Summary of SI2510 Statistical Mechanics

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August 28, 2020

Abstract

This is a summary of SI2510 Statistical Mechanics.

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1 Basic Concepts 1

1 Basic Concepts

Phase Transitions Landau introduced the concept that phase transitions are defined by spontaneous symmetry breaking.

Order Parameters An order parameter describes spontaneous symmetry breaking. It is zero in one phase and non-zero in another.

The Ising Model The Ising model is a simple model of magnets. In this model, a magnet is a collection of interacting spins on a lattice under the influence of an external field. Its generalized coordinates are σ_i , which may take the values ± 1 , signifying a particular spin pointing up or down. The Hamiltonian is

$$\mathcal{H} = -J \sum_{i} \sum_{j=\text{nn}(i)} \sigma_i \sigma_j - h \sum_{i} \sigma_i.$$

The inner summation is carried out over the nearest neighbours of site i in the Ising model, but is generally a sum over the whole lattice. The order parameter defining its phase transition is $m = \langle \sigma_i \rangle$.

This model will be used to demonstrate core concepts in the course.