CS 205: Artificial Intelligence Assignment 1

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In completing this assignment I consulted:

- 1. The Project Statement Handout provided.
 - a. https://d1u36hdvoy9y69.cloudfront.net/cs-205-ai/Project_1_The_Eight_Puzzle_CS_2 https://d1u36hdvoy9y69.cloudfront.net/cs-205-ai/Project_1_The_Eight_Puzzle_CS_2 https://d1u36hdvoy9y69.cloudfront.net/cs-205-ai/Project_1_The_Eight_Puzzle_CS_2
- 2. For Randomly generated puzzles
 - a. https://www.andrew.cmu.edu/course/15-121/labs/HW-7%20Slide%20Puzzle/lab.ht ml
- 3. To check if a puzzle is solvable or not in constant time and by not exploring the entire search space. This was used only for generating puzzle problems and was not used in original search code.
 - a. https://www.geeksforgeeks.org/check-instance-8-puzzle-solvable/

All the code is original **Except**

- Using the math module to calculate the square root of a number
- Using the copy module to make deep copies of a node
- Using the time module to keep track of time
- Using the numpy module to generate random numbers
- Using the matplotlib module to plot graphs and figures
- To check if a puzzle is solvable or not in constant time and by not exploring the entire search space. This was used only for generating puzzle problems and was not used in original search code.
 - https://www.geeksforgeeks.org/check-instance-8-puzzle-solvable/

Link to Code

- The code is available on github → <u>https://github.com/yashUcr773/CS_205_Al/tree/main/Projects/Project%201</u>
- The code can also be run on google colab →
 https://colab.research.google.com/drive/18yNb0bLmRX-0jsQMP5Q_JEtD-t0i4NMS

Outline of this report

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CS 205: Artificial Intelligence Project 1: The 8-Puzzle Project Report

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1. Introduction

A sliding tile puzzle, Figure 1, is a combinatorial puzzle that consists of numbers from 1 to N-1 where N is a perfect square (4,9,16,25...) and the numbers are arranged in a N x N grid. The last tile is removed from the puzzle leaving 1 spot open. The goal of the puzzle is to move the tiles in such a way that all the numbers are arranged in ascending order and the empty spot is the last tile. The 8 puzzle is a sub-problem of the sliding puzzle with N set as 9 and tiles are numbered from 1 to 8.



Figure 1: An 8 puzzle

Source: https://play.google.com/store/apps/details?id=com.gsr.npuzzle

This report details the findings for the 8-puzzle solved using different algorithms and a comparison between the algorithms.

In this project we attempt to solve the 8-puzzle using

- 1) Uniform Cost Search Algorithm
- 2) A* Algorithm with Misplaced Tile Heuristic
- 3) A* Algorithm with Manhattan Distance Heuristic

The project and report are a requirement for completion of the course CS 205: Artificial Intelligence taken under professor Dr. Eamonn Keogh in the Spring Quarter of 2023 at the University of California, Riverside.

The Language of choice is Python (version 3.9.X) and additional imports include (matplotlib, numpy, time, math, copy and os). The Report also includes the original source code.

Within this report the word puzzle and problem are used interchangeably and denote the state of the puzzle board provided by the user.

Also puzzles will be classified as Easy, Medium and Hard.

- Puzzles with depth <= 9 are considered to be Easy.
- Puzzles with depth >= 10 and depth <= 19 are considered medium.
- Puzzles with depth >= 20 are considered Hard.

This is an informal metric for puzzle classification used in this report.

2. Algorithms

The algorithms used to solve the 8-puzzle are

- 1) Uniform Cost Search Algorithm
- 2) A* Algorithm with Misplaced Tile Heuristic
- 3) A* Algorithm with Manhattan Distance Heuristic

2.1 Uniform Cost Search Algorithm

Uniform Cost search, also known as the Uninformed search, is a search algorithm that assigns a uniform cost (say 0) as a cost of expansion of every node. This means that the total cost to expand a node is only its depth. This also means that the cost of expanding all the nodes at any given depth d is the same for all the nodes.

When compared to A* Search and while implementing the algorithm in the project, g(n) = depth of the node h(n) = 0Total cost to expand a node = h(n) + g(n) = g(n)

2.2 A* Search Algorithm

A* search, also known as the Informed search, is a search algorithm that uses a heuristic or a cost function for each node to measure how farther or closer the expansion will take us to the solution. It is referred to as Informed search as we make informed decisions based on cost function for which nodes need to be expanded next. The node with the smallest cost is selected. This means all the nodes have different cost of expansion that depends on their depth and how close to the final state we are.

For this project we have chosen 2 Heuristic functions.

- 1) Misplaced Tile Heuristic
- 2) Manhattan Distance Heuristic

2.2.1 Misplaced Tile Heuristic

The Misplaced tile heuristic or the hamming distance heuristic counts the total number of tiles that are not in their correct position when compared to the goal state. While calculating the heuristic, we do not consider the placeholder (blank, _, 0) in the calculations.

In Figure 2, we can see there are 5 tiles namely (1,2,5,6,8) that are in incorrect positions and only 3 tiles (3,4,7) that are in correct positions. Therefore the misplaced tile heuristic or the hamming heuristic for the problem is 5.

Let us say this node is at depth d.

The total cost of expansion of this node would be g(n) + h(n) = d + 5.

Instead of just d in case of uniform search.

With this heuristic cost function we could expand the nodes with the smallest cost and thus expand cheaper nodes first, leading to goal nodes in fewer expansions.

2.2.2 Manhattan Distance Heuristic

The Manhattan distance heuristic counts the minimum number of moves that would be required to move a tile to its correct place assuming there are no other tiles on the board. While calculating the heuristic, we do not consider the placeholder (blank, _, 0) in the calculations.

In Figure 2, we can see there are 5 tiles namely (1,2,5,6,8) that are in incorrect positions and it would take (1,2,2,2,3) moves respectively for each tile to be in the correct position. Therefore the Manhattan heuristic value is 10.

Let us say this node is at depth d.

The total cost of expansion of this node would be g(n) + h(n) = d + 10.

Instead of just d in case of uniform search.

With this heuristic cost function we could expand the nodes with the smallest cost and thus expand cheaper nodes first, leading to goal nodes in fewer expansions.

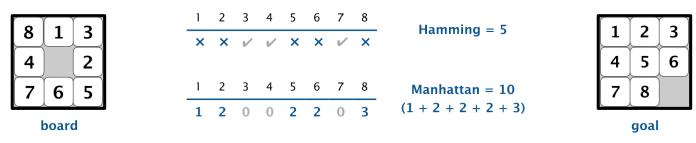


Figure 2: Misplaced Tile (Hamming) Heuristic and Manhattan Heuristic

Source: https://coursera.cs.princeton.edu/algs4/assignments/8puzzle/hamming-manhattan.png

3. Comparison of Algorithms

We will now be running our program on various 8-puzzles of varied depths and visualizing the results.

Figure 3 Denotes the list of puzzles used in testing. These were a good starting point to test the algorithms in early development stages.

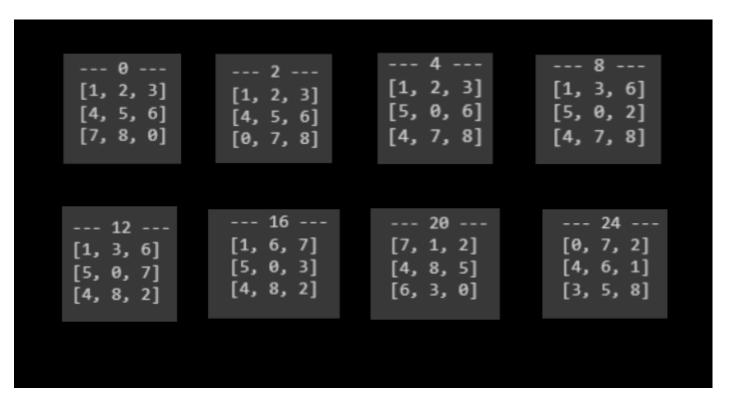


Figure 3: List of Problem States provided by Professor Keogh

Figure 4 Denotes some of the puzzles that I created for other depths. These were generated by me using the code that is attached with this report. These were helpful in generating the reports for analysis.

```
--- 6 ---
[1, 2, 3]
             [7, 8, 6]
                           [2, 0, 3]
                                        [4, 7, 8]
             [7, 8, 6]
[4, 5, 6]
                           [1, 5, 6]
                                        [4, 7, 8]
[7, 0, 8]
             [7, 8, 6]
                           [4, 7, 8]
                                        [4, 7, 8]
                        --- 10 ---
 [4, 1, 2]
             [1, 4, 8]
                          [2, 3, 5]
                                       [5, 0, 6]
 [5, 8, 3]
             [1, 4, 8]
                          [1, 4, 6]
                                       [5, 0, 6]
                          [0, 7, 8]
 [7, 0, 6]
             [1, 4, 8]
                                       [5, 0, 6]
             --- 14 ---
                                        --- 17 ---
 [7, 2, 3]
             [7, 8, 6]
                          [4, 2, 1]
                                       [2, 7, 6]
[0, 5, 6]
             [7, 8, 6]
                          [0, 3, 6]
                                       [2, 7, 6]
[1, 4, 8]
             [7, 8, 6]
                          [7, 5, 8]
                                       [2, 7, 6]
--- 18 ---
             --- 19 ---
                          --- 21 ---
[7, 5, 3]
                          [3, 5, 4]
             [7, 0, 8]
                                       [6, 4, 2]
[1, 4, 6]
             [7, 0, 8]
                          [8, 7, 0]
                                       [6, 4, 2]
             [7, 0, 8]
                          [2, 6, 1]
[2, 8, 0]
                                       [6, 4, 2]
--- 23 ---
              --- 25 ---
                          --- 26 ---
[1, 0, 8]
             [7, 3, 6]
                          [6, 3, 1]
                                       [8, 1, 3]
             [7, 3, 6]
                          [4, 0, 7]
 [4, 7, 2]
                                       [8, 1, 3]
 [3, 5, 6]
             [7, 3, 6]
                          [8, 2, 5]
                                       [8, 1, 3]
--- 28 ---
                              --- 30 ---
                   29 ---
[6, 4, 7]
                              [6, 4, 7]
               [5, 2, 1]
                              [8, 3, 5]
[3, 2, 8]
               [3, 8, 4]
[0, 5, 1]
                              [1, 2, 0]
               [6, 0, 7]
```

Figure 4: List of Problem States generated by me.

In Figure 5, we can see the comparison of algorithms based on time taken to solve the puzzles at various depths. A* Search with Manhattan distance heuristic seems to be performing the best among the three algorithms. Even on the hardest puzzle with depth 30, the algorithm seems to take merely 10 seconds to search for the answer.

The second best algorithm seems to be A* search with Misplaced Tile heuristic. For easy to medium puzzles, The Misplaced Tile Heuristic takes little to no time. However as we move towards harder problems, we can see the sharp increase in time taken to run the algorithm with the hardest taking close to 600 seconds to run a problem with depth 30.

Finally the Uniform Search performed the worst among the three algorithms. Half way through the medium puzzles we can see it taking longer to search for the goal state with the algorithm taking close to 700 seconds for the depth 30 puzzle.

The better performance of A* algorithms can be attributed to the cost function heuristic that helps the algorithm expand only the best tile closest to solution as opposed to uniform search that uses no cost function.

As for the manhattan and misplaced tile heuristics, the former runs better than the latter as it better estimates the cost function and thus expands the nodes closest to goal.

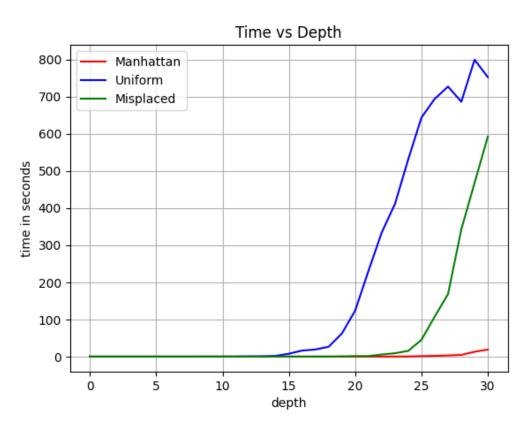


Figure 5: Comparison of all three algorithms based on time taken to reach goal state vs the depth of solution

In Figure 6, we can see the comparison of algorithms based on the number of nodes expanded to solve the puzzles of various depths. Similar results can be drawn here as Figure 5.

A* Search with Manhattan distance heuristic seems to be performing the best among the three algorithms. Even on the hardest puzzle with depth 30, the algorithm expands around 13,000 nodes to reach the goal state.

The second best algorithm seems to be A* search with Misplaced Tile heuristic. For easy to medium puzzles, The Misplaced Tile Heuristic expanded a low amount of nodes. However as we move towards harder problems, we can see the sharp increase in total nodes expanded with the hardest taking close to 120,000 nodes for a problem with depth 30

Finally the Uniform Search performed the worst among the three algorithms. Half way through the medium puzzles we can see it expanding a large number of nodes to search for the goal state

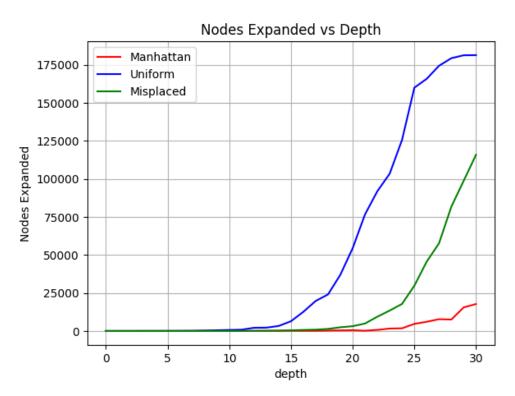


Figure 6: Comparison of all three algorithms based on number of nodes expanded to reach goal state vs the depth of solution

In Figure 7, we can see the comparison of algorithms based on the maximum length of the frontier queue at various solution depths. Similar results can be drawn here as Figure 5 and 6.

A* Search with Manhattan distance heuristic seems to be performing the best among the three algorithms. Even on the hardest puzzle with depth 30, the algorithm had a maximum of 6000 nodes in its queue.

The second best algorithm seems to be A* search with Misplaced Tile heuristic. For easy to medium puzzles, The Misplaced Tile Heuristic had a low amount of nodes in its queue. However

as we move towards harder problems, we can see a sharp increase in queue size with the largest queue size of approximately 24000 for a problem with depth 30

Finally the Uniform Search performed the worst among the three algorithms. At the start of medium puzzles, we can see it has a very large queue size and the trend continues as we move towards the hard puzzles.

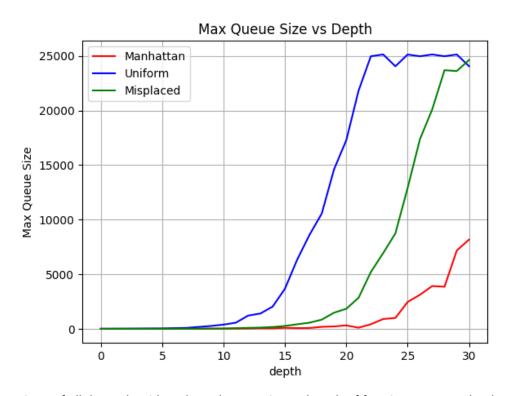


Figure 7: Comparison of all three algorithms based on maximum length of frontier queue vs the depth of solution

4. Conclusions

After testing the puzzles on all the algorithms, it was found that.

- 1. All the algorithms did similar in terms of time, nodes expanded and max length of queue for easier puzzles (depth < 10)
- 2. For the medium puzzles (depth >= 10 and depth <20), we see that uniform search takes a lot more time whereas Manhattan and Misplaced heuristics are still comparable. Same is true for total nodes expanded and Max nodes in queue.
- 3. For the Hard Puzzles (depth >= 20), we can see that uniform search seems to take a considerable amount or time with Misplaced Heuristic not far behind but Manhattan Heuristic still seems to be very fast taking less than 10 seconds for the hardest puzzle.
- 4. Manhattan Distance Heuristics outperforms Misplaced Tile and Uniform cost search by a large margin and Misplaced tile heuristic performs considerably better than Uniform Cost search

5. Traceback of easy puzzle

Figures 8, 9 and 10 show the code running for an easy problem and its traceback.

In Figure 8, we can see that by choosing A* Search with Manhattan distance heuristic on an easy puzzle of depth 7, we can find the solution in 0.001 secs with expanding only 7 nodes and having a max frontier size of 8

```
---- N Puzzle Solver ----
1. Uniform Cost Search
2. A* with Misplaced Tile
3. A* with Manahattan Distance
Enter choice: 3
---- Choose Puzzle Type ----

    Random Default Easy (depth 0-9)
    Random Default Medium (depth 10-19)

3. Random Default Hard (depth >20)
4. Custom Puzzle
Enter choice: 1
---- Enter Goal State ----
1. Default State (1 2 3 4 5 6 ... n-1 n 0)
2. Custom Goal
Enter choice: 1
Initial State
| 4 || 1 || 2 |
| 5 || 8 || 3 |
| 7 || 0 || 6 |
Solving for A* with Manahattan Distance
SUCCESS
path ['U', 'L', 'U', 'R', 'R', 'D', 'D']
| 1 || 2 || 3 |
| 4 || 5 || 6 |
| 7 || 8 || 0 |
Total nodes Expanded: 7
Max Queue Size : 8
time taken is 0.001 secs
---- Want to print the puzzle traceback? ----
1. Yes
2. No. Exit
Enter choice: 1
```

Figure 8: Take Input from user, search to find the solution. Display the result. (Easy)

```
---- Want to print the puzzle traceback? ----
1. Yes
2. No. Exit
Enter choice: 1
Problem State
| 4 || 1 || 2 |
| 5 || 8 || 3 |
| 7 || 0 || 6 |
The best state to expand with g(n): 1 and h(n): 6
Move blank to: Up
Updated State
| 4 || 1 || 2 |
| 5 || 0 || 3 |
| 7 || 8 || 6 |
The best state to expand with g(n): 2 and h(n): 5
Move blank to: Left
Updated State
| 4 || 1 || 2 |
| 0 || 5 || 3 |
| 7 || 8 || 6 |
The best state to expand with g(n): 3 and h(n): 4
Move blank to: Up
Updated State
| 0 || 1 || 2 |
| 4 || 5 || 3 |
| 7 || 8 || 6 |
The best state to expand with g(n): 4 and h(n): 3 Move blank to: Right
Updated State
| 1 || 0 || 2 |
| 4 || 5 || 3 |
| 7 || 8 || 6 |
```

Figure 9: Print Traceback with best move and its cost for the problem in figure 8

```
The best state to expand with g(n): 4 and h(n): 3
Move blank to: Right
Updated State
| 1 || 0 || 2 |
| 4 || 5 || 3 |
| 7 || 8 || 6 |
The best state to expand with g(n): 5 and h(n): 2
Move blank to: Right
Updated State
| 1 || 2 || 0 |
| 4 || 5 || 3 |
| 7 || 8 || 6 |
The best state to expand with g(n): 6 and h(n): 1
Move blank to: Down
Updated State
| 1 || 2 || 3 |
| 4 || 5 || 0 |
| 7 || 8 || 6 |
The best state to expand with g(n): 7 and h(n): 0
Move blank to: Down
Updated State
| 1 || 2 || 3 |
| 4 || 5 || 6 |
| 7 || 8 || 0 |
```

Figure 10: Continued Printing of Traceback from figure 9

6. Solution of a Medium Puzzle without Traceback

Figure 11 shows the code running for a medium problem without its traceback.

In Figure 11, we can see that by choosing A* Search with Misplaced tile distance heuristic on a medium puzzle of depth 15, we can find the solution in 0.05 secs with expanding 637 nodes and having a max frontier size of 379

```
---- N Puzzle Solver ----
1. Uniform Cost Search
2. A* with Misplaced Tile
3. A* with Manahattan Distance
Enter choice: 2
---- Choose Puzzle Type ----
1. Random Default Easy (depth 0-9)
2. Random Default Medium (depth 10-19)
3. Random Default Hard (depth >20)
4. Custom Puzzle
Enter choice: 2
---- Enter Goal State ----
1. Default State (1 2 3 4 5 6 ... n-1 n 0)
2. Custom Goal
Enter choice: 1
Initial State
| 4 || 2 || 1 |
| 0 || 3 || 6 |
| 7 || 5 || 8 |
Solving for A* with Misplaced Tile
SUCCESS
path ['R', 'U', 'R', 'D', 'L', 'L', 'U', 'R', 'D', 'R', 'U', 'L', 'D', 'D', 'R']
| 1 || 2 || 3 |
| 4 || 5 || 6 |
| 7 || 8 || 0 |
Total nodes Expanded: 637
Max Queue Size : 379
time taken is 0.05 secs
---- Want to print the puzzle traceback? ----

    Yes

2. No. Exit
Enter choice: 2
```

Figure 11: Take Input from user, search to find the solution. Display the result. (Medium)

7. Solution of a Hard Puzzle without Traceback

Figure 12 shows the code running for a Hard problem without its traceback.

In Figure 12, we can see that by choosing A* Search with Manhattan distance heuristic on a hard puzzle of depth 30, we can find the solution in 11 secs with expanding 17722 nodes and having a max frontier size of 8174

```
---- N Puzzle Solver ----
1. Uniform Cost Search
2. A* with Misplaced Tile
3. A* with Manahattan Distance
Enter choice: 3
---- Choose Puzzle Type ----
1. Random Default Easy (depth 0-9)
2. Random Default Medium (depth 10-19)
3. Random Default Hard (depth >20)
4. Custom Puzzle
Enter choice: 3
---- Enter Goal State ----
1. Default State (1 2 3 4 5 6 ... n-1 n 0)
2. Custom Goal
Enter choice: 1
Initial State
| 8 || 3 || 5 |
| 1 || 2 || 0 |
Solving for A* with Manahattan Distance
path ['L', 'U', 'U', 'R', 'O', 'D', 'L', 'U', 'L', 'O', 'R', 'U', 'U', 'R', 'O', 'D', 'L', 'U', 'U', 'L', 'O', 'R', 'U', 'U', 'R', 'D', 'R']
| 4 || 5 || 6 |
| 7 || 8 || 0 |
Total nodes Expanded: 17722
Max Queue Size : 8174
time taken is 11 secs
---- Want to print the puzzle traceback? ----
1. Yes
2. No. Exit
Enter choice: 2
```

Figure 12: Take Input from user, search to find the solution. Display the result. (Hard)

8. Original Code

The original code can be found at

Initial.py

- The code is available on github → https://github.com/yashUcr773/CS_205_Al/tree/main/Projects/Project%201
- The code can also be run on google colab → https://colab.research.google.com/drive/18yNb0bLmRX-0jsQMP5Q_JEtD-tOi4NMS

```
Solve 8 puzzle with
- Uniform cost search
- A* with misplaced tile
- A* with manhattan distance
extensible code
- can work for any N puzzle.
- can update heuristic function to use any custom function
########
             LIBRARY IMPORTS
                                 ########
# for square root of numbers
import math
# clear output screen
import os
# to make deep copies of nodes' states
import copy as cpy
# to track the time used for execution
import time
# for creating random states
import numpy as np
# for plotting results and graphs
import matplotlib.pyplot as plt
########
              CONSTANTS
                               ########
UNIFORM = 'Uniform'
MISPLACED = 'Misplaced'
MANHATTAN = 'Manhattan'
COLOR_MAP = {
 MANHATTAN: 'red',
 MISPLACED: 'green',
 UNIFORM: 'blue',
}
DIRECTIONS_MAP = {
```

```
'R': 'Right',
  'L': 'Left',
  'U': 'Up',
  'D': 'Down'
}
########
                                                  ########
                    LIST OF PUZZLES
# Stores some randomly generated puzzles with puzzle state and true depth
list_of_easy_puzzles = [
  ([1, 2, 3, 4, 5, 6, 7, 8, 0], 0),
  ([1, 2, 3, 4, 5, 6, 7, 0, 8], 1),
  ([1, 2, 3, 4, 5, 6, 0, 7, 8], 2),
  ([1, 0, 3, 4, 2, 5, 7, 8, 6], 3),
  ([1, 2, 3, 5, 0, 6, 4, 7, 8], 4),
  ([2, 0, 3, 1, 5, 6, 4, 7, 8], 5),
  ([2, 5, 3, 1, 0, 6, 4, 7, 8], 6),
  ([4, 1, 2, 5, 8, 3, 7, 0, 6], 7),
  ([1, 3, 6, 5, 0, 2, 4, 7, 8], 8),
  ([2, 5, 3, 0, 7, 6, 1, 4, 8], 9),
]
list of medium puzzles = [
  ([2, 3, 5, 1, 4, 6, 0, 7, 8], 10),
  ([1, 4, 2, 7, 8, 3, 5, 0, 6], 11),
  ([1, 3, 6, 5, 0, 7, 4, 8, 2], 12),
  ([7, 2, 3, 0, 5, 6, 1, 4, 8], 13),
  ([1, 5, 0, 3, 2, 4, 7, 8, 6], 14),
  ([4, 2, 1, 0, 3, 6, 7, 5, 8], 15),
  ([1, 6, 7, 5, 0, 3, 4, 8, 2], 16),
  ([4, 8, 1, 0, 3, 5, 2, 7, 6], 17),
  ([7, 5, 3, 1, 4, 6, 2, 8, 0], 18),
  ([5, 4, 6, 3, 1, 2, 7, 0, 8], 19),
]
list of hard puzzles = [
  ([7, 1, 2, 4, 8, 5, 6, 3, 0], 20),
  ([3, 5, 4, 8, 7, 0, 2, 6, 1], 21),
  ([7, 1, 8, 5, 0, 3, 6, 4, 2], 22),
  ([1, 0, 8, 4, 7, 2, 3, 5, 6], 23),
  ([0, 7, 2, 4, 6, 1, 3, 5, 8], 24),
  ([5, 2, 1, 0, 8, 4, 7, 3, 6], 25),
  ([6, 3, 1, 4, 0, 7, 8, 2, 5], 26),
  ([4, 0, 7, 2, 6, 5, 8, 1, 3], 27),
  ([8, 6, 4, 2, 0, 7, 3, 1, 5], 28),
  ([5, 2, 1, 3, 8, 4, 6, 0, 7], 29),
  ([6, 4, 7, 8, 3, 5, 1, 2, 0], 30),
]
```

```
def generate_random_states(state_len):
  generate random states for evaulating and testing
  arr = [i for i in range(state len)]
  np.random.shuffle(arr)
  return arr
def validate_state(problem_state: list) -> bool:
  check if the state passed is valid or not.
  checks that state length is a perfect sqaure.
  checks that all numbers are unique.
  checks that numbers are in range 0-len(state)
  # get length of puzzle
  # is it 8 puzzle, 15 puzzle etc
  puzzle_size = len(problem_state)
  # check that length is perfect square
  sqrt = int(math.sqrt(puzzle_size))
  if(sqrt*sqrt) != puzzle size:
    return False
  # generate valid inputs.
  # valid inputs range from 0 - n for n puzzle
  valid_inputs = [i for i in range(puzzle_size)]
  # put the problem state in a set to remove duplicates.
  problem_state_set = set(problem_state)
  for i in problem state set:
    if i not in valid_inputs:
       return False
  return True
def print_formatted_time(time_input):
  funtion to take in seconds as input and
  print in Hours, minutes, and seconds
  hrs = int(time_input // 3600)
  mins = int((time_input % 3600) // 60)
  secs = int((time_input % 3600) % 60)
```

```
if hrs:
    print(f'time taken is {hrs} hrs, {mins} mins and {secs} secs')
  elif mins:
    print(f'time taken is {mins} mins and {secs} secs')
  else:
    print(f'time taken is {secs} secs')
def print time(time input):
  function to print the time with appropritate precision if between 0 and 1
  else print in HH, MM, SS format
  if time_input <= 1e-5:
    print(f'time taken is {time input:.6f} secs')
  elif time input <= 1e-4:
    print(f'time taken is {time_input:.5f} secs')
  elif time input <= 1e-3:
    print(f'time taken is {time_input:.4f} secs')
  elif time input <= 1e-2:
    print(f'time taken is {time_input:.3f} secs')
  elif time_input <= 1e-1:
    print(f'time taken is {time input:.2f} secs')
  elif time_input >= 0 and time_input <= 1:
    print(f'time taken is {time input} secs')
  else:
    print_formatted_time(time_input)
def print_trace(node, goal_state):
  take in any node and print the trace on how to reach this node from the parent node
  if node is None:
    return
  print trace(node.parent, goal state)
  node.print trace info(goal state)
####### NODE CLASS AND CORRESPONDING FUNCTION
class Node():
  create a node class for the states.
  stores path to current node from parent, depth etc and other properties.
  has uitlity methods.
```

```
# to store the states that have already been generated.
  # prevents exploring repeating states.
  # If a state is present here, then it has already been generated at higher depth
  global states manager = {}
  # initialize the node
  # depth of node.
  # path stores the path to be taken to reach till current node.
  # state of node
  # link to parent node
  def __init__(self, depth, path, state, parent):
    self.depth = depth
    self.path = path
    self.state = state
    self.parent = parent
    # puzzle length 8/15/24
    self.state length = len(state)
    # length per row
    self.row length = int(math.sqrt(self.state length))
    # length per column
    self.col_length = int(math.sqrt(self.state_length))
    # in case the current node is parent node, empty the globally stored states.
    if self.parent is None:
       Node.global states manager = {}
       Node.global_states_manager[self._get_state_string(
          self.state)] = self.depth
  def spawn_children(self):
    create child nodes after making valid moves on parent node.
    children are not generated is their states are already present in global states manager
    # get index of blank tile
    blank idx = self.state.index(0)
    children_list = []
    for move in self.get valid moves():
       state_copy = cpy.deepcopy(self.state)
       path = cpy.deepcopy(self.path)
       if move == 'U':
          path.append('U')
          state_copy[blank_idx], state_copy[blank_idx -
                                self.row length] = state copy[blank idx-self.row length],
state copy[blank idx]
       elif move == 'L':
          path.append('L')
```

```
state_copy[blank_idx], state_copy[blank_idx -
                                1] = state_copy[blank_idx-1], state_copy[blank_idx]
       elif move == 'R':
          path.append('R')
          state_copy[blank_idx], state_copy[blank_idx +
                                1] = state_copy[blank_idx+1], state_copy[blank_idx]
       elif move == 'D':
          path.append('D')
          state_copy[blank_idx], state_copy[blank_idx +
                                self.row_length] = state_copy[blank_idx+self.row_length],
state copy[blank idx]
       # check if the node is already generated.
       past_depth_if_generated = self._is_state_already_generated(
          state_copy)
       # if the node is never generated or if the node generated earlier has
       # depth greater than current node, then generate another node with lower depth
       if past_depth_if_generated == -1 or past_depth_if_generated > self.depth+1:
          child node = Node(self.depth+1, path, state copy, self)
          Node.global_states_manager[self._get_state_string(
            child_node.state)] = self.depth+1
          children list.append(child node)
    return children_list
  def get_valid_moves(self):
    get list of valid operators for each puzzle state
    checks the position of blank and returns array of valid moves possible
    # total Valid moves.
    # Move the blank space in following directions
    # Up, Left, Right, Down
    valid = ['U', 'L', 'R', 'D']
    # get index of blank tile
    blank_idx = self.state.index(0)
    # if the blank tile is in first row, cant move up
    if blank_idx >= 0 and blank_idx < self.col_length:
       valid.remove('U')
    # if the blank tile is in last row, cant move down
    if blank idx >= (self.col length*self.col length - self.col length) and blank idx <
self.col length*self.col length:
       valid.remove('D')
    # if the blank tile is in first column, cant move left
```

```
if blank idx % self.col length == 0:
     valid.remove('L')
  # if the blank tile is in last column, cant move right
  if (blank idx + 1) % self.col length == 0:
     valid.remove('R')
  return valid
def manhattan distance heuristic(self, goal state):
  get value for manhattan distance for a current state and goal state
  it is the shortest distance a tile needs to be moved to get to correct position
  total distance is sum of all individual distances
  does not include blank for calculation
  total manhattan distance = 0
  for value in goal state:
     if value == 0:
       continue
     goal_state_row, goal_state_colums = self._get_row_col_position(
       goal state, value)
     random_state_row, random_state_colums = self._get_row_col_position(
       self.state, value)
     total manhattan distance += abs(goal state colums-random state colums)+abs(
       goal_state_row-random_state_row)
  return int(total manhattan distance)
def misplaced_tile_heuristic(self, goal_state):
  get value of misplaced tile heuristic for a current state and goal state.
  it is the count of all the tiles that are not in correct position
  does not include blank for calculation
  misplaced count = 0
  for idx,value in enumerate(goal_state):
     if value == 0:
       continue
     if self.state[idx] != goal_state[idx]:
       misplaced count += 1
  return misplaced count
def get_heuristic_cost(self, heuristic_measure, goal_state):
  get the heuristic value cost of expanding this node.
```

```
takes in heuristic measure and goal state.
    return g(n) + h(n).
    g(n) is the depth of node.
    g n = self.depth
    h n = 0
    if heuristic measure == MANHATTAN:
       h n = self.manhattan distance heuristic(goal state)
    elif heuristic measure == MISPLACED:
       h_n = self.misplaced_tile_heuristic(goal_state)
    elif heuristic measure == UNIFORM:
       h n = 0
    else:
       h n = 0
    return g_n + h_n
  def print state(self, verbose=False):
    print the current node in puzzle view.
    if verbose is True, also print the path to reach this node
    and its depth
    if verbose:
       print('depth', self.depth)
       print('path', self.path)
    self. print horizontal divider(self.state length)
    for i in range(self.state length):
       print(f'| {self.state[i]:2} |', end="")
       if (i+1) % self.row length == 0:
          self._print_horizontal_divider(self.state_length)
    print()
  def print_trace_info(self, goal_state):
    print the trace of the current node.
    start from the parent and print out the heuristic code and cumulative cost.
    print the path to take from parent to reach this node.
    if len(self.path):
       print(
          f'The best state to expand with g(n): {self.depth} and h(n):
{self.manhattan distance heuristic(goal state)}')
       print('Move blank to: ', DIRECTIONS_MAP[self.path[-1]])
       print('Updated State', end=")
    else:
       print('\nProblem State', end=")
```

```
self._print_horizontal_divider(self.state_length)
    for i in range(self.state length):
      print(f'| {self.state[i]:2} |', end="")
      if (i+1) % self.row length == 0:
         self. print horizontal divider(self.state length)
    print()
  def _get_row_col_position(self, state, element):
    get row and column positions for a given element in a given state
    used for manhattan distance
    idx = state.index(element)
    column val = int(idx % self.row length)
    r_val = int(idx // self.row_length)
    return r val, column val
  def _print_horizontal_divider(self, size=8):
    print horizontal dividers after each row for better UI
    if size == 9:
      print('\n----')
    elif size == 16:
      print('\n----')
  def _is_state_already_generated(self, state):
    check if the potential child state is already generated
    return the depth if state exists, else return -1
    state_string = "".join([str(i) for i in state])
    return Node.global_states_manager[state_string] if state_string in Node.global_states_manager else
-1
  def _get_state_string(self, state):
    convert the child node to a string for unique and easy representation
    state_string = "".join([str(i) for i in state])
    return state string
########
                 GENERAL SEARCH
                                             ########
def make_queue(node: Node, goal_state: list, heuristic_measure: str):
  Initialize an empty queue.
```

```
take in a node and add it to the queue.
  return the queue
  return [(node.get_heuristic_cost(heuristic_measure, goal_state), node)]
def is_queue_empty(queue: list):
  take in queue and check if the queue is empty
  return False if len(queue) > 0 else True
def remove_front(queue: list):
  take in queue and sort it.
  remove the first node.
  return the first removed node.
  queue = sorted(queue, key=lambda x: x[0])
  node = queue.pop(0)[1]
  return queue, node
def expand_nodes(node: Node):
  takes in node and operators and expands the node based on operators.
  returns a list of nodes
  children = node.spawn_children()
  return children
def make_node_from_state(state: list):
  call in the Node class to create Parent Node
  parent node = Node(0, [], state, None)
  return parent_node
def queueing_function(queue, children, heuristic_measure, goal_state):
  take in queue,
  take in children
  put children in priority queue based on heuristic value
  sort the queue
  return the queue
```

```
child_queue = []
  for child in children:
    child queue.append((child.get heuristic cost(
       heuristic measure, goal state), child))
  queue = queue + child queue
  queue = sorted(queue, key=lambda x: x[0])
  return queue
def general_search(initial_state, goal_state, queueing_function, heuristic_measure, verbose=False):
  # general search function
  # refered from the problem statement doc provided.
  # https://d1u36hdvoy9y69.cloudfront.net/cs-205-ai/Project_1_The_Eight_Puzzle_CS_205.pdf
  # takes in problem state, goal state, queueing function and heuristic measure
  # solves the problem using the gueueing function
  # returns final node, total nodes expanded, max queue size
  # create parent node
  nodes = make_queue(make_node_from_state(initial_state),
             goal state, heuristic measure)
  # store total nodes expanded count and max size of queue
  total nodes expanded = 0
  max_queue_size = 0
  while True:
    max_queue_size = max(max_queue_size, len(nodes))
    if is_queue_empty(nodes):
       print("FAILURE")
       return -1, total_nodes_expanded, max_queue_size
    else:
       nodes, node = remove front(nodes)
       if goal state == node.state:
         if verbose:
            print("SUCCESS")
            node.print state(True)
            print('Total nodes Expanded : ', total_nodes_expanded)
            print('Max Queue Size : ', max_queue_size)
         return node, max queue size, total nodes expanded
       else:
         total nodes expanded += 1
         nodes = queueing function(nodes, expand nodes(
            node), heuristic measure, goal state)
```

```
######### UI LANDING PAGE AND INPUT VALIDATION
                                                     ########
def main block(clear previous=True):
 Print out the Landing Page.
 Get Algo Choice From user
 Get Puzzle Choice From user
 Get Goal State From user
 Search the goal state
 Print Traceback
 if clear previous:
    os.system('cls')
 GET ALGO CHOICE
                                           ################################
 print('---- N Puzzle Solver ----')
 print('1. Uniform Cost Search')
 print('2. A* with Misplaced Tile')
 print('3. A* with Manahattan Distance')
 algo_choice = int(input('Enter choice: '))
 if algo choice not in [1, 2, 3]:
    os.system('cls')
    print('Please enter correct choice.\n')
    main block(clear previous=False)
    return
 GET PUZZLE CHOICE
                                           print('\n---- Choose Puzzle Type ----')
 print('1. Random Default Easy (depth 0-9)')
 print('2. Random Default Medium (depth 10-19)')
 print('3. Random Default Hard (depth >20)')
 print('4. Custom Puzzle')
 puzzle choice = int(input('Enter choice: '))
 if puzzle_choice not in [1, 2, 3, 4]:
    os.system('cls')
    print('Please enter correct choice.\n')
    main_block(clear_previous=False)
    return
 ###################
                     INPUT CUSTOM PUZZLE
                                              problem state = []
 if puzzle choice == 1:
    problem_state = list_of_easy_puzzles[np.random.choice(len(list_of_easy_puzzles))][0]
 elif puzzle choice == 2:
```

```
problem_state = list_of_medium_puzzles[np.random.choice(len(list_of_medium_puzzles))][0]
elif puzzle_choice == 3:
  problem state = list of hard puzzles[np.random.choice(len(list of hard puzzles))][0]
elif puzzle choice == 4:
  print('\nEnter the numbers in puzzle as space seperated list.')
  print('Represent blank with 0')
  print('For Example: 1 2 3 4 0 5 6 7 8\n')
  problem input = input('Numbers: ')
  problem state = problem input.split(' ')
  # convert string to integers
  problem_state = [int(i) for i in problem_state]
  if not validate_state(problem_state):
    os.system('cls')
    print('Pleae enter valid input state.\n')
    main_block(clear_previous=False)
    return
#################
                      print('\n---- Enter Goal State ----')
print('1. Default State (1 2 3 4 5 6 ... n-1 n 0)')
print('2. Custom Goal')
puzzle_choice = int(input('Enter choice: '))
if puzzle_choice not in [1, 2]:
  os.system('cls')
  print('Please enter correct choice.\n')
  main_block(clear_previous=False)
  return
goal state = []
if puzzle choice == 1:
  goal state = list(range(1, len(problem state)))
  goal_state.append(0)
elif puzzle choice == 2:
  print('\nEnter the numbers in goal as space seperated list.')
  print('Represent blank with 0')
  print('For Example: 1 2 3 4 0 5 6 7 8\n')
  problem_input = input('Numbers: ')
  goal state = problem input.split(' ')
  # convert string to integers
  goal_state = [int(i) for i in goal_state]
  if not validate_state(goal_state):
    os.system('cls')
    print('Pleae enter valid input state.\n')
    main_block(clear_previous=False)
    return
```

```
os.system('cls')
  print('Initial State\n')
  parent_node = Node(0, [], problem_state, None)
  parent node.print state()
  if algo_choice == 1:
    print('\nSolving for Uniform cost\n')
    time before = time.time()
    final_node, _, _ = general_search(problem_state, goal_state, queueing_function, UNIFORM,
verbose=True)
    time after = time.time()
    total_time = time_after - time_before
    print time(total time)
  elif algo_choice == 2:
    print('\nSolving for A* with Misplaced Tile\n')
    time before = time.time()
    final_node, _, _ = general_search(problem_state, goal_state, queueing_function, MISPLACED,
verbose=True)
    time_after = time.time()
    total_time = time_after - time_before
    print_time(total_time)
  elif algo_choice == 3:
    print('\nSolving for A* with Manahattan Distance\n')
    time_before = time.time()
    final_node, _, _ = general_search(problem_state, goal_state, queueing_function, MANHATTAN,
verbose=True)
    time after = time.time()
    total time = time_after - time_before
    print_time(total_time)
  print('\n---- Want to print the puzzle traceback? ----')
  print('1. Yes')
  print('2. No. Exit')
  traceback_choice = int(input('Enter choice: '))
  if traceback choice not in [1, 2]:
    os.system('cls')
    print('Please enter correct choice.\n')
    main_block(clear_previous=False)
    return
  if traceback choice == 1:
    print_trace(final_node, goal_state)
```

```
return
```

```
main block()
Multiple TESTS and Result Analysis
# code to run all the puzzles and generate graphs
def run_analysis(combined_puzzles_list):
  runs analysis on all list of puzzles provided.
  solves the puzzles using all three algorithms
  stores the time taken per algorithm per puzzle
  stores the max queue size
  stores the total nodes expanded
  Plots the results in graphs
  goal_state = [1,2,3,4,5,6,7,8,0]
  time collection = {}
  queue_collection = {}
  nodes collection = {}
  for heuristic in [MANHATTAN, UNIFORM, MISPLACED]:
    time collection[heuristic] = []
    queue_collection[heuristic] = []
    nodes_collection[heuristic] = []
  for puzzle, true depth in combined puzzles list:
    for heuristic in [MANHATTAN, UNIFORM, MISPLACED]:
      print (heuristic, puzzle, true depth)
      time before = time.time()
      final_node, max_queue, total_nodes = general_search(puzzle, goal_state, queueing_function,
heuristic, verbose=False)
      time_after = time.time()
      total time = time after - time before
      print (final_node.depth)
      time collection[heuristic].append((true depth, total time))
      queue_collection[heuristic].append((true_depth, max_queue))
      nodes_collection[heuristic].append((true_depth, total_nodes))
    print ()
  plt.figure(1)
  for heuristic in [MANHATTAN, UNIFORM, MISPLACED]:
    temp arr = np.array(time collection[heuristic])
    plt.plot(temp_arr[:,0], temp_arr[:,1], color = COLOR_MAP[heuristic], label=heuristic)
```

```
plt.title('Time vs Depth')
  plt.xlabel('depth')
  plt.ylabel('time in seconds')
  plt.grid()
  plt.legend()
  plt.show()
  plt.figure(2)
  for heuristic in [MANHATTAN, UNIFORM, MISPLACED]:
    temp arr = np.array(nodes collection[heuristic])
    plt.plot(temp_arr[:,0], temp_arr[:,1], color = COLOR_MAP[heuristic], label=heuristic)
  plt.title('Nodes Expanded vs Depth')
  plt.xlabel('depth')
  plt.ylabel('Nodes Expanded')
  plt.grid()
  plt.legend()
  plt.show()
  plt.figure(3)
  for heuristic in [MANHATTAN, UNIFORM, MISPLACED]:
    temp arr = np.array(queue collection[heuristic])
    plt.plot(temp_arr[:,0], temp_arr[:,1], color = COLOR_MAP[heuristic], label=heuristic)
  plt.title('Max Queue Size vs Depth')
  plt.xlabel('depth')
  plt.ylabel('Max Queue Size')
  plt.grid()
  plt.legend()
  plt.show()
# this will take ~2hrs to run
# run analysis(list of easy puzzles + list of medium puzzles + list of hard puzzles)
########
           Generating puzzles at different depths #######
# code to generate random puzzles and solving them to find the depth of puzzles.
# used to create multiple puzzles to test the algorithms and for benchmarking
# the original method to let the algorithm run till all nodes are explored to get failure takes a lot of time.
# therefore using a constant time algorithm to generate puzzles.
# code is taken from
# https://www.geeksforgeeks.org/check-instance-8-puzzle-solvable/
def get_int_count(arr):
  counts the total number of inversions to be made
  inv_count = 0
  empty_value = 0
```

```
for i in range(0, 9):
    for j in range(i + 1, 9):
      if arr[j] != empty value and arr[i] != empty value and arr[i] > arr[j]:
        inv count += 1
  return inv count
def is_solvable(puzzle):
  checks if the 8 puzzle is solvable or not
  # Count inversions in given 8 puzzle
  inv_count = get_int_count(puzzle)
  # return true if inversion count is even.
  return (inv count % 2 == 0)
def create_puzzle_book(n_iters):
  create a puzzle book that stores a list of problem states are various depths
  puzzle book = {}
  for in range(n iters):
    # generate a random 8 puzzle
    random state = generate random states(9)
    # check if the puzzle is solvable
    if (is_solvable(random_state)):
      # if solvable, solve the puzzle to get depth
      goal_state = [1, 2, 3, 4, 5, 6, 7, 8, 0]
      final_node, _, _ = general_search(
        random_state, goal_state, queueing_function, MANHATTAN, verbose=False)
      # store the puzzle at appropriate depth entry
      if final node.depth not in puzzle book:
        puzzle book[final node.depth] = []
      puzzle book[final node.depth].append(random state)
  return puzzle_book
# print(create puzzle book(30))
######## Pretty Print Puzzles to display in Report #######
def pretty print puzzles(combined puzzles):
  prints the puzzles in matrix form so they can be added to report
```

"

```
for puzzle, true_depth in combined_puzzles:
```

```
print (f' --- {true_depth} ---')
print (' ', puzzle[:3])
print (' ', puzzle[3:6])
print (' ', puzzle[6:9])
print ()
print ()

# pretty_print_puzzles(list_of_easy_puzzles + list_of_medium_puzzles + list_of_hard_puzzles)
# pretty_print_puzzles(list_of_easy_puzzles)
```