

21/10/2021

Mid Sem
ADSA - Set - 3

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Q-1

$$(a) \quad T(n) = \begin{cases} T(n-5) + n^2 & \text{if } n > 5 \\ 1 & \text{if } n = 0 \end{cases}$$

$$T(n) = T(n-5) + n^2$$

$$T(n-5) = T(n-10) + (n-5)^2$$

$$T(n) = T(n-10) + (n-5)^2 + n^2$$

$$\therefore T(n) = T(n-15) + (n-10)^2 + (n-5)^2 + n^2$$

$$T(n) = n^2 + (n-5)^2 + (n-10)^2 + (n-15)^2 + \dots + 1$$

$$= an^2 + bn + c$$

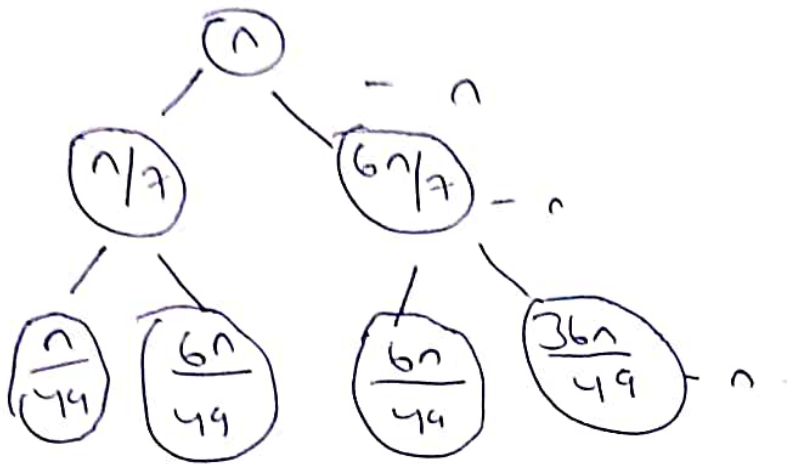
$$a = 1/5$$

$$= \frac{n^3}{5} + bn + c$$

Hence Time complexity $\equiv O(n^3)$

(b)

$$T(n) = T(n/7) + T(6n/7) + n$$



Let no of level $= n + 1$

$$\left(\frac{6}{7}\right)^n n = 1$$

$$\left(\frac{6}{7}\right)^n = 1/n$$

$$n \log \frac{6}{7} = \log 1/n$$

$$n = \log_{7/6} n$$

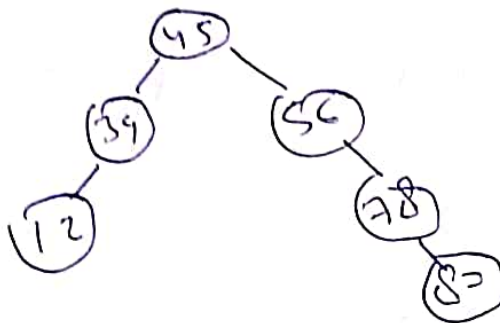
No. of nodes at last level $= 2^{\log_{7/6} n}$

$$\begin{aligned} \text{Total cost of last level} &= 2^{\log_{7/6} n} \times n \\ &= O(n^{\log_{7/6} 2}) \end{aligned}$$

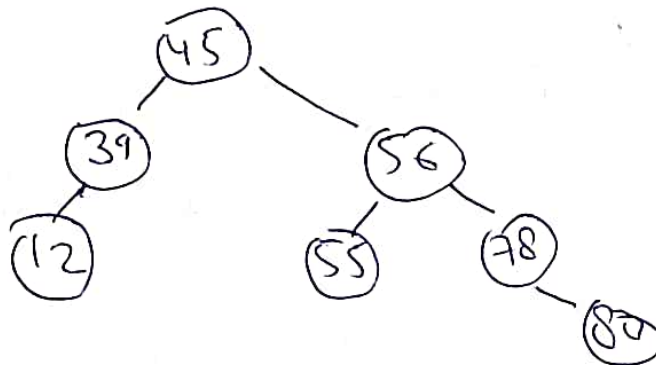
Total cost of all level

$$\begin{aligned} &= \cancel{n \log_{7/6} n} + \cancel{O(n \log_{7/6} 2)} \\ &= n \log_{7/6} n + O(n^{\log_{7/6} 2}) \\ &= O(n \log_{7/6} n) \end{aligned}$$

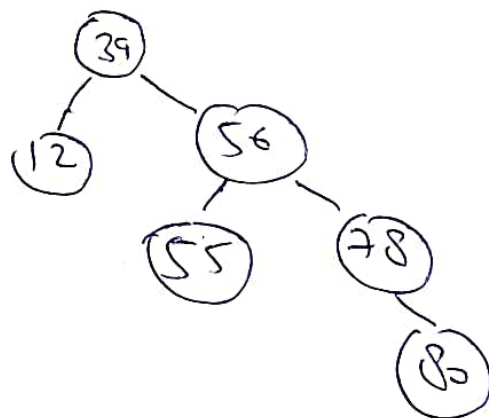
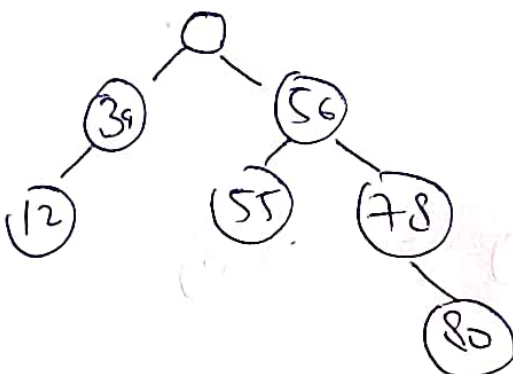
Q.2



Insert - 55

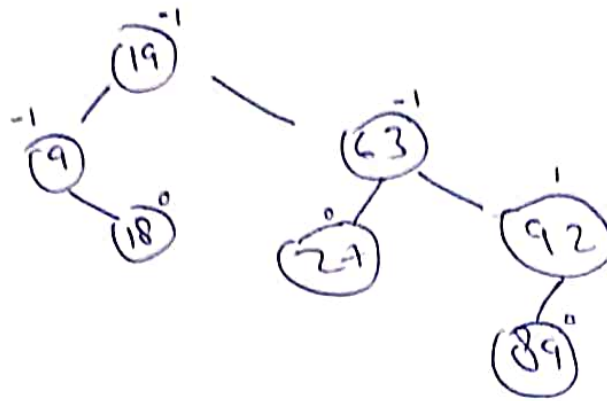


Delete - 45



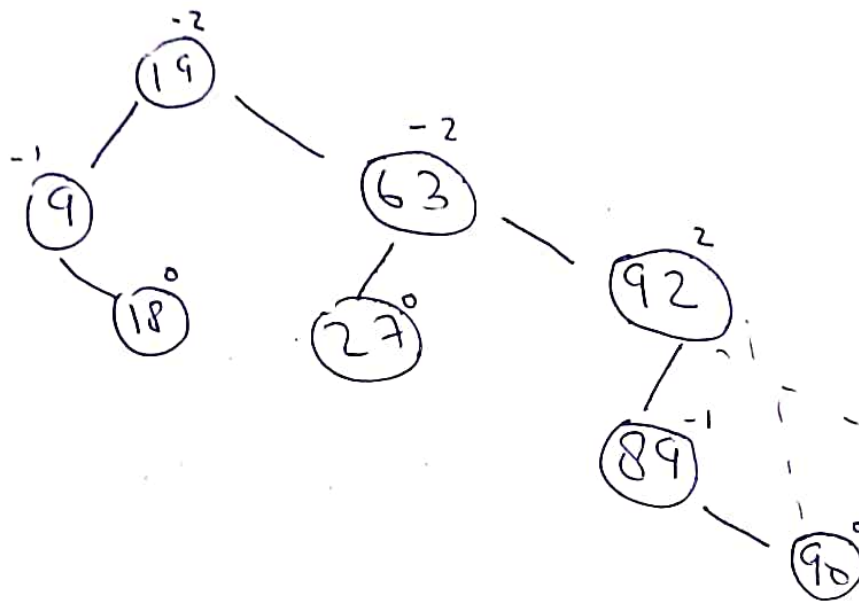
Q-3

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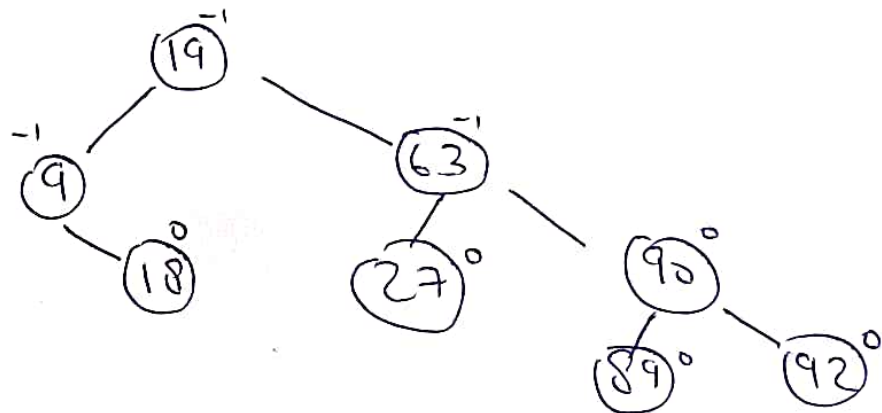
Insert (90)

(a)

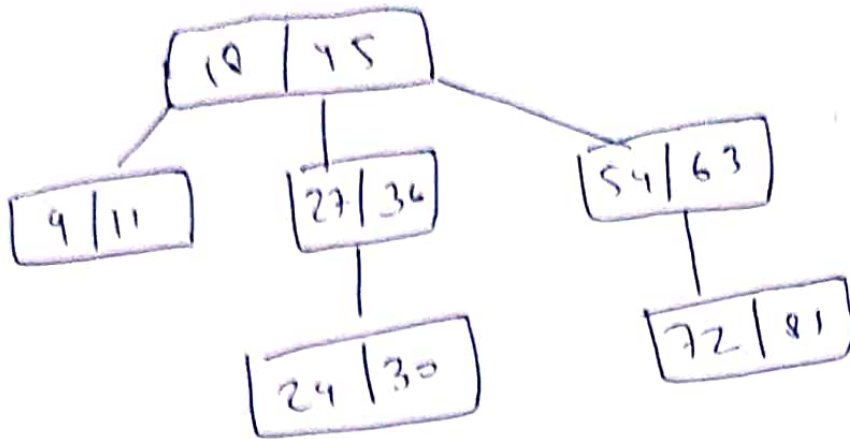


Rotation

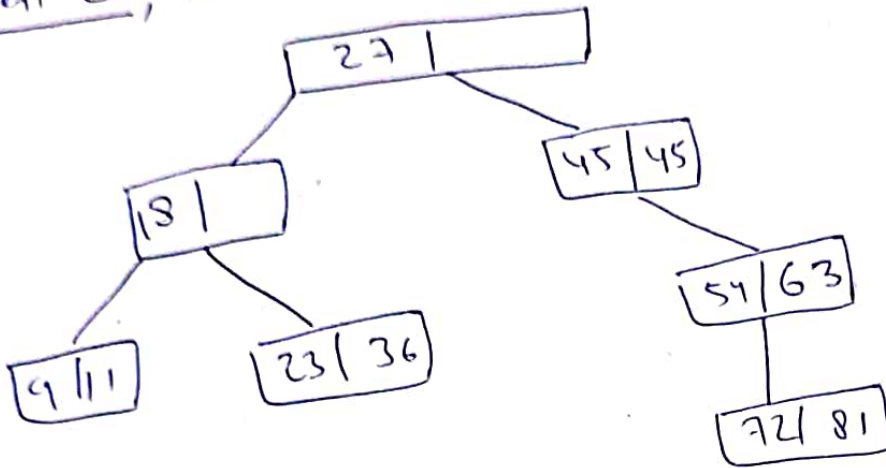
(b)



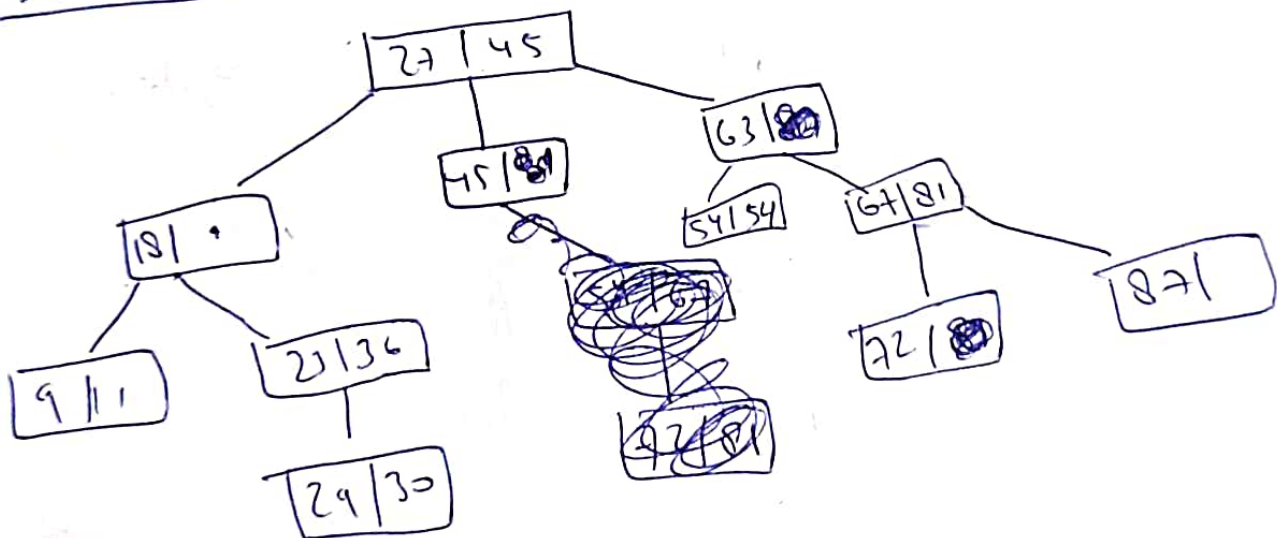
Q-4



Insert 23, 45



Insert 67, 87, 54



0-4

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Sep 2000 to 234

Insert 32

