

CS1231 Review 12

1. Modular Arithmetic

- Definition: a is congruent to b modulo m , we write as $a \equiv b \pmod{m}$, if

$$m \mid (a-b)$$

- Theorem. $a \equiv b \pmod{m}$ iff $a \bmod m = b \bmod m$ iff $a = b + km \quad k \in \mathbb{Z}$

- Theorem. $a \equiv b \pmod{m}$ and $c \equiv d \pmod{m}$, then $a + c \equiv b + d \pmod{m}$

2. 1 is NOT prime. 1 is NOT composite.

$$\begin{aligned} ac &\equiv bd \pmod{m} \\ a - c &\equiv b - d \pmod{m} \\ a^n &\equiv b^n \pmod{m} \\ n &\in \mathbb{Z}^+ \end{aligned}$$