| AVCOE SANGAMNER   | DSAL S.E. COMP SEM-II 2020-21 |
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| DATA STRUCTURES & | : ALGORITHMS                  |
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| 2021-202          |                               |
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# Amrutvahini College of Engineering, Sangamner Department of Computer Engineering Data Structures & Algorithms Laboratory INDEX

| Sr.  | Title of Europian onto  | Page | Dat                    | e of | Remark | Signature |
|------|---|------|------------------------|------|--------|-----------|
| No   | Title of Experiments  | No   | Performance Submission |      | =      |           |
| Grou | ıp C:   |      |                        |      |        |           |
| 1    | Represent a given graph using adjacency matrix/list to perform DFS and using adjacency list to perform BFS. Use the map of the area around the college as the graph. Identify the prominent land marks as nodes and perform DFS and BFS on that.  |      |                        |      |        |           |
| 2    | There are flight paths between cities. If there is a flight between city A and city B then there is an edge between the cities. The cost of the edge can be the time that flight takes to reach city B from A or the amount of fuel used for the journey. Represent this as a graph. The node can be represented by airport name or name of the city. Use adjacency list representation of the graph or use adjacency matrix representation of the graph. Check whether the graph is connected or not. Justify the storage representation used. |      |                        |      |        |           |
| Grou | ıр В:   |      |                        |      |        |           |
| 3    | A book consists of chapters, chapters consist of sections and sections consist of subsections.  Construct a tree and print the nodes. Find the time and space requirements of your method.  |      |                        |      |        |           |
| 4    | Construct an expression tree from<br>the given prefix expression<br>eg. +a*bc/def and traverse it<br>using post order traversal   |      |                        |      |        |           |

| VCO: | E SANGAMNER                            | DSAL S.E. | COMP SE  | EM-II 2020-2 |
|------|--|-----------|----------|--------------|
|      |  |           |          |              |
|      | A Dictionary stores keywords & its     |           |          |              |
|      | meanings. Provide facility for         |           |          |              |
|      | adding new keywords, deleting          |           |          |              |
|      | keywords, updating values of any       |           |          |              |
|      | entry. Provide facility to display     |           |          |              |
| 9    | whole data sorted in ascending/        |           |          |              |
|      | Descending order. Also find how        |           |          |              |
|      | many maximum comparisons may           |           |          |              |
|      | require for finding any keyword.       |           |          |              |
|      | Use Height balance tree and find       |           |          |              |
|      | the complexity for finding a           |           |          |              |
|      | keyword                                |           |          |              |
| Gro  | up E:                                  |           | <u> </u> |              |
|      | Read the marks obtained by             |           |          |              |
|      | students of second year in an          |           |          |              |
|      | online examination of particular       |           |          |              |
| 10   | subject. Find out maximum and          |           |          |              |
|      | minimum marks obtained in that         |           |          |              |
|      | subject. Use heap data structure.      |           |          |              |
|      | Analyze the algorithm.                 |           |          |              |
| Gro  | up F:                                  | l         | 1        |              |
|      | Department maintains a student         |           |          |              |
|      | information. The file contains roll    |           |          |              |
|      | number, name, division and             |           |          |              |
|      | address. Allow user to add, delete     |           |          |              |
|      | information of student. Display        |           |          |              |
| 11   | information of particular student. If  |           |          |              |
|      | record of student does not exist an    |           |          |              |
|      | appropriate message is displayed.      |           |          |              |
|      | If it is, then the system displays the |           |          |              |
|      | student details. Use sequential file   |           |          |              |
|      | to main the data.                      |           |          |              |
|      | Assume we have two input and           |           |          |              |
|      | two output tapes to perform the        |           |          |              |
|      | sorting. The internal memory can       |           |          |              |
| 12   | hold and sort m records at a time.     |           |          |              |
|      | Write a program in java for            |           |          |              |
|      | external sorting. Find out time        |           |          |              |
|      | complexity.                            |           |          |              |
| Gro  | up G:                                  |           |          |              |
|      | Design a mini project using JAVA       |           |          |              |
|      | which will use the different data      |           |          |              |
|      | structure with or without Java         |           |          |              |
| 14   | collection library and show the use    |           |          |              |
|      | of specific data structure on the      |           |          |              |
|      | efficiency (performance) of the        |           |          |              |
|      | enteries (performance) or the          |           |          |              |

| VCO   | E SANGAMNER                                     |   |           | DSAL S.1   | E. COMP SE   | M-II 2020-2 |
|-------|---|---|-----------|------------|--------------|-------------|
|       | T   | , |           | 1          |              | Г           |
|       | code.  Design a mini project to implement       |   |           |            |              |             |
| 14    | Snake and Ladders Game using                    |   |           |            |              |             |
|       | Python.   |   |           |            |              |             |
| 15    | Design a mini project to implement              |   |           |            |              |             |
|       | a Smart text editor.  Design a mini project for |   |           |            |              |             |
|       | automated Term work assessment                  |   |           |            |              |             |
|       | of student based on parameters like             |   |           |            |              |             |
| 16    | daily attendance, Unit Test/Prelim              |   |           |            |              |             |
|       | performance, Students                           |   |           |            |              |             |
|       | achievements if any, Mock Practical.            |   |           |            |              |             |
| his i | s to certify that Mr. /Ms                       | CERTIFIC                                |           |            |              | Roll r      |
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|       | Examination seat no                             |   | has perfe | ormed abov | e mentione   | ed practica |
| the o | college.  |   |           |            |              |             |
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#### Title:

Consider telephone book database of N clients. Make use of a hash table implementation to quickly look up client's telephone number. Make use of two collision handling techniques and compare them using number of comparisons required to find a set of telephone numbers

#### Learning Objectives:

- To understand concept of Hashing
- To understand to find record quickly using hash function.
- To understand collision handling techniques.

#### Learning Outcome:

- Understand & implement concept of hash table.
- Understand collision handling techniques.

#### Theory:

Hash tables are an efficient implementation of a keyed array data structure, a structure sometimes known as an associative array or map. If you're working in C++, you can take advantage of the STL map container for keyed arrays implemented using binary trees, but this article will give you some of the theory behind how a hash table works.

# Keyed Arrays vs. Indexed Arrays

One of the biggest drawbacks to a language like C is that there are no keyed arrays. In a normal C array (also called an indexed array), the only way to access an element would be through its index number. To find element 50 of an array named "employees" you have to access it like this:

employees[50];

In a keyed array, however, you would be able to associate each element with a "key," which can be anything from a name to a product model number. So, if you have a keyed array of employee records, you could access the record of employee "John Brown" like this:

employees["Brown, John"];

One basic form of a keyed array is called the hash table. In a hash table, a key is used to find an element instead of an index number. Since the hash table has to be coded using an indexed array, there has to be some way of transforming a key to an index number. That way is called the hashing function.

# **Hashing Functions**

A hashing function can be just about anything. How the hashing function is actually coded depends on the situation, but generally the hashing function should return a value

based on a key and the size of the array the hashing table is built on. Also, one important thing that is sometimes overlooked is that a hashing function has to return the same value every time it is given the same key.

Let's say you wanted to organize a list of about 200 addresses by people's last names. A hash table would be ideal for this sort of thing, so that you can access the records with the people's last names as the keys.

First, we have to determine the size of the array we're using. Let's use a 260 element array so that there can be an average of about 10 element spaces per letter of the alphabet.>
Now, we have to make a hashing function. First, let's create a relationship between letters and numbers:

```
A --> 0
B --> 1
C --> 2
D --> 3
...
and so on until Z --> 25.
```

The easiest way to organize the hash table would be based on the first letter of the last name. Since we have 260 elements, we can multiply the first letter of the last name by 10. So, when a key like "Smith" is given, the key would be transformed to the index 180 (S is the 19 letter of the alphabet, so  $S \rightarrow 18$ , and 18 \* 10 = 180).

Since we use a simple function to generate an index number quickly, and we use the fact that the index number can be used to access an element directly; a hash table's access time is quite small. A linked list of keys and elements wouldn't be nearly as fast, since you would have to search through every single key-element pair.

# **Basic Operations**

Following are the basic primary operations of a hash table.

- **Search** Searches an element in a hash table.
- **Insert** inserts an element in a hash table.
- **Delete** Deletes an element from a hash table.

#### DataItem

Define a data item having some data and key, based on which the search is to be conducted in a hash table.

```
struct DataItem
{
  int data;
  int key;
};
```

#### Hash Method

Define a hashing method to compute the hash code of the key of the data item.

```
int hashCode(int key){
return key % SIZE;
າ
```

# Search Operation

Whenever an element is to be searched, compute the hash code of the key passed and locate the element using that hash code as index in the array. Use linear probing to get the element ahead if the element is not found at the computed hash code.

# Example

```
struct DataItem *search(int key)
{
    //get the hash
    int hashIndex = hashCode(key);

    //move in array until an empty
while(hashArray[hashIndex] != NULL) {
    if(hashArray[hashIndex]->key == key)
        return hashArray[hashIndex];
    //go to next cell
    ++hashIndex;
    //wrap around the table
    hashIndex %= SIZE;
}
    return NULL;
}
```

# **Insert Operation**

Whenever an element is to be inserted, compute the hash code of the key passed and locate the index using that hash code as an index in the array. Use linear probing for empty location, if an element is found at the computed hash code.

# Example

```
void insert(int key,int data)
{
  struct DataItem *item = (struct DataItem*) malloc(sizeof(struct DataItem));
  item->data = data;
  item->key = key;
```

```
//get the hash
int hashIndex = hashCode(key);
//move in array until an empty or deleted cell
while(hashArray[hashIndex] != NULL &&
    hashArray[hashIndex]->key != -1) { //go to next cell
    ++hashIndex;
    //wrap around the table
    hashIndex %= SIZE;
}
hashArray[hashIndex] = item;
}
```

#### Delete Operation

Whenever an element is to be deleted, compute the hash code of the key passed and locate the index using that hash code as an index in the array. Use linear probing to get the element ahead if an element is not found at the computed hash code. When found, store a dummy item there to keep the performance of the hash table intact.

#### Example

```
struct DataItem* delete(struct DataItem* item) {
 int key = item->key;
 //get the hash
 int hashIndex = hashCode(key);
 //move in array until an empty
 while(hashArray[hashIndex] !=NULL) {
   if(hashArray[hashIndex]->key == key) {
    struct DataItem* temp = hashArray[hashIndex];
    //assign a dummy item at deleted position
    hashArray[hashIndex] = dummyItem;
    return temp;
   //go to next cell
   ++hashIndex;
   //wrap around the table
   hashIndex %= SIZE;
 return NULL;
```

#### Collision:

Since a hash function gets us a small number for a key which is a big integer or string, there is a possibility that two keys result in the same value. The situation where a newly inserted key maps to an already occupied slot in the hash table is called collision and must be handled using some collision handling technique.

#### How to handle Collisions?

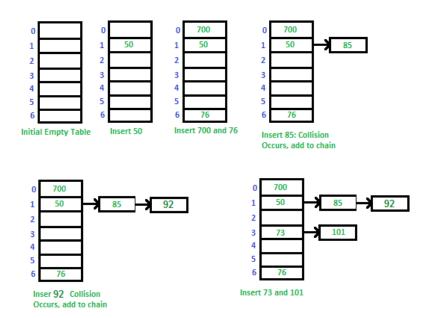
There are mainly two methods to handle collision:

- 1) Separate Chaining
- 2) Open Addressing

#### Separate Chaining:

The idea is to make each cell of hash table point to a linked list of records that have same hash function value.

Let us consider a simple hash function as "**key mod 7**" and sequence of keys as 50, 700, 76, 85, 92, 73, 101.



#### Advantages:

- 1) Simple to implement.
- 2) Hash table never fills up, we can always add more elements to the chain.
- 3) Less sensitive to the hash function or load factors.
- 4) It is mostly used when it is unknown how many and how frequently keys may be inserted or deleted.

# Disadvantages:

1) Cache performance of chaining is not good as keys are stored using a linked list. Open

addressing provides better cache performance as everything is stored in the same table.

- 2) Wastage of Space (Some Parts of hash table are never used)
- 3) If the chain becomes long, then search time can become O(n) in the worst case.
- 4) Uses extra space for links.

# Open Addressing

Like separate chaining, open addressing is a method for handling collisions. In Open Addressing, all elements are stored in the hash table itself. So at any point, the size of the table must be greater than or equal to the total number of keys. Open Addressing is done in the following ways:

a) Linear Probing: In linear probing, we linearly probe for next slot. For example, the typical gap between two probes is 1 as taken in below example also.

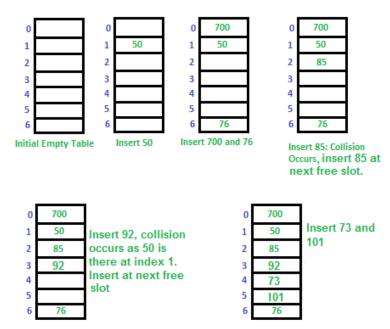
let hash(x) be the slot index computed using a hash function and S be the table size If slot hash(x) % S is full, then we try (hash(x) + 1) % S

If (hash(x) + 1) % S is also full, then we try (hash(x) + 2) % S

If (hash(x) + 2) % S is also full, then we try (hash(x) + 3) % S

•••••

Let us consider a simple hash function as "key mod 7" and a sequence of keys as 50, 700, 76, 85, 92, 73, 101.



# Challenges in Linear Probing:

1. **Primary Clustering:** One of the problems with linear probing is primary clustering, many consecutive elements form groups and it starts taking time to find a free slot or to search an element.

- 2. **Secondary Clustering:** Secondary clustering is less severe, two records do only have the same collision chain (Probe Sequence) if their initial position is the same.
- **b) Quadratic Probing** We look for i<sup>2</sup> th slot in i'th iteration.

let hash(x) be the slot index computed using hash function.

If slot hash(x) % S is full, then we try (hash(x) + 1\*1) % S

If (hash(x) + 1\*1) % S is also full, then we try (hash(x) + 2\*2) % S

If (hash(x) + 2\*2) % S is also full, then we try (hash(x) + 3\*3) % S

.....

c) Double Hashing We use another hash function hash2(x) and look for i\*hash2(x) slot in i'th rotation.

let hash(x) be the slot index computed using hash function.

If slot hash(x) % S is full, then we try (hash(x) + 1\*hash2(x)) % S

If (hash(x) + 1\*hash2(x)) % S is also full, then we try (hash(x) + 2\*hash2(x)) % S

If (hash(x) + 2\*hash2(x)) % S is also full, then we try (hash(x) + 3\*hash2(x)) % S

#### Comparison of above three:

Linear probing has the best cache performance but suffers from clustering. One more advantage of Linear probing is easy to compute.

Quadratic probing lies between the two in terms of cache performance and clustering.

Double hashing has poor cache performance but no clustering. Double hashing requires more computation time as two hash functions need to be computed.

| Sr. No. Separate Chaining |                                     | Open Addressing                          |
|---------------------------|-------------------------------------|--|
| 1.                        | Chaining is Simpler to implement.   | Open Addressing requires more            |
| 1.                        |                                     | computation.                             |
|                           | In chaining, Hash table never fills | In open addressing, table may become     |
| 2.                        | up, we can always add more          | full.                                    |
|                           | elements to chain.                  |  |
| 3.                        | Chaining is Less sensitive to the   | Open addressing requires extra care      |
| ٥.                        | hash function or load factors.      | for to avoid clustering and load factor. |
|                           | Chaining is mostly used when it is  | Open addressing is used when the         |
| 4.                        | unknown how many and how            | frequency and number of keys is          |
| 4.                        | frequently keys may be inserted     | known.                                   |
|                           | or deleted.                         |  |
|                           | Cache performance of chaining is    | Open addressing provides better          |
| 5.                        | not good as keys are stored using   | cache performance as everything is       |
|                           | linked list.                        | stored in the same table.                |
| 6.                        | Wastage of Space (Some Parts of     | In Open addressing, a slot can be used   |
| 0.                        | hash table in chaining are never    | even if an input doesn't map to it.      |

|           | 1100d)                                  |                             |
|-----------|---|-----------------------------|
|           | used). Chaining uses extra space for    | No links in Open addressing |
| 7.        | links.                                  | No miks in Open addressing  |
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| stions:   | -                                       |                             |
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| . Wha     | t is hashing?                           |                             |
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|           | tio difference as between leaved arress | and back of amore?          |
| <br>. Wha | it is difference between keyed array    | and hashed array?           |
| . Wha     | t is difference between keyed array     | and hashed array?           |
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|           | It is difference between keyed array    | and hashed array?           |
|           |   | and hashed array?           |

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|   |                              |
| 4. What are the various basic operation | s of a hash table?           |
|   |                              |
|   |                              |
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|   |                              |
|   |                              |
|   |                              |
| 5. How element will be searched from    | hash table?                  |
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#### Title:

Implement all the functions of a dictionary (ADT) using hashing and handle collisions using chaining with / without replacement.

Data: Set of (key, value) pairs, Keys are mapped to values, Keys must be comparable, Keys must be unique. Standard Operations: Insert(key, value), Find(key), Delete(key)

# Learning Objectives:

- 1. To understand Dictionary (ADT)
- 2. To understand concept of hashing and collision handling.
- 3. To understand concept & features like searching using hash function.

# Learning Outcome:

- Define class for Dictionary using Object Oriented features.
- Analyze working of hash function.

#### Theory:

# Dictionary ADT

Dictionary (map, association list) is a data structure, which is generally an association of unique keys with some values. One may bind a value to a key, delete a key (and naturally an associated value) and lookup for a value by the key. Values are not required to be unique. Simple usage example is an explanatory dictionary. In the example, words are keys and explanations are values.

# Dictionary Operations

- Dictionary create()
  - creates empty dictionary
- boolean isEmpty(Dictionary d)
- tells whether the dictionary **d** is empty
- put(Dictionary d, Key k, Value v)
- $\bullet \;\;$  associates key k with a value v; if key k already presents in the dictionary old value is replaced by v
- Value get(Dictionary d, Key k)
- returns a value, associated with key **k**or null, if dictionary contains no such key
- remove(Dictionary d, Key k) removes key k and associated value

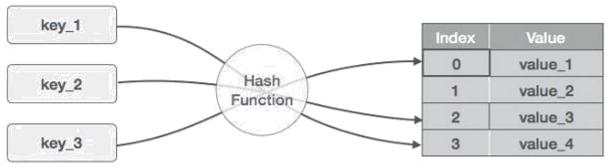
• **destroy(Dictionary d)** destroys dictionary **d** 

Hash Table is a data structure which stores data in an associative manner. In a hash table, data is stored in an array format, where each data value has its own unique index value. Access of data becomes very fast if we know the index of the desired data.

Thus, it becomes a data structure in which insertion and search operations are very fast irrespective of the size of the data. Hash Table uses an array as a storage medium and uses hash technique to generate an index where an element is to be inserted or is to be located from.

#### Hashing

Hashing is a technique to convert a range of key values into a range of indexes of an array. We're going to use modulo operator to get a range of key values. Consider an example of hash table of size 20, and the following items are to be stored. Item are in the (key, value) format.



| Conclusion:- |  |  |  |
|--------------|--|--|--|
|              |  |  |  |
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# Questions:-

1.

| What is Diction | onary? |  |  |
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|    | Why to use hash table to represent dictionary?                            |       |
|    |   |       |
|    |   |       |
|    | What are the various basic operations which can be performed on dictionar | y?    |
|    |   |       |
|    |   |       |
|    |   |       |
|    | How to delete and insert a value from dictionary?                         |       |
|    |   | _     |
|    |   |       |
|    | How to search a key from dictionary?                                      |       |
|    |   | _     |
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#### Title:

A book consists of chapters, chapters consist of sections and sections consist of subsections. Construct a tree and print the nodes. Find the time and space requirements of your method.

# **Learning Objectives:**

- To understand concept of tree data structure
- To understand concept & features of object oriented programming.
- To understand concept of class
- To understand concept of tree data structure.

# Learning Outcome:

- Define class for structures using Object Oriented features.
- Analyze tree data structure.

#### Theory:

#### Tree:

A tree T is a set of nodes storing elements such that the nodes have a parent-child relationship that satisfies the following

- if T is not empty, T has a special tree called the root that has no parent
- each node v of T different than the root has a unique parent node w; each node with parent w is a child of w

#### Recursive definition

- T is either empty
- or consists of a node r (the root) and a possibly empty set of trees whose roots are the children of r

Tree is a widely-used data structure that emulates a tree structure with a set of linked nodes. The tree graphically is represented most commonly as shown in figure below. The circles are the nodes and the edges are the links between them.

Trees are usually used to store and represent data in some hierarchical order. The data are stored in the nodes, from which the tree is consisted of.

A node may contain a value or a condition or represent a separate data structure or a tree of its own. Each node in a tree has zero or more child nodes, which are one level lower in the tree hierarchy (by convention, trees grow down, not up as they do in nature). A node that has a child is called the child's parent node (or ancestor node, or superior). A node has at most one parent. A node that has no child is called a leaf, and that node is of course at the bottommost level of the tree. The height of a node is the length of the longest path to a leaf from that node. The height of the root is the height of the tree. In other words, the "height" of

tree is the "number of levels" in the tree. Or more formally, the height of a tree is defined as follows:

- 1. The height of a tree with no elements is 0
- 2. The height of a tree with 1 element is 1
- 3. The height of a tree with > 1 element is equal to 1 + the height of its tallest subtree.

The depth of a node is the length of the path to its root (i.e., its root path). Every child node is always one level lower than his parent.

The topmost node in a tree is called the root node. Being the topmost node, the root node will not have parents. It is the node at which operations on the tree commonly begin (although some algorithms begin with the leaf nodes and work up ending at the root). All other nodes can be reached from it by following edges or links. (In the formal definition, a path from a root to a node, for each different node is always unique). In diagrams, it is typically drawn at the top.

In some trees, such as heaps, the root node has special properties.

A subtree is a portion of a tree data structure that can be viewed as a complete tree in itself. Any node in a tree T, together with all the nodes below his height, that are reachable from the node, comprise a subtree of T. The subtree corresponding to the root node is the entire tree; the subtree corresponding to any other node is called a proper subtree (in analogy to the term proper subset).

Every node in a tree can be seen as the root node of the subtree rooted at that node.

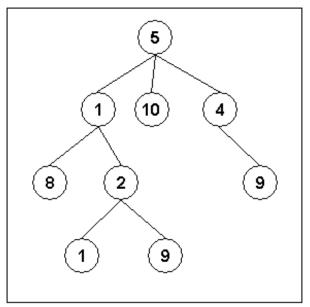


Fig1. An example of a tree

An internal node or inner node is any node of a tree that has child nodes and is thus not a leaf node.

There are two basic types of trees. In an unordered tree, a tree is a tree in a purely structural sense — that is to say, given a node, there is no order for the children of that node. A tree on which an order is imposed — for example, by assigning different natural numbers to each child of each node — is called an ordered tree, and data structures built on them are called ordered tree data structures. Ordered trees are by far the most common form of tree data structure. Binary search trees are one kind of ordered tree.

#### Important Terms

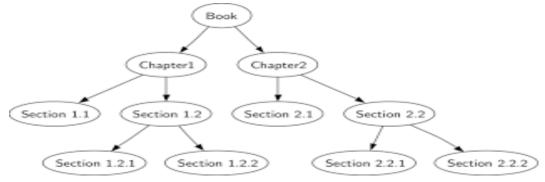
Following are the important terms with respect to tree.

- Path Path refers to the sequence of nodes along the edges of a tree.
- **Root** The node at the top of the tree is called root. There is only one root per tree and one path from the root node to any node.
- Parent Any node except the root node has one edge upward to a node called parent.
- **Child** The node below a given node connected by its edge downward is called its child node.
- **Leaf** The node which does not have any child node is called the leaf node.
- **Subtree** Subtree represents the descendants of a node.
- **Visiting** Visiting refers to checking the value of a node when control is on the node.
- **Traversing** Traversing means passing through nodes in a specific order.
- **Levels** Level of a node represents the generation of a node. If the root node is at level 0, then its next child node is at level 1, its grandchild is at level 2, and so on.
- **keys** Key represents a value of a node based on which a search operation is to be carried out for a node.

# Advantages of trees

Trees are so useful and frequently used, because they have some very serious advantages:

- Trees reflect structural relationships in the data
- Trees are used to represent hierarchies
- Trees provide an efficient insertion and searching
- Trees are very flexible data, allowing to move subtrees around with minumum effort For this assignment we are considering the tree as follows.



| AVCC | DE SANGAMNER                            | DSAL S.E. COMP SEM-II 2020    |
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| Conc | iusion                                  |                               |
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| 0    | · ·                                     |                               |
| Ques | tions:-                                 |                               |
| 1.   | What is a tree?                         |                               |
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|      |   |                               |
| 2.   | What is a class, object and data        | structure?                    |
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| 3.   | <b>Explain different types of tree?</b> |                               |
|      |   |                               |
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|      |   |                               |
| 4.   | What is root node, leaf node, in        | ernal node and external node? |
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| . What is level and height of a tree? |                   |
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#### Title:

Construct an expression tree from the given prefix expression eg. +--a\*bc/def and traverse it using post order traversal (non recursive) and then delete the entire tree.

**Learning Objectives:** To understand concept of Tree & Binary Tree.

To analyze the working of various Tree operations.

Learning Outcome: Students will be able to use various set of operations on Binary search.

# Theory:

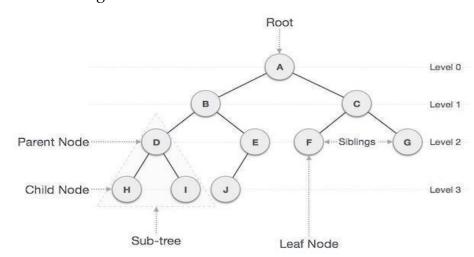
#### Tree

Tree represents the nodes connected by edges also a class of graphs that is acyclic is termed as trees. Let us now discuss an important class of graphs called trees and its associated terminology. Trees are useful in describing any structure that involves hierarchy. Familiar examples of such structures are family trees, the hierarchy of positions in an organization, and so on.

#### Binary Tree

A binary tree is made of nodes, where each node contains a "left" reference, a "right" reference, and a data element. The topmost node in the tree is called the root.

Every node (excluding a root) in a tree is connected by a directed edge from exactly one other node. This node is called a parent. On the other hand, each node can be connected to arbitrary number of nodes, called children. Nodes with no children are called leaves, or external nodes. Nodes which are not leaves are called internal nodes. Nodes with the same parent are called siblings.



#### **Insert Operation**

The very first insertion creates the tree. Afterwards, whenever an element is to be inserted, first locate its proper location. Start searching from the root node, then if the data is less than the key value, search for the empty location in the left subtree and insert the data. Otherwise, search for the empty location in the right subtree and insert the data.

#### Traversals

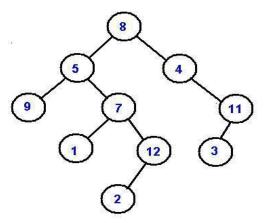
A traversal is a process that visits all the nodes in the tree. Since a tree is a nonlinear data structure, there is no unique traversal. We will consider several traversal algorithms with we group in the following two kinds

- depth-first traversal
- breadth-first traversal

There are three different types of depth-first traversals:

- PreOrder traversal visit the parent first and then left and right children;
- InOrder traversal visit the left child, then the parent and the right child;
- PostOrder traversal visit left child, then the right child and then the parent;

There is only one kind of breadth-first traversal--the level order traversal. This traversal visits nodes by levels from top to bottom and from left to right. As an example consider the following tree and its four traversals:



PreOrder - 8, 5, 9, 7, 1, 12, 2, 4, 11, 3 InOrder - 9, 5, 1, 7, 2, 12, 8, 4, 3, 11 PostOrder - 9, 1, 2, 12, 7, 5, 3, 11, 4, 8 LevelOrder - 8, 5, 4, 9, 7, 11, 1, 12, 3, 2

#### Algorithm to insert a node:

**Step 1 -** Search for the node whose child node is to be inserted. This is a node at some level i, and a node is to be inserted at the level i +1 as either its left child or right child. This is the node after which the insertion is to be made.

**Step 2 -** Link a new node to the node that becomes its parent node, that is, either the Lchild or the Rchild.

#### Algorithm to traverse a tree :

#### Inorder traversal

Until all nodes are traversed -

- **Step 1** Recursively traverse left subtree.
- **Step 2** Visit root node.
- **Step 3** Recursively traverse right subtree.

#### Preorder traversal

Until all nodes are traversed -

- **Step 1** Visit root node.
- **Step 2** Recursively traverse left subtree.
- **Step 3** Recursively traverse right subtree.

#### Postorder traversal

Until all nodes are traversed -

- **Step 1** Recursively traverse left subtree.
- **Step 2** Recursively traverse right subtree.
- Step 3 Visit root node.

#### Algorithm to copy one tree into another tree:

Step 1 - if (Root == Null)

Then return Null

Step 2 –Tmp = new TreeNode

Step 3 - Tmp->Lchild = TreeCopy(Root->Lchild);

Step 4 - Tmp->Rchild = TreeCopy(Root->Rchild);

**Step 5 -** Tmp-Data = Then Return

| Concident | Concl | lusion: |
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# Questions:-

# 1. What is a Binary Tree?

| AVCOE SANGAMNER      |                      | DSAL S.E. COMP SEM-II | 2020-21 |
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| 2. What are differer | nt tree traversal?   |                       |         |
|                      |                      |                       |         |
|                      |                      |                       |         |
|                      |                      |                       |         |
| 3. How to perform l  | Preorder traversal?  |                       |         |
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| 4. How to perform l  | norder traversal?    |                       |         |
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| 5. How to perform l  | Postorder traversal? |                       |         |
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#### Title:

Beginning with an empty binary search tree, Construct binary search tree by inserting the values in the order given. After constructing a binary tree -

i. Insert new node, ii. Find number of nodes in longest path from root, iii. Minimum data value found in the tree, iv. Change a tree so that the roles of the left and right pointers are swapped at every node, v. Search a value

#### Learning Objectives:

- To study how trees are used to represent data in hierarchical manner.
- To define binary search tree (BST) that allow both rapid retrieval by nkey and in order traversal.

#### Learning Outcomes:

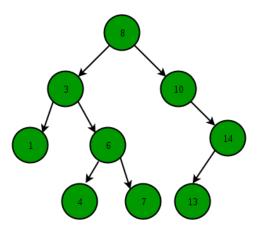
- Understand the basic concept of binary search tree.
- Understand the process of Tree traversal by visiting each node in the tree exactly once in a certain order.

#### Theory:

A binary search tree (BST) is a binary tree where each node has a Comparable key (and an associated value) and satisfies the restriction that the key in any node is larger than the keys in all nodes in that node's left subtree and smaller than the keys in all nodes in that node's right subtree.

Binary Search Tree A binary search tree is a rooted binary tree, whose internal nodes each store a key (and optionally, an associated value) and each have two distinguished subtrees, commonly denoted left and right. The tree additionally satisfies the binary search property, which states that the key in each node must be greater than or equal to any key stored in the left sub-tree, and less than or equal to any key stored in the right sub-tree. (The leaves (final nodes) of the tree contain no key and have no structure to distinguish them from one another. Leaves are commonly represented by a special leaf or nil symbol, a NULL pointer, etc.) Frequently, the information represented by each node is a record rather than a single data element. However, for sequencing purposes, nodes are compared according to their keys rather than any part of their associated records.

The major advantage of binary search trees over other data structures is that the related sorting algorithms and search algorithms such as in-order traversal can be very efficient; they are also easy to code. Binary search trees are a fundamental data structure used to construct more abstract data structures such as sets, multisets, and associative arrays.



The above properties of Binary Search Tree provides an ordering among keys so that the operations like search, minimum and maximum can be done fast. If there is no ordering, then we may have to compare every key to search for a given key.

To sort given input first creates a binary search tree from the elements of the input list or array and then performs an in-order traversal on the created binary search tree to get the elements in sorted order.

#### Algorithm:

Step 1: Take the elements input in an array.

Step 2: Create a Binary search tree by inserting data items from the array into the Binary search tree.

Step 3: Perform in-order traversal on the tree to get the elements in sorted order.

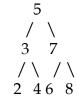
**Average Case Time Complexity**: O(n log n) Adding one item to a Binary Search tree on average takes O(log n) time. Therefore, adding n items will take O(n log n) time **Worst Case Time Complexity**: O(n²). The worst case time complexity of Tree Sort can be improved by using a self-balancing binary search tree like Red Black Tree, AVL Tree. Using self-balancing binary tree will take O(n log n) time to sort the array in worst case.

# Auxiliary Space: O(n)

Given a binary search tree, to sort list in decreasing order, the value of each node must be greater than the values of all the nodes at its right, and its left node must be NULL after flattening. We must do it in O(H) extra space where 'H' is the height of BST.

Examples:

# Input:



Output: 8765432

**Approach:** A simple approach will be to recreate the BST from its 'reverse in-order' traversal.

This will take O(N) extra space where N is the number of nodes in BST.

To improve upon that, let's simulate the reverse in-order traversal of a binary tree as follows:

- 1. Create a dummy node.
- 2. Create a variable called 'prev' and make it point to the dummy node.
- 3. Perform reverse in-order traversal and at each step.
  - Set prev -> right = curr
  - Set prev -> left = NULL
  - Set prev = curr

This will improve the space complexity to O(H) in the worst case as in-order traversal takes O(H) extra space.

| Conc | lusion:-<br>                  |
|------|-------------------------------|
|      |                               |
| Ques | tions:-                       |
| 1.   | What is a Binary Search Tree? |
|      |                               |
|      |                               |

| DE SANGAMNER                      | DSAL S.E. COMP SEM-II 20                      |
|-----------------------------------|---|
| How to sort the data in ascending | ng/descending order?                          |
|                                   |   |
|                                   |   |
|                                   |   |
| What is the complexity of sortin  | ng data using BST?                            |
|                                   |   |
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| Explain self-balanced BST with    | an ayampla?                                   |
| Explain sen-balanced b51 with     | an example:                                   |
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| How many maximum comparis         | ons are required to find any keyword from BST |
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#### Title:

Represent a given graph using adjacency matrix/list to perform DFS and using adjacency list to perform BFS. Use the map of the area around the college as the graph. Identify the prominent land marks as nodes and perform DFS and BFS on that.

#### **Learning Objectives:**

- To understand directed and undirected graph.
- To implement program to represent graph using adjacency matrix and list.
- To understand DFS and BFS

# Learning Outcome:

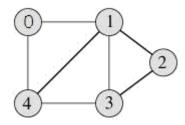
Student will be able to implement program for graph representation.

#### Theory:

Graph is a data structure that consists of following two components:

- 1. A finite set of vertices also called as nodes.
- 2. A finite set of ordered pair of the form (u, v) called as edge. The pair is ordered because (u, v) is not same as (v, u) in case of directed graph(di-graph). The pair of form (u, v) indicates that there is an edge from vertex u to vertex v. The edges may contain weight/value/cost.

Graphs are used to represent many real life applications: Graphs are used to represent networks. The networks may include paths in a city or telephone network or circuit network. Graphs are also used in social networks like linkedIn, facebook. For example, in facebook, each person is represented with a vertex (or node). Each node is a structure and contains information like person id, name, gender and locale. See this for more applications of graph. Following is an example undirected graph with 5 vertices.



Following two are the most commonly used representations of graph.

- 1. Adjacency Matrix
- 2. Adjacency List

There are other representations also like, Incidence Matrix and Incidence List. The choice of the graph representation is situation specific. It totally depends on the type of operations to be performed and ease of use.

# Adjacency Matrix:

Adjacency Matrix is a 2D array of size V x V where V is the number of vertices in a graph. Let the 2D array be adj[][], a slot adj[i][j] = 1 indicates that there is an edge from vertex i to vertex j. Adjacency matrix for undirected graph is always symmetric. Adjacency Matrix is also used to represent weighted graphs. If adj[i][j] = w, then there is an edge from vertex i to vertex j with weight w.

The adjacency matrix for the above example graph is:

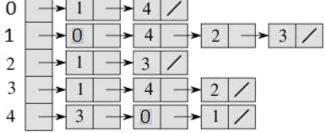
|    | 0 | , 1 | 2 | 3 | 4 |
|----|---|-----|---|---|---|
| 0  | 0 | 1   | 0 | 0 | 1 |
| 1. | 1 | 0   | 1 | 1 | 1 |
| 2  | 0 | 1   | 0 | 1 | 0 |
| 3  | 0 | 1   |   | 0 | 1 |
| 4  | 1 | 1   | 0 | 1 | 0 |

**Pros**: Representation is easier to implement and follow. Removing an edge takes O(1) time. Queries like whether there is an edge from vertex 'u' to vertex 'v' are efficient and can be done in O(1).

**Cons**: Consumes more space  $O(V^2)$ . Even if the graph is sparse(contains less number of edges), it consumes the same space. Adding a vertex is  $O(V^2)$  time.

# Adjacency List:

An array of linked lists is used. Size of the array is equal to number of vertices. Let the array be array[]. An entry array[i] represents the linked list of vertices adjacent to the ith vertex. This representation can also be used to represent a weighted graph. The weights of edges can be stored in nodes of linked lists. Following is adjacency list representation of the above graph.



**Pros**: Saves space O(|V|+|E|). In the worst case, there can be C(V, 2) number of edges in a graph thus consuming  $O(V^2)$  space. Adding a vertex is easier.

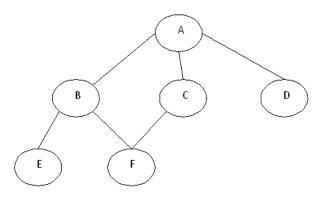
Cons: Queries like whether there is an edge from vertex u to vertex v are not efficient and can be done O(V).

# Graph Traversal:

The breadth first search (BFS) and the depth first search (DFS) are the two algorithms used for traversing and searching a node in a graph. They can also be used to find out whether a node is reachable from a given node or not.

#### Depth First Search (DFS)

The aim of DFS algorithm is to traverse the graph in such a way that it tries to go far from the root node. Stack is used in the implementation of the depth first search. Let's see how depth first search works with respect to the following graph:



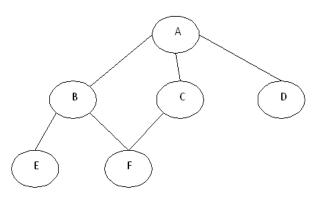
As stated before, in DFS, nodes are visited by going through the depth of the tree from the starting node. If we do the depth first traversal of the above graph and print the visited node, it will be "A B E F C D". DFS visits the root node and then its children nodes until it reaches the end node, i.e. E and F nodes, then moves up to the parent nodes.

#### Algorithmic Steps

- 1. **Step 1**: Push the root node in the Stack.
- 2. **Step 2**: Loop until stack is empty.
- 3. **Step 3**: Peek the node of the stack.
- 4. **Step 4**: If the node has unvisited child nodes, get the unvisited child node, mark it as traversed and push it on stack.
- 5. **Step 5**: If the node does not have any unvisited child nodes, pop the node from the stack.

#### Breadth First Search (BFS)

This is a very different approach for traversing the graph nodes. The aim of BFS algorithm is to traverse the graph as close as possible to the root node. Queue is used in the implementation of the breadth first search. Let's see how BFS traversal works with respect to the following graph:



If we do the breadth first traversal of the above graph and print the visited node as the output, it will print the following output. "A B C D E F". The BFS visits the nodes level by level, so it will start with level 0 which is the root node, and then it moves to the next levels which are B, C and D, then the last levels which are E and F.

# Algorithmic Steps

- 1. **Step 1**: Push the root node in the Queue.
- 2. **Step 2**: Loop until the queue is empty.
- 3. **Step 3**: Remove the node from the Queue.
- 4. **Step 4**: If the removed node has unvisited child nodes, mark them as visited and insert the unvisited children in the queue.

| Conci |  |      |
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|       | rions:-  |      |
| Quest |  |      |
|       | An undirected graph having n edges, then find out no. of vertices that graph l | have |
|       |  | have |

| DE SANGAMNER                     | DSAL S.E. COMP SEM-II 202                  |
|----------------------------------|--|
| How to represent graph?          |  |
|                                  |  |
|                                  |  |
| What are different methods to o  | display graph?                             |
|                                  |  |
|                                  |  |
| Explain briefly various algorith | nm for graph traversal?                    |
|                                  |  |
|                                  |  |
|                                  |  |
| What is the complexity of repre  | esenting graph in various representations? |
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#### Title:

There are flight paths between cities. If there is a flight between city A and city B then there is an edge between the cities. The cost of the edge can be the time that flight takes to reach city B from A or the amount of fuel used for the journey. Represent this as a graph. The node can be represented by airport name or name of the city. Use adjacency list or use adjacency matrix representation for graph. Check whether the graph is connected or not. Justify the storage representation used.

# **Learning Objectives:**

- To understand concept of Graph data structure
- To understand concept of representation of graph.

#### Learning Outcome:

- Define class for graph using Object Oriented features.
- Analyse working of functions.

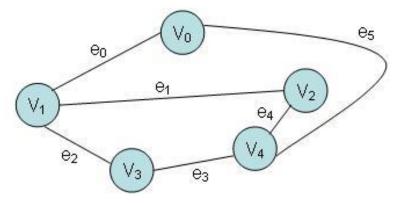
# Theory:

# Graph:

Graphs are the most general data structure. They are also commonly used data structures. A non-linear data structure consisting of nodes and links between nodes.

# Undirected graph:

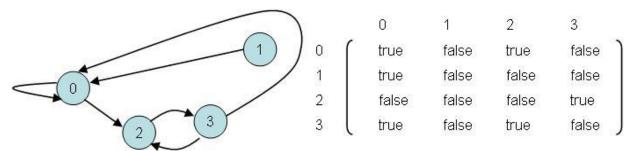
- An undirected graph is a set of nodes and a set of links between the nodes.
- Each node is called a **vertex**, each link is called an **edge**, and each edge connects two vertices.
- The order of the two connected vertices is unimportant.
- An undirected graph is a finite set of vertices together with a finite set of edges. Both sets might be empty, which is called the empty graph.



## **Graph Implementation:**

Different kinds of graphs require different kinds of implementations, but the fundamental concepts of all graph implementations are similar. We'll look at several representations for one particular kind of graph: directed graphs in which loops are allowed.

#### Representing Graphs with an Adjacency Matrix



Graph and adjacency matrix

#### Adjacency Matrix:

An adjacency matrix is a square grid of true/false values that represent the edges of a graph

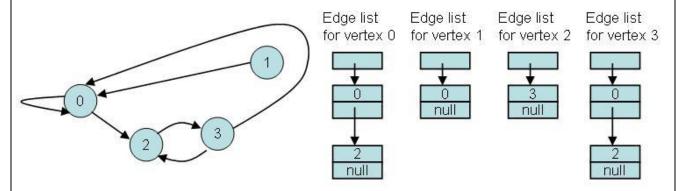
- If the graph contains n vertices, then the grid contains n rows and n columns.
- For two vertex numbers *i* and *j*, the component at row *i* and column *j* is true if there is an edge from vertex *i* to vertex *j*; otherwise, the component is false.

We can use a two-dimensional array to store an adjacency matrix:

## boolean[][] adjacent = new boolean[4][4];

Once the adjacency matrix has been set, an application can examine locations of the matrix to determine which edges are present and which are missing.

## Representing Graphs with Edge Lists



Graph and adjacency list for each node

## Adjacency List:

- A directed graph with *n* vertices can be represented by *n* different linked lists.
- List number *i* provides the connections for vertex *i*.
- For each entry j in list number i, there is an edge from i to j.

Loops and multiple edges could be allowed.

|   | DSAL S.E. COMP SEM-II 202        |
|---|----------------------------------|
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| Which operations are possible if graph is rep   | presented as adjacency list?     |
| . Which operations are possible it graph is rep | resented as adjacency list.      |
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| . What are the advantages and disadvantages o   | of various graph representation? |
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#### Title:

Given sequence k = k1 < k2 < ... < kn of n sorted keys, with a search probability pi for each key ki. Build the Binary search tree that has the least search cost given the access probability for each key?

#### Learning Objectives:

- To understand concept of OBST.
- To understand concept & features like extended binary search tree.

#### **Learning Outcome:**

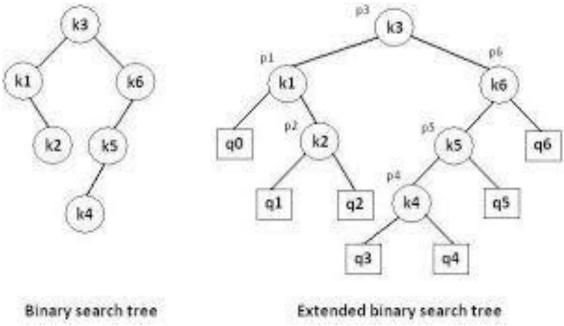
- Define class for Extended binary search tree using Object Oriented features.
- Analyse OBST.

#### Theory:

An optimal binary search tree is a binary search tree for which the nodes are arranged on levels such that the tree cost is minimum.

For the purpose of a better presentation of optimal binary search trees, we will consider "extended binary search trees", which have the keys stored at their internal nodes. Suppose "n" keys k1, k2, ... k n are stored at the internal nodes of a binary search tree. It is assumed that the keys are given in sorted order, so that k1 < k2 < ... < kn.

An extended binary search tree is obtained from the binary search tree by adding successor nodes to each of its terminal nodes as indicated in the following figure by squares:



#### In the extended tree:

- The squares represent terminal nodes. These terminal nodes represent unsuccessful searches of the tree for key values. The searches did not end successfully, that is, because they represent key values that are not actually stored in the tree;
- The round nodes represent internal nodes; these are the actual keys stored in the tree;
- Assuming that the relative frequency with which each key value is accessed is known, weights can be assigned to each node of the extended tree (p1 ... p6). They represent the relative frequencies of searches terminating at each node, that is, they mark the successful searches.
- If the user searches a particular key in the tree, 2 cases can occur:
  - o the key is found, so the corresponding weight 'p' is incremented;
  - o the key is not found, so the corresponding 'q' value is incremented.

#### Generalization:

The terminal node in the extended tree that is the left successor of k1 can be interpreted as representing all key values that are not stored and are less than k1. Similarly, the terminal node in the extended tree that is the right successor of kn, represents all key values not stored in the tree that are greater than kn. The terminal node that is successes between ki and ki-1 in an inorder traversal represent all key values not stored that lie between ki and ki-1.

## Algorithm

```
We have the following procedure for determining R(i, j) and C(i, j) with 0 \le i \le j \le n:

PROCEDURE COMPUTE_ROOT(n, p, q; R, C)

begin

for i = 0 to n do

C(i, i) \leftarrow 0

W(i, i) \leftarrow q(i)

for m = 0 to n do

for i = 0 to (n - m) do

j \leftarrow i + m

W(i, j) \leftarrow W(i, j - 1) + p(j) + q(j)

*find C(i, j) and R(i, j) which minimize the tree cost

end

The following function builds an optimal binary search tree
```

| AVCOE SANGAMNER  | DSAL S.E. COMP SEM-II 2020-21              |
|--|--|
| FUNCTION CONSTRUCT(R, i, j)  |  |
| begin  |  |
| *build a new internal node N labeled (i, j)  |  |
| $k \leftarrow R(i, j)$   |  |
| f i = k then   |  |
| *build a new leaf node N" labeled (i, i)   |  |
| else   |  |
| *N" $\leftarrow$ CONSTRUCT(R, i, k)  |  |
| *N" is the left child of node N  |  |
| if $k = (j - 1)$ then  |  |
| *build a new leaf node N'''' labeled (j, j)  |  |
| else   |  |
| *N'''' $\leftarrow$ CONSTRUCT(R, k + 1, j)   |  |
| *N'''' is the right child of node N  |  |
| return N   |  |
| end  |  |
| The algorithm requires O (n²) time and O (n²) out of storage even before it runs out of time. I half by implementing the two-dimensional array | The storage needed can be reduced by almos |
| Conclusion:-   |  |
|  |  |
| Questions:- 1. What is Binary Tree?  |  |
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|---------------------------------------|---------------------------|
| . What is binary search tree and exte | ended binary search tree? |
|                                       |                           |
|                                       |                           |
|                                       |                           |
| . What is OBST?                       |                           |
|                                       | _                         |
|                                       |                           |
|                                       |                           |
|                                       |                           |
| . Which is the best way of represent  | ting OBST?                |
|                                       |                           |
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|                                       |                           |
|                                       |                           |
| . What is the complexity of OBST?     |                           |
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#### Title:

A Dictionary stores keywords and its meanings. Provide facility for adding new keywords, deleting keywords, updating values of any entry. Provide facility to display whole data sorted in ascending/ Descending order. Also find how many maximum comparisons may require for finding any keyword. Use Height balance tree and find the complexity for finding a keyword.

#### Learning Objectives:

- To understand concept of height balanced tree data structure.
- To understand procedure to create height balanced tree.

### Learning Outcome:

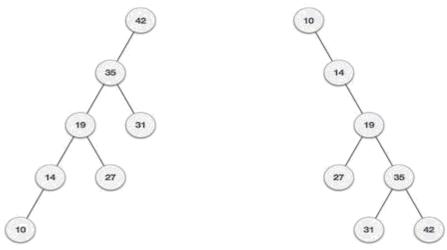
- Define class for AVL using Object Oriented features.
- Analyze working of various operations on AVL Tree .

#### Theory:

An empty tree is height balanced tree if T is a nonempty binary tree with TL and TR as its left and right sub trees. The T is height balance if and only if Its balance factor is 0, 1, -1.

**AVL** (Adelson- Velskii and Landis) Tree: A balance binary search tree. The best search time, that is O (log N) search times. An AVL tree is defined to be a well-balanced binary search tree in which each of its nodes has the AVL property. The AVL property is that the heights of the left and right sub-trees of a node are either equal or if they differ only by 1.

What if the input to binary search tree comes in a sorted (ascending or descending) manner? It will then look like this –



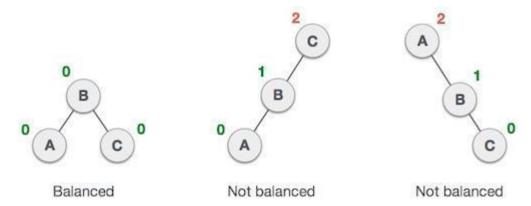
If input 'appears' non-increasing manner

If input 'appears' in non-decreasing manner

It is observed that BST's worst-case performance is closest to linear search algorithms, that is O(n). In real-time data, we cannot predict data pattern and their frequencies. So, a need arises to balance out the existing BST.

Named after their inventor **Adelson**, **Velski** & **Landis**, **AVL trees** are height balancing binary search tree. AVL tree checks the height of the left and the right sub-trees and assures that the difference is not more than 1. This difference is called the **Balance Factor**.

Here we see that the first tree is balanced and the next two trees are not balanced -



In the second tree, the left subtree of **C** has height 2 and the right subtree has height 0, so the difference is 2. In the third tree, the right subtree of **A** has height 2 and the left is missing, so it is 0, and the difference is 2 again. AVL tree permits difference (balance factor) to be only 1.

BalanceFactor = height(left-sutree) - height(right-sutree)

If the difference in the height of left and right sub-trees is more than 1, the tree is balanced using some rotation techniques.

#### **AVL Rotations**

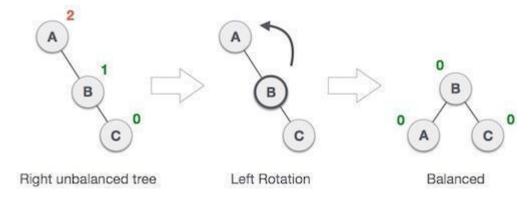
To balance itself, an AVL tree may perform the following four kinds of rotations –

- Left rotation
- Right rotation
- Left-Right rotation
- Right-Left rotation

The first two rotations are single rotations and the next two rotations are double rotations. To have an unbalanced tree, we at least need a tree of height 2. With this simple tree, let's understand them one by one.

#### Left Rotation

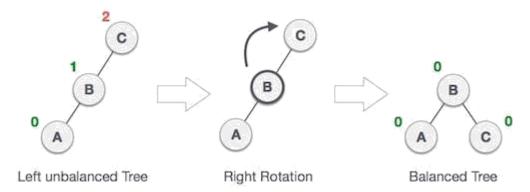
If a tree becomes unbalanced, when a node is inserted into the right subtree of the right subtree, then we perform a single left rotation –



In our example, node  $\bf A$  has become unbalanced as a node is inserted in the right subtree of A's right subtree. We perform the left rotation by making  $\bf A$  the left-subtree of B.

## Right Rotation

AVL tree may become unbalanced, if a node is inserted in the left subtree of the left subtree. The tree then needs a right rotation.



As depicted, the unbalanced node becomes the right child of its left child by performing a right rotation.

### Left-Right Rotation

Double rotations are slightly complex version of already explained versions of rotations. To understand them better, we should take note of each action performed while rotation. Let's first check how to perform Left-Right rotation. A left-right rotation is a combination of left rotation followed by right rotation.

| State       | Action   |
|-------------|--|
| C C B       | A node has been inserted into the right subtree of the left subtree. This makes C an unbalanced node. These scenarios cause AVL tree to perform left-right rotation. |
| C A B       | We first perform the left rotation on the left subtree of <b>C</b> . This makes <b>A</b> , the left subtree of <b>B</b> .  |
| 2<br>C<br>B | Node <b>C</b> is still unbalanced, however now, it is because of the left-subtree of the left-subtree.   |
| B           | We shall now right-rotate the tree, making <b>B</b> the new root node of this subtree. <b>C</b> now becomes the right subtree of its own left subtree.               |
| O B C O     | The tree is now balanced.  |

# Right-Left Rotation

The second type of double rotation is Right-Left Rotation. It is a combination of right rotation followed by left rotation.

| State   | Action   |
|---------|--|
| A 1 C D | A node has been inserted into the left subtree of the right subtree. This makes <b>A</b> , an unbalanced node with balance factor 2.   |
| A C B   | First, we perform the right rotation along <b>C</b> node, making <b>C</b> the right subtree of its own left subtree <b>B</b> . Now, <b>B</b> becomes the right subtree of <b>A</b> . |
| A 1 B C | Node A is still unbalanced because of the right subtree of its right subtree and requires a left rotation.   |
| A B C   | A left rotation is performed by making B the new root node of the subtree. A becomes the left subtree of its right subtree B.  |
| O B C O | The tree is now balanced.  |

#### Algorithm AVL TREE:

```
Insert:-
```

1. If P is NULL, then I. P =

new node

II.  $P \rightarrow element = x$ 

III.  $P \rightarrow left = NULL$ 

IV. P ->right = NULL

 $V. P \rightarrow height = 0$ 

2. else if x>1 => x<P ->element

a.)  $insert(x, P \rightarrow left)$ 

b.) if height of P->left -height of P ->right =2

1.  $insert(x, P \rightarrow left)$ 

2. if  $height(P \rightarrow left) - height(P \rightarrow right) = 2$ 

if x<P ->left ->element

P = singlerotateleft(P)

else

P = doublerotateleft(P)

3. else

if x<P ->element

a.)  $insert(x, P \rightarrow right)$ 

b.) if height (P -> right) -height (P ->left) =2

if(x<P ->right) ->element

P = singlerotateright(P)

else

P = doublerotateright(P)

4. else

Print already exits

5. int m, n, d.

6. m = AVL height (P->left)

7. n = AVL height (P->right)

 $8. d = \max(m, n)$ 

9. P->height = d+1

Stop

### RotateWithLeftChild( AvlNode k2)

- AvlNode k1 = k2.left;
- k2.left = k1.right;
- k1.right = k2;
- k2.height = max(height(k2.left), height(k2.right)) + 1;
- k1.height = max( height( k1.left ), k2.height ) + 1;

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|---|-------------------------------|
| 3. What is balance tree and various ways to bal | ance it?                      |
|   |                               |
|   |                               |
| 4. In which condition balancing has to be done  | e in an AVL tree?             |
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| 5. In which condition balanced binary tree is p | referable than array?         |
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#### Title:

Read the marks obtained by students of second year in an online examination of particular subject. Find out maximum and minimum marks obtained in that subject. Use heap data structure. Analyze the algorithm.

### Learning Objectives:

- To understand concept of heap
- To understand concept & features like max heap, min heap.

#### Learning Outcome:

- Define class for heap using Object Oriented features.
- Analyze working of functions.

#### Theory:

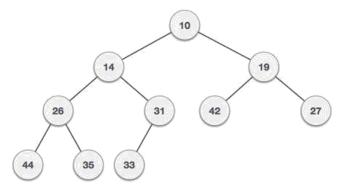
Heap is a special case of balanced binary tree data structure where the root-node key is compared with its children and arranged accordingly. If  $\alpha$  has child node  $\beta$  then–

$$key(\alpha) \ge key(\beta)$$

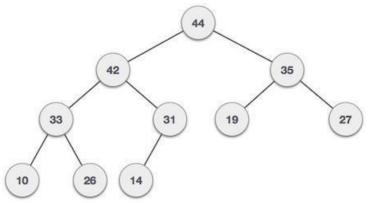
As the value of parent is greater than that of child, this property generates **Max Heap**. Based on this criteria, a heap can be of two types –

For Input  $\rightarrow$  35 33 42 10 14 19 27 44 26 31

**Min-Heap** – Where the value of the root node is less than or equal to either of its children.



**Max-Heap** – Where the value of the root node is greater than or equal to either of its children.



#### Max Heap Construction Algorithm

We shall use the same example to demonstrate how a Max Heap is created. The procedure to create Min Heap is similar but we go for min values instead of max values.

We are going to derive an algorithm for max heap by inserting one element at a time. At any point of time, heap must maintain its property. While insertion, we also assume that we are inserting a node in an already heapified tree.

- **Step 1** Create a new node at the end of heap.
- Step 2 Assign new value to the node.
- **Step 3** Compare the value of this child node with its parent.
- **Step 4** If value of parent is less than child, then swap them.
- Step 5 Repeat step 3 & 4 until Heap property holds.

**Note** – In Min Heap construction algorithm, we expect the value of the parent node to be less than that of the child node.

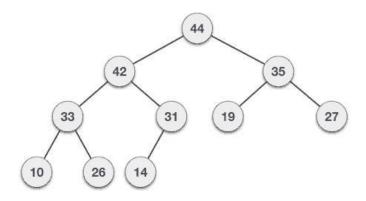
Let's understand Max Heap construction by an animated illustration. We consider the same input sample that we used earlier.

INPUT:35,33,42,10,14,19,27,44,16,31

#### Max Heap Deletion Algorithm

Let us derive an algorithm to delete from max heap. Deletion in Max (or Min) Heap always happens at the root to remove the Maximum (or minimum) value.

- Step 1 Remove root node.
- Step 2 Move the last element of last level to root.
- **Step 3** Compare the value of this child node with its parent.
- Step 4 If value of parent is less than child, then swap them.
- **Step 5** Repeat step 3 & 4 until Heap property holds.



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|   |                               |
| Conclusion:-  |                               |
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| Questions:-   |                               |
| 1. What is heap?  |                               |
| in this is near the second to |                               |
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| 2. Explain various operations which can be perf   | Formed on heap?               |
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| 3. What is max heap and min heap?   |                               |
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| 4. How to represent a heap?   |                               |
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#### Title:

Department maintains a student information. The file contains roll number, name, division and address. Allow user to add, delete information of student. Display information of particular employee. If record of student does not exist an appropriate message is displayed. If it is, then the system displays the student details. Use sequential file to main the data.

#### Learning Objectives:

- To understand concept of file organization in data structure.
- To understand concept & features of sequential file organization.

### Learning Outcome:

- Define class for sequential file using Object Oriented features.
- Analyze working of various operations on sequential file .

#### Theory:

File organization refers to the relationship of the key of the record to the physical location of that record in the computer file. File organization may be either physical file or a logical file. A physical file is a physical unit, such as magnetic tape or a disk. A logical file on the other hand is a complete set of records for a specific application or purpose. A logical file may occupy a part of physical file or may extend over more than one physical file.

There are various methods of file organizations. These methods may be efficient for certain types of access/selection meanwhile it will turn inefficient for other selections. Hence it is up to the programmer to decide the best suited file organization method depending on his requirement.

Some of the file organizations are

- 1. Sequential File Organization
- 2. Heap File Organization
- 3. Hash/Direct File Organization
- 4. Indexed Sequential Access Method
- 5. B+ Tree File Organization
- 6. Cluster File Organization

## Sequential File Organization:

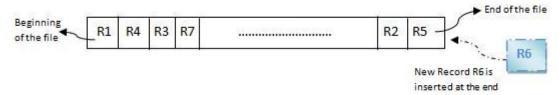
It is one of the simple methods of file organization. Here each file/records are stored one after the other in a sequential manner. This can be achieved in two ways:

Records are stored one after the other as they are inserted into the tables. This method
is called pile file method. When a new record is inserted, it is placed at the end of the

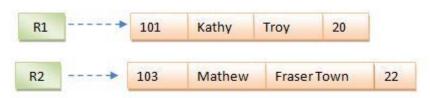
file. In the case of any modification or deletion of record, the record will be searched in the memory blocks. Once it is found, it will be marked for deleting and new block of record is entered.



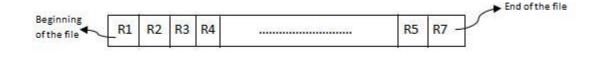
#### Inserting a new record:



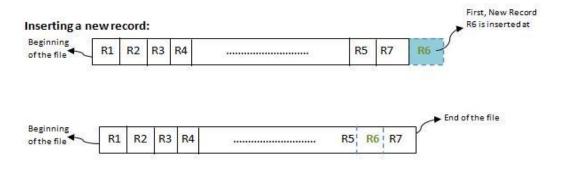
In the diagram above, R1, R2, R3 etc are the records. They contain all the attribute of a row. i.e.; when we say student record, it will have his id, name, address, course, DOB etc. Similarly R1, R2, R3 etc can be considered as one full set of attributes.



In the second method, records are sorted (either ascending or descending) each time they are inserted into the system. This method is called **sorted file method**. Sorting of records may be based on the primary key or on any other columns. Whenever a new record is inserted, it will be inserted at the end of the file and then it will sort – ascending or descending based on key value and placed at the correct position. In the case of update, it will update the record and then sort the file to place the updated record in the right place. Same is the case with delete.



### Inserting a new record:



## Advantages:

- Simple to understand.
- Easy to maintain and organize
- Loading a record requires only the record key.
- Relatively inexpensive I/O media and devices can be used.
- Easy to reconstruct the files.
- The proportion of file records to be processed is high.

#### Disadvantages:

- Entire file must be processed, to get specific information.
- Very low activity rate stored.
- Transactions must be stored and placed in sequence prior to processing.
- Data redundancy is high, as same data can be stored at different places with different keys.

| <ul> <li>Impossible to handle random enquiries.</li> </ul> |    |
|--|----|
| Conclusion:-   |    |
|  |    |
|  |    |
| Questions:-  |    |
| 1. What is file organization?                              |    |
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|  |    |
|  |    |
| 2. Explain various methods of file organization?           |    |
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| 3. Explain sequential file organization?                   |                               |
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| 4. How records are stored in sequential file organization? |                               |
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| 5. What are pros and cons of file organization?            |                               |
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#### Title:

Assume we have two input and two output tapes to perform the sorting. The internal memory can hold and sort m records at a time. Write a program in Java for external sorting. Find out time complexity.

#### **Learning Objectives:**

- To understand the concept and basic of Sorting, internal and external memory handling.
- To analyse time complexity of sorting algorithm.

#### Learning Outcome:

- Internal and external memory handling.
- Sorting and its complexity.

#### Theory:

#### External Sorting:

External Sorting is sorting the lists that are so large that the whole list cannot be contained in the internal memory of a computer.

Assume that the list(or file) to be sorted resides on a disk. The term block refers to the unit of data that is read from or written to a disk at one time. A block generally consists of several records. For a disk, there are three factors contributing to read/write time:

- a. Seek time: time taken to position the read/write heads to the correct cylinder. This will depend on the number of cylinders across which the heads have to move.
- b. Latency time: time until the right sector of the track is under the read/write head.
- c. Transmission time: time to transmit the block of data to/from the disk.

## Example of External Sorting:

2-way Merge Sort, k-way Merge Sort, Polyphase Merge sort etc.

## External Sorting with Disks:

The most popular method for sorting on external storage devices is merge sort. This method consists of essentially two distinct phases.

**First Phase (Run Generation Phase):** Segments of the input file are sorted using a good internal sort method. These sorted segments, known as runs, are written out onto external storage as they are generated.

**Second Phase (Merge Phase):** The runs generated in phase one are merged together following the merge tree pattern, until only one run is left.

2-way Merging/Basic External Sorting Algorithm Assume unsorted data is on disk at start.

Let M=maximum number of records that can be sorted & sorted in internal memory at one time.

#### Algorithm:

#### Repeat

- 1. Read M records into main memory & sort internally.
- 2. Write this sorted sub-list into disk. (This is one "run"). Until data is processed into runs.

### Repeat

- 1. Merge two runs into one sorted run twice as long.
- 2. Write this single run back onto disk

Until all runs processed into runs twice as long

Merge runs again as often as needed until only one large run: The sorted list.

## Pseudo Code for merging of M records:

```
open N input files and one output file (* initialize buffers *)
loop from i = 1 to N if end_of_file (file i)
then buffer[i] <- invalid_key else buffer[i] <- first record of file i;
(* merge *) stop <- false repeat
s <- index of smallest buffer element if buffer[s] = invalid_key
then stop <- true else write buffer[s] if end_of_file (file s)
then buffer[s] <- invalid_key
else buffer[s] <- next record from file s until stop = true
close files
```

## Measuring Performance: Time Complexity:

The size of a run and number of initial runs (nr) is dictated by the number of file blocks (b) and the available buffer space (nb)

- Nr = b/nb
- E.g b = 1024 blocks and nb = 5 blocks then 205 initial runs will be needed

The degree of merging (dm) is the number of runs that can be merged together in each pass.

- One buffer block is needed to hold one block from each run being merged
- One buffer block is needed for containing one block of merged result
- Dm is the smaller of (nb 1) and nr
- Number of passes = logdm(nr)

#### Analysis

This algorithm requires log(N/M) passes with initial run pass. Therefore, at each pass the N records are processed and at last we will get a time complexity as  $O(N \log(N/M)$ .

## How to compile java file

If you are not using any IDE, you need to follow the syntax given below:

javac -d directory javafilename

For example

javac -d . Simple.java

The -d switch specifies the destination where to put the generated class file. You can use any directory name like /home (in case of Linux), d:/abc (in case of windows) etc. If you want to keep the package within the same directory, you can use . (dot).

| How to run java program  |   |
|--|---|
| You need to use fully qualified name e.g. Simple etc to run the class. |   |
| To Compile: javac -d . Simple.java                                     |   |
| To Run: java Simple  |   |
| Output: Welcome to Java  |   |
| Conclusion:-   |   |
|  |   |
|  |   |
| Questions:-  |   |
| 1. What is external sorting?   |   |
|  |   |
|  |   |
|  |   |
| 2. Which package stores all the standard java classes?                 |   |
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