Analysis and Modeling of US Pollution Data for 1980-2018 and its implications on the atmosphere

Ву:

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Course: (19-603) Data Science for Technology, Innovation and Public Policy

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Abstract

Pollution has become a word of widespread discussion all over the world, mainly due to its increasing presence in our lives. Be it New Delhi in India, or be it Beijing in China, air pollution has caused rapid disruption in daily activities leading to closure of schools and public places. Apart from harming the social life, pollution has also affected the environment in an adverse manner, which rampant fluctuations in atmospheric parameter. This report considers four major pollutants, Carbon monoxide (CO), Sulphur dioxide (SO₂), Nitrogen dioxide (NO₂) and Ozone (O₃). These pollutants are the key components of any industrial smog or emission which is released into the atmosphere. Moreover, it is easier to measure these concentrations because of readily available techniques. The report aims to correlate the concentrations of these species with two atmospheric parameters, Temperature and %RH (Relative Humidity). Apart from finding direct correlations, the report also takes into account spatial and temporal considerations. For the scope of this report, the area under scrutiny is the United States of America, considering the 50 states and several cities in each state. The report uses different data visualization techniques to establish correlations between the involved parameters. Robust models are developed using data science techniques and are tabulated. Moreover, apart from the concentration factors, the model also aims to correlate the number of samples chosen to arrive at the mean reading to the states in the USA.

Data

Apart from the four pollutants mentioned here, there are several other undetected pollutants, which are present in negligible amounts. For the scope of this project, the concentration of all these pollutants are assumed to have no effect on the proposed models and predictions. They can either be considered as an inclusion in the intercept or a part of the residual error. For the scope of this project, the region in focus is the USA, considering all the 50 states, with a variable number of cities in each state, depending upon the size and feasibility of data collection. The data was obtained from: 'https://aqs.epa.gov/aqsweb/airdata/download_files.html', which is the official data repository for US EPA (Environment Protection Agency). The referred data is in the form of multiple .csv files, with files separated by each year and every pollutant. The data collected for each pollutant follows a general pattern:

(StateCode - CountryCode - SiteCode - ParameterCode - POC - Latitude - Longitude - Datum-SampleDuration - Date - Units - ObservationCount - Percent - Arithmetic Mean-Maxvalue - AQI - Method - State - Country - City)

The required features are extracted from the files for further modeling.

The scattered .csv files were combined into a single file for each pollutant, for the years 1980-2018. Lastly, each of those files for individual parameters were combined into a final .csv files, so as to correlate the pollutants to these dependant parameters.

The combined .csv files are made publicly available at:

https://drive.google.com/drive/folders/1yKqv8DsB6o1szznw1qjfyM8zmG-egUOE?usp=sharing.

Data Visualization

Time variance of Pollutants

In order to understand the trend of each individual pollutant over time, the graphs of pollutant concentration was plotted as shown in Figure 1.

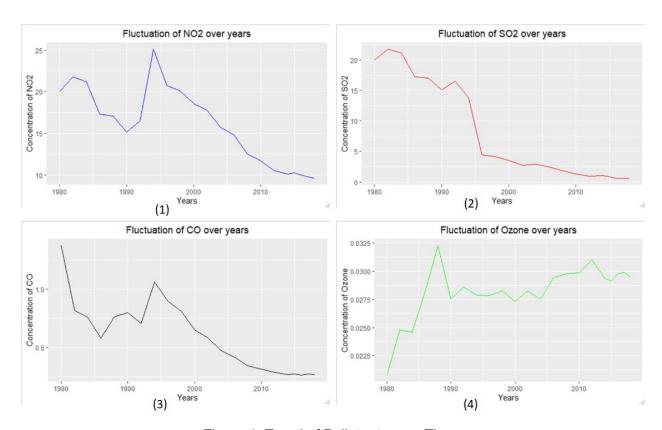


Figure 1: Trend of Pollutants over Time

From the plots, the trend of each pollutant over time can be roughly estimated. The concentration of NO_2 , SO_2 and CO have been on the decline for the past 25 years and keep on declining with subsequent years. On the contrary, the concentration of Ozone has a fluctuating pattern, with frequent peaks in the curve. No definite conclusion can be drawn about the Ozone concentration.

For the trend of NO₂, SO₂ and CO, there is a sudden peak observed in the pollutant concentration in the decade of the 1990s, roughly around 1994-96. There seems to be a

correlation between each of the individual pollutant's behavior, and thus, these pollutants are correlated later in the regression models.

Time variance of Atmospheric Parameters

In order to understand the trend of Temperature and Relative Humidity over time, the graphs were plotted as shown in Figure 2.

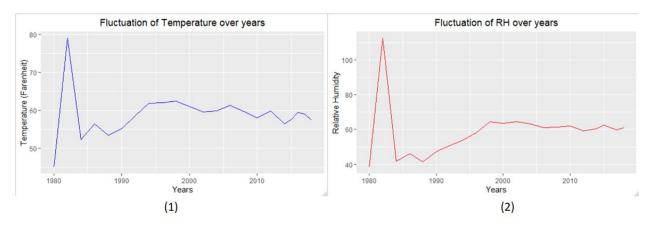
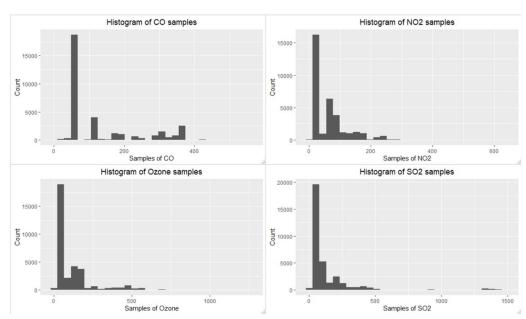


Figure 2: Temperature and %RH fluctuations over Time

The trend observed for Temperature and Relative Humidity over the years is similar to each other, with a significant peak at the exact time. Moreover, the Temperature and RH seems to have minor fluctuations over the past two decades. Also, the sudden drop in Temperature and RH over the third time instant is unexpected and is thus analyzed in the further sections.



Consideration of Sample Size

Figure 3: Frequency distribution of sample size

Sample size is an important consideration in the design of experiments. A sample size is the number of times each sample is repeated for better accuracy. In case of areas with tougher atmospheric conditions, multiple samples are collected to ensure higher perfection.. However, here, it is observed that maximum readings have less than 10 samples, while some samples are collected multiple times. Also, the sample size may vary state to state depending upon the ease of setting up measurement instruments. This analysis is done in further part of the report.

Data Modeling

Temperature Model (LM)

Temperature, a dependant parameter was modeled against the following independent parameters:

- 1) Pollutant concentration
- 2) Time (Years)
- 3) State

Thus, the temperature is a spatial-temporal dependant parameter, with State treated as categorical variable whereas the pollutant concentrations and years as continuous. The model thus fit was:

$$T_{i} = \beta_{0} + \beta_{1}(SO_{2})_{i} + \beta_{2}(NO_{2})_{i} + \beta_{3}(O_{3})_{i} + \beta_{4}(CO)_{i} + \sum \beta_{i}(year)_{i} + \sum \beta_{i}(state)_{i}$$

Months and states were modelled as factors. In order to avoid the dummy variable trap, coefficients are reported except for April (with month as a categorical variable) and Alabama (with state as a categorical variable).

From the tabulated results, it can be inferred that the coefficients of CO and O_3 are satisfactorily high, which implies that these two pollutants have a greater impact on the Temperature in comparison to NO_2 and SO_2 , which have sufficiently low coefficients.

The coefficients for months were obtained as follows:

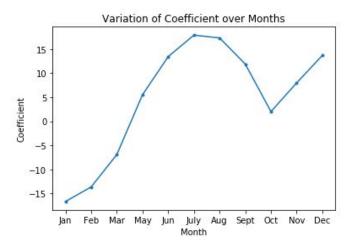


Figure 4: Plot of Regression Coefficients (Monthwise)

As for the states, regression coefficients were tabulated.

| term | estimate t | term | estimate | term | estimate |
|-------------|------------|----------------------|----------|----------------|----------|
| (Intercept) | -226.83 | Connecticut | -12.5631 | Nevada | -5.91858 |
| Avg_CO | 4.56914 | Delaware | -7.92631 | New Hampshire | -14.6006 |
| Avg_NO2 | -0.0471 | District Of Columbia | -13.7595 | New Jersey | -7.67752 |
| Avg_O3 | 36.0408 | Florida | 10.73616 | New Mexico | 1.351426 |
| Avg_SO2 | 0.00023 | Georgia | -3.34047 | New York | -10.1976 |
| Year | 0.14349 H | Hawaii | 11.7086 | North Carolina | -3.65689 |
| Jan | -16.659 I | ldaho | -16.2028 | North Dakota | -21.5627 |
| Feb | -13.627 I | Illinois | -7.43708 | Ohio | -12.0193 |
| Mar | -6.9051 I | Indiana | -7.60816 | Oklahoma | -2.9541 |
| May | 5.51411 I | lowa | -10.9539 | Oregon | -10.2493 |
| Jun | 13.4188 | Kansas | -6.42664 | Pennsylvania | -2.0768 |
| Jul | 17.8756 H | Kentucky | -6.38002 | Rhode Island | -8.37961 |
| Aug | 17.2962 l | Louisiana | 5.971581 | South Carolina | 0.103814 |
| Sep | 11.864 | Maine | -18.5837 | South Dakota | -14.5063 |
| Oct | 2.01426 | Maryland | -8.05173 | Tennesse | -8.21806 |
| Nov | -7.9724 | Massachusetts | -12.876 | Texas | 3.83385 |
| Dec | -13.669 | Michigan | -13.7403 | Utah | -9.72425 |
| Alaska | -34.074 | Minnesota | -17.014 | Vermont | -16.1446 |
| Arizona | 6.1712 | Mississippi | 2.795587 | Virginia | -11.0988 |
| Arkansas | -1.4125 | Missouri | -13.315 | Washington | -13.1707 |
| California | -2.8004 | Montana | -19.1562 | Wisconsin | -11.8774 |
| Colorado | -14.213 | Nebraska | -20.9554 | Wyoming | -21.4451 |

Table 1: Regression Coefficients for Temperature Model

The adjusted R^2 value for the model was 0.8149. The inclusion of states in the regression model helps improve the prediction and helps in obtaining a better R^2 value.

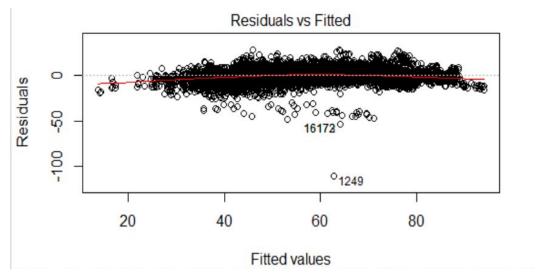


Figure 5: Simple Linear Model for Temperature

Relative Humidity Model (LM)

Being an environmental impact factor as temperature, RH was modeled in a similar manner, with the same number of variables. The equation used to model the RH was:

$$RH_i = \beta_0 + \beta_1(SO_2)_i + \beta_2(NO_2)_i + \beta_3(O_3)_i + \beta_4(CO)_i + \sum_i \beta_i(year)_i + \sum_i \beta_i(state)_i$$

The entire modeling for Relative Humidity was identical to that of Temperature. In this case, however, it was assumed that there is no correlation between temperature and Relative Humidity.

Tabulated results are as follows:

| term | estimate ten | m | estimate | term | estimate |
|-------------|----------------|-------------------|----------|----------------|----------|
| (Intercept) | -226.308 Cor | nnecticut | -14.7157 | Nevada | -23.7249 |
| Avg_CO | -1.74626 Del | laware | -6.35304 | New Hampshire | 4.476569 |
| Avg_NO2 | -0.20441 Dis | trict Of Columbia | 6.453698 | New Jersey | -0.96659 |
| Avg_O3 | -541.845 Flo | rida | 2.239833 | New Mexico | -15.0416 |
| Avg_SO2 | -0.00491 Geo | orgia | 7.295611 | New York | 10.25815 |
| Year | 0.15398 Hav | waii | -3.70599 | North Carolina | -3.01871 |
| Jan | -8.58173 Ida | ho | -5.06825 | North Dakota | 0.7829 |
| Feb | -6.05071 Illir | nois | 1.134144 | Ohio | -4.9674 |
| Mar | -2.05021 Ind | iana | -14.1086 | Oklahoma | 2.074709 |
| May | 4.09492 low | va . | 3.851344 | Oregon | 3.478888 |
| June | 5.08343 Kar | nsas | 1.546353 | Pennsylvania | 5.634234 |
| Jul | 8.54221 Ker | ntucky | 1.725784 | Rhode Island | 12.42894 |
| Aug | 7.47955 Lou | uisiana | 15.88261 | South Carolina | 1.282601 |
| Sep | 4.277 Ma | ine | 5.459046 | South Dakota | -0.74717 |
| Oct | 0.22345 Ma | ryland | 2.169051 | Tennesse | 9.312006 |
| Nov | -3.6903 Ma | ssachusetts | 2.392554 | Texas | -28.7471 |
| Dec | -0.05086 Mid | chigan | 1.088144 | Utah | -15.6283 |
| Alaska | -38.6861 Mir | nnesota | -15.3924 | Vermont | 2.704089 |
| Arizona | -18.7296 Mis | ssissippi | -5.84055 | Virginia | -7.10243 |
| Arkansas | -27.874 Mis | ssouri | -0.69322 | Washington | 7.256789 |
| California | -4.27962 Mo | ntana | -2.07241 | Wisconsin | -13.136 |
| Colorado | -15.1254 Nel | braska | -40.0889 | Wyoming | -1.61903 |

Table 2: Regression Coefficients for RH Model

In case of the Relative Humidity, it was observed that the coefficient for O_3 was much higher as compared to the other coefficients. Although, inherently, the value of ozone concentration is low (ppm or ppb) and thus, the coefficient is high. While considering the coefficients for months, there was an increasing trend from January to July, thereby again going to smaller values till December.

The adjusted R² value for the model was 0.5574. The fit was not satisfactory as compared to the temperature model, however, the trends were similar to that of the temperature fit.

The plot for the residuals indicate a more uniform distribution of the residuals.

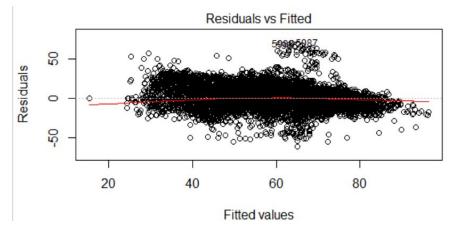


Figure 6: Simple Linear Model for RH

Level Log Transform

Level Log Transform Model was implemented to determine the fit and see its effect on the residuals.

The model implemented was:

$$log(T)_{i} = \beta_{0} + \beta_{1}(SO_{2})_{i} + \beta_{2}(NO_{2})_{i} + \beta_{3}(O_{3})_{i} + \beta_{4}(CO)_{i} + \sum \beta_{i}(year)_{i} + \sum \beta_{i}(state)_{i}$$

$$log(RH)_i = \beta_0 + \beta_1(SO_2)_i + \beta_2(NO_2)_i + \beta_3(O_3)_i + \beta_4(CO)_i + \sum_i \beta_i(year)_i + \sum_i \beta_i(state)_i$$

The model gave a lower R² value of 0.6916 for Temperature whereas an R² value of 0.506 was obtained for the RH Model. Also, the residual errors were higher in both the cases of Temperature and RH.

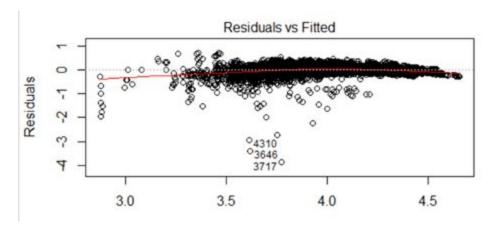


Figure 7: Residual Plot for Temperature Level Log Transform

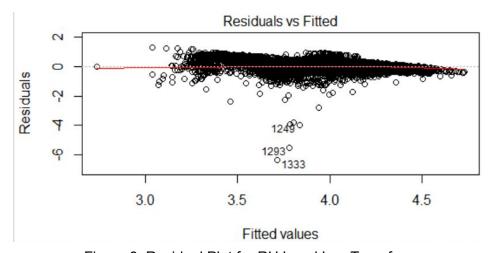


Figure 8: Residual Plot for RH Level Log Transform

The residual plot for Temperature and RH are identical in all sorts. Moreover, the residual values are scattered with an improper fit. The linear model, thus has a better fit as compared to the Level Log Model. An alternate option would be to model a Box-Cox model.

Log Log Model

All the continuous variables (Dependent and Independent Variables) were transformed logarithmically, while keeping the binary variables as same.

$$log(T)_{i} = \beta_{0} + \beta_{1}log(SO_{2})_{i} + \beta_{2}log(NO_{2})_{i} + \beta_{3}log(O_{3})_{i} + \beta_{4}log(CO)_{i} + \sum \beta_{i}(year)_{i} + \sum \beta_{i}(state)_{i}$$

$$log(RH)_{i} = \beta_{0} + \beta_{1}log(SO_{2})_{i} + \beta_{2}log(NO_{2})_{i} + \beta_{3}log(O_{3})_{i} + \beta_{4}log(CO)_{i} + \sum \beta_{i}(year)_{i} + \sum \beta_{i}(state)_{i}$$

The adjusted R² obtained for the temperature model was 0.6823, whereas that for the RH model was 0.4931. Residual plots obtained were:

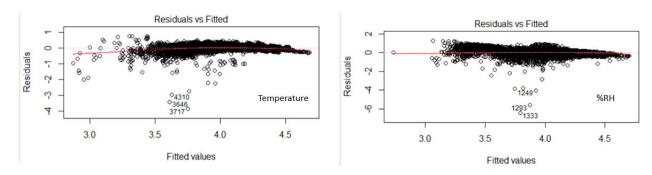


Figure 9: Log-Log Transform model results for the Dependant Variables

The distribution of residuals was uniform for the Log Log model as compared to the Simple

Model, in spite of having a lower R² fit. From all the models,a general regression model seemed optimum.

| Model | Temperature | %RH |
|-------------------------|-------------|--------|
| Linear Regression Model | 0.8149 | 0.5574 |
| Level Log Model | 0.6916 | 0.506 |
| Log Log Model | 0.6823 | 0.4921 |

Table 3: Adjusted R² values for the parameters

Sample Size Analysis

The number of samples collected is an important parameter influencing the value of the concentration obtained. For instance, if the ease of obtaining a sample is higher, then the number of samples are lesser. In order to assess the states with the maximum number of samples collected, a regression model was fitted for each of the four pollutants.

The regression model followed was:

$$N_i = \beta_0 + \sum \beta_i(state)_i$$

The states with the maximum number of samples collected were as follows:

| Sample coefficient | СО | NO ₂ | SO ₂ | O ₃ |
|--------------------|--------------|-----------------|-----------------|----------------|
| Maximum | Arizona | Wyoming | Indiana | Wyoming |
| 2nd Maximum | Newyork | North Dakota | North Dakota | Maine |
| 3rd Maximum | Wisconsin | Montana | Montana | Virginia |
| Median | Kentucky | New Mexico | Maine | Utah |
| 3rd Least | Rhode Island | Mississippi | Rhode Island | Alaska |
| 2nd Least | Minnesota | Delaware | Maryland | Hawaii |
| Least | Delaware | South Carolina | Nebraska | South Carolina |

Table 4: Sample Size Coefficients for Pollutants

The regression analysis can be found at:

https://drive.google.com/drive/u/0/folders/111DjKMK0DRxnhsi3S5dY5gntBFBsBW3K.

From the analysis of samples, it can be observed that there is no uniform pattern in location for each of the pollutants. The extent of ease and difficulty of collecting samples varies from pollutant to pollutant. For instance, it is comparatively tough to measure the O_3 concentration in Maine (3rd highest coefficient of regression), whereas it is moderately difficult to collect samples of SO_2 in Maine (Median coefficient of regression). This analysis can be applied in designing new experiments for measurements of pollutants in future. A measurement exercise set up to measure CO concentration in Arizona would take up more effort than setting it up in Delaware or Minnesota.

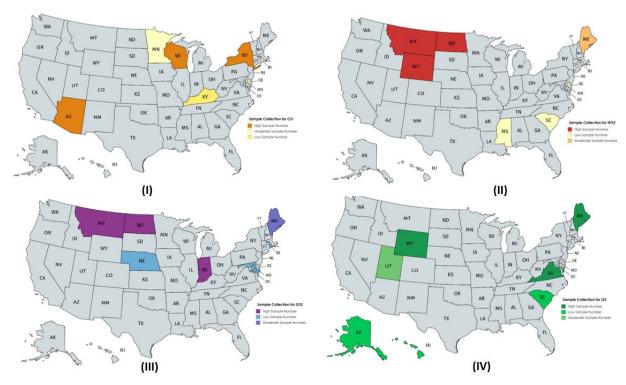


Figure 10: Spatial Distribution Graph for Sample Collections: I-CO, II-NO₂, III-SO₂, IV-O₃

From the spatial map of the sample size, it can be inferred that location plays a part in the number of samples being collected. In the case of NO₂, there seems to be a predilection for the northern states for higher number of samples. A similar observation can be made in case for SO₂. Similarly, lower number of samples are collected for ozone for the islandic states such as Alaska and Hawaii.

Thus, a spatial study of the number of samples collected are useful in determining the future collection strategy for a particular pollutant. For instance, more effective methods for NO_2 sample collection must be used for the northern states so as to reduce the number of samples collected and hence the cost involved.

Gauss Markov Assumptions

In order to implement a regression model, we need to be assured that the Gauss Markov Assumptions are satisfied. For the model implemented in the report, the Gauss Markov Assumptions are satisfied as follows:

1) Linearity in parameters

In all the three models implemented in the report, it has been modeled by satisfying this assumption. The general structure of any model implemented in the paper is as follows:

$$y = \sum \beta_i * x_i$$

Here, the independent variable x_i is not necessarily a linear value. For instance, in the log-log transformation model, the independent variable has been transformed into a logarithmic value of that variable. However, there is no effect on the nature of parameters in this case. The individual parameters are independent of each other. Each value of β_i is calculated through a standard linear regression model and none of these have interaction amongst each other. Thus, the first condition of Linearity is satisfied.

2) Random Sampling

The nature of the data is such that the condition of Random Sampling is inherently satisfied. All of the concentrations recorded have been noted at a particular time instant and at a particular location. The concentration of pollutants in the atmosphere are not manually modeled or structured. In case of temperature and Relative Humidity, the data collection is done in a manner similar to that of the pollutants. There is no fixed method in which the data is recorded. Thus, due to the nature of data under consideration, the second condition is satisfied.

3) Zero conditional mean of errors

The model developed here has a total of 5 independent continuous variables and a large number of independent categorical variables. For every model mentioned here, there are 2 omitted variables, one for the months and one for the States. However, even if certain variables are dropped from the regression coefficients does not imply that they have dropped from the model. Correspondingly, the omitted variables are included in the

intercept of the regression. The presence of an intercept ensures that there is indeed a zero condition mean of errors and thus, the third condition is satisfied.

$$E(u_i|x_{ik}) = 0$$
, for all regressors

4) No perfect collinearity

In the model developed, each of the categorical variable has been converted into a dummy variable. However, in order to avoid the dummy variable trap, a variable of each type has been dropped. For instance, in the case of months, the dummy variable for April has been dropped in the model. Similarly, for the categorical variable 'State', the state of Arizona has been dropped. This is done by the linear regressor automatically and the analysis of the regression coefficients confirms this observation.

Thus, all the four Gauss Markov Assumptions have been satisfied, concluding that our model is indeed robust.

Conclusion

The modeling of Temperature and Relative Humidity through several models has been instrumental in analysing the trend of Pollutants and Atmospheric Parameters over the years. From the analysis of the fitted data, it can be proclaimed that the Temperature and Relative Humidity is dependant, not just on the pollutant, but also the spatial and temporal conditions. For instance, even though the concentration might play a visible atmospheric role in influencing the natural parameters, other factors, inherently present in the state and time variables have a significant effect.

As for the trends of Pollutants over time are concerned, there are certain peaks in the graphs, which indicate two possibilities:

- 1) There were sudden changes in the atmospheric conditions, leading to rather detrimental effects.
- 2) As the data is averaged over months and state, there might be a case that the values recorded for a particular time period or a particular state were higher or lower, which leads to an unwanted spike in the curve.

In order to have a detailed look at the parameters, the values for each variable (independant or dependant) were split into state and time, in order to obtain a detailed output. From the analysis of the regression coefficients, it can be judged, as to which state has a larger effect on the data. Apart from correlating the atmospheric variables to independent variables, an additional study of the number of samples recorded was carried out, which gave out interesting results. Assuming that all samples are recorded by the same data collection technique, certain patterns in the ideal number of samples for a state can be understood. In the report, the spatial distribution for number of samples collected was mentioned. It can be concluded that the behavior of the optimal sample number was not constant, and varied from state to state. Certain spatial clusters could be observed upon deeper scrutiny (example of high NO₂ samples in the northern United States). Thus, although the number of samples collected are considered insignificant in the concentration of pollutants, it plays a major role in the spatial analysis of a region.

Through the mentioned project, trends in a particular pollutant over time was observed.

Moreover, with the filtering techniques employed in this study, it is possible to dig deeper into

the data and find trends for each pollutant for every state and the corresponding city. In totality, this project stresses upon correlating atmospheric characteristics to the physical particles. This study can be employed universally to any region in the world, provided it has ample access to valid and consistent data. Although the project is based on analysing the concentrations of a handful of pollutants, it can be further extended to other gaseous intensive studies such as fuel emissions, industrial emissions or natural phenomenon like forest fires. Moreover, additional environmental parameters like Salinity, Turbulence and Productivity can also be studied, with easy access to data.

```
title: "Appendix"
title: "Analysis and Modeling of US Pollution Data for '1980-2018'
and its implications on the atmosphere"
title: "R Notebook"
output: pdf_document
Importing Libraries
```{r}
setwd("C:\\Users\\yashg\\OneDrive\\Desktop\\CMU\\Fall 2019\\Data Science\\Project\\")
library(readxl)
library(ggplot2)
library(tidyverse)
library(lubridate)
data<-read_csv('combined.csv')
Plots of individual pollutants are plotted with time using individual files of the concentrations over
time.
```{r}
SO2<-read_csv('SO2.csv')
CO<-read_csv('CO.csv')
NO2<-read csv('NO2.csv')
O3<-read_csv('Ozone.csv')
T<-read_csv('T.csv')
RH<-read_csv('RH.csv')
Each file was further grouped over years and plotted. The plots are mentioned in the report.
````{r}
data_f<-data%>%
 group_by(State_Name)%>%
 group_by(City_Name)%>%
 group_by(Year)%>%
 mutate(avgS=mean(Avg_SO2),
 avgCO=mean(Avg CO),
 avgO3=mean(Avg_O3),
```

```
avgNO2=mean(Avg_NO2),
 avgT=mean(Avg T),
 avgRH=mean(Avg_RH)
)
#1 (Sample Plot)
`ggplot()+
 geom_line(mapping=aes(x=Year,y=avgRH),data=data_f,color='red')`+
 xlab("Years")+
 ylab("Relative Humidity")+
 ggtitle("Fluctuation of RH over years")+
 theme(plot.title = element text(hjust = 0.5))
Regression Models:
Linear Model (As the number of variables was high, the output was exported to a .csv file)
```{r}
linear_T<-lm(Avg_T~Avg_CO+Avg_NO2+Avg_O3+Avg_SO2+Year+Month+State_Name,data=
data)
summary(linear T)
plot(linear_T)
linear RH<-lm(Avg RH~Avg CO+Avg NO2+Avg O3+Avg SO2+Year+Month+State Name,da
ta=data)
summary(linear_RH)
plot(linear_RH)
The Log-level and Log-Log transforms were carried out as follows:
```{r}
levellog_T<-Im(log(Avg_T)~Avg_CO+Avg_NO2+Avg_O3+Avg_SO2+Year+Month+State_Name
,data=data)
summary(levellog_T)
write.csv(tidy(levellog_T) , "levloT.csv")
levellog_RH<-Im(log(Avg_RH)~Avg_CO+Avg_NO2+Avg_O3+Avg_SO2+Year+Month+State_N
ame,data=data)
summary(levellog_RH)
write.csv(tidy(levellog_RH) , "levellogrh.csv")
loglog T<-lm(log(Avg T+0.0001)~log(Avg CO+0.0001)+log(Avg NO2+0.0001)+log(Avg O3+0.
0001)+log(Avg_SO2+0.0001)+log(Year)+Month+State_Name,data=data)
```

```
summary(loglog_RH)

loglog_RH<-lm(log(Avg_RH+0.0001)~log(Avg_CO+0.0001)+log(Avg_NO2+0.0001)+log(Avg_O 3+0.0001)+log(Avg_SO2+0.0001)+log(Year)+Month+State_Name,data=data)
summary(loglog_RH)

...

In order to assess the spatial variance of number of samples:

...

{r}

s1<-lm(num_x~State_Name,data=data_f)

s2<-lm(num_y_1~State_Name,data=data_f)

s3<-lm(num_x_1~State_Name,data=data_f)

s4<-lm(num_x_2~State_Name,data=data_f)

write.csv(tidy(s4) , "pollutant4.csv")
```