

Title :- Random variable

Q1 Find the mean and variance for the following :

a)	x	-1	0	1	2
	$P(x)$	0.1	0.2	0.3	0.4

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	0.1	-0.1	0.1	0.01
0	0.2	0	0	0
1	0.3	0.3	0.3	0.09
2	0.4	0.8	0.16	0.64
Total	$\Sigma = 1$	$\Sigma = 1$	$\Sigma E(x)^2 = 0.20$	$[E(x)]^2 = 0.74$

$$\therefore \text{Mean} = E(x) = \Sigma x_i P(x) = 1$$

$$\therefore \text{Variance} = V(x) = \Sigma E(x)^2 - [E(x)]^2 \\ = 2 - 0.74$$

~~$$\therefore \text{Mean } E(x) = 1.29$$~~

~~$$\text{And Variance } V(x) = 0.29$$~~

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x	-1	0	1	2
$h(x)$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$

solution :

x	$h(x)$	$x \cdot h(x)$	$E(x^2)$	$[E(x)]^2$
-1	$\frac{1}{8}$	$-\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{64}$
0	$\frac{1}{8}$	0	0	0
1	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{16}$
2	$\frac{1}{2}$	1	2	1
Total	$\Sigma = 1$	$\Sigma = \frac{1}{8}$	$\Sigma = \frac{1}{4}$	$\Sigma = \frac{69}{64}$

$$\therefore \text{mean} = E(x) = \Sigma x \cdot h(x) = \frac{1}{8}$$

$$\therefore \text{variance } = V(x) = \Sigma E(x)^2 - [E(x)]^2$$

$$= \frac{1}{8} - \frac{69}{64}$$

$$= \frac{152 - 69}{64}$$

$$= \frac{83}{64}$$

$$\therefore \text{mean}(x) = \frac{1}{8} \text{ and variance } V(x) = \frac{83}{64}$$

C	x	-3	10	15
	h(x)	0.4	0.35	0.25

Solution

x	$h(x)$	$x \cdot h(x)$	$E(x)^2$	$\{E(x)\}^2$
-3	0.4	-1.2	3.6	1.44
10	0.35	3.5	3.5	12.25
15	0.25	3.75	56.25	18.0625
Total	$\Sigma = 1$	$\Sigma = 6.05$	$\Sigma = 298.85$	$\Sigma = 27.7525$

$$\therefore \text{mean } E(x) = \sum x \cdot h(x) = 6.05$$

$$\begin{aligned}\therefore \text{variance } V(x) &= \sum E(x)^2 - \sum [E(x)]^2 \\ &= 298.85 - 27.7525 \\ &= 67.0975\end{aligned}$$

$$\therefore \text{mean } E(x) = 6.05 \text{ and variance } V(x) = 67.0975$$

if $h(x)$ is pmf of a random variable x if $h(x_i)$ represent pmf for random variable x_i find value of k then evaluate mean and variance.

Solution : as $h(x_i)$ is a pmf it should satisfy the properties of pmf which are

- $h(x_i) \geq 0$ for all sample space
- $\sum h(x_i) = 1$

x	-1	k_0	1	2
Σ	$k+1/13$	$k/13$	$1/13$	$k-4/13$

$$\begin{aligned} \text{1. } \sum P(x) &= 1 = \frac{k+1}{13} + \frac{k}{13} + \frac{1}{13} + \frac{k-2}{13} \\ 1 &= \frac{k+1+k+1+k-2}{13} \\ 13 &= 3k-2 \\ 15 &= 3k \\ k &= 5 \end{aligned}$$

x	$h(x)$	$x \cdot h(x)$	$E(x)$	$E(x)^2$
-1	6/13	-6/13		
0	5/13	0		25/189
1	1/13	1/13	0	0
2	1/13	2/13	1/13	4/189
Total	$\Sigma = 1$	$\Sigma = -3/13$	$E = -1/13$	$\Sigma = 7/1189$
				$\Sigma = 7/1189$

$$\therefore \text{mean} = E(x) = \Sigma x \cdot h(x) = \frac{-3}{13}$$

$$\therefore \text{Variance} = V(x) = \Sigma E(x)^2 - [E(x)]^2$$

$$= \frac{11}{13} - \frac{41}{169}$$

$$= \frac{143}{169} - \frac{41}{169}$$

$$\frac{62}{169}$$

$$\therefore \text{mean} = -3/13 \text{ and variance} = 62/169$$

Q3 The sum of random variable x is given by

x	-3	-1	0	1	2	3	5	8
$h(x)$	0.1	0.2	0.5	0.2	0.1	0.15	0.05	0.05

obtain cdf find 1) $h(-1 \leq x \leq 2)$ 2) $h(1 \leq x \leq 5)$
3) $E(x \leq 2)$ 4) $h(x \geq 0)$

solution

x	-3	-1	0	1	2	3	5	8
$h(x)$	0.1	0.2	0.5	0.2	0.1	0.15	0.05	0.05
$f(x)$	0.1	0.3	0.75	0.65	0.75	0.90	0.95	1.

$$\begin{aligned}1) h(-1 \leq x \leq 2) &= h(x \leq 2) - h(x \leq -1) + h(x = -1) \\&= f(x_b) - f(x_a) + h(a) \\&= f(2) - f(-1) + h(-1) \\&= 0.75 - 0.3 + 0.2 \\&= 0.25\end{aligned}$$

$$\begin{aligned}3) h(1 \leq x \leq 5) &= f(x_b) - f(x_a) + h(a) \\&= f(5) - f(1) + f(1) \\&= 0.95 - 0.65 + 0.2 \\&= 0.15\end{aligned}$$

$$3) h(x \leq 2) = p(x = -3) + h(x = -1) + h(x = 0) + p(x = 1) + h(x = 5)$$
$$= 0.1 + 0.2 + 0.15 + 0.2 + 0.1$$
$$= 0.75$$

$$\begin{aligned}4) h(x \geq 0) &= 1 - f(0) + h(0) \\&= 1 - 0.95 + 0.15 \\&= 0.90\end{aligned}$$

Let f be continuous random variable with pdf
 $\therefore f(x) = \begin{cases} \frac{x+1}{2} & -1 < x < 1 \\ 0 & \text{otherwise} \end{cases}$

Obtain cdf of x Find mean

Solution : by definition of cdf we have

$$\begin{aligned} F(x) &= \int_{-1}^x \frac{x+1}{2} dt \\ &= \int_{-1}^x \frac{x+1}{2} dx \\ &= \frac{1}{2} \left(\frac{1}{2}x^2 + x \right) \text{ for } -1 \leq x \leq 1 \end{aligned}$$

Hence the cdf is

$$\begin{aligned} F(x) &= 0 \text{ for } x \leq -1 \\ &= \frac{1}{2}x^2 + x \text{ for } -1 \leq x \leq 1 \end{aligned}$$

$$= 0 \text{ for } x \geq 1$$

Plot

Q3

Let $f(x)$ be continuous random variable with cdf
 $f(x) = \frac{1}{18}x^2 + 2$ for $-2 \leq x < 4$
otherwise

calculate cdf

solution : by definition of cdf we have
 $F(x) = \int_2^x t dt$

$$= \int_2^x \frac{5t+2}{18} dt$$

$$= \frac{1}{18} \left(\frac{5x^2}{2} + 2x \right)$$

for $-2 \leq x \leq 4$

hence cdf is

$$F(x) = 0 \text{ for } x < -2$$

$$= \frac{1}{18} \left(\frac{5x^2}{2} + 2x \right)$$

for $-2 \leq x < 4$

= 1 for $x \geq 4$

Title : Binomial distribution

- Q) An unbiased coin is tossed 8 times calculate the probability of obtaining no head, at least one head and more than one tail

No head

$$> d \text{ binom}(0, 8, 0.5)$$

$$[1] 0.0625$$

atleast one head

$$> 1 - d \text{ binom}(0, 8, 0.5)$$

$$[1] 0.9375$$

more than one tail

$$> h \text{ binom}(1, 8, 0.5) \text{ (lower tail = F)}$$

$$[1] 0.9375$$

The probability that a student is accepted to a prestigious college is 0.3 if 5 student apply what is the probability of atleast 2 were accepted

~~$$> p \text{ binom}(2, 5, 0.3)$$~~

2f

- Q3 An unbiased coin is tossed 6 times. The probability of head at any toss = 0.3. Let x be no. of heads. Calculate $P(x=2)$, $P(x=3)$, $P(1 \leq x \leq 5)$

> d binom (2, 6, 0.3)

$$\Sigma 13 \quad 0.324135$$

> d binom (3, 6, 0.3)

$$0.18522$$

> d binom (2, 6, 0.3) + d binom (3, 6, 0.3) d binom
0.74373

- Q4 For $n=10$, $p=0.6$ evaluate binomial probabilities and plot the graph of pdf and cdf.

> $x = \text{seq}(0, 10)$

> $y = h \cdot d \text{ binom}(x, 10, 0.6)$

> y

$$\Sigma 13 \quad 0.0001048576 \quad 0.0015728640 \quad 0.0106160321$$

$$6.00424673280 \quad 0.1118767360 \quad 6.2006581281$$

$$6.2508226580 \quad 0.2149408780 \quad 0.1209323827$$

$$0.0903107890 \quad 0.0660466176$$

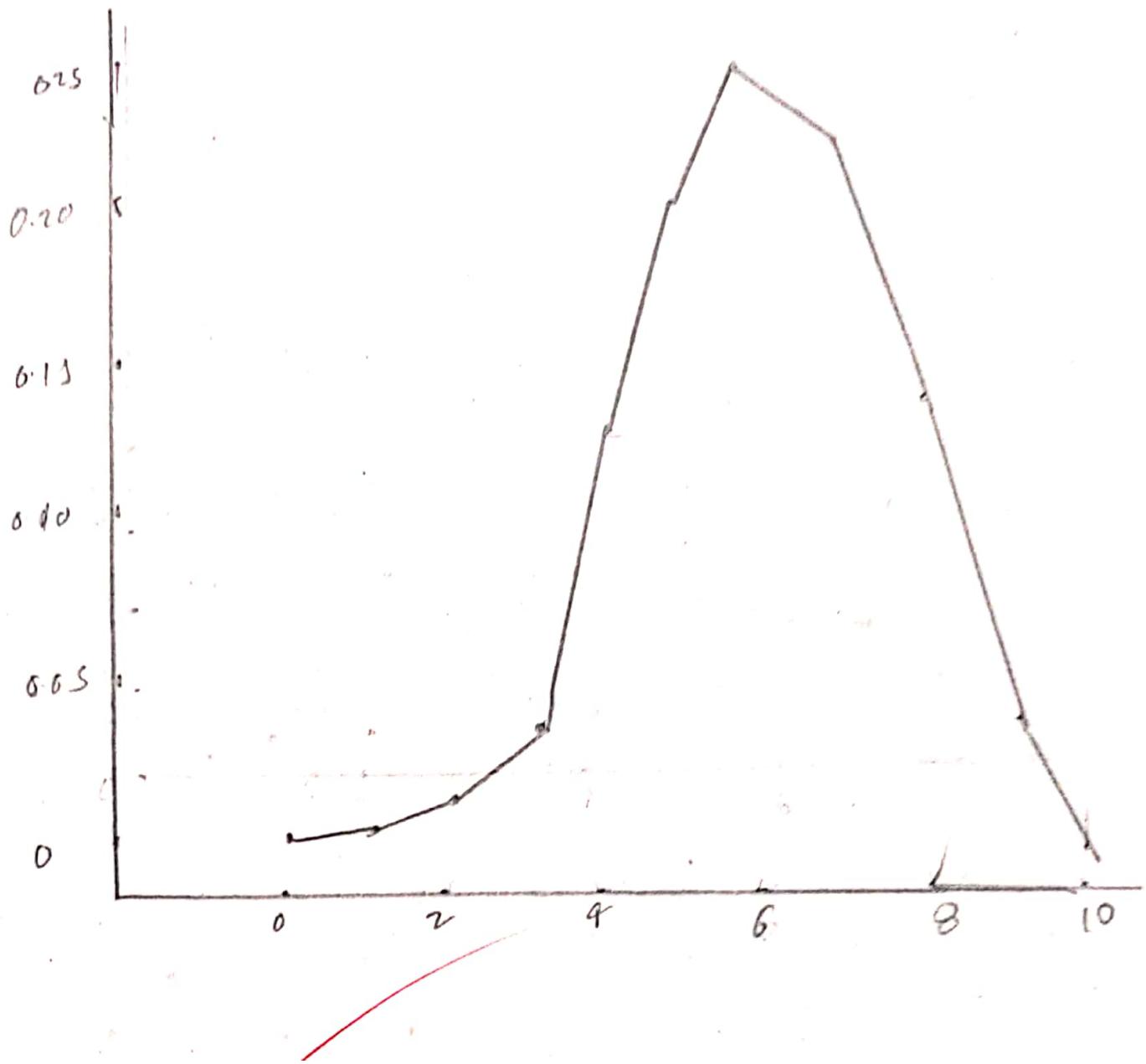
> plot (x, y , xlab = "sequence", ylab = "probability", 0, 10), hch = 10).

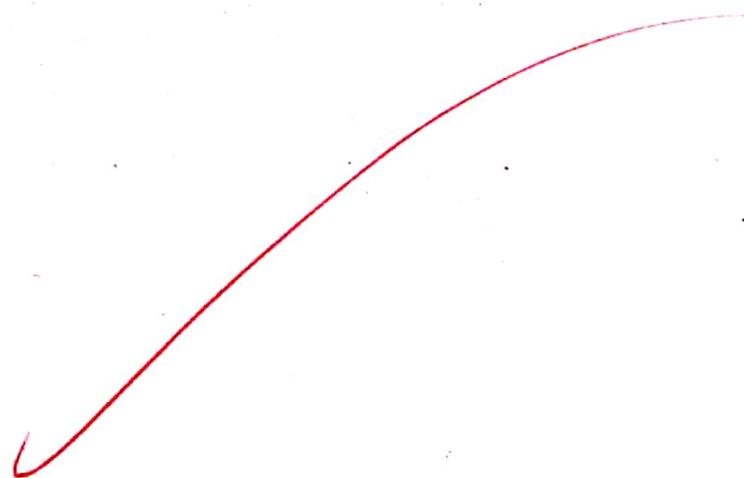
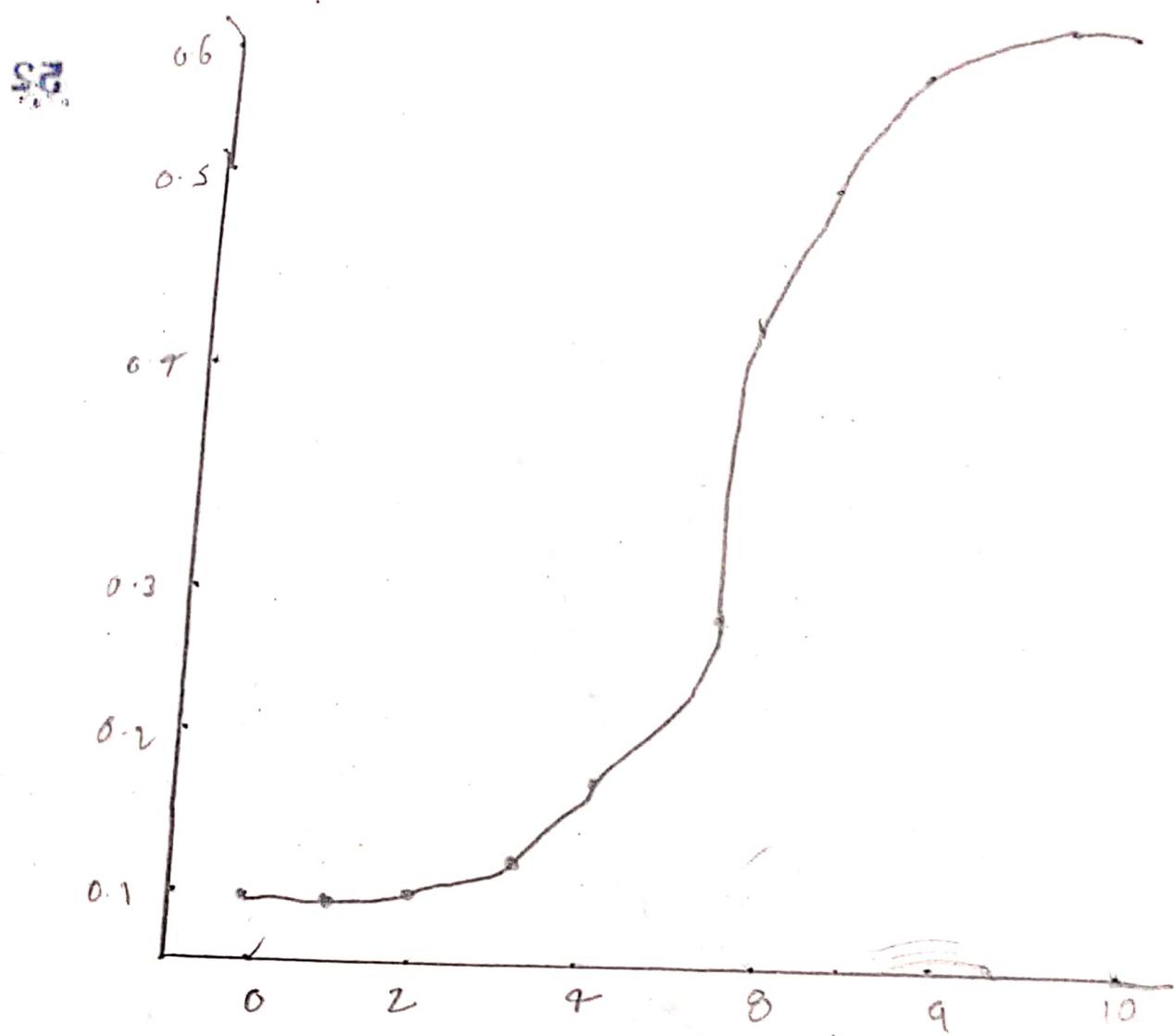
> $x = \text{seq}(0, 10)$

> $y = h \cdot \text{binom}(x, 10, 0.6)$

> plot (x, y , xlab = "sequence", ylab = "probabilities", 0, 10), hch = 10)

a random variable sample of size 10 for a b.d
 $\rightarrow B(10, 0.3)$ Find the mean and the variance of the distribution





> $x \sim \text{Binom}(8, 0.3)$

$$\{1\} 2^8 3^4 \cdot {}^8C_4 \cdot 0.3^4 \cdot 0.7^4$$

> summary(x)

$$\{1\} 2^8 3^4$$

> var(x)

$$\{1\} 3.125$$

The probability of men hitting the target is 11% if he shoots 10 times what is the probability that he hits the target exactly 3 times probability that he hits target atleast one time

> dbinom(3, 10, 0.25)

$$\{1\} 0.25 \cdot 0.2823$$

> 1 - dbinom(1, 10, 0.25)

$$\{1\} 0.812288$$

bits are sent for communication channel in hacket of 12 if the probability of bit being corrected is 0.1 what is the probability of no more than 2 bits are corrupted in a hacket

> pbinom(2, 12, 0.1) lower tail = $\frac{1}{2}$ + dbinom(3, 12, 0.1)

$$\{1\} 0.3409972$$

plus

R>

practical no 3

Title: normal distribution

a) normal distribution of 100 student with mean ≈ 70 ,
 $sD = 15$

Find no of student whose marks are
1) $h(x < 30)$
2) $h(240 < x < 70)$ 3) $h(25 < x < 35)$ 4) $h(x > 80)$

> $hnorm(30, 70, 15)$

[1] 0.2529925

> $hnorm(70, 70, 15) - hnorm(40, 70, 15)$

[1] 0.4772499

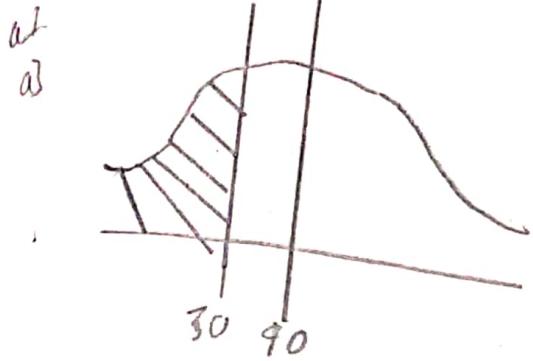
> $hnorm(35, 70, 15) - hnorm(25, 70, 15)$

[1] 0.2107861

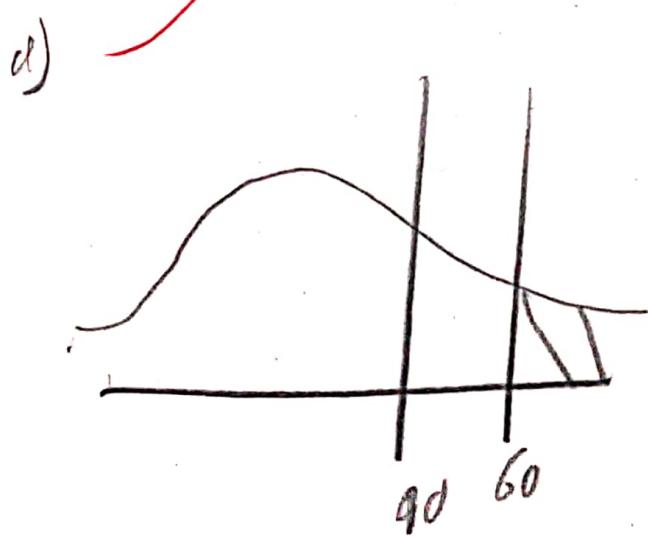
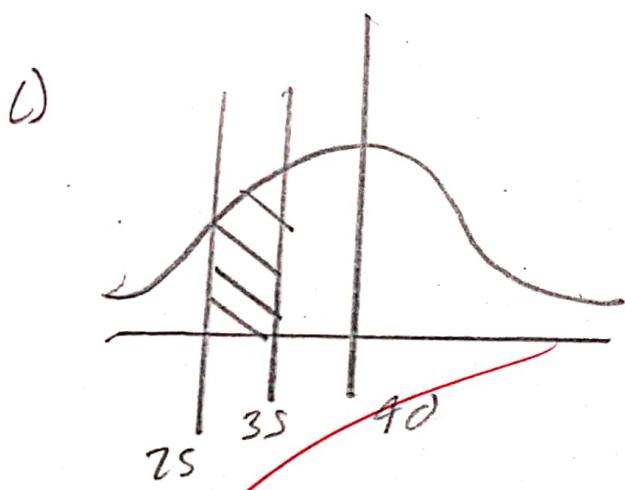
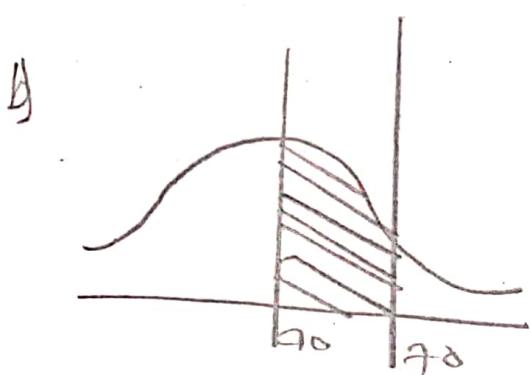
> 1 - $hnorm(60, 70, 15)$

[1] 0.09121122

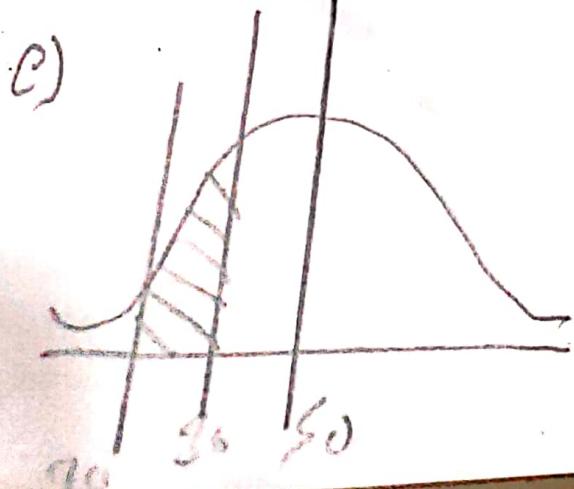
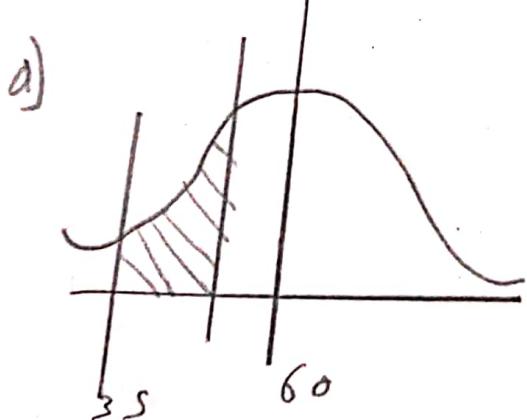
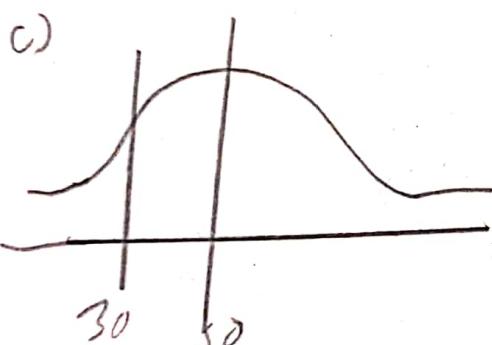
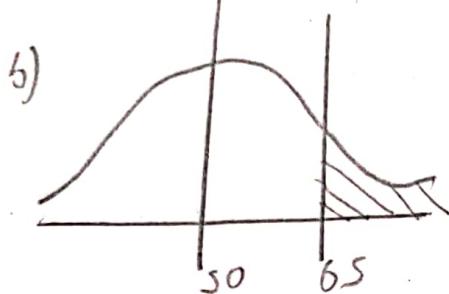
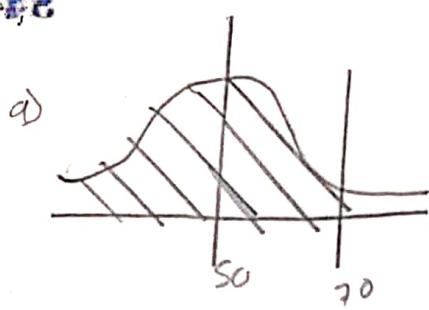




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if with mean = 50 $\sigma = 10$ variable x follows normal distribution
Find 1) $P(x < 70)$ 2) $P(x > 65)$ 3) $P(x \leq 30)$

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> $h_{norm}(70, 50, 10)$

[1] 0.9772 0.99

> $1 - h_{norm}(65, 50, 10)$
0.068072

> $h_{norm}(60, 50, 10) - h_{norm}(35, 50, 10)$
0.7785 375

> $h_{norm}(30, 50, 10) - h_{norm}(20, 50, 10)$
0.02190023

Let $x \sim N(160, 400)$ find k_1 and R_2 such that
 $P(x < k_1) = 0.6$ and $P(x > R_2) = 0.6$

> ~~qnorm~~ 0.6, 160, 20
[1] 165.0869

> ~~qnorm~~ (0.8, 160, 20)
[1] 176.8328

Q8

a random variable x follows normal distribution with $\mu=10$ σ^2 generate 100 observations and evaluate its mean median and variance

$x = rnorm(100, 10, 2)$

> summary(x)

[1] min 1st quartile median mean 3rd quartile max
9.723 9.914 11.325 12.298 13.713 8.928

> var(x)

[1] 3.648924

S a to write a command to generate 10 random numbers from normally distribution with $\mu=50$ $\sigma=4$. Find the sample mean and median

$x = rnorm(10, 50, 4)$

> summary(x)

min 1st quartile median mean 3rd quartile max
40.73 50.96 52.01 52.35 53.39 58.85

peru

sample mean and deviation given single workstation

suppose the food level 2 gms of saturated fat in a single cookie it was found that mean and of saturated fat per cookie it was assume that the sample std deviation is 0.3 at 1% level of significance can be rejected the food level

To check whether reject or accept level hypothesis at 1% level of confidence or 5% level of 10 significance

$$\sigma = 0.3 \quad n = 35 \quad \bar{x} = 2.1 \quad \mu = 2$$

H_0 (null hypothesis) = $\mu \leq 2$

H_1 (alt. hypothesis) = $\mu > 2$

$$Z = \frac{\bar{x} - \mu}{\sigma}$$

S_n

$$Z = \frac{2.1 - 2}{0.3 / \sqrt{35}} = 1.972027$$

$$\begin{aligned} p\text{-value} &= 1 - \text{norm}(2) \\ &= 0.0203 \end{aligned}$$

reject the null hypothesis $\therefore p\text{-value} < 0.05$
 \therefore accepted alternative hypothesis

n A sample of 100 customers was randomly selected
 It was found that average was 275%
 $s_d = 30$ using 0.05 level of significance we
 can conclude that the amt spent by
 customer is more than 250% whereas the
 restaurant claim it is not $> 250\%$

$$\bar{x} = 275 \quad u = 250 \quad \sigma = 30 \quad n = 100$$

$$H_0: \bar{x} \leq 250$$

$$x_1 = 275 > 250$$

$$z = \frac{\bar{x} - u}{\sigma}$$

$$\sqrt{n}$$

$$= 275 - 250 = 0.333$$

$$\frac{30}{\sqrt{100}}$$

$$P(Z \geq 0.333) \text{ lower tail} = F$$

reject the null hypothesis if value $Z > 0.05$

A quality control engineer find that sample of 100 have average of 970 hours assuming H_0 : whether the population mean < 980 hrs at $\alpha = 0.05$

$$n = 100 \quad \bar{x} = 970 \quad H_0: \mu < 980 \quad \sigma = 25 \quad u = 980$$

$$z = \frac{\bar{x} - u}{\sigma} = -9$$

$$P(Z \leq -9) \text{ lower tail} = F$$

$$= 6.1175 + 60 - 0.5$$

reject the null

- accept or reject the hypothesis ($H_0 < H_1$)

- (Q) A principal at school claims that he in 100 of the student a random sample 30 student whose CG was found to be the SD of population is 15 test the claim of the principal

→ method t-tail test

$$H_0 = \mu = 100$$

$$H_1 = \mu \neq 100$$

$$\bar{x} = 112 \quad SD = 15 \quad \mu = 100 \quad n = 30$$

$$Z = \frac{\bar{x} - \mu}{\frac{SD}{\sqrt{n}}} = \frac{112 - 100}{\frac{15}{\sqrt{30}}} = 4.38178$$

$$p\text{-value} = 6.86 \times 10^{-5}$$

reject in tail test

$$H_0 = \mu = 100$$

$$H_1 = \mu \neq 100$$

$$p\text{-value} = 2 \times C(1 - \text{norm}(\text{abs}(Z))) = 1.771278 \times 10^{-5}$$

reject the null hypothesis

p-value < 0.05

~~single population proportion~~

- (Q) it is believed that coin is fair the coin is tossed 90 times 75 times head comes indicate whether the coin is fair or not
95% LOC

$Z = \frac{h - h_0}{\sqrt{\frac{p_0 q_0}{n}}}$ probability of hypothesis

$$p_0 = 0.5$$

$$q_0 = 1 - p_0 = 0.5$$

$$h = 75$$

$$Z = \frac{0.2 - 0.5}{\sqrt{\frac{0.5 \times 0.5}{90}}}$$

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$$H_0 = p = 0.5 \quad H_1: p \neq 0.5$$

$$\text{value} = 0.0117209$$

reject the null hypothesis

$$\because P < 0.05$$

accept the alternative hypothesis

QZ in a hospital 880 female and 520 male was born in a week to confirm male and female were equal in 1:1

$$z = \frac{n - n_0}{\sqrt{p_0 q_0 / n}} \quad p \rightarrow \frac{520}{100} = 0.5 \\ q_0 = 0.5 \quad n = 1000$$

$$H_0 = [p = p_0]$$

$$H_1 = [p \neq p_0]$$

$$z = (n - n_0)$$

$$z = (n - n_0) (\sqrt{p_0 q_0 / n})$$

$$z = 1.2695$$

$$\text{value} = 2 \times C(-\text{norms}(\text{abs}(z)))$$

$$\text{value} = 6.2060506$$

reject the null hypothesis < 0.5

\therefore accept the alternative hypothesis

$$\text{if } n = 100$$

in a big city Z value out of 600 men were found to be found to be self employed conclusion is that maximum men is were self employed

$$z = \frac{n - n_0}{\sqrt{p_0 q_0 / n}}$$

$$p \rightarrow \frac{325}{600} = 0.541667 \quad n = 0.5$$

$$q_0 = 0.5 \quad n = 600$$

$$H_0 = [p = p_0]$$

$$H_1 = [p \neq p_0]$$

$$n \text{ value} = 2 \times (1 - \text{norm}(\text{tsub}(2)))$$

$$\text{sqrt } 10.5 * 0.5 / (1000)$$

$$n \text{ value} = 0.04155289$$

\therefore reject the null hypothesis

$n \text{ value} > 0.5$

\therefore accept the alternate hypothesis
i.e. $p = p_0$

Experience shows that 2% of manufacturers
reject use of top quality in 1 day
production of 900 hypothesis that experience
of 10% of manufacturers product of wrong

$$Z = \frac{n - n_0}{\sqrt{\frac{p_0 q_0}{n}}}$$

$$p = 0.125 (50/900)$$

$$p_0 = 0.2 \quad q_0 = 0.8$$

$$n = 900$$

$$H_0 = [P = 0.2]$$

$$H_1 = [P \neq 0.2]$$

$$Z = (0.125 - 0.2) / \text{sqrt}(0.2 * 0.8 / 900)$$

$$Z = -2.75$$

$$n \text{ value} = 2 \times (1 - \text{norm}(\text{tsub}(2)))$$

$$n \text{ value} = 0.0001708$$

\therefore Reject the null hypothesis. $n \text{ value} < 0.2$

\therefore accept the alternate hypothesis

$$p = 0.2$$

formula

$$Z = \sqrt{pq} \left(\frac{l}{n} + \frac{h}{m} \right) \text{ where } p = \frac{p_1 n_1 + p_2 n_2}{n_1 + n_2}$$

Q1 in an election campaign a telephone poll of 800 registered voters shows 400 out of 800 registered voters found the candidate at 0.50% confidence level. Is there sufficient evidence that nonvoter turnout has decreased from 50% to 40%?

$n = 800$ $n_1 = 400/800 = 0.50$
 $m = 100$ $n_2 = 50/100 = 0.50$
 $r = 0.50 * 800 + 0.50 * 100 / (800 + 100)$
 $r = \sqrt{(0.50 * 0.50) * 1/18}$
 $r = 0.0112398$

$H_0: p = 0.50$
 $H_1: p < 0.50$

P-value $\approx 2 \times (1 - \text{norm}(\text{abs}(r)))$
 ≈ 0.9991053

accept the null hypothesis
 P-value > 0.05
 accept $p = 0.50$

from a consignment of 100 articles we draw a sample of 200 items. From the assignment, 30 items are defective. Test whether the proportion of defective items in 2 consignment are significantly different.

$$H_0: \pi_1 = \pi_2$$

$$H_1: \pi_1 \neq \pi_2$$

$$n_1 = 18/200 = 0.22$$

$$n = 200 = n$$

$$n_2 = 30/200 = 0.15$$

$$n = \frac{p_1 n + p_2 m}{n+m}$$

$$n = 0.22 * 200 + 0.15 * 200 / 200$$

$$n = 0.1225$$

$$Z = \text{Isart} (0.183 + 0.815) * (2/200)$$

$$Z = 0.003884986$$

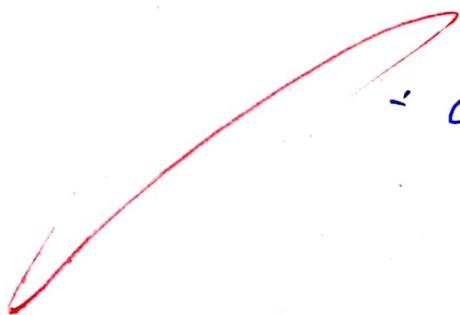
$$\text{value} = Z * (1 - \text{norm}(\text{abs}(Z)))$$

$$\text{value} = 0.9969018$$

$$\text{value} \geq p$$

accept the null hypothesis

$$n_1 = n_2$$



data

Q2

practical - 5

Title :- chi square test

a) use the following data to test whether the attribute condition of snow and child are independent

Ans:-

condition of law

dim	dirty
70	50
80	20
35	45

condition of child

dim
dirty

H_0 = both are independent

H_1 = both are dependent

$\chi^2 = C(70, 80, 35)$

$\gamma = C(50, 20, 45)$

$\gtreqless \text{ data from } (x, y)$

	x	y
1	70	50
2	80	20
3	35	45

$\gtreqless \text{ chisq test}(z)$

Pearson is a square test

data :-

$\chi^2 \text{ squared} = 25.676 \quad df = 2$

p-value = 2.648 x

\therefore both are independent

\therefore Reject the null hypothesis

a dice is tossed	120 times and full results we obtained
no of terms	frequency
1	30
2	25
3	18
4	10
5	22
6	15

test the hypothesis that dice is unbiased

$$H_0 = \text{dice is unbiased}$$

$$H_1 = \text{dice is biased}$$

$$\text{obs} = ((30, 25, 18, 10, 22, 15))$$

$$\text{aor} = \frac{\text{sum}(\text{obs})}{\text{length}(\text{obs})}$$

$$\Rightarrow \text{aor}$$

$$110/20$$

$$\Rightarrow Z = \text{sum}((\text{obs} - \text{aor})^2 / \text{aor})$$

$$\Rightarrow \chi^2_{\text{chisq}} (Z), df = \text{length}(\text{obs} - 1)$$

$$(1) 0.956659$$

-: accept the null hypothesis

-: dice is unbiased

in if test was conducted and the student were observed before and after training the result we fall-

before after

110 120

120 118

123 125

132 136

125 121

test whether there is change in the iq after the training

H_0 = no damage in iq

H_1 = iq increased after training

$$a = C(120, 118, 125, 136, 121)$$

$$b = C(110, 120, 123, 132, 125)$$

$$\chi^2 = \text{sum} ((b-a)/n)^2 / a$$

$$\geq \text{NChisq}(2, df = \text{length}(b) - 1)$$

$$\{1\} 0.1135951$$

accept the null hypothesis

\therefore there is no change in iq after training

Q7

	graduate	undergraduate
online	20	20
face to face	40	5

is there any association between student preference for type of education and method

$\therefore H_0$ = independent

H_1 = dependent

$$\bar{x} = C(20, 90, 25, 5)$$

\bar{z} = matrix (x , nrow = 2)

$\Rightarrow \text{chisq.test}(2)$

pearson chi squared test with gates corrfi continuity correction data = 7

χ^2 squared = 18.08 df = 1

p-value = 2.157

\therefore Reject null hypothesis

\therefore both are dependent

8) a dice is tossed 180 times

62

no of terms	frequency
1	20
2	30
3	36
4	40
5	12
6	73

test the hypothesis that dice is unbiased

H_0 = dice is biased

H_1 = dice is unbiased

$$\chi^2 = CC(20, 30, 36, 40, 12, 73)$$

> chisq.test(x)

chi squared test for given probability

data : z

$$\chi^2\text{-squared} = 28.483 \ df=5$$

$$p\text{-value} = 0.0002236$$

∴ Reject the null hypothesis

dice is unbiased

Join

Q1 $\alpha = C(3386, 3337, 3381, 3710, 3316, 3337, 3398, 3356, 3376, 3382, 3397, 3399, 3398)$
 $\beta = C(3708, 3701, 3390, 3422, 3383, 3377, 3387, 3379)$

test the hypothesis

$$1) H_0: \mu = 3700, H_1: \mu \neq 3700$$

$$2) H_0: \mu = 3700, H_1: \mu > 3700$$

$$3) H_0: \mu = 3700, H_1: \mu < 3700$$

also check at 97% LOC

$$> Shapiro (so = testbc)$$

$$p\text{-value} = 0.987$$

t-test (x , mu = 3700, alter = "two sided", conf level = 0.95)
 $p\text{-value} = 0.000258$
 $p\text{-value} < 0.05$

∴ Reject the null hypothesis.

t-test (x , mu = 3700, alter = "greater", conf level = 0.95)
 $p\text{-value} = 0.9999$

t-test (x , mu = 3700, alter = "less", conf. level = 0.97)

(a) below are the data of weight onto different diets A and B
 list A: (25, 32, 30, 23, 28, 18, 32, 28, 31, 31, 35, 25)
 list B: (44, 34, 22, 10, 87, 31, 90, 30, 32, 33, 19, 21)

$$H_0: \mu_A - \mu_B = 0$$

$$H_1: \mu_A - \mu_B \neq 0$$

$$\geq a = C(25, 32, 30, 23, 28, 18, 32, 28, 31, 31, 35, 25)$$

$$\geq b = C(44, 34, 22, 10, 87, 31, 90, 30, 32, 33, 19, 21)$$

t-test (a, b, paired = +, unpaired = -, alter = "two sided", conf level = 0.95)

data a and b

$$t = 0.02787$$

alternative hypothesis H_1 = "p value = 0.5429"

these diff difference in mean wt of

95 percent confidence interval

$$\sim 14.267330$$

$$7.933999$$

sample estimate

mean of the difference

accept H_0

-3.16667

there is no difference in weight

a) student gave the test after 1 month they gave their test after the tuition etc the main give evidence that student have benefited by coaching

$E_1: 23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19$

$E_2: 28, 19, 22, 18, 20, 22, 20, 20, 23, 20, 17$

test at 99 level of confidence

$E_1: 28, 23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19$

$E_2: 28, 19, 22, 18, 20, 22, 20, 20, 23, 20, 17$

$$H_0 = E_1 = E_2$$

$$H_1 = E_1 < E_2$$

→ t-test (E_1, E_2 paired = after = "less"), conf level = 0.99
paired t test

data E_1 and E_2

$t = -1.482$, $n = 10$, p-value = 0.0841

alternative hypothesis there difference in mean is less than 0
99% confidence method

0.86333

sample estimate

mean of the difference

-1

∴ accept H_0

Q3
at two days for u to was given and data was created
 $d_1 = 0.7, -1.6, -0.2, -1.2, -0.1, 3.7, 3.7, 0.8, 0.2$
 $d_2 = 0.9, 0.8, 1.1, 0.1, -0.1, 7.7, 5.5, 1.6, 7.6, 3.7$

the two drugs always have some effect check whether two drugs have same effect on patient

$$H_0: d_1 = d_2$$

$$H_1: d_1 \neq d_2$$

$$\geq d_1 = C(0.7, -1.6, 0.2, 5.1, -0.1, 3.7, 3.7, 0.8, 0.2)$$

$$\geq d_2 = C(1.9, 0.8, 1.1, 0.1, -0.1, 7.7, 5.5, 1.6, 7.6, 3.7)$$

> t-test (d_1, d_2) salter = "two-sided", paired = T

conf level = 0.95

paired t-test

delta = d_1 and d_2

$$t = -8.0621 \quad df = 9 \quad p\text{-value} = 0.00283$$

alternative hypothesis: true difference in mean not equal to 0

95% confidence interval

mean of the difference

-1.50

∴ Reject H_0

∴ accept H_1

if there is difference in salaries for the sum in 2 different countries

(A: 5300, 4995, 4197, 1838, 2070, 36963

(B: 6290, 5880, 4949, 5220, 17670, 835

$$H_0: S_1 = S_2$$

$$H_1: S_1 \neq S_2$$

> ca = ((133000, 999.50, 81972), 19366, 10970, 36963)
> cb = ((62140, 59850, 81795), 523203, 87037, 93552) 64
> t-test ('ca', 'cb', paired = T, alter = "two-sided", conf.level = 0.95)
paired t test

data 'ca' and 'cb'

t = -7.4564 df = 5 p-value = 0.00666

alternative hypothesis true difference in means not equal
95% confidence interval

-10.80821 - 27.97296

Sample mean

estimate of the difference

= 6.598.043

Reject H₀

accept H_a

practical \rightarrow f-test

at life expectancy in 10 region of India in 1990 and 2000
we give below test whether two variances at the 2 times are same

1990: 98, 137, 39, 36, 42, 29, 5, 8, 96, 19, 2000: 131, 51, 31, 27, 132, 32, 27, 131, 38

2000: 131, 51, 31, 27, 132, 32, 27, 131, 38

var. test (3, 52)

n-value = 0.9176

accept H_0

Q2 I: 25, 28, 26, 22, 23, 24, 31, 31, 32, 31
II: 13, 25, 31, 32, 23, 23, 36, 26, 31, 132, 32, 27, 131, 38

$$H_0: \sigma^2 = \sigma_2^2$$

$$H_1: \sigma^2 \neq \sigma_2^2$$

$S_1 = CC(25, 28, 26, 22, 23, 24, 31, 31, 32, 31)$

$S_2 = CC(13, 25, 31, 32, 23, 23, 36, 26, 31, 132, 32, 27, 131, 38)$

n-value = 0.3381

accept H_0

Q3 for the following data test the hypothesis for equality of 2 population mean regarding variance

$$H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

X = CC(175, 168, 175, 140, 180, 185, 175, 180)

Y = CC(180, 170, 153, 180, 174, 183, 197, 205)

var. test (x, y)

n-value = 0.8218

accept H_0

the fall one the voices of commodity in the sample
 of shops selected at random from different a tie
 city A = (74.10, 77.07, 75.35, 78, 78.80, 79.30, 75.30)
 city B = (70.80, 79.10, 76.90, 76.70, 72.80, 78.10, 74.70,
 $\bar{x} = CC\ 70.10, 77.70, 75.35, 70, 73.80, 79.30, 75.80, 76.90$
 $y = CC\ 70.80, 78.90, 76.20, 72.80, 78.10, 74.70, 69.80, 81.20$

→ Shapiro - Test (x)

n value = 0.655 9

→ Shapiro test (y)

n value = 0.9309

∴ delta is normal

$$H_0 : \sigma_1^2 = \sigma_2^2$$

$$H_1 : \sigma_1^2 \neq \sigma_2^2$$

n. value = 0.0928

2 Variance are not equal : reject H_0 = accept

$$H_0 : \bar{x}_1 = \bar{x}_2$$

$$H_1 : \bar{x}_1 \neq \bar{x}_2$$

→ t-test (x , var equal = F)

n. value = 3.488

t-test (y , var. equal = F)

n. value = 1.06

accept H_0

Q3:

Recreate esv file in excel import the file and apply the test to check the equality of variance of 2 data.

$$\text{obs 1: } 10, 15, 17, 16, 16, 20$$

$$\text{obs 2: } 15, 18, 16, 15, 12, 14$$

$$H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

?Data = read.csv(file - choose w, header = T)

?Data

observation 1 observation 2

10	15
15	18
17	16
11	11
16	12
20	19

?attach(data)

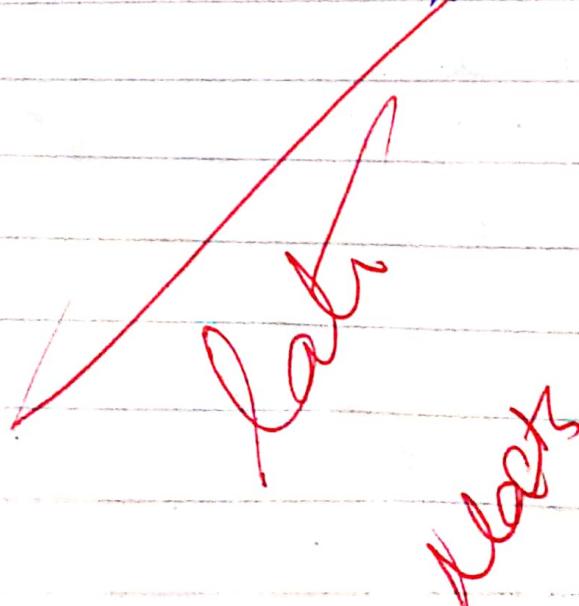
?mean(observation 1)

$$(14.8333)$$

?var.test(observation 1, observation 2)

$$p\text{-value} = 0.51717$$

∴ accept H_0



non parametric test

66

- (1) the lifespan of failure in hours of 10 random selected batteries is given. Test the hypothesis that the population median is 63 against the null hypothesis that the population median is then 63.

solution: $H_0: \text{median} = 63$

$H_1: \text{median} < 63$

$$x = (28.9, 15.2, 28.9, 72.5, 78.5, 52.7, 37.6, 49.5, 62.1, 57.5)$$

$s_n = \text{len which } (x < 63)$

$a_n = \text{len which } (x \geq 63)$

$n = s_n + a_n$

2 binom ($0.05, n, 0.5$)

s_n

9

2 binom ($s_n, n, 0.5$)

0.9490205

H_0 is accepted

- 2) date of weight of 40 student in random sample are

46, 49, 57, 69, 46, 67, 54, 78, 69, 61, 77, 57, 52, 50, 78, 63, 56, 67, 94, 60, 69, 53, 50, 78, 51, 53, 57

Use the sign test to test whether the mean weight of population is less than the alternative that is greater than 50.

$H_0: \leq 50$

$H_1: > 50$

$$x = (46, 49, 57, 64, 46, 67, 59, 78, 69, 61, 57, 50, 50, 78, 65, 61, 50, 58, 59, 62, 77, 79, 77, 56, 59, 63, 53, 55, 60, 64, 53, 50, 98, 51, 52, 58)$$

$s_n = \text{len which } (x > 50)$

$a = \text{length } (s_n)$

2d

Q2) $H_0: \mu \leq 50$
 $H_a: \mu > 50$

$b = \text{length}(sn)$

$> b$

> 7

$n = a + b$

$> n$
 > 28

$q_{\text{binom}}(0.05, n, 0.5)$

> 16

$n_{\text{binom}}(a, n, 0.5)$

> 0.9981404

$\therefore n_{\text{binom}}$ value is greater than 0.5
 \therefore accept the null hypothesis

Q3) the median age of tourist visiting a certain place
gives a random sample of 17 tourist have the age

(25, 29, 52, 28, 57, 39, 45, 36, 30, 99, 28, 39, 78, 63, 32, 48)

$H_0: \text{which } (\bar{x} < 41)$

$x = [23, 29, 52, 28, 57, 39, 45, 36, 30, 99, 28, 39, 78, 63, 32, 48]$

$H_0: \text{which } (\bar{x} \geq 41)$

$a = \text{length}(sn)$

$> a$

$H_0: \text{which } (\bar{x} < 41)$

$b = \text{length}(sn)$

b

$> b$

$n = a + b$

$> n$

17

≥ 5 (coarsen 0-5)

- q binos value is less than or equal
- accept the null hypothesis

at the weight in kgs of the person before and after
smoking are as follows
before :- 65, 75, 75, 62, 72 after 72, 82, 72, 66, 73

use the wilcoxon test to check whether the weight
of the person increases after the smoking of
so smoking by 5% level of significance
 $x = (65, 75, 75, 62, 72)$
 $y = (72, 82, 72, 66, 73)$
 $n = x - y$

n

> -7 -7 3 -4 -1

> wilcoxon test (n , $\mu = 0$)

n-value = 0.1750

n-value ≈ 0.5

accept the null hypothesis

The time in min that a patient has to
wait for consultation is recorded as follows

is 17, 15, 24, 25, 20, 21, 33, 28, 12, 25, 28, 28

Use wilcoxon sign test whether the
medium of waiting time is more than 20%
level of sig significance

5a

$\alpha = c(15, 7, 28, 25, 20, 21, 32, 28, 12, 21, 28, 20)$

$H_0: \geq 20$ $H_1: < 20$
willcox t-test
 $p\text{-value} = 0.999$
 $\therefore p\text{-value} > 0.5$
accept the null hypothesis.

Practical 9

Q) the following are of three treatment

$$\text{ans } \begin{aligned} a &= 2, 3, 7, 2, 6 \\ b &= 10, 8, 7, 5, 10 \\ c &= 10, 13, 18, 13, 15 \end{aligned}$$

68

ans:-

```
a=c(2, 3, 7, 2, 6)
b=c(10, 8, 7, 5, 10)
c=c(10, 13, 18, 13, 15)
d=data.frame(a,b,c)
>d
```

	a	b	c
1	2	10	10
2	3	8	13
3	7	7	18
4	2	5	15
5	8	10	13

>stack(d)

>l

	values	ind
2	2	a
3	3	a
4	7	a
5	2	a
6	6	a
7	10	a
8	8	b
9	7	b
10	5	b
11	10	b
12	10	c
13	13	c
14	18	c
15	13	c

`R> oneway.test(values ~ ind, data=)`
 one-way analysis of mean (not assuming equal variances)
 data: values and ind
 $F = 21.537$, num df = 2.0, denom df = 7.9317, p-value = 0.0000000

2) the following gives life of tire of F brands

a = 20, 23, 18, 17, 22, 24

b = 19, 15, 17, 20, 10, 17

c = 21, 19, 22, 17, 20

d = 15, 19, 18, 17, 16

ans:-

a = c(20, 23, 18, 17, 22, 24)

b = c(19, 15, 17, 20, 16, 17)

c = c(21, 19, 22, 17, 20)

d = c(15, 19, 16, 18, 17, 16)

> e = list(a, b, c, d)

or

a1

[1] 20, 23, 18, 17, 22, 24

a2

[2] 19, 15, 17, 20, 16, 17

a3

[3] 21, 19, 22, 17, 20

a4

15, 19, 16, 18, 17, 16

f = stack(e)

> ef

	values	ind
1	20	a1
2	23	a1
3	18	a1
4	17	a1
5	22	a1
6	24	a1
7	19	a2
8	15	a2
9	17	a2
10	20	a2

11		
12	16	a2
13	17	a2
14	21	a3
15	19	a3
16	22	a3
17	17	a3
18	26	a3
19	15	a4
20	17	a4
21	18	a4
22	18	a4
23	17	a4
	18	a4

> one way test (values & ind) data = f)

data: one way analysis of means (not assuming equal variances)
 values and ind
 $F = 7.453$, num df = 3.000, denom df = 10-207, p-value
 $= 0.006291$
 Reject H_0

3 types of war are applied for the protection of
 cov and no of list of protection were noted
 test this are equally effective

- a:- 77, 75, 96, 17, 18, 74
- b:- 90, 42, 51, 53, 55
- c:- 50, 53, 58, 59

ea

ans

$a = CC(44, 45, 76, 97, 98, 17, 18)$

$b = CC(10, 12, 13, 14, 15, 16, 17)$

$c = CC(50, 53, 58, 59)$

$d = list(a_1=a, b_1=b, c_1=c)$

$\rightarrow d$

a_1
 $\{1\} 79 \ 45 \ 96 \ 47 \ 98 \ 19$

b_1
 $\{1\} 40, 42, 51, 52, 55$

c_1

$\{1\} 50, 53, 58, 59$

$\rightarrow e = stack(d)$

$\rightarrow e$

values index

1 98 a1

2 45 a1

3 46 a1

4 47 a1

5 78 a1

6 99 a1

7 90 b1

8 52 b1

9 51 b1

10 52 b1

11 55 b1

12 50 b1

13 53 b1

18 58 51
15 59 59
9

> one-way test (values and data =)

One-way analysis of means (not assuming equal variances)

data: values and ind

$F = 6.3398$, num df = 2.000, denom df = 5.7059, p-value = 0.038

70

Q) an experiment

noted they was conducted on minutes 16 exercise. were three group not exercise 20

a = 23, 26, 51, 78, 58, 37, 29, 90

b = 22, 27, 29, 39, 46, 98, 99, 65

c = (59, 66, 38, 99, 56, 60, 56, 62)

> d = data-frame

ans:-

a = c(23, 26, 51, 78, 58, 37, 29, 90)

b = c(22, 27, 29, 39, 46, 98, 99, 65)

c = c(59, 66, 38, 99, 56, 60, 56, 62)

> d = data-frame(a, b, c)

	a	b	c
1	23	22	59
2	26	27	66
3	51	29	38
4	78	39	46
5	58	46	56
6	37	98	60
7	29	49	56
8	90	65	62

> l = stack(d)

51

	values	ind
1	23	a
2	26	a
3	51	g
4	98	g
5	58	g
6	37	4
7	79	4
8	78	a
9	22	N
10	27	b
11	29	b
12	39	b
13	86	b
14	88	b
15	99	b
16	65	b
17	59	b
18	66	b
19	38	c
20	49	c
21	56	c
22	60	c
23	56	c
24	62	c

one way test (values in ind, data)
 one way analysis of means (not assuming equal var.)
 data: values and ind
 $F = 25.69$ num df = 7.00 denom df = 13.333
 $P-value = 0.01333$

pw

reject H_0