

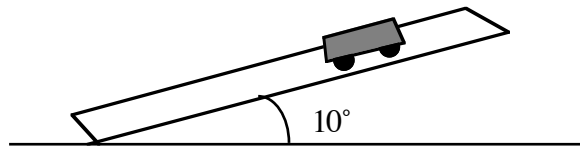
## Homework IV

### Session IV.2

1. One of the nice features of the velocity vs distance formula derived in Unit IV.2 -13 is that it can be used to easily calculate how high an object can be thrown. We learned earlier in the semester that it takes a professional-caliber arm to throw a ball as fast as 50 m/sec. If a ball is thrown straight up at 50 m/sec, how high will the ball go? Use the method of Unit IV.2.
2. I'm going sledding. At the bottom of the hill I travel over level ground, and the snow exerts a force of 200 N on my sled. How much work does that force do on me as I travel 20 m?
3. Continuing on the example in 2, my velocity at the bottom of the hill is 15 m/sec. What is my velocity reduced to after I sled those 20 m? My mass is 70 kg.

### Session IV.3

4. In this problem and the next, you will consider a cart rolling down a tilted board. The cart is released from rest at the top of the board, and then rolls down the full length of the 2 m board. The angle between the board and the table is  $10^\circ$ , as shown.



We saw earlier that the component of the gravity force acting down the plane is  $mg\sin(10^\circ)$ . Given this, calculate the acceleration down the board, and from there, the velocity at the end of the board using the techniques of Unit IV, session 2 (Intro to Conservation of Energy).

5. Now, solve problem 4 again using conservation of energy and  $U=mgh$  for the gravitational force. First, solve for the vertical distance traveled in the 2 m down the board, and from there use conservation of energy to get the velocity at the bottom. You should get the same answer as you got in 4!
6. A weight is oscillating back and forth on a spring. The spring constant  $k$  is 50 N/m, and the weight has mass of 300 g. If it is moving at a velocity of 2 m/sec at the equilibrium ( $x = 0$ ) position, what is the farthest away from this point that it will move?
7. A 2 kg ball rolling at 5 m/sec bumps into a 1 kg ball which is initially at rest. The 1 kg ball takes off at 15 m/sec, and the 2 kg ball rolls backwards at 2.5 m/sec. Was

momentum conserved in this collision? Was kinetic energy conserved in this collision? Do you think this could easily happen? Explain.

#### Session IV.4

8. For the following three force rules, decide if energy is conserved or not. If it is, find the corresponding potential energy:

- a)  $F = -x^3$
- b)  $F = -v^3$
- c)  $F = xv$

9. I have an elastic slingshot that can be approximated as a spring. I put a 0.05 kg ball in it and pull it back 0.3 m, and let it go. The ball shoots straight up for a total distance of 25 m.

- a) What is the spring constant of the slingshot?
- b) What was the maximum force I had to apply to pull the elastic back the full 0.3 m?

10. I am skateboarding along at 5 m/s. A friend ahead of me throws me a 1 kg physics book at  $-1$  m/s. If I weigh 70 kg, how much do I slow down when I catch the book? How much energy is lost in the process?