

Shortest Path Edge

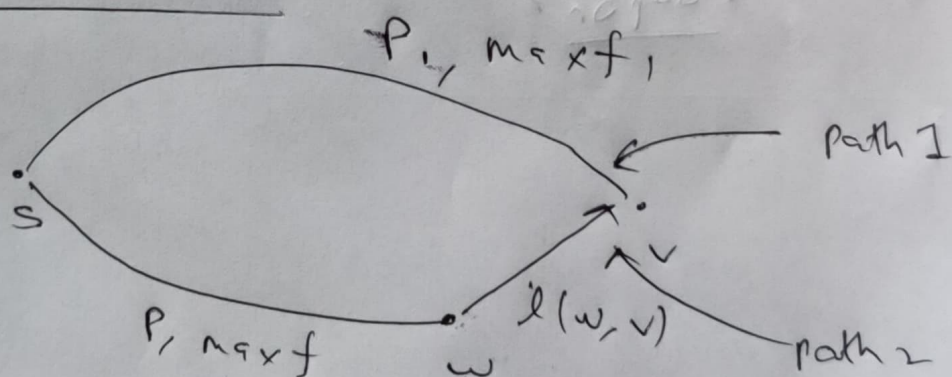
(Using Coupon)

$P_i$ : shortest path from  $s$  to  $v$  and  
 till now, [Coupon Used =  $\max f_i$ ]

$P$ : shortest path from  $s$  to  $w$ .

[Coupon Used =  $\max f$ ]

While Updating



Actual length of path 1 =  $\underline{P_i} + \max f_i$

Actual — — path 2 =  $\text{length}(s \rightarrow w) + l(w, v)$   
 $= P + \max f + l(w, v)$

$\Rightarrow$  Maximum edge in path  $s - w - v$

$\text{Coupon}_{s-w-v} = \max \{ l(w, v), \max f \}$

∴ shortest path  $s - w - v$

= Actual length - Coupon

$$P_{\text{new}} = P + \max f + l(w, v) - \text{Coupon}$$

$\max\{\max f, l(w, v)\}$

Now in the Node 'v' if the path  $P_1$  is still shorter we won't update.

But if  $P_{\text{new}} < P_1$ , then we update path length to  $P_{\text{new}}$  &  $\max f_v$  to 'Coupon'.

Ex:



$P_{\text{new}} + \text{Coupon} = \text{Actual length of path}$

$P_{\text{new}} = \text{Actual length of path} - \text{Coupon}$

$P_{\text{new}} = \text{Actual length of path} - \text{Coupon}$

$s - w - v$  is the shortest path

∴ shortest path  $s - w - v$