

Homework 1

PHYS 600

Sep 8, 2023

Numerical Integration

```
In[111]:=
f[Ω_, z_] := 
$$\frac{1}{\left(\Omega (1+z)^3 + (1-\Omega) (1+z)^{\frac{3}{2}}\right)^{\frac{1}{2}}};$$


In[112]:=
integrateFunction[Ω_?NumericQ, z0_?NumericQ] := NIntegrate[f[Ω, z], {z, 0, z0}];

In[113]:=
ΩValues = {0, 0.3, 0.7, 1};

In[114]:=
(*Generate a plot for each Ω*)
plots = Table[
  Plot[
    integrateFunction[i, z0], {z0, 0, 1},
    PlotStyle → ColorData[97, "ColorList"][[i]],
    AxesLabel → {"z", "Integration Result"},
    Frame → True,
    FrameLabel → {"Integration Result", None}, {"z", None},
    LabelStyle → {FontSize → 14},
    PlotRange → All,
    PlotLegends → Placed[
      {"Ω = " <> ToString[ΩValues[[i]]}], {0.7, 0.1}
    ]
  ], {i, Length[ΩValues]}
];
```

Analytic Integration

```
In[115]:=
Ω = 0 :
```

$$\int_0^z \frac{1}{(1+z')^{\frac{3}{4}}} dz' = \int_1^{1+z} u^{-\frac{3}{4}} du = \boxed{4 (1+z)^{\frac{1}{4}} - 4}$$

In[115]:=

 $\Omega = 1 :$

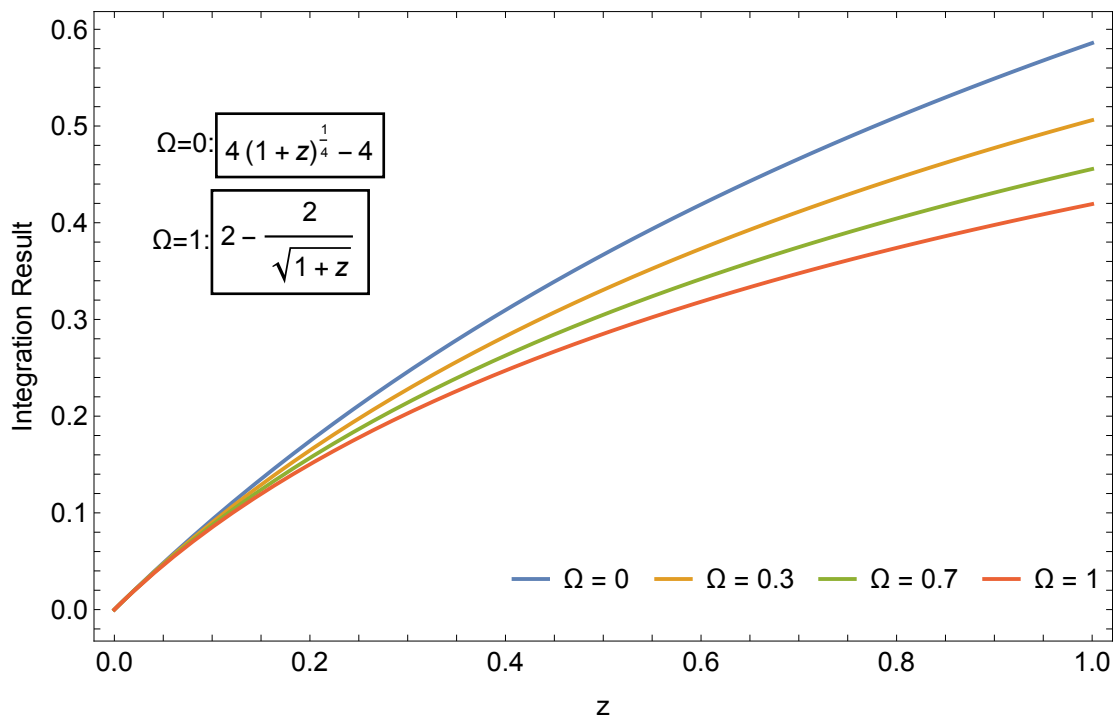
$$\int_0^z \frac{1}{(1+z')^{\frac{3}{2}}} dz' = \int_1^{1+z} u^{-\frac{3}{2}} du = \boxed{2 - \frac{2}{(1+z)^{\frac{1}{2}}}}$$

Plot

In[115]:=

```
combinedPlot = Show[
  plots,
  PlotRange -> All,
  ImageSize -> Large,
  Epilog -> {Text[Style["Ω=0:  $4(1+z)^{\frac{1}{4}} - 4$ ", 14], {0.16, 0.48}],
    Text[Style["Ω=1:  $2 - \frac{2}{\sqrt{1+z}}$ ", 14], {0.15, 0.38}]}
]
```

Out[115]=



In[116]:=

```
(*Export image to png*)
Export["/Users/yaronetokayer/Yale Drive/Classes/PHYS
600/phys600 hw/phys600 hw 1/combined_plot.png", combinedPlot];
```

In[117]:=

```
(*Export the notebook as a PDF*)
NotebookSave[];
NotebookPrint[InputNotebook[],
  "/Users/yaronetokayer/Yale Drive/Classes/PHYS 600/phys600
  hw/phys600 hw 1/phys600 hw 1 printout.pdf"]
```