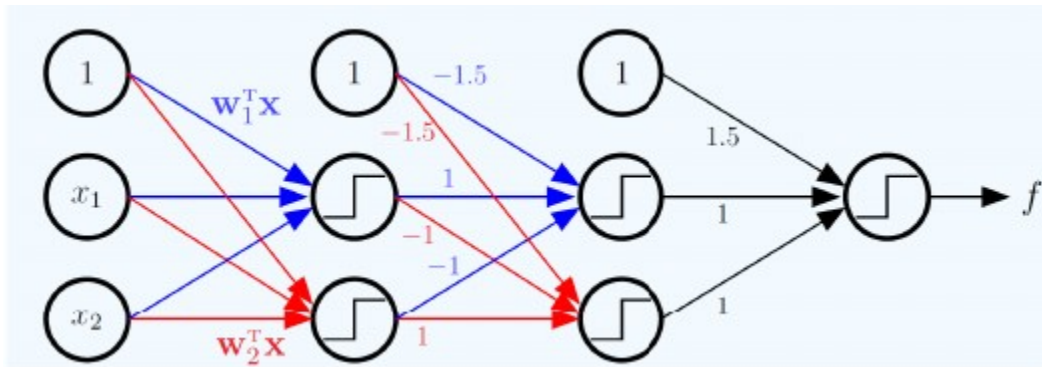


## Task 1 – Explicit Formula for $f$



The given network takes the input vector:

$$\mathbf{x} = [1, x_1, x_2]^T$$

and uses several threshold (step) units defined as:

$$H(z) = 1, \text{ if } z \geq 0; 0, \text{ if } z < 0$$

### Step 1 – First Hidden Layer

Let the first two neurons compute:

$$h_1 = H(w_1^T \mathbf{x}), \quad h_2 = H(w_2^T \mathbf{x})$$

These are the basic activations from the input layer.

### Step 2 – Second Hidden Layer

From the diagram, both second-layer units have a bias of  $-1.5$ .

- The first one connects with  $+1$  from  $h_1$  and  $-1$  from  $h_2$ .
- The second one connects with  $-1$  from  $h_1$  and  $+1$  from  $h_2$ .

Therefore:

$$g_1 = H(-1.5 + h_1 - h_2)$$

$$g_2 = H(-1.5 - h_1 + h_2)$$

### Step 3 – Output Layer

The final node has bias  $+1.5$  and takes inputs from both  $g_1$  and  $g_2$  with weight  $1$ :

$$f = H(1.5 + g_1 + g_2)$$

#### Step 4 – Combined Formula

Substituting all the terms, the final formula becomes:

$$f(\mathbf{x}) = H(1.5 + H(-1.5 + H(\mathbf{w}_1^T \mathbf{x}) - H(\mathbf{w}_2^T \mathbf{x})) + H(-1.5 - H(\mathbf{w}_1^T \mathbf{x}) + H(\mathbf{w}_2^T \mathbf{x})))$$