

Lecture #19

Sequential Logic



Lecture #19: Sequential Logic (1/2)

- 1. Introduction
- 2. Memory Elements
- 3. Latches
 - 3.1 S-R Latch
 - 3.2 D Latch
- 4. Flip-flops
 - 4.1 S-R Flip-flop
 - 4.2 D Flip-flop
 - 4.3 J-K Flip-flop
 - 4.4 T Flip-flop

Lecture #19: Sequential Logic (2/2)

- 5. Asynchronous Inputs
- 6. Synchronous Sequential Circuit
 - 6.1 Flip-flop Characteristic Tables
 - 6.2 Analysis
 - 6.3 Flip-flop Excitation Tables
 - 6.4 Design

7. Memory

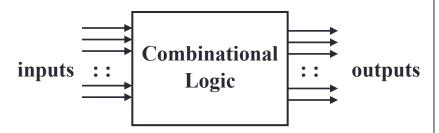
- 7.1 Memory Unit
- 7.2 Read/Write Operations
- 7.3 Memory Cell
- 7.4 Memory Arrays

1. Introduction (1/2)

- Two classes of logic circuits
 - Combinational
 - Sequential

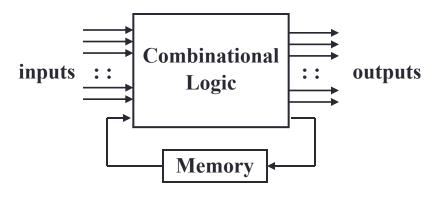
Combinational Circuit

 Each output depends entirely on the immediate (present) inputs.



Sequential Circuit

Each output depends on both present inputs and state.

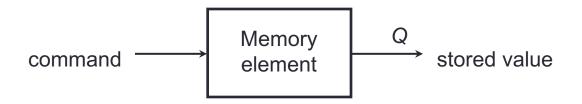


1. Introduction (2/2)

- Two types of sequential circuits:
 - Synchronous: outputs change only at specific time
 - Asynchronous: outputs change at any time
- Multivibrator: a class of sequential circuits
 - Bistable (2 stable states)
 - Monostable or one-shot (1 stable state)
 - Astable (no stable state)
- Bistable logic devices
 - Latches and flip-flops.
 - They differ in the methods used for changing their state.

2. Memory Elements (1/3)

 Memory element: a device which can remember value indefinitely, or change value on command from its inputs.



Characteristic table:

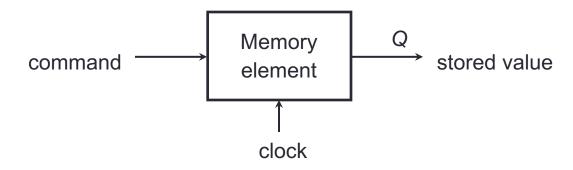
Command (at time t)	Q(t)	Q(t+1)
Set	Х	1
Reset	Х	0
Memorise /	0	0
No Change	1	1

Q(t) or **Q**: current state

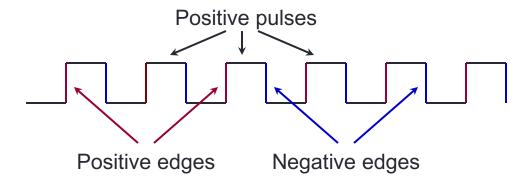
Q(t+1) or Q+: next state

2. Memory Elements (2/3)

Memory element with clock.

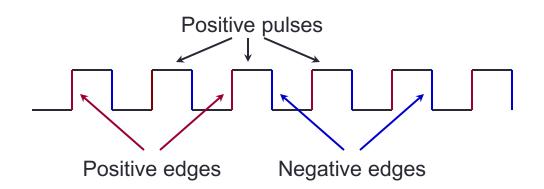


Clock is usually a square wave.



2. Memory Elements (3/3)

- Two types of triggering/activation
 - Pulse-triggered
 - Edge-triggered
- Pulse-triggered
 - Latches
 - ON = 1, OFF = 0



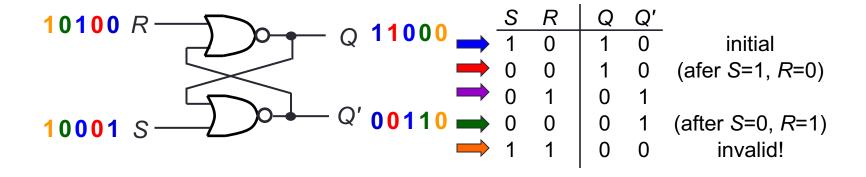
- Edge-triggered
 - Flip-flops
 - Positive edge-triggered (ON = from 0 to 1; OFF = other time)
 - Negative edge-triggered (ON = from 1 to 0; OFF = other time)

3.1 *S-R* Latch (1/3)

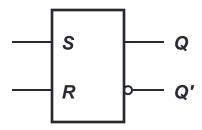
- Two inputs: S and R.
- Two complementary outputs: Q and Q'.
 - When Q = HIGH, we say latch is in SET state.
 - When Q = LOW, we say latch is in RESET state.
- For active-high input S-R latch (also known as NOR gate latch)
 - $R = HIGH \text{ and } S = LOW \rightarrow Q \text{ becomes LOW (RESET state)}$
 - $S = HIGH \text{ and } R = LOW \rightarrow Q \text{ becomes HIGH (SET state)}$
 - Both R and S are LOW → No change in output Q
 - Both R and S are HIGH →Outputs Q and Q' are both LOW (invalid!)
- Drawback: invalid condition exists and must be avoided.

3.1 *S-R* Latch (2/3)

Active-high input S-R latch:

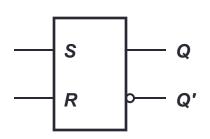


Block diagram:



3.1 *S-R* Latch (3/3)

Characteristic table for active-high input S-R latch:



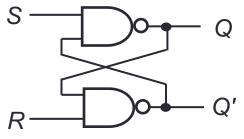
S	R	Q	Q'	
0	0	NC	NC	No change. Latch remained in present state.
1	0	1	0	Latch SET.
0	1	0	1	Latch RESET.
1	1	0	0	Invalid condition.

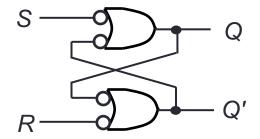
S	R	Q(t+1)	
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	indeterminate	

$$Q(t+1) = ?$$

3.1 Active-Low S-R Latch

- (You may skip this slide.)
- What we have seen is active-high input S-R latch.
- There are active-low input S-R latches, where NAND gates are used instead. See diagram on the left below.



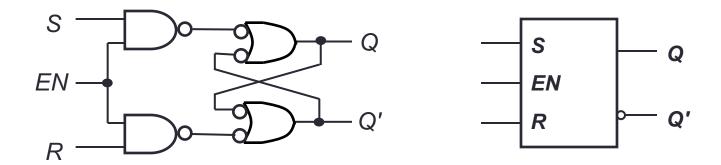


- In this case,
 - when R=0 and S=1, the latch is reset (i.e. Q becomes 0)
 - when R=1 and S=0, the latch is set (i.e. Q becomes 1)
 - when *S=R*=1, it is a no-change command.
 - when S=R=0, it is an invalid command.
- Sometimes, we use the alternative gate diagram for the NAND gate. See diagram on the right above. (This appears in more complex latches/flip-flops in the later slides.)

(Sometimes, the inputs are labelled as S' and R'.)

3.1 Gated S-R Latch

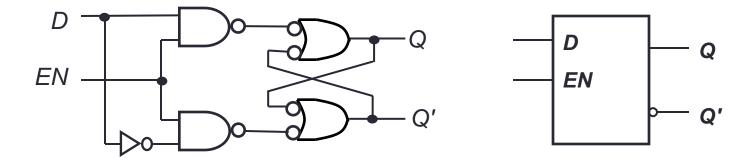
S-R latch + enable input (EN) and 2 NAND gates
 → a gated S-R latch.



Outputs change (if necessary) only when EN is high.

3.2 Gated *D* Latch (1/2)

- Make input R equal to $S' \rightarrow \text{gated } D$ latch.
- D latch eliminates the undesirable condition of invalid state in the S-R latch.



3.2 Gated *D* Latch (2/2)

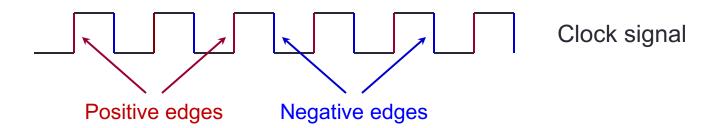
- When EN is high,
 - $D = HIGH \rightarrow latch$ is SET
 - $D = LOW \rightarrow latch$ is RESET
- Hence when EN is high, Q "follows" the D (data) input.
- Characteristic table:

EN	D	Q(t+1)	Q(t+1)	
1	0	0	Reset	
1	1	1	Set	
0	X	Q(t)	No change	

When
$$EN=1$$
, $Q(t+1) = ?$

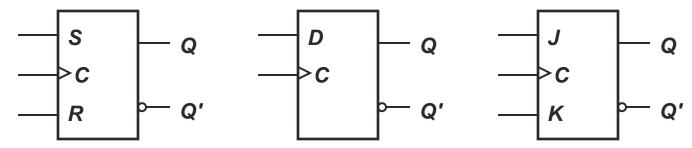
4. Flip-flops (1/2)

- Flip-flops are synchronous bistable devices.
- Output changes state at a specified point on a triggering input called the clock.
- Change state either at the positive (rising) edge, or at the negative (falling) edge of the clock signal.

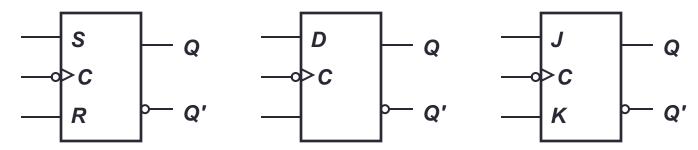


4. Flip-flops (2/2)

- S-R flip-flop, D flip-flop, and J-K flip-flop.
- Note the ">" symbol at the clock input.



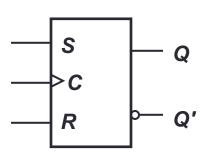
Positive edge-triggered flip-flops



Negative edge-triggered flip-flops

4.1 S-R Flip-flop

- S-R flip-flop: On the triggering edge of the clock pulse,
 - $R = HIGH \text{ and } S = LOW \rightarrow Q \text{ becomes LOW (RESET state)}$
 - $S = HIGH \text{ and } R = LOW \rightarrow Q \text{ becomes HIGH (SET state)}$
 - Both R and S are LOW → No change in output Q
 - Both R and S are HIGH → Invalid!
- Characteristic table of positive edge-triggered S-R flip-flop:



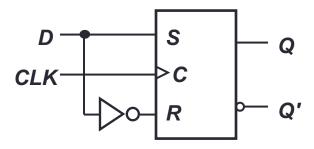
S	R	CLK	Q(t+1)	Comments
0	0	X	Q(t)	No change
0	1	\uparrow	0	Reset
1	0	\uparrow	1	Set
1	1	\uparrow	?	Invalid

X = irrelevant ("don't care")

↑ = clock transition LOW to HIGH

4.2 *D* Flip-flop (1/2)

- D flip-flop: Single input D (data). On the triggering edge of the clock pulse,
 - $D = HIGH \rightarrow Q$ becomes HIGH (SET state)
 - $D = LOW \rightarrow Q$ becomes LOW (RESET state)
- Hence, Q "follows" D at the clock edge.
- Convert S-R flip-flop into a D flip-flop: add an inverter.



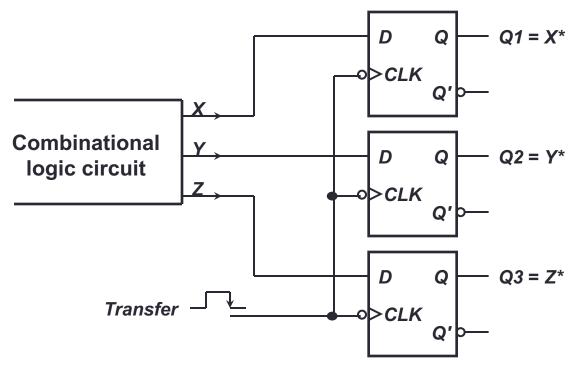
A positive edge-triggered D flip-flop formed with an S-R flip-flop.

D	CLK	Q(t+1)	Comments
1	<u></u>	1	Set
0	\uparrow	0	Reset

↑ = clock transition LOW to HIGH

4.2 *D* Flip-flop (2/2)

- Application: Parallel data transfer.
 - To transfer logic-circuit outputs X, Y, Z to flip-flops Q1, Q2 and Q3 for storage.



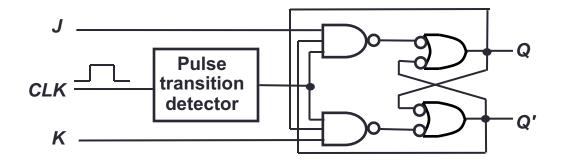
* After occurrence of negative-going transition

4.3 *J-K* Flip-flop (1/2)

- J-K flip-flop: Q and Q' are fed back to the pulse-steering NAND gates.
- No invalid state.
- Include a toggle state
 - J = HIGH and $K = LOW \rightarrow Q$ becomes HIGH (SET state)
 - $K = HIGH \text{ and } J = LOW \rightarrow Q \text{ becomes LOW (RESET state)}$
 - Both J and K are LOW → No change in output Q
 - Both J and K are HIGH \rightarrow Toggle

4.3 *J-K* Flip-flop (2/2)

■ *J-K* flip-flop circuit:



Characteristic table:

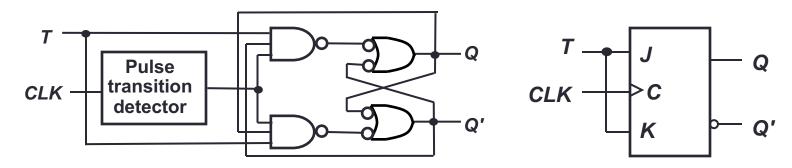
J	K	CLK	Q(t+1)	Comments
0	0	<u></u>	Q(t)	No change
0	1	\uparrow	0	Reset
1	0	\uparrow	1	Set
1	1	\uparrow	Q(t)'	Toggle

$$Q(t+1) = ?$$

Q	J	K	Q(t+1)
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

4.4 T Flip-flop

T flip-flop: Single input version of the J-K flip-flop, formed by tying both inputs together.



Characteristic table:

T	CLK	Q(t+1)	Comments
0	↑	Q(t)	No change
1	↑	Q(t)'	Toggle

$$Q(t+1) = ?$$

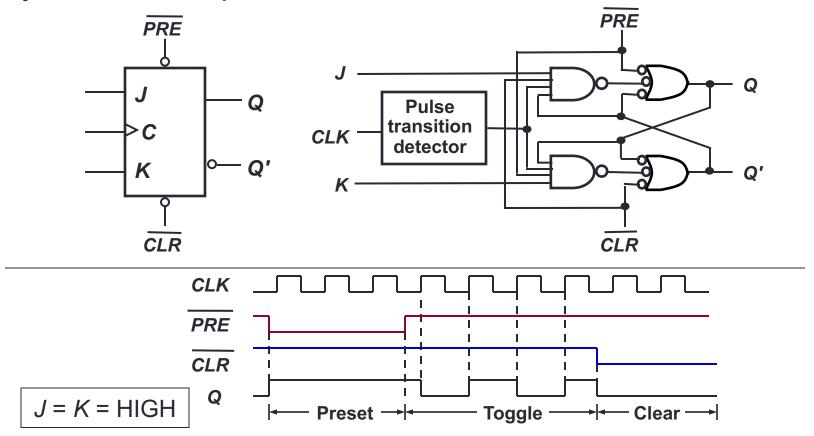
Q	T	Q(t+1)
0	0	0
0	1	1
1	0	1
1	1	0

5. Asynchronous Inputs (1/2)

- S-R, D and J-K inputs are synchronous inputs, as data on these inputs are transferred to the flip-flop's output only on the triggered edge of the clock pulse.
- Asynchronous inputs affect the state of the flip-flop independent of the clock; example: preset (PRE) and clear (CLR) [or direct set (SD) and direct reset (RD)].
- When *PRE*=HIGH, Q is <u>immediately</u> set to HIGH.
- When CLR=HIGH, Q is immediately cleared to LOW.
- Flip-flop in normal operation mode when both PRE and CLR are LOW.

5. Asynchronous Inputs (2/2)

 A J-K flip-flop with active-low PRESET and CLEAR asynchronous inputs.



6. Synchronous Sequential Circuits

- Building blocks: logic gates and flip-flops.
- Flip-flops make up the memory while the gates form one or more combinational sub-circuits.
- We have discussed S-R flip-flop, J-K flip-flop, D flip-flop and T flip-flop.

6.1 Flip-flop Characteristic Tables

Each type of flip-flop has its own behaviour, shown by its characteristic table.

J	K	Q(t+1)	Comments
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	Q(t)'	Toggle

S	R	Q(t+1)	Comments
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	?	Unpredictable

D	Q(t+1)	
0	0	Reset
1	1	Set

T	Q(t+1)	
0	Q(t)	No change
1	Q(t)'	Toggle

6.2 Sequential Circuits: Analysis (1/7)

- Given a sequential circuit diagram, we can analyze its behaviour by deriving its state table and hence its state diagram.
- Requires state equations to be derived for the flip-flop inputs, as well as output functions for the circuit outputs other than the flip-flops (if any).
- We use A(t) and A(t+1) (or simply A and A+) to represent the present state and next state, respectively, of a flip-flop represented by A.

6.2 Sequential Circuits: Analysis (2/7)

Example using D flip-flops

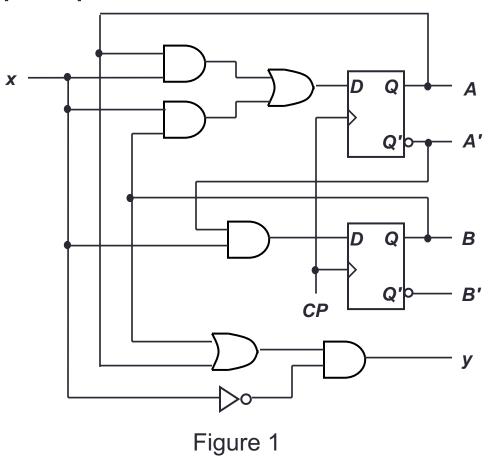
State equations:

 $A^+ = A \cdot x + B \cdot x$

 $B^+ = A' \cdot x$

Output function:

$$y = (A + B) \cdot x'$$



6.2 Sequential Circuits: Analysis (3/7)

- From the *state equations* and *output function*, we derive the *state table*, consisting of all possible binary combinations of present states and inputs.
- State table
 - Similar to truth table.
 - Inputs and present state on the left side.
 - Outputs and next state on the right side.
- *m* flip-flops and *n* inputs $\rightarrow 2^{m+n}$ rows.

6.2 Sequential Circuits: Analysis (4/7)

State table for circuit of Figure 1:

State equations:

Output function:

$$A^+ = A \cdot x + B \cdot x$$

$$y = (A + B) \cdot x'$$

$$B^+ = A' \cdot x$$

Pre	sent		Next			
State		<u>Input</u>	_State_		<u>Output</u>	
_ A _	В	X	A^{\dagger}	$B^{^{+}}$	у	
0	0	0	0	0	0	
0	0	1	0	1	0	
0	1	0	0	0	1	
0	1	1	1	1	0	
1	0	0	0	0	1	
1	0	1	1	0	0	
1	1	0	0	0	1	
1	1	1	1	0	0	

6.2 Sequential Circuits: Analysis (5/7)

• Alternative form of state table:

Full table

Present State		Input	Next State		Output
A	В		\overline{A}^{\dagger}	B^{\dagger}	у
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	1
0	1	1	1	1	0
1	0	0	0	0	1
1	0	1	1	0	0
1	1	0	0	0	1
1	1	1	1	0	0

Compact table

Present	Next State		Output	
State	x=0	<i>x</i> =1	<i>x</i> =0	<i>x</i> =1
AB	$A^{\dagger}B^{\dagger}$	$A^{\dagger}B^{\dagger}$	У	У
00	00	01	0	0
01	00	11	1	0
10	00	10	1	0
11	00	10	1	0

6.2 Sequential Circuits: Analysis (6/7)

- From the *state table*, we can draw the *state diagram*.
- State diagram
 - Each state is denoted by a circle.
 - Each arrow (between two circles) denotes a transition of the sequential circuit (a row in state table).
 - A label of the form a/b is attached to each arrow where a (if there is one) denotes the inputs while b (if there is one) denotes the outputs of the circuit in that transition.
- Each combination of the flip-flop values represents a state. Hence, m flip-flops → up to 2^m states.

1/0

10

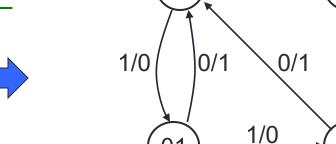
1/0

6.2 Sequential Circuits: Analysis (7/7)

State diagram of the circuit of Figure 1:

Present	Next State		Out	put
State	<i>x</i> =0	<i>x</i> =1	<i>x</i> =0	<i>x</i> =1
AB	$A^{\dagger}B^{\dagger}$	$A^{\dagger}B^{\dagger}$	У	У
00	00	01	0	0
01	00	11	1	0
10	00	10	1	0
11	00	10	1	0





01

00

0/1



6.2 Flip-flop Input Functions (1/3)

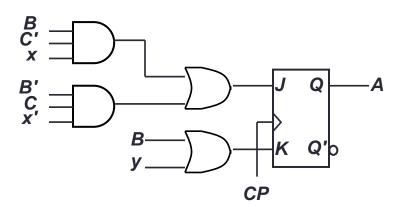
- The outputs of a sequential circuit are functions of the present states of the flip-flops and the inputs. These are described algebraically by the *circuit output functions*.
 - In Figure 1: $y = (A + B) \cdot x'$
- The part of the circuit that generates inputs to the flipflops are described algebraically by the flip-flop input functions (or flip-flop input equations).
- The flip-flop input functions determine the next state generation.
- From the flip-flop input functions and the characteristic tables of the flip-flops, we obtain the next states of the flip-flops.

6.2 Flip-flop Input Functions (2/3)

- Example: circuit with a JK flip-flop.
- We use 2 letters to denote each flip-flop input: the first letter denotes the input of the flip-flop (J or K for J-K flipflop, S or R for S-R flip-flop, D for D flip-flop, T for T flipflop) and the second letter denotes the name of the flipflop.

$$JA = B \cdot C' \cdot x + B' \cdot C \cdot x'$$

 $KA = B + y$



6.2 Flip-flop Input Functions (3/3)

In Figure 1, we obtain the following state equations by observing that Q⁺ = DQ for a D flip-flop:

```
A^+ = A \cdot x + B \cdot x (since DA = A \cdot x + B \cdot x)

B^+ = A' \cdot x (since DB = A' \cdot x)
```

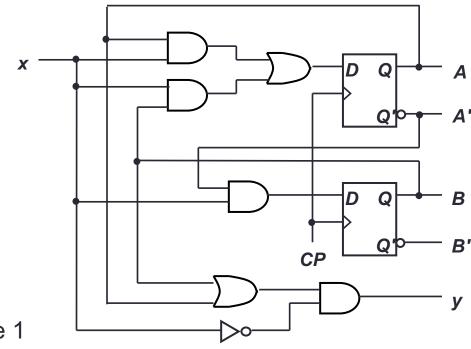
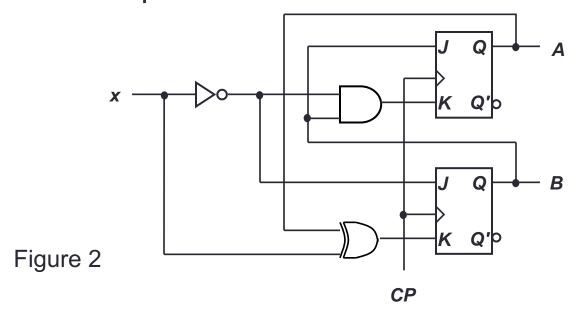


Figure 1

6.2 Analysis: Example #2 (1/3)

Given Figure 2, a sequential circuit with two J-K flip-flops
 A and B, and one input x.



Obtain the flip-flop input functions from the circuit:

$$JA = B$$
 $JB = x'$
 $KA = B \cdot x'$ $KB = A' \cdot x + A \cdot x' = A \oplus x$

6.2 Analysis: Example #2 (2/3)

$$JA = B$$
 $JB = x'$
 $KA = B \cdot x'$ $KB = A' \cdot x + A \cdot x' = A \oplus x$

Fill the state table using the above functions, knowing the characteristics of the flip-flops used.

J	K	Q(t+1)	Comments
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	Q(t)'	Toggle

Pres	sent		Ne	ext				
sta	ate	<u>Input</u>	_sta	ate_	<u>FI</u>	ip-flo	<mark>p inp</mark> ւ	ıts_
A	В	X	A^{\dagger}	B^{\dagger}	JA	KA	JB	KB
0	0	0			0	0	1	0
0	0	1			0	0	0	1
0	1	0			1	1	1	0
0	1	1			1	0	0	1
1	0	0			0	0	1	1
1	0	1			0	0	0	0
1	1	0			1	1	1	1
1	1	1			1	0	0	0

6.2 Analysis: Example #2 (3/3)

Draw the state diagram from the state table.

	sent			ext				
sta	ate	<u>Input</u>		ate	<u>-FI</u>	ip-flo	<u>p inpι</u>	<u>its </u>
Α	В	X	A^{\dagger}	B ⁺	JA	KA	JB	KB
0	0	0			0	0	1	0
0	0	1			0	0	0	1
0	1	0			1	1	1	0
0	1	1			1	0	0	1
1	0	0			0	0	1	1
1	0	1			0	0	0	0
1	1	0			1	1	1	1
1	1	1			1	0	0	0







6.2 Analysis: Example #3 (1/3)

Derive the state table and state diagram of this circuit.

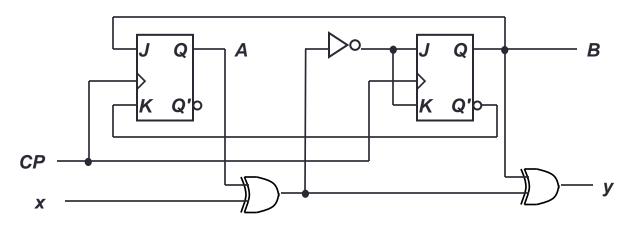


Figure 3

Flip-flop input functions:

$$JA = B$$
 $JB = KB = (A \oplus x)' = A \cdot x + A' \cdot x'$
 $KA = B'$

6.2 Analysis: Example #3 (2/3)

Flip-flop input functions:

$$JA = B$$
 $JB = KB = (A \oplus x)' = A \cdot x + A' \cdot x'$ $KA = B'$

State table:

Pre	sent		Ne	ext					
sta	ate	<u>Input</u>	_st	ate_	<u>Output</u>	_FI	ip-flo	<mark>p inp</mark> ւ	<u>ıts</u>
A	В	X	A^{\dagger}	$B^{^{+}}$	y	JA	KA	JB	KE
0	0	0			0	0	1	1	1
0	0	1			1	0	1	0	0
0	1	0			1	1	0	1	1
0	1	1			0	1	0	0	0
1	0	0			1	0	1	0	0
1	0	1			0	0	1	1	1
1	1	0			0	1	0	0	0
1	1	1			1	1	0	1	1



6.2 Analysis: Example #3 (3/3)

State diagram:

	sent			ext	0 1 1				
sta	ate	<u>Input</u>	_sta	ate_	<u>Output</u>	<u>FI</u>	<u>ıp-tlo</u>	<mark>p inp</mark> ւ	<u>its</u>
A	В	X	A^{\dagger}	B^{\dagger}	y	JA	KA	JB	KB
0	0	0			0	0	1	1	1
0	0	1			1	0	1	0	0
0	1	0			1	1	0	1	1
0	1	1			0	1	0	0	0
1	0	0			1	0	1	0	0
1	0	1			0	0	1	1	1
1	1	0			0	1	0	0	0
1	1	1			1	1	0	1	1







6.3 Flip-flop Excitation Tables (1/2)

- Analysis: Starting from a circuit diagram, derive the state table or state diagram.
- Design: Starting from a set of specifications (in the form of state equations, state table, or state diagram), derive the logic circuit.
- Characteristic tables are used in analysis.
- Excitation tables are used in design.

6.3 Flip-flop Excitation Tables (1/2)

 Excitation tables: given the required transition from present state to next state, determine the flip-flop input(s).

Q	\mathbf{Q}^{\dagger}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

JK Flip-flop

Q	Q^{\dagger}	D			
0	0	0			
0	1	1			
1	0	0			
1	1	1			
D Flip-flop					

Q	Q^{\dagger}	S	R
0	0	0	X
0	1	1	0
1	0	0	1
1	1	X	0

SR Flip-flop

Q	$\mathbf{Q}^{^{\dagger}}$	T
0	0	0
0	1	1
1	0	1
1	1	0

T Flip-flop

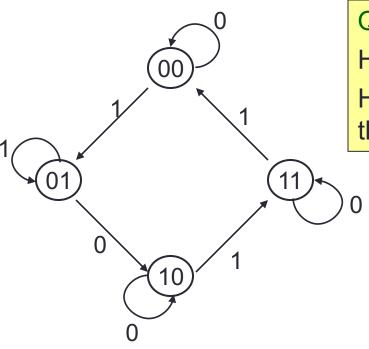
6.4 Sequential Circuits: Design

Design procedure:

- Start with circuit specifications description of circuit behaviour, usually a state diagram or state table.
- Derive the state table.
- Perform state reduction if necessary.
- Perform state assignment.
- Determine number of flip-flops and label them.
- Choose the type of flip-flop to be used.
- Derive circuit excitation and output tables from the state table.
- Derive circuit output functions and flip-flop input functions.
- Draw the logic diagram.

6.4 Design: Example #1 (1/5)

 Given the following state diagram, design the sequential circuit using JK flip-flops.

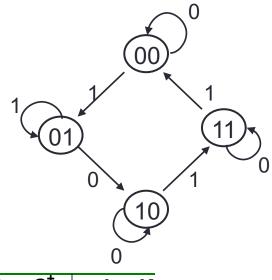


Questions:

How many flip-flops are needed? How many input variable are there?

6.4 Design: Example #1 (2/5)

Circuit state/excitation table, using JK flip-flops.



Q	Q^{\dagger}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

JK Flip-flop's excitation table.

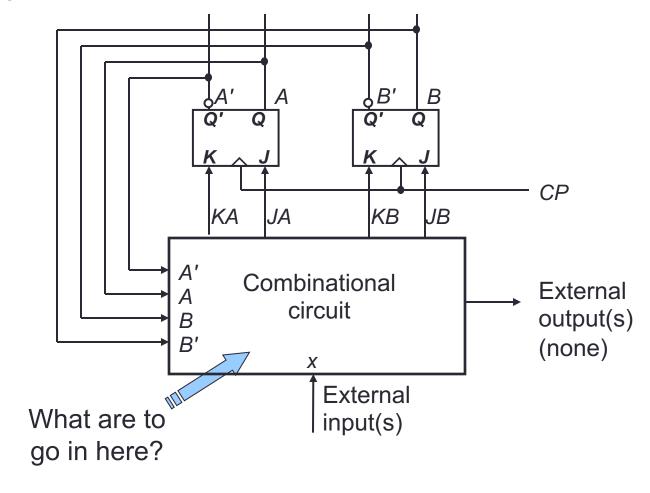


Present	Next State				
State	x=0	<i>x</i> =1			
AB	$A^{\dagger}B^{\dagger}$	$A^{\dagger}B^{\dagger}$			
00	00	01			
01	10	01			
10	10	11			
11	11	00			

Present state		Input		ext ate	F	lip-flo	p inpu	ts
A	В	X	A^{+}	B^{\dagger}	JA	KA	JB	KB
0	0	0	0	0				
0	0	1	0	1				
0	1	0	1	0				
0	1	1	0	1				
1	0	0	1	0				
1	0	1	1	1				
1	1	0	1	1				
1	1	1	0	0				

6.4 Design: Example #1 (3/5)

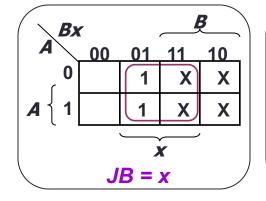
Block diagram.

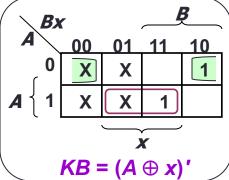


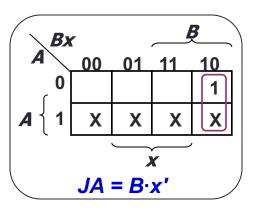
6.4 Design: Example #1 (4/5)

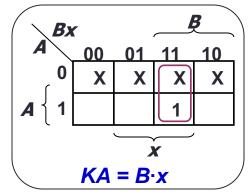
From state table, get flip-flop input functions.

Present state					ext ate Flip-flop inputs					
A	В	X	A^{\dagger}	B ⁺	JA	KA	JB	KB		
0	0	0	0	0	0	X	0	Х		
0	0	1	0	1	0	X	1	X		
0	1	0	1	0	1	X	X	1		
0	1	1	0	1	0	X	X	0		
1	0	0	1	0	X	0	0	X		
1	0	1	1	1	X	0	1	X		
1	1	0	1	1	X	0	X	0		
1	1	1	0	0	X	1	X	1		







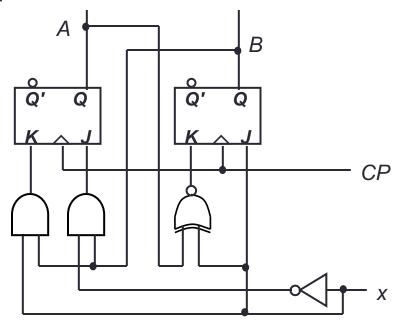


6.4 Design: Example #1 (5/5)

Flip-flop input functions:

$$JA = B \cdot x'$$
 $JB = x$
 $KA = B \cdot x$ $KB = (A \oplus x)'$

Logic diagram:



6.4 Design: Example #2 (1/3)

 Using D flip-flops, design the circuit based on the state table below. (Exercise: Design it using JK flip-flops.)

Present state		Input		ext ate	Output		
A	В	X	A^{+}	B^{+}	У		
0	0	0	0	0	0		
0	0	1	0	1	1		
0	1	0	1	0	0		
0	1	1	0	1	0		
1	0	0	1	0	0		
1	0	1	1	1	1		
1	1	0	1	1	0		
1	1	1	0	0	0		

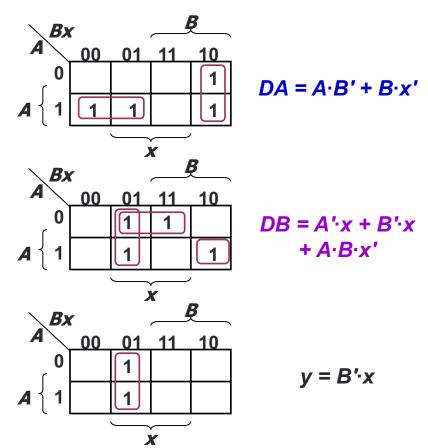
6.4 Design: Example #2 (2/3)

 Determine expressions for flip-flop inputs and the circuit output y.

	sent ate	Input		ext ate	Output		
A	В	X	A^{+}	B^{+}	У		
0	0	0	0	0	0		
0	0	1	0	1	1		
0	1	0	1	0	0		
0	1	1	0	1	0		
1	0	0	1	0	0		
1	0	1	1	1	1		
1	1	0	1	1	0		
1	1	1	0	0	0		

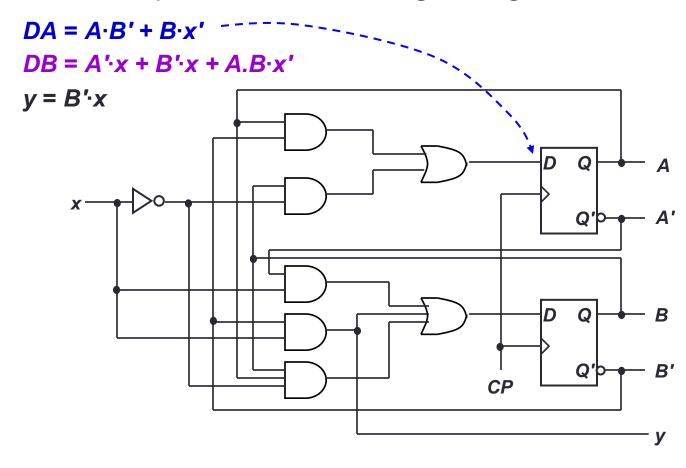
$$DA(A,B,x) = \Sigma \text{ m}(2,4,5,6)$$

 $DB(A,B,x) = \Sigma \text{ m}(1,3,5,6)$
 $y(A,B,x) = \Sigma \text{ m}(1,5)$



6.4 Design: Example #2 (3/3)

From derived expressions, draw logic diagram:



6.4 Design: Example #3 (1/4)

Design involving unused states.

Pi	rese	nt			Nex	t							
:	state	9	Input		state	<u> </u>	Flip-flop inputs					Output	
Α	В	С	х	A ⁺	B ⁺	C ⁺	SA	RA	SB	RB	SC	RC	У
0	0	1	0	0	0	1	0	Χ	0	Χ	Х	0	0
0	0	1	1	0	1	0	0	Χ	1	0	0	1	0
0	1	0	0	0	1	1	0	Χ	Х	0	1	0	0
0	1	0	1	1	0	0	1	0	0	1	0	Х	0
0	1	1	0	0	0	1	0	Χ	0	1	Х	0	0
0	1	1	1	1	0	0	1	0	0	1	0	1	0
1	0	0	0	1	0	1	Χ	0	0	Χ	1	0	0
1	0	0	1	1	0	0	Χ	0	0	Χ	0	Х	1
1	0	1	0	0	0	1	0	1	0	Х	Х	0	0
1	0	1	1	1	0	0	Х	0	0	Х	0	1	1

Given these

Derive these

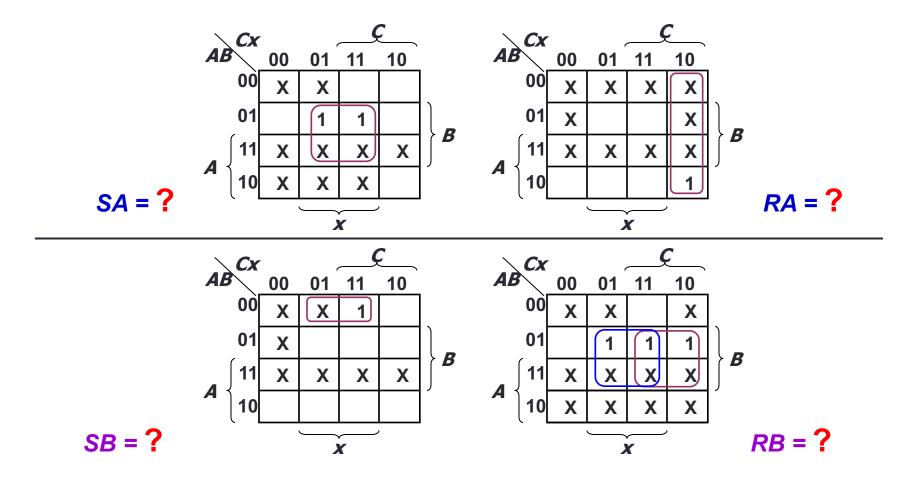
Are there other unused states?

Unused state 000:

0	0	0	0	X	X	X	X	X	X	X	Х	Х	Х
0	0	0	1	X	X	X	X	X	X	X	X	X	X

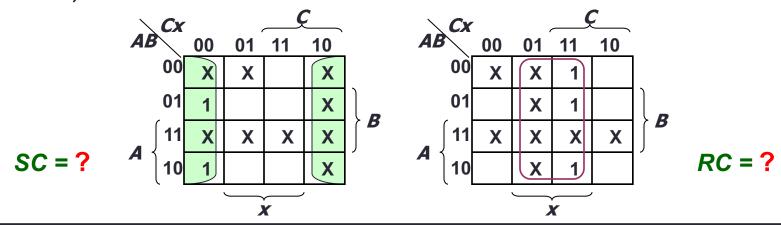
6.4 Design: Example #3 (2/4)

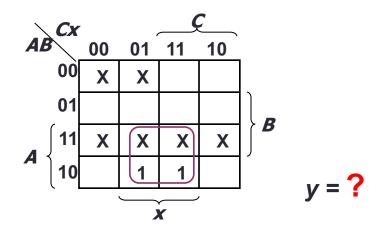
From state table, obtain expressions for flip-flop inputs.



6.4 Design: Example #3 (3/4)

 From state table, obtain expressions for flip-flop inputs (cont'd).

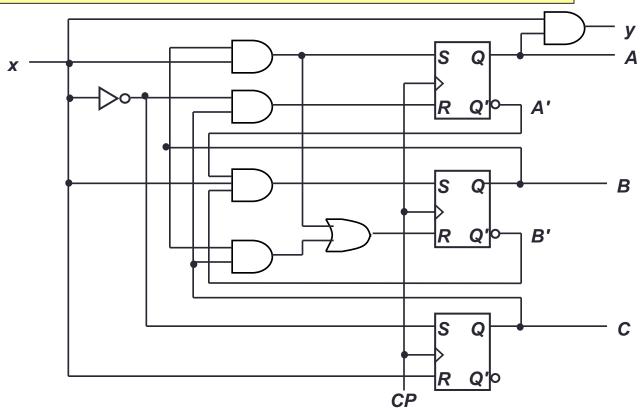




6.4 Design: Example #3 (4/4)

From derived expressions, draw the logic diagram:

```
SA = B \cdot x SB = A' \cdot B' \cdot x SC = x' y = A \cdot x RA = C \cdot x' RB = B \cdot C + B \cdot x RC = x
```

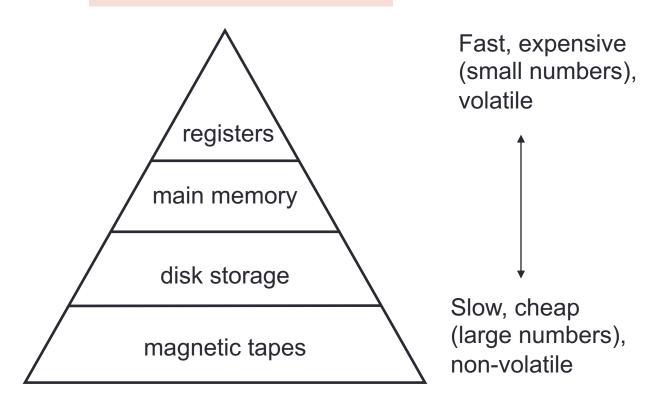


7. Memory (1/4)

- Memory stores programs and data.
- Definitions:
 - 1 byte = 8 bits
 - 1 word: in multiple of bytes, a unit of transfer between main memory and registers, usually size of register.
 - 1 KB (kilo-bytes) = 2¹⁰ bytes; 1 MB (mega-bytes) = 2²⁰ bytes;
 1 GB (giga-bytes) = 2³⁰ bytes; 1 TB (tera-bytes) = 2⁴⁰ bytes.
- Desirable properties: fast access, large capacity, economical cost, non-volatile.
- However, most memory devices do not possess all these properties.

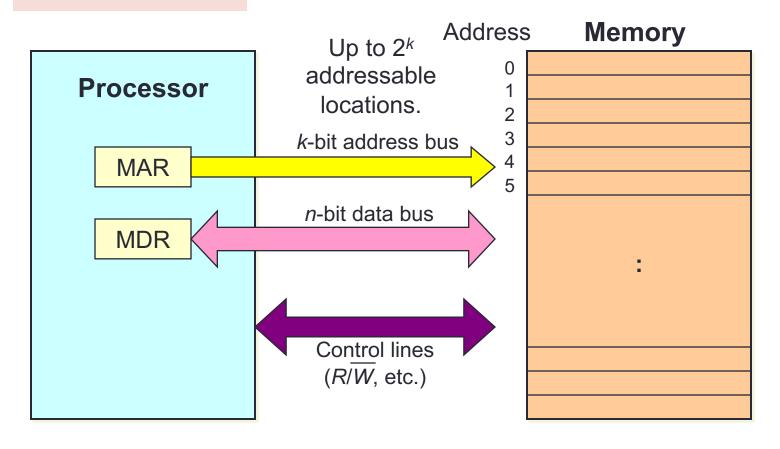
7. Memory (2/4)

Memory hierarchy



7. Memory (3/4)

Data transfer

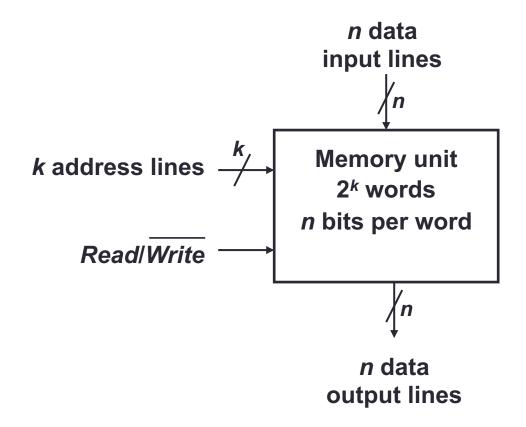


7. Memory (4/4)

- A memory unit stores binary information in groups of bits called words.
- The data consists of *n* lines (for *n*-bit words). Data input lines provide the information to be stored (*written*) into the memory, while data output lines carry the information out (*read*) from the memory.
- The address consists of k lines which specify which word (among the 2^k words available) to be selected for reading or writing.
- The control lines Read and Write (usually combined into a single control line Read/Write) specifies the direction of transfer of the data.

7.1 Memory Unit

Block diagram of a memory unit:



7.2 Read/Write Operations

Write operation:

- Transfers the address of the desired word to the address lines.
- Transfers the data bits (the word) to be stored in memory to the data input lines.
- Activates the Write control line (set Read/Write to 0).

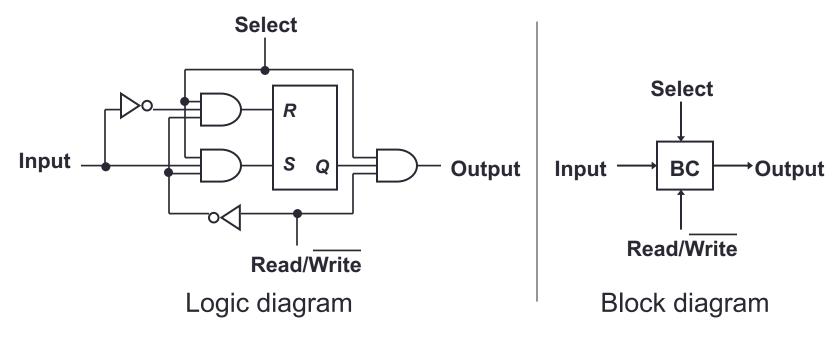
Read operation:

- Transfers the address of the desired word to the address lines.
- Activates the Read control line (set Read/Write to 1).

Memory Enable	Read/Write	Memory Operation
0	X	None
1	0	Write to selected word
1	1	Read from selected word

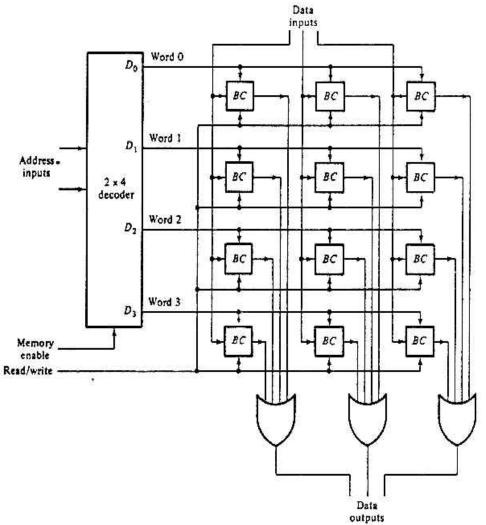
7.3 Memory Cell

- Two types of RAM
 - Static RAMs use flip-flops as the memory cells.
 - Dynamic RAMs use capacitor charges to represent data. Though simpler in circuitry, they have to be constantly refreshed.
- A single memory cell of the static RAM has the following logic and block diagrams:



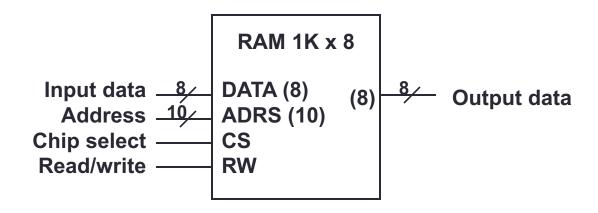
7.4 Memory Arrays (1/4)

Logic construction of a 4×3 RAM (with decoder and OR gates):



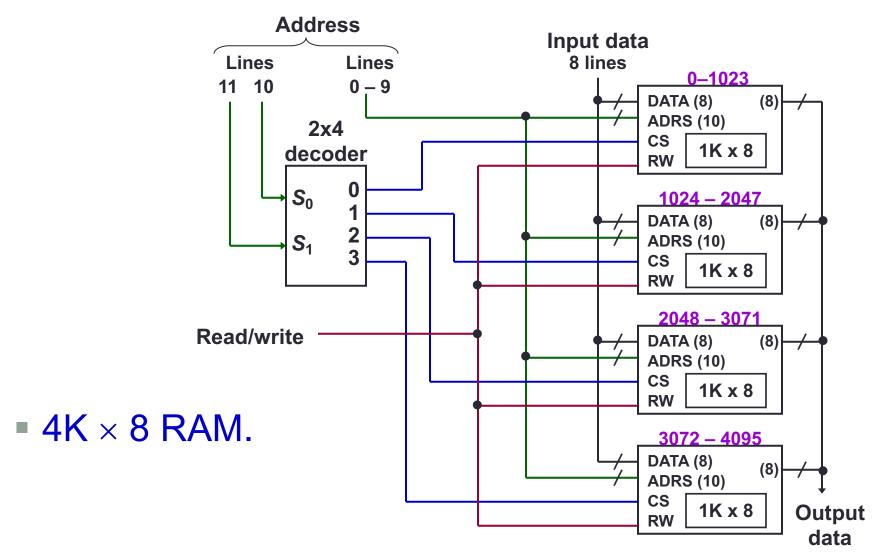
7.4 Memory Arrays (2/4)

- An array of RAM chips: memory chips are combined to form larger memory.
- A 1K × 8-bit RAM chip:

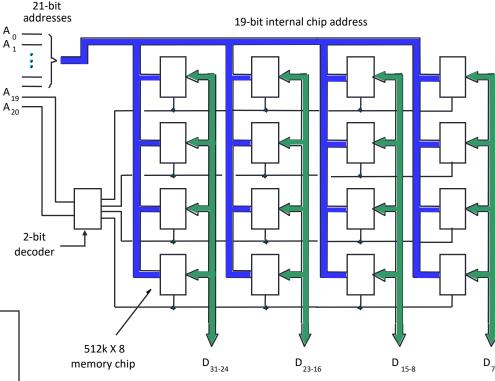


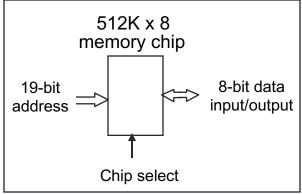
Block diagram of a 1K x 8 RAM chip

7.4 Memory Arrays (3/4)



7.4 Memory Arrays (4/4)





- 2M × 32 memory module
 - Using 512K × 8 memory chips.

End of File