```python
from flask import Flask, request, jsonify
import pymysql

app = Flask(__name__)

db_host = "*****.ctawqgog6faj.eu-north-1.rds.amazonaws.com"
db_user = "*********"
db_password = "***********"
db_name = "*******"

@app.route('/')
def index():
    return "Flask API is running!"

@app.route('/messages', methods=['GET'])
def get_messages():
    try:
        connection = pymysql.connect(host=db_host, user=db_user, password=db_password,
database=db_name)
        cursor = connection.cursor()
        cursor.execute("SELECT content FROM messages")
        results = cursor.fetchall()
        return jsonify([row[0] for row in results])
    except Exception as e:
        return jsonify({"error": str(e)})

@app.route('/add', methods=['POST'])
def add_message():
    try:
        data = request.get_json()
        message = data.get("message", "")
        if not message:
            return jsonify({"error": "No message provided"}), 400

        connection = pymysql.connect(host=db_host, user=db_user, password=db_password,
database=db_name)
        cursor = connection.cursor()
        cursor.execute("INSERT INTO messages (content) VALUES (%s)", (message,))
        connection.commit()
        return jsonify({"status": "Message added!"})
    except Exception as e:
        return jsonify({"error": str(e)})

if __name__ == '__main__':
    app.run(host='0.0.0.0', port=5000)
```