

Machine data and learning

Assignment 5 part 1

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P(Observation = Red State = Red)	0.85
P(Observation = Green State = Green)	0.9

Initially, the agent knows that it is in one of the red states i.e S1, S2 or S5.

Initial belief state = $[1/3, 1/3, 0, 0, 1/3]$

$P[\text{success}] = 0.71$

$B[s] = (O(s', a, o) \sum T(s, a, s') b(s)) \Pr(o | a, b)$

$O(s', a, o)$ represents probability of observing o after action ' a ' was taken to reach s' i.e. $Pr(o | s, a)$

$T(s, a, s')$ represents probability of going to state s after action ' a ' was taken on s' i.e. $Pr(s | s', a)$

For calculating new belief state

$$b[s] = Pr(o | s, a) \sum Pr(s | s', a) * b(s')$$

The above is an unnormalised probability, we will normalise it by dividing each probability by the sum of all the probabilities.

NOTE: And in our case, $Pr(o | s, a)$ is not dependent on action.

Agent took the action Right and observed Red .

$$b[s1] = 0.85[0.29 * 0.333 + 0.29 * 0.333 + 0 * 0 + 0 * 0 + 0 * 0.333] = 0.164169$$

$$b[s2] = 0.85[0.71 * 0.333 + 0 * 0.333 + 0.29 * 0 + 0 * 0 + 0 * 0.333] = 0.2009655$$

$$b[s3] = 0.1[0 * 0.333 + 0.71 * 0.333 + 0 * 0 + 0.29 * 0 + 0 * 0.333] = 0.023643$$

$$b[s4] = 0.1[0 * 0.333 + 0 * 0.333 + 0.71 * 0 + 0 * 0 + 0.29 * 0.333] = 0.009657$$

$$b[s5] = 0.85[0 * 0.333 + 0 * 0.333 + 0 * 0 + 0.71 * 0 + 0.71 * 0.333] = 0.2009655$$

sum of unnormalised belief state = 0.5994

New belief state = [0.27388, 0.33527, 0.03944, 0.01611, 0.33527]

Agent took the action Left and observed Green .

$$b[s1]=0.15[0.71 * 0.27388 + 0.71 * 0.33527 + 0 * 0.03944 + 0 * 0.01611 + 0 * 0.33527] = 0.06487$$

$$b[s2]=0.15[0.29 * 0.27388 + 0 * 0.33527 + 0.71 * 0.03944 + 0 * 0.01611 + 0 * 0.33527] = 0.01611$$

$$b[s3]=0.9[0 * 0.27388 + 0.29 * 0.33527 + 0 * 0.03944 + 0.71 * 0.01611 + 0 * 0.33527] = 0.09780$$

$$b[s4]=0.9[0 * 0.27388 + 0 * 0.33527 + 0.29 * 0.03944 + 0 * 0.01611 + 0.71 * 0.33527] = 0.22453$$

$$b[s5]=0.15[0 * 0.27388 + 0 * 0.33527 + 0 * 0.03944 + 0.29 * 0.01611 + 0.29 * 0.33527] = 0.01528$$

sum of unnormalised belief state = 0.41861

New belief state = [0.15497, 0.03849, 0.23363, 0.53637, 0.03651]

Agent took the action Left and observed Green .

$$b[s1]=0.15[0.71 * 0.15497 + 0.71 * 0.03849 + 0 * 0.23363 + 0 * 0.53637 + 0 * 0.03651] = 0.02060$$

$$b[s2]=0.15[0.29 * 0.15497 + 0 * 0.03849 + 0.71 * 0.23363 + 0 * 0.53637 + 0 * 0.03651] = 0.03162$$

$$b[s3]=0.9[0 * 0.15497 + 0.29 * 0.03849 + 0 * 0.23363 + 0.71 * 0.53637 + 0 * 0.03651] = 0.35279$$

$$b[s4]=0.9[0 * 0.15497 + 0 * 0.03849 + 0.29 * 0.23363 + 0 * 0.53637 + 0.71 * 0.03651] = 0.08431$$

$$b[s5]=0.15[0 * 0.15497 + 0 * 0.03849 + 0 * 0.23363 + 0.29 * 0.53637 + 0.29 * 0.03651] = 0.02492$$

sum of unnormalised belief state = 0.51425

New belief state = [0.04006, 0.06149, 0.68603, 0.16394, 0.04846]