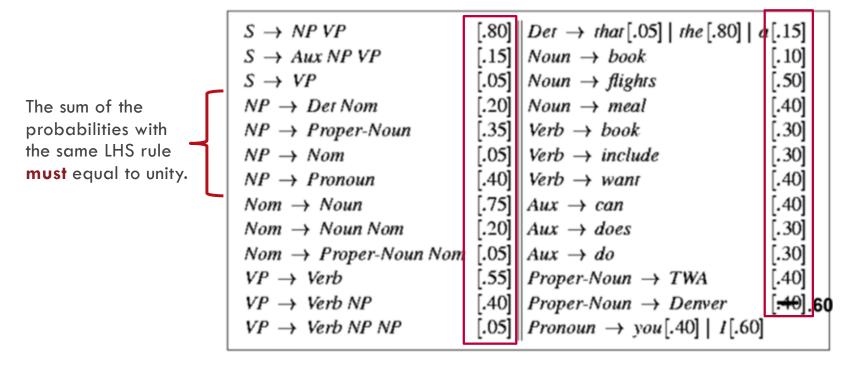
CFG and PCFG

A CFG tells us whether a sentence is in the language it defines.

A PCFG gives us a mechanism for assigning scores (here, probabilities) to different parses for the same sentence.



Probabilistic Context-Free Grammar





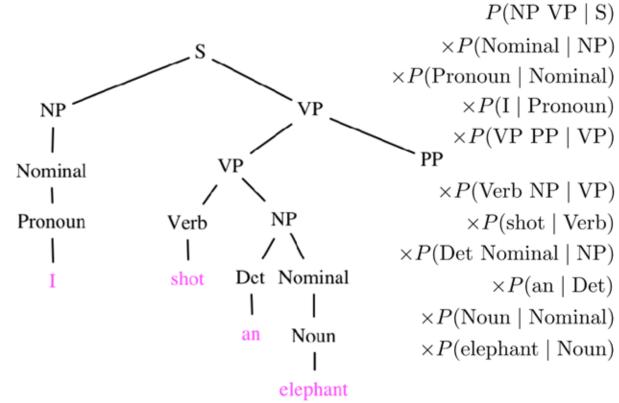
Estimating PCFG Probabilities

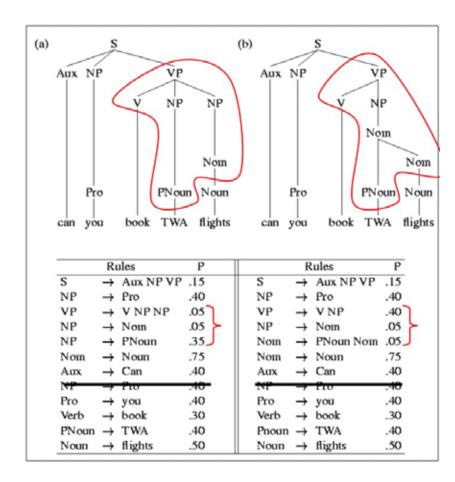
$$\sum_{\beta} P(A \to \beta) = 1 \qquad \Longrightarrow \qquad \sum_{\beta} P(\beta|A) = 1$$

$$\sum_{\beta} P(\beta|A) = \frac{C(A \to \beta)}{\sum_{\gamma} C(A \to \gamma)} \qquad \Longrightarrow \qquad \sum_{\beta} P(\beta|A) = \frac{C(A \to \beta)}{C(A)}$$



PCFG Example





Comparing Possible Parses



$$P(T) = \prod_{n \in T} P(r(n))$$

$$P(T_a)$$

= 0.15 * 0.4 * 0.05 * 0.05 * 0.35 * 0.75
* 0.40 * 0.40 * 0.30 * 0.40 * 0.5
= 3.78 * 10⁻⁷

$$P(T_b)$$

= 0.15 * 0.4 * 0.4 * 0.05 * 0.05 * 0.75
* 0.40 * 0.40 * 0.30 * 0.40 * 0.5
= 4.32 * 10⁻⁷



Standard CYK

• Table[i,j] = all possibleparses for span [i,j)

• Table[0, N] = all possibleparses for the given input sentence

Probabilistic CYK

• Table[i, j, A] =the highest score for span [i, j) resulting in constituent A

• Table[0, N, S] = the highest score for a parse for the given input sentence

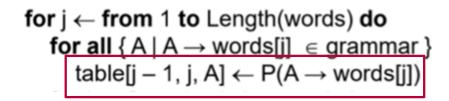


function Probabilistic-CKY(words, grammar) **returns** most probable parse and its probability

```
\label{eq:formula} \begin{split} &\text{for all } \{A \mid A \to \text{words[j]} \in \text{grammar} \,\} \\ &\quad \text{table[j-1, j, A]} \leftarrow P(A \to \text{words[j]}) \\ &\text{for } i \leftarrow \text{from } j - 2 \text{ downto } 0 \text{ do} \\ &\quad \text{for } k \leftarrow i + 1 \text{ to } j - 1 \text{ do} \\ &\quad \text{for all } \{A \mid A \to BC \in \text{grammar and} \\ &\quad \text{table[i, k, B]} > 0 \text{ and } \text{table[k, j, C]} > 0 \,\} \\ &\quad \text{if } (\text{table[i, j, A]} < P(A \to BC) \times \text{table[i, k, B]} \times \text{table[k, j, C]}) \text{ then} \\ &\quad \text{table[i, j, A]} \leftarrow P(A \to BC) \times \text{table[i, k, B]} \times \text{table[k, j, C]} \\ &\quad \text{back[i, j, A]} \leftarrow \{k, B, C \,\} \\ &\quad \text{return Build-Tree(back[0, Length(words), S]), } \text{ table[0, Length(words), S]} \end{split}
```



function Probabilistic-CKY(words, grammar) **returns** most probable parse and its probability



Base cases: filling the cells by assigning with the probability based on a particular rule





A. Recursive case: assigning each cells with the highest score

B. Backtracking purposes: storing the best parses

```
for i \leftarrow from j - 2 downto 0 do

for k \leftarrow i + 1 to j - 1 do

for all { A | A \rightarrow BC \in grammar and

table[i, k, B] > 0 and table[k, j, C] > 0 }

if (table[i, j, A] < P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]) then

table[i, j, A] \leftarrow P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]

back[i, j, A] \leftarrow { k, B, C }

return Build-Tree(back[0, Length(words), S]), table[0, Length(words), S]
```





From Sequences to Trees

Parsing assigns structure (trees) to sequences of natural language.

Grammars give acceptability, and probabilistic ones help resolve structural ambiguity to find probable interpretations

CKY parsing memoizes basic building block parses to assemble larger blocks, leading to a sentence parse

There are modern neural forms of parsing that outperform the traditional ones we've presented today