

# Combinational Logic

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# Logic Circuits

- Combinational circuit
  - Logic gate circuit, whose output at a particular time instant is dependent on input combination at that particular time instant
- Sequential circuit
  - Logic gate circuit + Storage element
  - Output depends on the input combination and the state of the memory element

# Combinational Circuit

- Logic circuit that consists of interconnection of logic gates
- For  $m$  inputs, the possible combinations of binary inputs =  $2^m$
- For each possible input combination, there is one possible value at the output
- A combinational circuit can be described by truth table



Block diagram of combinational circuit

# Combinational Circuits

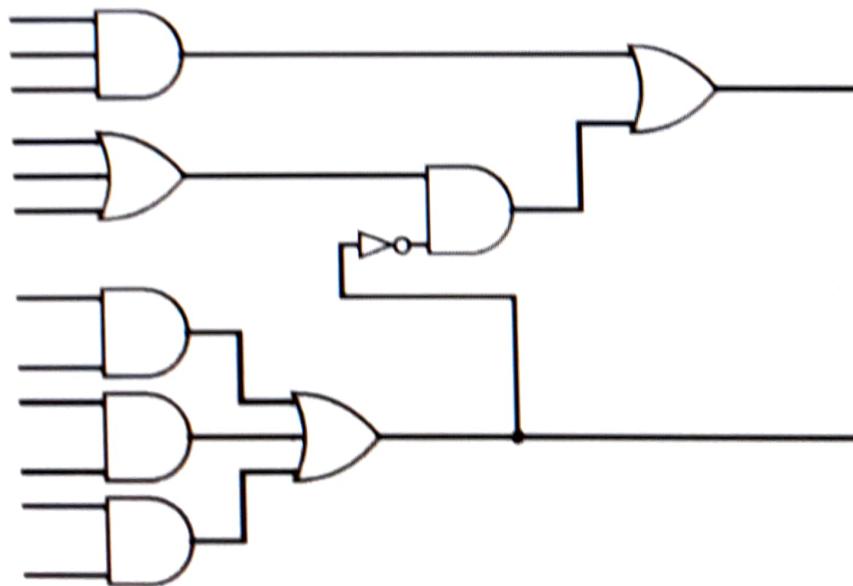
- Binary Adder, Subtractor
- Decimal Adder
- Binary multiplier
- Magnitude comparator
- Decoder
- Encoder
- Multiplexer

# Analysis of Combinational Circuit

- Determine the function the circuit implements
- Start with
  - Logic circuit
  - Boolean functions
  - Truth table
  - Explanation of the circuit operation
- Make sure the circuit is not sequential
- Make sure there is no feedback path or memory elements

# Procedure to obtain Boolean function from logic circuit

- Label all gate first stage outputs with unique names
- Proceed to the next stage, till you reach final output



# Combinational Circuit

$$P = ABC$$

$$Q = A + B + C$$

$$R = AB$$

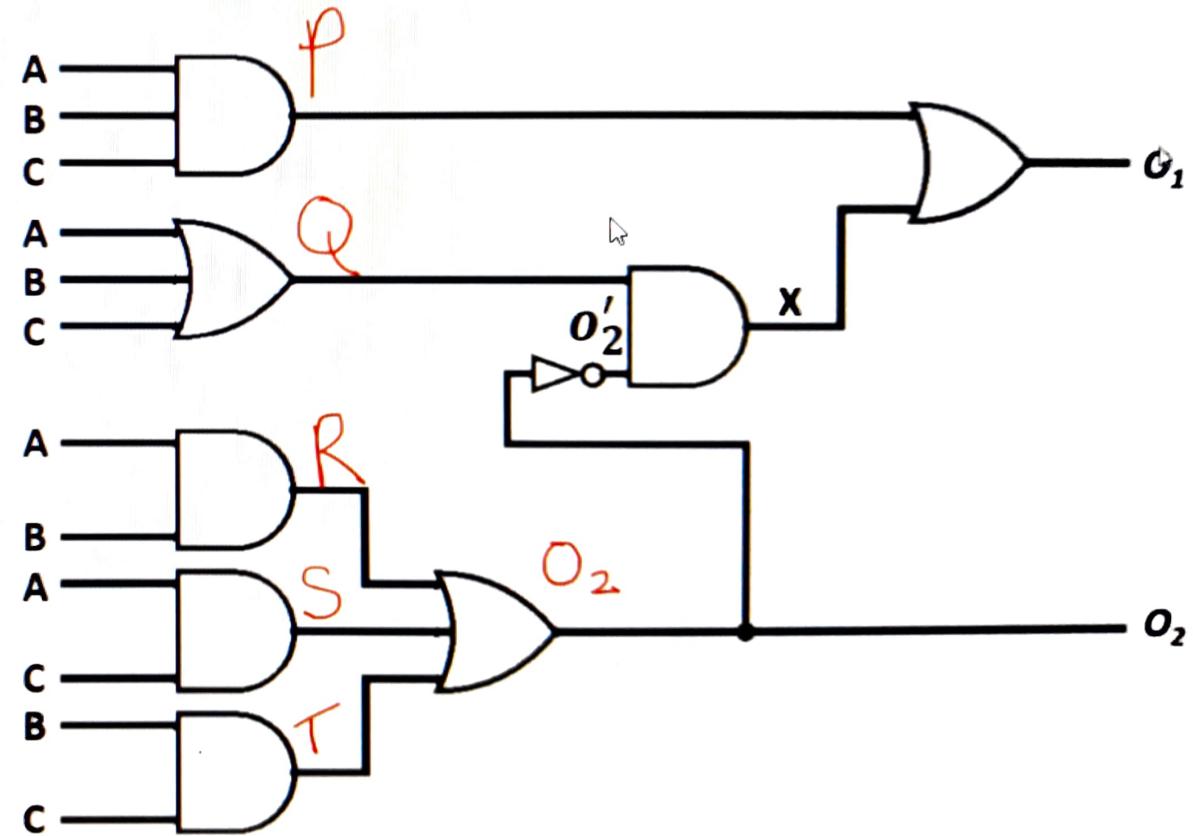
$$S = AC$$

$$T = BC$$

$$O_2 = R + S + T$$

$$O_2 = AB + AC + BC$$

$$O_1 = P + X = (ABC) + (QO_2)$$



# Code conversion example combinational logic circuit

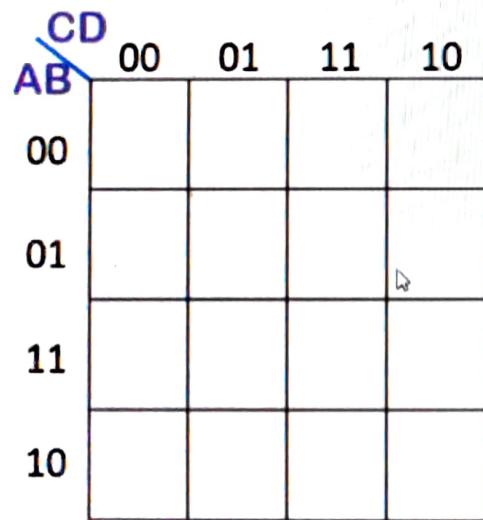
Decimal	Binary	Excess-3
0	0000	0011
1	0001	0100
2	0010	0101
3	0011	0110
4	0100	0111
5	0101	1000
6	0110	1001
7	0111	1010
8	1000	1011
9	1001	1100



Input BCD				Output Excess-3			
A	B	C	D	P	Q	R	S
0	0	0	0	0	0	1	1
0	0	0	1	0	1	0	0
0	0	1	0	0	1	0	1
0	0	1	1	0	1	1	0
0	1	0	0	0	1	1	1
0	1	0	1	1	0	0	0
0	1	1	0	1	0	0	1
0	1	1	1	0	1	0	0
1	0	0	0	1	0	1	1
1	0	0	1	1	1	0	0

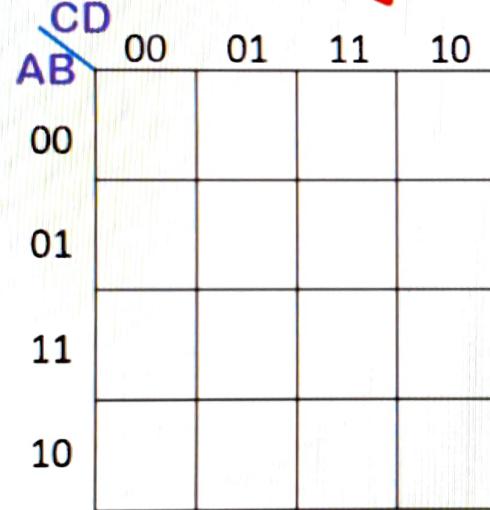
# K-maps for the output variables

P

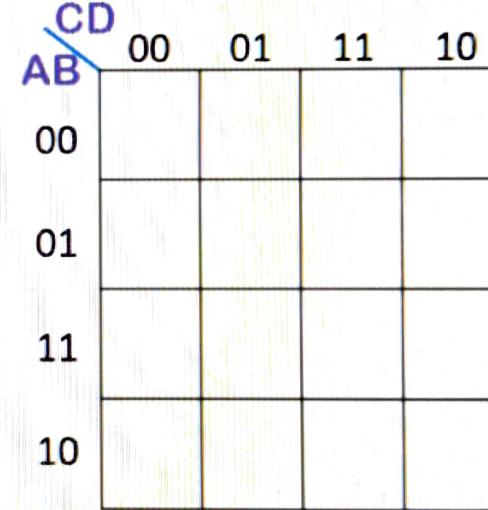


$m_0$	$m_1$	$m_3$	$m_2$
$m_4$	$m_5$	$m_7$	$m_6$
$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
$m_8$	$m_9$	$m_{11}$	$m_{10}$

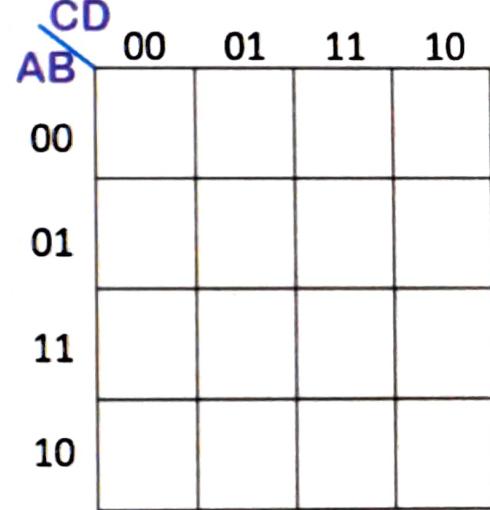
Q



R



S



# Don't care conditions

- The six bit combinations not listed beyond 1001 for input are don't-care combinations
- These values have no meaning in BCD and we assume that they will never occur in actual operation of the circuit
- Therefore we have the liberty to take either 0 or 1
- Don't care is represented by X
- Idea is to get simple circuit

Binary	Excess-3
0000	0011
0001	0100
0010	0101
0011	0110
0100	0111
0101	1000
0110	1001
0111	1010
1000	1011
1001	1100

# Four-variable K-map

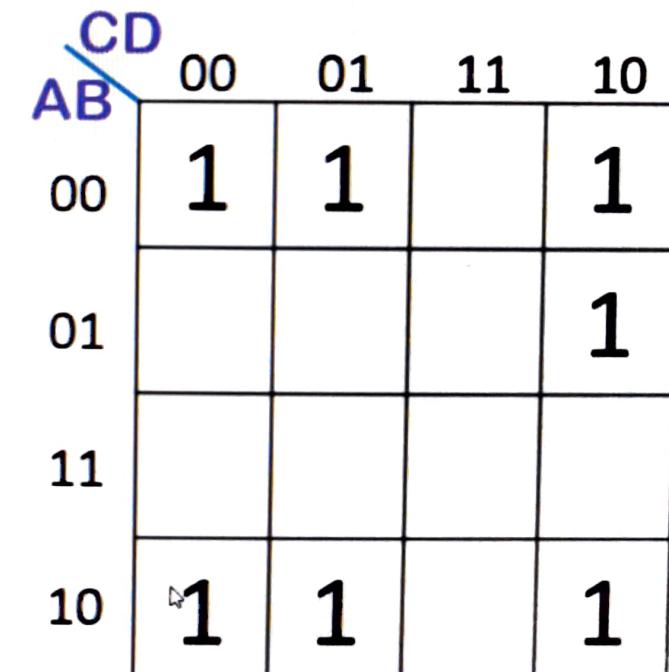
Simplify the Boolean function given in standard SOP form

$$F = A'B'C' + B'CD' + A'BCD' + AB'C'$$

Add missing variables

$$F = A'B'C'(D+D') + (A+A')B'CD' + A'BCD' + AB'C'(D+D')$$

$m_0$	$m_1$	$m_3$	$m_2$
$m_4$	$m_5$	$m_7$	$m_6$
$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
$m_8$	$m_9$	$m_{11}$	$m_{10}$



# K-maps for the output variables

P

	CD	00	01	11	10
AB	00				
	00	1	1	1	
	01	X	X	X	X
	11	X	X	X	X
	10	1	1	X	X

$m_0$	$m_1$	$m_3$	$m_2$
$m_4$	$m_5$	$m_7$	$m_6$
$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
$m_8$	$m_9$	$m_{11}$	$m_{10}$

Q

	CD	00	01	11	10
AB	00				
	00	1	1	1	
	01	1			
	11	X	X	X	X
	10	1	X	X	

R

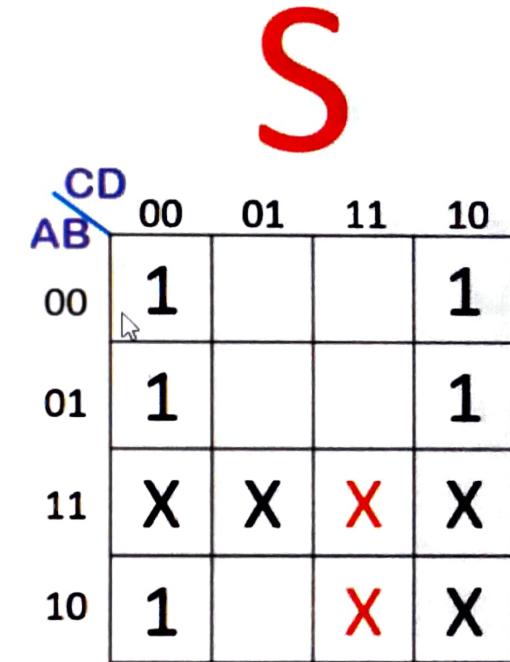
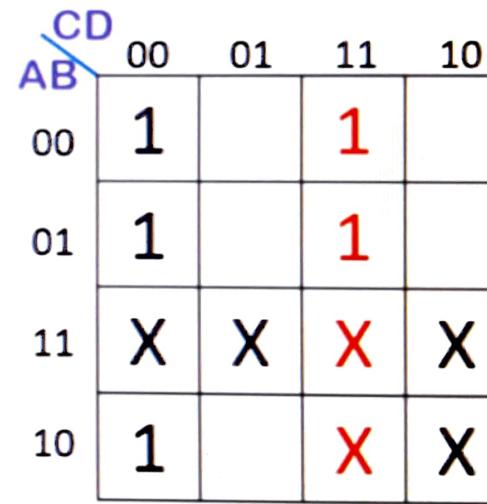
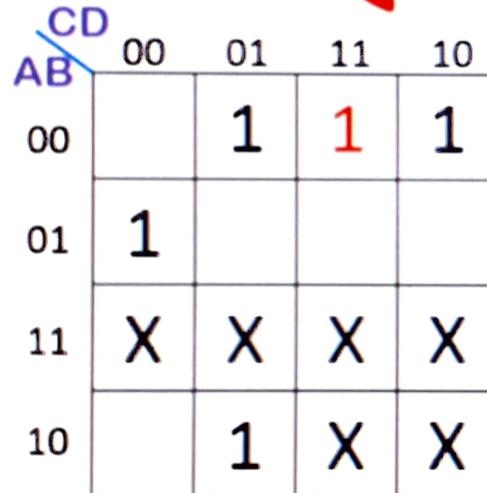
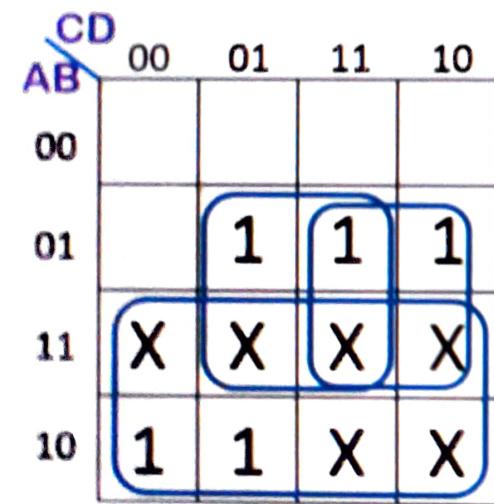
	CD	00	01	11	10
AB	00				
	00	1		1	
	01	1		1	
	11	X	X	X	X
	10	1		X	X

S

	CD	00	01	11	10
AB	00				
	00	1			1
	01	1			1
	11	X	X	X	X
	10	1		X	X

# K-maps for the output variables

$$P = \overline{A} + \overline{B}P + BC$$



# Full Adder

Input			Output	
A	B	C	Carry	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

# Two-bit multiplier

		$A_1 A_0$	$\times B_1 B_0$	
		$A_1 B_0$	$A_0 B_0$	Partial products
$A_1 B_1$	$A_0 B_1$			
$P_3$	$P_2$	$P_1$	$P_0$	

$$P_0 = A_0 B_0$$

$$P_1 = A_1 B_0 + A_0 B_1$$

$$P_2 = A_1 B_1$$

$$P_3 = \text{Carry out from } P_2$$

2 bit  $\times$  2bit  
multiplier

Product

$P_3 \ P_2 \ P_1 \ P_0$

$A_1$	$A_0$	$B_1$	$B_0$	$P_3$	$P_2$	$P_1$	$P_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	0	0	0	0	0
0	1	0	1	0	0	0	1
0	1	1	0	0	0	0	0
0	1	1	1	0	0	1	1
1	0	0	0	0	0	0	0
1	0	0	1	0	0	1	0
1	0	1	0	0	1	0	0
1	0	1	1	0	1	1	0
1	1	0	0	0	0	0	0
1	1	0	1	0	0	1	1
1	1	1	0	0	1	1	0
1	1	1	1	1	0	0	1

# Magnitude comparator

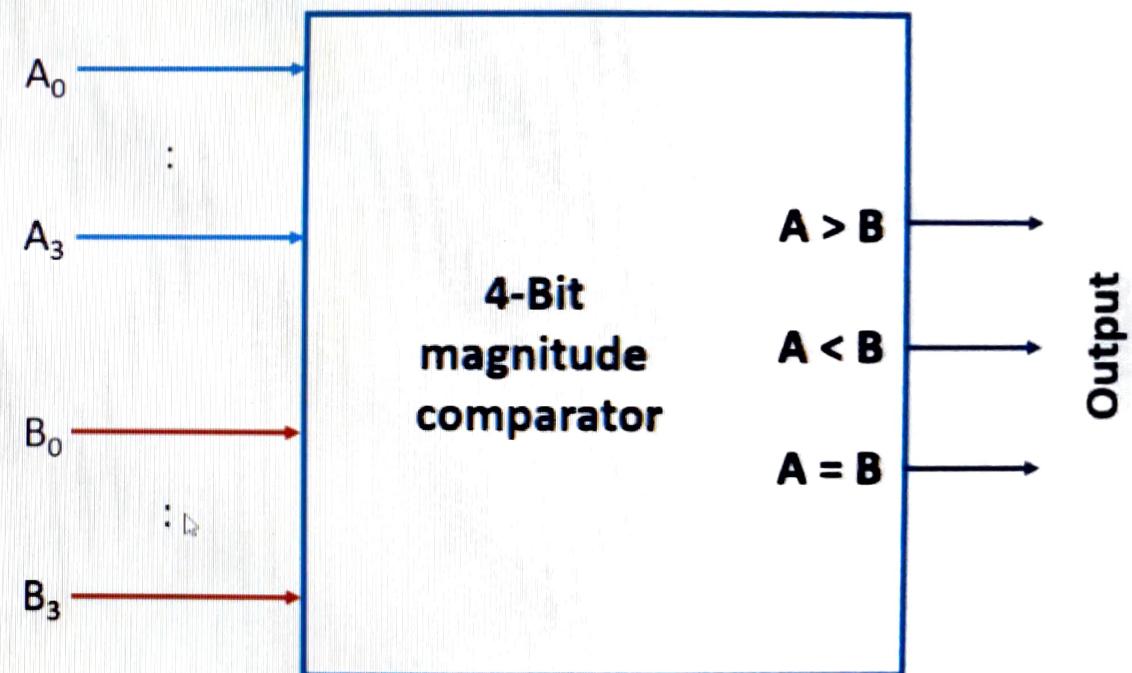
- Comparison of two numbers to determine whether a number is
  - $>$
  - $<$
  - $=$the other number
- A magnitude comparator is a combinational circuit that compares two numbers A and B and results in a output to indicate

$A > B$

$A < B$

$A = B$

# 4-Bit Magnitude comparator



# 4-Bit Magnitude comparator

A3 & B3	A2 & B2	A1 & B1	A0 & B0	A > B	A < B	A = B
A3 > B3				1		0
A3 < B3					1	0
A3 = B3	A2 > B2			1		0
A3 = B3	A2 < B2				1	0
A3 = B3	A2 = B2	A1 > B1		1		0
A3 = B3	A2 = B2	A1 < B1			1	0
A3 = B3	A2 = B2	A1 = B1	A0 > B0	1		0
A3 = B3	A2 = B2	A1 = B1	A0 < B0		1	0
A3 = B3	A2 = B2	A1 = B1	A0 = B0			1

## Decoder

- A combinational circuit that converts binary information from  $n$  input lines to a maximum of  $2^n$  unique output lines