

# BST

- ✓ Variet of Binary tree

- ✓

Every node must have atmost(0, 1, 2) two children

**Binary Tree + Binary Search = Binary Search Tree**

**All the elements of left sub tree are less than Root.**

**All the elements of right sub tree are Greater than Root.**

# Delete

1. Deleting a node with no child
2. Deleting a node having one child
3. Deleting a node having two child

Deleting a node with no child

# Deleting a node having one child

**Child will replace the position of parent**

# Deleting a node having two child

**Replace parent with Child**

**Child = Minimum element of Right Sub tree**

**Child = Maximum element of Left Sub tree**

# DISJOINT SETS

**Definition:** If  $S_i$  and  $S_j$  are two sets and  $i \neq j$  and there is no element that is in both  $S_i$  and  $S_j$ , then the two sets  $S_i$  and  $S_j$  are called disjoint sets. For example, consider the following three sets:

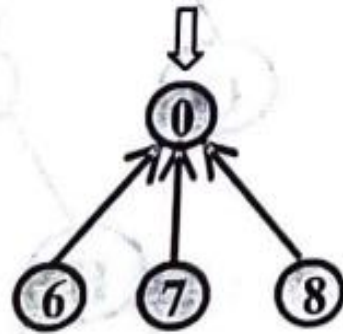
$$S_0 = \{0, 6, 7, 8\} \quad S_1 = \{1, 4, 9\} \quad S_2 = \{2, 3, 5\}$$

Note that there are no common items in any of the three sets  $S_1$ ,  $S_2$  and  $S_3$ . So, the sets  $S_1$ ,  $S_2$  and  $S_3$  are disjoint sets.

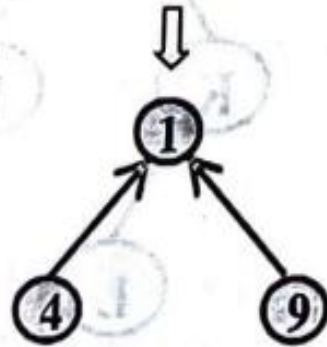
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For example, consider three disjoint sets and their tree representations

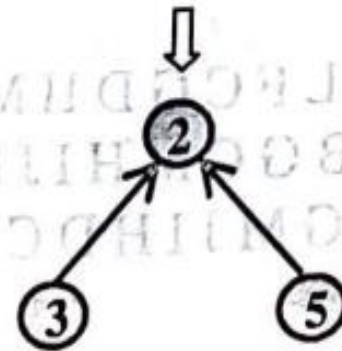
$S_0 = \{0, 6, 7, 8\}$



$S_1 = \{1, 4, 9\}$



$S_2 = \{2, 3, 5\}$



Note that the first item in each set is the subscript in the name of the set and it will be the root node. For example, in set  $S_0 = \{0, 6, 7, 8\}$ , the name of the set is  $S_0$ . The subscript 0 in  $S_0$  indicates that 0 is the first element of set  $S_0$ . All other remaining items are the children of 0 from left to right and the directions are given from children to the parent.

Since set is collection of similar data items, the set can be implemented using arrays. The sets  $S_0$ ,  $S_1$  and  $S_2$  represented in the form of a tree can be implemented using array as shown below:

- ◆ When a node does not have a parent, let us store -1 in the array using appropriate index. The root nodes in all the three trees i.e., node 0 in first tree, node 1 in second tree and node 2 in third tree do not have parents. So, in the array, we can write:  

$$S[0] = S[1] = S[2] = -1$$

- ◆ The parent for node 6, 7, 8 is the node 0. So, in the array, we can write:  

$$S[6] = S[7] = S[8] = 0$$

- ◆ The parent for node 4 and node 9 is node 1. So, in the array, we can write:  

$$S[4] = S[9] = 1$$

- ◆ The parent for node 3 and node 5 is 2. So, in the array, we can write:  

$$S[3] = S[5] = 2$$



So, the array corresponding to sets  $S_0, S_1$  and  $S_2$  is shown below:

$i$	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
$S$	-1	-1	-1	2	1	2	0	0	0	1

# Operations on Disjoint sets

✓ Union

✓ Find

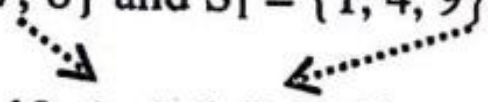
# union

## 6.15.1 Disjoint set union

If  $S_i$  and  $S_j$  are two disjoint sets, then their union is given by:

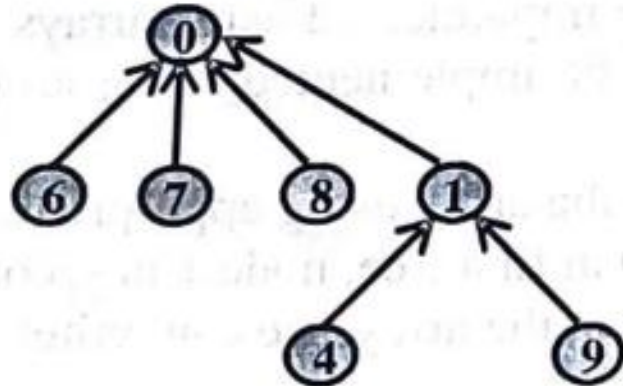
$$S_i \cup S_j = \{ \text{all elements } x \mid x \text{ is in } S_i \text{ or } S_j \}$$

For example, let  $S_0 = \{0, 6, 7, 8\}$  and  $S_1 = \{1, 4, 9\}$  then,


$$S_0 \cup S_1 = \{0, 1, 4, 6, 7, 8, 9\}$$

After finding  $S_0 \cup S_1$ , the sets  $S_0$  and  $S_1$  does not exist where as their union  $S_0 \cup S_1$  exists. That is,  $S_0$  and  $S_1$  will be replaced by their union  $S_0 \cup S_1$ . The tree equivalent of  $S_0 \cup S_1$  is shown below:

# Equivalent tree & Array representation

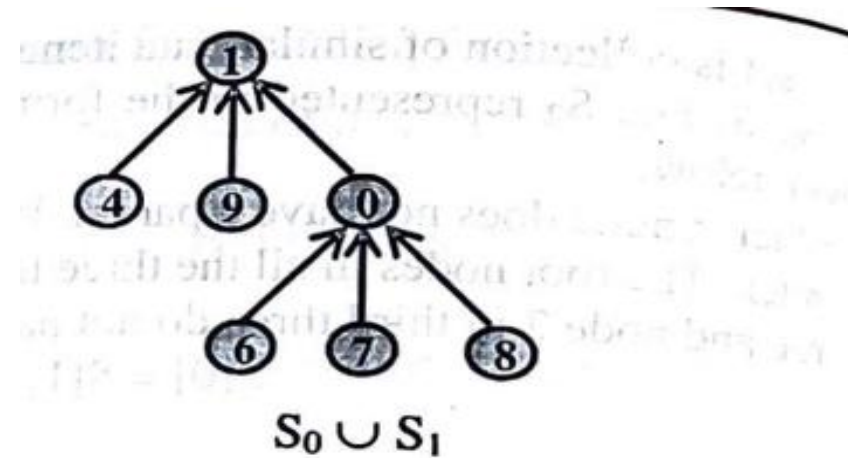


$S_0 \cup S_1$

s[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
-1	0			1		0	0	0	1

**Note:** The root node corresponding to set  $S_1$  will be the child for root node 0. The array representation is shown below:

# Equivalent tree & Array representation



**Note:** The root node corresponding to set  $S_0$  will be the child for root node 1. The array representation is shown below:

s[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	-1			1		0	0	0	1

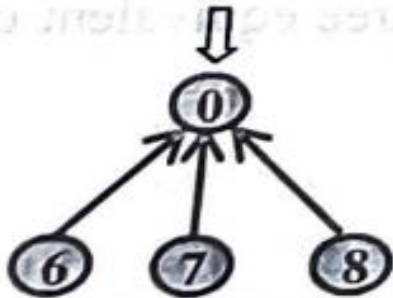
# Find

Find( $i$ )  $i$  is a node.

## 6.15.2 Find( $i$ )

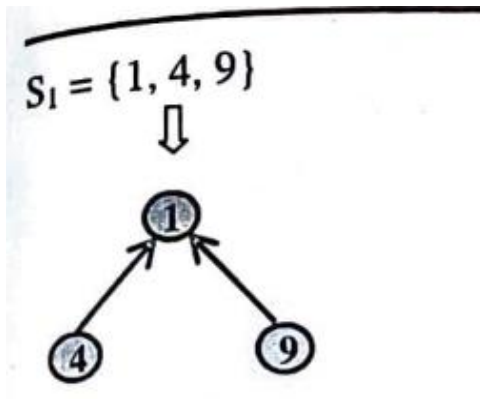
If  $i$  is a node in a tree, this function returns the root of the corresponding tree. For example, consider the sets :

$S_0 = \{0, 6, 7, 8\}$

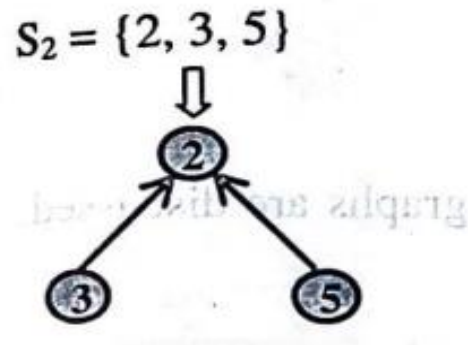


The root for node 6, node 7 and node 8 is 0. So, Find(6), Find(7) and Find(8) will be 0

# Cont..



The root for node 4 and node 9 is 1. So, Find(4) and Find(9) will be 1

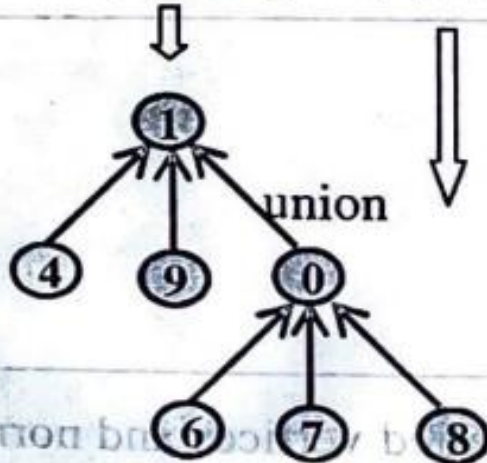


The root for node 3 and node 5 is 2. So, Find(3) and Find(5) will be 2



# Array representation

$$S_1 \cup S_0 = \{1, 4, 9\} \cup \{0, 6, 7, 8\}$$



The root for node 4, node 9 and node 0 is node 1 whereas root for node 6, node 7 and node 8 is also node 1. The array representation of the tree is shown below:

s[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	-1			1		0	0	0	1



# To find(8)

**Note:** Now, let us see, how to find(8). This can be done by starting from 8 as shown below:

find(8)  
is 1

→ S[8] in array is 0. So, 8's parent is 0 in the tree.

← S[0] in array is 1. So, 0's parent is 1 in the tree.

→ S[1] in array is -1. Since, we get s[1] as negative number we do not proceed further and return the index 1. Hence, find(8) is 1.