

	Name: 0	er-soundr	(alda)		
	Due Date:	02/03	5/2018		
List Your Co	ollaborat	ors:			
• Problem 1:					
• Problem 2:					
• Problem 3:					
• Problem 4:					
• Problem 5:	•				
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Assignment: Problem Set 3

White both The converse and contrapositive of each of the following statements (No new to argue whether and of tem are true or false), In each case, get in of all opecarrences of NOT in the final statement.

The contra fositive of the Statement "If A, Then B" is "It NOTCE, then NOTCA)"

a) If a 6 Z and a 22, then da > 7

We can rewrite this as "For all a 6 %, If a 22, Then da >7"

Althying the definition of contra Positie, we get: "For all a EL, It NOT (Au) 7), Then NOT (azz)."
Which becomes, "For all a EZ, If da & 7, Then a < 2."
This best statement is the contratos: the of the Statement given.

6) If X, Y G IR and X4+ Y4=1, then x2+ y2 < 2

We conservite this as "Forati X, TEIR, If x 9+49=+, Then x2+4 \(\frac{1}{12} \). I'

AFRYING the definition of conta Positive We got:
"For all XX CIR, If NOT (x2+x242), then NOT (x4+x9=1),"
Which becomes;

Which becomes; "For all xxiell, If x2+x2>2, then x4+x4 + 1."
This last statement is the contra Positive of the Stellement given

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	Problem 3.
	Let A= {ex; XEIR}
	a) Write a description of A by conving it out of a set
	Using a flotest's with a "the exists" quartities.
	Let A= {YEIR, There exists XEIR with Y= ex }
	b) Find another west to describe A by carring it out of
	a Set using a property without any quantifiers. Briefly explain
	Why your Set is equal.
	A= {YEIR: Y>0}
	This Sex is equivalent to the Sex given becase forevery YETR with
	Y70, there exists can XEIR Good that Y=ex.
,	•
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Problem 9 Let A= {121-7:16 Z} and Let B= {41+7, 116 Z} as show that B & A By lefinition, BEA means that every ellement of Bisalso an element of A. So we just need to find One Element of B Keef is not an element of A. We choose 9 as our example. No tice that 9=9.2 +1, and 26 % so 9 is an element of B. Now Suppose that 9 is con elemny of A, that is, that there exists a NEZL with 9=120-7. We manifulate this equation to find 1: Out assuming That 9EA ted to the contradiction that 1=3, but 16 % by setimition out 3 & 76, 50 9 & A. There fore, it must be the case that B & A. b) Fill in the blanks below with appropriate Phrases So that the result is a correct froof of the Statement that A SB Let a 6A be arbitrary. By definition of A, we can fix a MEZ with a=12m-7, Now notice that Q=12m-7 =12m-8+1= 4(3m-2)+1 Since 3m-267, we conclude that a EB Since a 6A was arbitrary, The result follows.

Problem 5 Let A= {X2+S; X6/23 and Let B= {X6/R: X253 In This Platen, we know that A=B by doing a double containment Proof. a) Prove that ACB Let a. E.A be estimate. By definition of A, we can fix a YER with a= 12+5. By definition, for all a EIR, a=20. So 0125 for every y EIR. Because YEIR, a EIR, so CLGB by definition. Because a was arbitrary, The result follows. 6) Fill in the blanks below with appropriate Phrases so that the result is a correct proof of the Statement that & S.A. Let YEB be arbitian, Bracfinition of B, we know that for all YEIR, YZ5, Now notice that for every XEIR, X20 50 X2+5 EIR, and that X2+5=Y, so YEA. Since YEB was arbitrary The result follows.

() IF a E Z and thre ckists m & Z with a = 10 m, then There exists mEZ with a=5m. We can punite This stentement as " A MFOR ON ACK, It there chists me I with a = 10m, Then there exists, MGTL with a = 5m."

B Athring the betinition of Contlatosities we get "For all a t Z if NOT (there exists in t Z with a=5m), then NOT (There exists mt Z with a=10m)." which becomes! "For an aEZ if for all mEZ we have that at 5 m, then for all mEZ we have that a \$ 10 m." This last statement is the contrapositive of the statement yillen. BITE NYGIR ON X Y X = I The X TX & EZ For all 18 1 1 1 1 1 23 Her 191 4 1 1 1 ... PAGE 2 OF Z FOR ROBLEM 1