



School Name:	UDAAN
Test Name:	Weekly Assessment Class XI Week 2
Total Questions:	45
Marks:	45
Duration:	90 minutes

Instructions for Assessment:

- The test is of **1 1/2 hours (90 minutes) duration.**
- The test consists of **45 questions.**
- There are three parts in the question paper **A, B, C consisting of Physics, Chemistry and Mathematics** having 15 questions in each part of equal weightage.
- There is only one correct response for each question. Filling up more than one response in any question will be treated as wrong response.
- No candidate is allowed to use any textual material, printed or written, pager, mobile, any electronic device, etc

Section: Physics

Questions: 15

Marks: 15

1.	<p>A physical quantity X is given by $X = \frac{2K^3l^2}{m\sqrt{n}}$. The % error in measurement in K, l, m, n is 1%, 2%, 3%, 4% respectively. The value of X is uncertain by</p> <p>a. 2% b. 14% c. 12% d. None of these</p>	1.0
2.	<p>The focal length of two spherical lens is given as $f_1 = (20 \pm 0.02)$ cm and $f_2 = (10 \pm 0.01)$ cm. If these two lens are placed in contact with each other, what will be the % error of a combined lens?</p> <p>a. 0.10% b. 0.20% c. 0.30% d. 0.40%</p>	1.0
3.	<p>The length and breadth of a rectangular plate are measured to be (15.30 ± 0.05) cm and (12.80 ± 0.05) cm, respectively. The area of the plate and the approximate uncertainty in the calculated area are (in cm^2)</p> <p>a. $195.8 \pm 0.7\%$ b. $196.0 \pm 0.7\%$ c. $196.0 \pm 0.07\%$ d. $195.84 \pm 1.4\%$</p>	1.0
4.	<p>If energy (E), velocity of light (c) and force (F) are chosen as fundamental units, which of the following could be the dimensions of time in this system?</p> <p>a. $E^{-1}C^1F^{-1}$ b. $E^1C^{-1}F^{-1}$ c. $E^{-1}C^{-1}F^1$ d. $E^1C^1F^{-1}$</p>	1.0
5.	<p>If $x = at + bt^2$, where x is the distance travelled by the body in kilometers and t is the time in seconds. Which of the following could be the unit of a?</p> <p>a. km/s b. kms c. km/s^2 d. kms^2</p>	1.0
6.	<p>The displacement of a particle is given by $y = A \sin^2(wx)$ where x is position. The unit of w is</p> <p>a. m^{-2}</p>	1.0

	b. m^{-1} c. hertz d. radian	
7.	<p>What is the relation between the dimensions of ohm and those of h (Plank's constant) & e (electric charge)?</p> <p>a. $\frac{h}{e}$</p> <p>b. $\frac{h^2}{e}$</p> <p>c. $\frac{h}{e^2}$</p> <p>d. $\frac{h^2}{e^2}$</p>	1.0
8.	<p>Dimension of $\frac{L}{RCV}$ are [where L, C, R & V are inductance, capacitance, resistance & voltage respectively]</p> <p>a. A^{-1}</p> <p>b. A^{-2}</p> <p>c. A</p> <p>d. A^2</p>	1.0
9.	<p>The magnetic energy stored in an inductor is given by $E = \frac{1}{2} L^a I^b$. Find the values of a and b.</p> <p>a. $a=1, b=0$</p> <p>b. $a=-2, b=4$</p> <p>c. $a=1, b=-2$</p> <p>d. $a=1, b=2$</p>	1.0
10.	<p>A new system of a unit is chosen such that the unit of mass is u kg, unit of length is v m, and unit of time is w s. The value of 1N in the new unit is?</p> <p>a. $u^{-1}v^{-1}w^2$ new unit</p> <p>b. uvw^{-2} new unit</p> <p>c. $u^{-1}v^{-2}w^2$ new unit</p> <p>d. uv^2w^{-2} new unit</p>	1.0
11.	<p>A voltmeter has a least count of 0.1V & an ammeter has a least count of 0.1A. The voltage drop V across a resistance is measured as 10.0V and current through it is measured as 1.0A. Which of the following alternative is incorrect?</p> <p>a. The value of R is $(1.0 \pm 0.1) \times 10^2 \Omega$</p> <p>b. The relative error in measurement of current is $\frac{1}{10}$</p>	1.0

	<p>c. The accuracy in measurement of potential drop is $\frac{1}{1000}$</p> <p>d. The value of R is $(10 \pm 0.2)\Omega$</p>	
12.	<p>A student performs an experiment to determine the Young's modulus of wire, exactly 2 m long, by Searle's method. In a particular reading, the student measures the extension in the length of the wire as 0.8 mm with an uncertainty of ± 0.05 mm at a load of exactly 1.0 kg. The student also measures the diameter of the wire to be 0.4 mm with an uncertainty of ± 0.01 mm. The Young's modulus obtained from the reading is</p> <p>(Take $g = 9.8 \text{ m/s}^2$)</p> <p>a. $(2.0 \pm 0.3) \times 10^{11} \text{ N/m}^2$</p> <p>b. $(2.0 \pm 0.2) \times 10^{11} \text{ N/m}^2$</p> <p>c. $(2.0 \pm 0.1) \times 10^{11} \text{ N/m}^2$</p> <p>d. $(2.0 \pm 0.05) \times 10^{11} \text{ N/m}^2$</p>	1.0
13.	<p>An athlete's coach told his team that muscle times speed equals power. What dimensions does he view to 'muscle'?</p> <p>a. $[ML^{-1}T^{-2}]$</p> <p>b. $[ML^2T^{-2}]$</p> <p>c. $[MLT^{-2}]$</p> <p>d. L</p>	1.0
14.	<p>Which of the following quantities has not been expressed in proper units?</p> <p>a. Co-efficient of elasticity (Nm^{-2})</p> <p>b. Surface tension (Nm^{-1})</p> <p>c. Energy (kgms^{-2})</p> <p>d. Pressure (Nm^{-2})</p>	1.0
15.	<p>The velocity of a particle 'v' is given in terms of time 't' as</p> $v = at + \frac{b}{t+c}$ <p>The dimensions of a, b & c , respectively are</p> <p>a. L^2, T, LT^{-2}</p> <p>b. LT^2, LT, L</p> <p>c. LT^{-2}, L, T</p> <p>d. L, LT, T^2</p>	1.0

Section: Chemistry

Questions: 15

Marks: 15

16.	<p>A sugar syrup of weight 214.2g contains 34.2g of sugar ($C_{12}H_{22}O_{11}$). What is the mole fraction of sugar in syrup?</p> <p>a. 9.9×10^{-2} b. 0.0091 c. 9.9×10^{-3} d. 1.99</p>	1.0
17.	<p>A gaseous mixture contains oxygen and nitrogen in the ratio of is 1:4 by weight. What is the ratio of their number of molecules?</p> <p>a. 1:4 b. 7:32 c. 1:8 d. 3:16</p>	1.0
18.	<p>What is the molarity of NaOH solution, prepared by dissolving its 4g in enough water to form 250mL of the solution?</p> <p>a. 0.04 M b. 0.4M c. 0.004M d. 0.40M</p>	1.0
19.	<p>If 1 mL of water has 20 drops and N_A is the Avogadro's constant, the number of water molecules in one drop of water is ($\rho_{water} = 1 \text{ g mL}^{-1}$)</p> <p>a. $0.5 N_A / 18$ b. $0.05 N_A$ c. $0.5 N_A$ d. $0.05 N_A / 18$</p>	1.0
20.	<p>How many molecules of H_2O are present (at STP) in a drop of H_2O which has radius of 2.3mm?</p> <p>a. 1.7058×10^{21} molecules b. 1.7058×10^{23} molecules c. 6.022×10^{23} molecules d. 0.05098 molecules</p>	1.0
21.	<p>The atomic mass of two elements A and B are 40 and 80 respectively. If x_g of A contain y atoms, how many atoms are present in $2x_g$ of B?</p>	1.0

	<p>a. $2y$</p> <p>b. $2x$</p> <p>c. y</p> <p>d. $y/2$</p>	
22.	<p>From 392mg of H_2SO_4, 1.24×10^{21} molecules are removed. How many moles of H_2SO_4 are left behind?</p> <p>a. 2×10^{-3}</p> <p>b. 1.2×10^{-3}</p> <p>c. 4×10^{-3}</p> <p>d. 1.5×10^{-3}</p>	1.0
23.	<p>Assertion: Both 106g of sodium carbonate and 12g of carbon have same number of carbon atoms.</p> <p>Reason: Both contain 1g atom of carbon which contains 6.023×10^{23} carbon atoms.</p> <p>a. Both assertion and reason are true and reason is the true explanation of assertion</p> <p>b. Assertion is true, reason is false</p> <p>c. Both assertion and reason are false</p> <p>d. Both assertion and reason are true but reason is not the true explanation of assertion</p>	1.0
24.	<p>The equivalent weight of MnSO_4 is half of its molecular weight when it converts to</p> <p>a. Mn_2O_3</p> <p>b. MnO_2</p> <p>c. MnO_4^-</p> <p>d. MnO_4^{2-}</p>	1.0
25.	<p>0.2 g of a metal combines with 46.6 mL of O_2 at 273 K and 1 atm pressure. The equivalent mass of the metal is</p> <p>a. 6</p> <p>b. 12</p> <p>c. 24</p> <p>d. 36</p>	1.0
26.	<p>50g of iron, 5g atoms of nitrogen , 0.1g atom of silver , 10^{23} atoms of carbon. Which of the following statements is correct?</p> <p>a. 5g atoms of nitrogen weigh most.</p> <p>b. 5g atoms of nitrogen weigh less than 50g of iron</p> <p>c. 10^{23} atoms of carbon weigh most</p> <p>d. 50g of iron weigh least</p>	1.0
27.	<p>A certain gaseous mixture contains methane and sulphur dioxide in the ratio of 1: 8 by mass. The ratio of number of their molecules in the mixture is:</p> <p>a. 1:8</p> <p>b. 1:2</p> <p>c. 1:1</p> <p>d. 2:1</p>	1.0
28.	<p>A drop of water is about 0.05 mL. The density of water at room temperature is about 1.0 g / mL, the number of water molecules present in a drop of water are</p> <p>a. 1.67×10^{21}</p>	1.0

	b. 3.01×10^{21} c. 6.023×10^{23} d. 3.01×10^{23}	
29.	<p>The density of water at 4°C is $1.0 \times 10^3 \text{ kgm}^{-3}$. The volume occupied by one molecule of water is approximately</p> a. $3.0 \times 10^{-23} \text{ ml}$ b. $6.0 \times 10^{-22} \text{ ml}$ c. $3.0 \times 10^{-21} \text{ ml}$ d. $9.0 \times 10^{-23} \text{ ml}$	1.0
30.	<p>By dissolving 1 mole each of following acids in 4L water, the acid which does not give a solution of 1N strength is</p> a. H_3PO_4 b. HClO_4 c. HNO_3 d. H_3PO_3	1.0

Section: Mathematics

Questions: 15

Marks: 15

31.	<p>The set of values of a for which the quadratic equation: $(a+2)x^2-2ax-a=0$ has two roots on the number line symmetrically placed about point 1 is:</p> <p>a. R b. $[-1, \infty)$ c. $(2, \infty)$ d. ϕ</p>	1.0
32.	<p>If α, β are roots of the equation $ax^2+bx+c=0$, then roots of $ax^2-bx(x-2)+c(x-2)^2=0$ are:</p> <p>a. $\frac{\alpha-1}{\alpha+1}, \frac{\beta-1}{\beta+1}$ b. $\alpha-2, \beta-2$ c. $\frac{2\alpha}{\alpha+1}, \frac{2\beta}{\beta+1}$ d. $-\frac{2\alpha}{\alpha+1}, -\frac{2\beta}{\beta+1}$</p>	1.0
33.	<p>If $\alpha^2 = 7\alpha - 5$ and $\beta^2 = 7\beta - 5$, then equation whose roots are $\frac{\alpha}{\beta}$ and $\frac{\beta}{\alpha}$ is:</p> <p>a. $7x^2-5x+7=0$ b. $39x^2-5x+39=0$ c. $5x^2+39x+5=0$ d. $5x^2-39x+5=0$</p>	1.0
34.	<p>The number of solutions of the equation $x^2-5 x +6=0$ is:</p> <p>a. 2 b. 1 c. 4 d. 0</p>	1.0
35.	<p>If the quadratic equations $ax^2+cx-b=0$ and $ax^2-3bx+\frac{c}{3}=0$ ($3b+c \neq 0$), have a common root, then $a+3c-ab$ is equal to:</p> <p>a. -1 b. 0 c. $1/2$</p>	1.0

	d. $9/2$	
36.	<p>If $\tan 27^\circ$ and $\tan 18^\circ$ are roots of $x^2+2ax+b=0$, then $2a-b$ is equal to:</p> <p>a. 0 b. 1 c. -1 d. $\frac{1}{\sqrt{5}}$</p>	1.0
37.	<p>If $y = \frac{x^2+3x+4}{x^2+3x+3}$, $x \in \mathbb{R}$, then y lies in the interval</p> <p>a. $\left(1, \frac{7}{3}\right]$ b. $\left(\frac{7}{3}, \infty\right)$ c. $\left(\frac{4}{3}, \infty\right)$ d. $(1, \infty)$</p>	1.0
38.	<p>Suppose α, β are roots of $8x^2-14x+3=0$, then sum of the series $\sum_{n=1}^{\infty} (\alpha^n + \beta^n)$ is:</p> <p>a. 7 b. $3/8$ c. 10 d. $10/3$</p>	1.0
39.	<p>If the roots of $x^2+bx+c=0$ are two consecutive odd numbers, then b^2-4c is equal to</p> <p>a. 1 b. -4 c. -1 d. 4</p>	1.0
40.	<p>Sum of the real roots of $(x+3)^4+(x+5)^4=16$ is:</p> <p>a. 0 b. -2 c. -4 d. -8</p>	1.0
41.	<p>If $(1-p)$ is a root of the quadratic equation $x^2+px+(1-p)=0$, then its roots are:</p> <p>a. 0,1 b. $-1 \pm \sqrt{2}$</p>	1.0

	<p>c. 0,-1</p> <p>d. $-1+\sqrt{2}$</p>	
42.	<p>If one root of $5x^2 + 13x + k = 0$ is reciprocal of the other, then</p> <p>a. $k = \frac{1}{5}$</p> <p>b. $k = 5$</p> <p>c. $k = 13$</p> <p>d. $k = -5$</p>	1.0
43.	<p>Ramesh and Mahesh solve an equation. In solving Ramesh commits a mistake in constant term and finds the roots 8 and 2. Mahesh commits a mistake in the coefficient of x and finds the roots - 9 and -1. The correct roots are</p> <p>a. -2, -8</p> <p>b. 9, 1</p> <p>c. 9, -1</p> <p>d. 2, -8</p>	1.0
44.	<p>If α and β are the roots of quadratic equation $4x^2 + 3x + 7 = 0$ then find the value of $\frac{1}{\alpha^3} + \frac{1}{\beta^3}$</p> <p>a. $\frac{-279}{343}$</p> <p>b. $\frac{279}{343}$</p> <p>c. $\frac{225}{343}$</p> <p>d. $\frac{-225}{343}$</p>	1.0
45.	<p>The equation $(b-c)x^2 + (c-a)x + (a-b) = 0$ has</p> <p>a. Equal roots</p> <p>b. Irrational roots</p> <p>c. Rational roots</p> <p>d. Only one root</p>	1.0

Key

Question Number	Correct Option	Question Number	Correct Option	Question Number	Correct Option
1.	C	16.	C	31.	D
2.	C	17.	B	32.	C
3.	A	18.	B	33.	D
4.	B	19.	D	34.	C
5.	A	20.	A	35.	B
6.	B	21.	C	36.	C
7.	C	22.	A	37.	A
8.	A	23.	A	38.	D
9.	D	24.	B	39.	D
10.	A	25.	B	40.	D
11.	A	26.	A	41.	C
12.	B	27.	B	42.	B
13.	C	28.	A	43.	B
14.	C	29.	A	44.	C
15.	C	30.	A	45.	C

Explanation

Question Number	Explanation
1.	$X = \frac{2K^3 l^2}{m\sqrt{n}}$ $\frac{\Delta x}{x} \times 100 = \frac{3\Delta K}{K} \times 100 + 2 \frac{\Delta l}{l} \times 100 + \frac{\Delta m}{m} \times 100 + \frac{1}{2} \times \frac{\Delta n}{n} \times 100$ $= 3 \times 1 + 2 \times 2 + 3 + \frac{1}{2} \times 4$ $3 + 4 + 3 + 2 = 12\%$
2.	<p>Since $\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$ or $f = \frac{f_1 f_2}{f_1 + f_2}$</p> <p>So</p> $\frac{\Delta f}{f} = \frac{\Delta f_1}{f_1} + \frac{\Delta f_2}{f_2} + \frac{\Delta f_1 + \Delta f_2}{f_1 + f_2}$ <p>So $\frac{\Delta f}{f} = \left(\frac{.02}{20} + \frac{.01}{10} + \frac{.02 + .01}{20 + 10} \right)$</p> $= (.001 + .001 + .001) = .003$ <p>% error in $f = .003 \times 100 = 0.3\%$</p>
3.	<p>To solve this problem, recall the following:</p> <p>In multiplication or division, the final result should retain as many significant figures as they are there in the original number with least significant figures.</p> <p>When two or more experimentally obtained numbers are multiplied, the percentage uncertainty of the final result is equal to the sum of the percentage uncertainties of the original numbers.</p> <p>Area of the plate = $15.30 \times 12.80 = 195.84$</p> <p>Since the data is given only up to 4 significant figures, the answer should be only in 4 significant figures. The acceptable value of the area is 195.8 cm^2.</p> <p>The percentage error in the given data is</p> $\frac{\Delta A}{A} = \left(\frac{\Delta L}{L} \times 100 + \frac{\Delta B}{B} \times 100 \right)$ $= \left[\left(\frac{0.05}{15.3} \times 100 \right) + \left(\frac{0.05}{12.8} \times 100 \right) \right] = 0.7\%$ <p>Here the given uncertainty has only one significant figure, the final percentage error has also one significant figure. The answer is $195.8 \pm 0.7\%$.</p> <p>Therefore the correct choice is (1).</p>
4.	<p>Dimensions of energy $[E] = M^2 L^2 T^{-2}$. Dimensions of $[c] = M^0 L^1 T^{-1}$ and dimensions of</p>

	<p>$[F] = M00^{-2}$. Therefore dimensions of $[T]$ in terms of these quantities chosen as fundamental units $= 0^1 C^{-1} 0^{-1}$. Therefore Correct choice is (2).</p>
5.	<p>Compare $x = at + bt^2$ with $s = ut + \frac{1}{2} at^2$ 'a' will have dimension as 'u' and hence unit of u or velocity i.e. km/s. ∴ Option (1) is correct</p>
6.	<p>In a trigonometric function such as $\sin \theta$, or $\sin^2 \theta$, theta is an angle defined as arc divided by radius making it a dimension less quantity, so wx must be dimensionless. So, if x has a dimension of position or length (say metre) , w must have the unit of $\frac{1}{m}$ or m^{-1}.</p>
7.	<p>The dimensions of Planck's constant (h) = $[ML^2T^{-1}]$ And that of charge e is $[AT]$ And Dimensions of resistance in terms of MLT & A works out to be $[R] = [ML^2T^{-3}A^{-2}]$ ∴ Putting dimensions of h & e in option (a), (b) (c) & (d) ∴ We get $\frac{h}{e^2} = \frac{[ML^2T^{-1}]}{[AT]^2} = [ML^2T^{-3}A^{-2}] = \text{same as resistance}$ So option (3) is correct</p>
8.	<p>Electric voltage = $\frac{\text{work}}{\text{charge}} = [ML^2T^{-3}A^{-1}]$ Resistance = $\frac{\text{voltage}}{\text{current}} = [ML^2T^{-3}A^{-2}]$ Capacitance = $\frac{\text{charge}}{\text{voltage}} = [M^{-1}L^{-2}T^4A^2]$ & Inductance = $\frac{\text{voltage}}{\text{current / time}} = [ML^2T^{-2}A^{-2}]$ So dimension of $\frac{L}{RCV}$ works out to be A^{-1}.</p>

9.	<p>By Principle of homogeneity:</p> $[E] = \left[\frac{1}{2} L^a T^b \right]$ <p>OR $[ML^2T^{-2}] = \left[(ML^2T^{-2}A^{-2})^a A^b \right]$</p> $[ML^2T^{-2}] = [M^a L^{-2a} T^{-2a} A^{-2a+b}]$ <p>Comparing powers of M, L, A and T</p> $a = 1$ $-2a + b = 0 \Rightarrow b = 2$ <p>Therefore, $a = 1, b = 2$</p>
10.	<p>$1N = 1 \text{ kg ms}^{-2}$</p> <p>New unit $1 u \text{ kg } v \text{ m (w s)}^{-1}$</p> $1 \text{ } \underline{uvw}^{-2} \text{ kg ms}^{-2} = \underline{uvw}^{-2} N$ $1N = \frac{1}{\underline{uvw}^{-2}} \times (\text{new unit})$ $1N = u^{-1} v^{-1} w^2 \times \text{new unit}$
11.	<p>The value of $R = \frac{V}{I} = \frac{10}{1} = 10\Omega$</p> $\frac{\Delta R}{R} = \frac{\Delta V}{V} + \frac{\Delta I}{I} = \frac{0.1}{10} + \frac{0.1}{1.0} = 0.01 + 0.1 = 0.11 = 0.1$ <p>$\therefore \Delta R = 0.1 \times 10 = 1\Omega$</p> <p>So value of $R = (10 \pm 1) \Omega$ or $(1.0 \pm 0.1) \times 10 \Omega$ Hence, option 1 A is correct choice.</p>
12.	<p>Use the formula for the Young's modulus of the wire.</p> $Y = \frac{FL}{A\ell} = \frac{4MgL}{\pi d^2 l}$ <p>Where $M = 1.0\text{kg}$, $g = 9.8 \text{ ms}^{-2}$, $L = 2\text{m}$, $I = 0.8\text{mm} = 0.8 \times 10^{-3}$</p> <p>$\Delta I = \pm 0.05\text{mm}$, $d = 0.4\text{mm} = 0.4 \times 10^{-3}$, $\Delta d = 0.01\text{mm}$</p> <p>First find the value of Y substituting the values of M, g, L, d and l in the above equation, which is obtained as $Y = 2.0 \times 10^{11} \text{ Nm}^{-2}$. Then write is above equation expressing the uncertainty in Y as $\frac{\Delta Y}{Y} = \frac{\Delta M}{M} + \frac{\Delta g}{g} + \frac{\Delta L}{L} + \frac{2\Delta d}{d} + \frac{\Delta l}{l}$. The value of M, g, L are exact. Therefore $\Delta M = 0$, $\Delta g = 0$ and $\Delta L = 0$. Thus, we have $\frac{\Delta Y}{Y} = \frac{2\Delta d}{d} + \frac{\Delta l}{l} = \frac{2 \times 0.01}{0.4} + \frac{0.05}{0.8} = 0.05 + 0.0625$.</p> <p>Therefore, $\Delta Y = 0.1125 \times Y = 0.0225 \times 10^{11} \text{ Nm}^{-2}$. Since the value of Y is correct only up to the first decimal place, the value of ΔY must be rounded off to the place. The correct result is $Y + \Delta Y$</p>

	$= (2.0 \pm 0.2) \times 10^{11} \text{ Nm}^{-2}$. The correct choice is therefore (B).
13.	$\text{Power} = \frac{\text{Work done}}{\text{Time}} = \frac{\text{Force} \times \text{displacement}}{\text{Time}} = \text{Force} \times \text{velocity}$ <p>= muscle times speed</p> <p>Muscle represents force = $[\text{MLT}^{-2}]$</p>
14.	<p>The unit of energy $\text{kgm}^2\text{s}^{-2}$</p> <p>Energy = $\vec{F} \cdot \vec{S}$</p> <p>= (m.a)\vec{S}</p> <p>Kg (ms^{-2}).m</p> <p>$\text{Kgm}^2\text{s}^{-2}$</p>
15.	<p>Since c is added to t in RHS, so dimensions of c= dimension of t = [T]</p> <p>As $\frac{b}{t}$ is equal to v so dimension of $Vt = [LT^{-1}] \times T = L$</p> <p>And at = v so dimension of $a = \frac{v}{t} = \frac{LT^{-1}}{T} = [LT^{-2}]$</p> <p>So dimension of a, b, c works out to be $[LT^{-2}]$, L & T</p> <p>So option C is correct</p>
16.	<p>Moles of sugar = $\frac{34.2}{342} = 0.1$</p> <p>Moles of water in syrup = $214.2 - 34.2 = 180\text{g}$</p> <p>Moles ($\text{H}_2\text{O}$) = $\frac{180}{18} = 10$</p> <p>$X_{\text{sugar}} = \frac{n_{\text{sugar}}}{n_{\text{sugar}} + n_{\text{H}_2\text{O}}} = \frac{0.1}{0.1 + 10} = 9.9 \times 10^{-3}$</p>
17.	<p>$\frac{\text{Weight of a compound}(w)}{\text{Molar mass}(M)} = \text{Moles}(n) = \frac{\text{Number of molecules}(N)}{\text{Avogadro number}(N_a)}$</p> <p>$\Rightarrow \frac{W(\text{O}_2)}{32} = \frac{N(\text{O}_2)}{N_A} \quad (1)$</p> <p>$\Rightarrow \frac{W(\text{N}_2)}{28} = \frac{N(\text{N}_2)}{N_A} \quad (2)$</p> <p>(1) \div (2)</p>

	$\frac{N(O_2)}{N(N_2)} = \frac{1}{4} \times \frac{28}{32} = \frac{7}{32}$
18.	$M = \frac{\text{Mass of NaOH} / \text{Molar mass of NaOH}}{0.250L}$ $= \frac{4g / 40g}{.250L} = \frac{0.1mol}{.250}$ $= 0.4mol L^{-1}$ <p>0.4M</p>
19.	<p>Volume of 1 drop of water = $\frac{mass}{density}$</p> <p>Density = $1 \frac{g}{ml}$</p> <p>Volume of 1 drop = $\frac{1}{20} ml$</p> <p>Mass of 1 drop of water = volume of one drop of water x density of water = $0.05mL \times 1g mL^{-1} = 0.05g$</p> <p>Moles of water in 1 drop = Number of molecules of water = $0.05 \frac{N_A}{18}$</p>
20.	<p>radius = 2.3mm or 0.23 cm</p> <p>volume of droplet of water = $\frac{4}{3} \pi r^3$</p> $= \frac{4}{3} \times \frac{22}{7} \times 0.23 \times 0.23 \times 0.23$ $= 0.05098 cm^3$ <p>Now, Assume density of water to be</p> <p>$1 gm / cm^3$ so</p> $= .d = \frac{m}{u} \text{ or } m = d \times u$ $= 1 \times 0.05098$ $= 0.05098 gm$ <p>Now,</p> <p>18 gm water contains = 6.022×10^{23} molecules</p> <p>$\therefore 0.05098 gm \text{ water} = 0.17058 \times 10^{23} \text{ molecules}$</p> $= 1.7058 \times 10^{21} \text{ molecules}$

21.	<p>No. of Moles of A = $\frac{x}{40}$</p> <p>No. of atoms of A = $\frac{x}{40} \times N_A$ (Avogadro no.) = y</p> <p>$x = \frac{40y}{N_A}$</p> <p>No. of Moles of B = $\frac{2x}{80}$</p> <p>No. of atoms of B = $\frac{2x}{80} \times N_A$</p> <p>$= \frac{2}{80} \times \frac{40y}{N_A} \times N_A$</p> <p>= y</p>
22.	<p>No. of Moles of $H_2SO_4 = \frac{0.392}{98} = 0.004$</p> <p>No. of Moles of H_2SO_4 removed = $\frac{1.24 \times 10^{21}}{6.02 \times 10^{23}}$</p> <p>= 0.002</p> <p>No. of Moles of H_2SO_4 left = $0.004 - 0.002$</p> <p>= 0.002</p> <p>= 2×10^{-3}</p>
23.	
24.	<p>n factor</p> <p>$MnSO_4 \rightarrow \frac{1}{2}Mn_2O_3$ 1</p> <p>$MnSO_4 \rightarrow MnO_2$ 2</p> <p>$MnSO_4 \rightarrow MnO_4^-$ 5</p> <p>$MnSO_4 \rightarrow MnO_4^{2-}$ 4</p>
25.	Equivalent mass of oxygen = 8 g

	<p>At 1 atm and 273 K, 22400 mL of $O_2(g) = 1 \text{ mol} = 2 \times 16 = 32 \text{ g}$</p> <p>$= \frac{32}{8} = 4 \text{ equivalents}$</p> <p>At 1 atm and 273 K, 46.6 mL of $O_2(g) = \frac{4}{22400} \times 46.60 = .00832 \text{ equivalents}$</p> <p>1 equivalent of O_2 reacts with 1 equivalent of metal</p> <p>\therefore 0.00832 equivalents of O_2 react with 0.00832 equivalents of metal.</p> <p>Thus, mass of 0.00832 equivalents of metal = 0.1 g</p> <p>\therefore Mass of 1 equivalent = Equivalent mass, E, of metal = $\frac{0.1}{0.00832} = 12.0 \text{ g eqvt}^{-1}$.</p>
26.	5g atoms of nitrogen = 70g
27.	<p>Molar mass of methane (CH_4) = $(12 + 4 \times 1) = 16 \text{ g mol}^{-1}$.</p> <p>Molar mass of sulphur dioxide (SO_2) = $(32 + 2 \times 16) = 64 \text{ g mol}^{-1}$</p> <p>Ratio of CH_4 and SO_2 in the mixture = 1:8 (w/w)</p> <p>Moles of CH_4 in the mixture = $\frac{1}{16} \text{ mol}$</p> <p>Mol of SO_2 in the mixture = $\frac{8}{64} = \frac{1}{8} \text{ mol}$</p> <p>Molar ratio of CH_4 and SO_2 in the mixture = $\frac{1}{16} : \frac{1}{8} = 1:2$</p>
28.	<p>Mass of $H_2O = 18 \text{ g}$.</p> <p>No. of moles in $H_2O = \frac{\text{given mass}}{\text{molar mass}} \text{ --- (1)}$</p> <p>$d = \frac{m}{v}$</p> <p>Given mass = density \times volume</p> <p>$= 0.05 \text{ ml} \times 1$</p> <p>$= 0.05 \text{ g}$</p> <p>Put this in equation (1)</p> <p>$\frac{0.05}{18} \times 6.022 \times 10^{23}$</p> <p>No. of water molecules = 1.67×10^{21}</p>
29.	Volume = $\frac{\text{mass}}{\text{density}}$

	<p>Mass of one molecule of water = $\frac{18}{6.02 \times 10^{23}}$</p> <p>Density = $1.0 \times 10^3 \text{ kgm}^{-3}$</p> <p>$= 1.0 \times 10^3 \times 1000 \times 10^{-6} \text{ gcm}^{-3}$</p> <p>So $V = \frac{18}{6.02 \times 10^{23} \times 1.0} = 3.0 \times 10^{-23} \text{ ml}$</p>
30.	H_3PO_4 is tribasic acid
31.	<p>As the roots are symmetrically placed about point, we take roots to be $1-\alpha, 1+\alpha$</p> <p>Now, $(1-\alpha) + (1+\alpha) = \frac{2a}{a+2}$</p> <p>$\Rightarrow a+2 = a \Rightarrow 0 = 2$</p> <p>Not possible.</p> <p>Thus, set of values of a is ϕ.</p>
32.	<p>We can write</p> <p>$ax^2 - bx(x-2) + c(x-2)^2 = 0 \quad (1)$</p> $a\left(\frac{-x}{x-2}\right)^2 + b\left(\frac{-x}{x-2}\right) + c = 0$ <p>as,</p> <p>$\therefore -\frac{x}{x-2} = \alpha, \beta$</p> <p>$\Rightarrow x = \frac{2\alpha}{\alpha+1}, \frac{2\beta}{\beta+1}$</p> <p>Thus, roots of (1) are</p> <p>$\frac{2\alpha}{\alpha+1}, \frac{2\beta}{\beta+1}$</p>
33.	<p>α, β are roots of</p> <p>$x^2 - 7x + 5 = 0$</p> <p>$\therefore \alpha + \beta = 7, \alpha\beta = 5$</p> <p>Now, $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{(\alpha+\beta)^2 - 2\alpha\beta}{\alpha\beta}$</p> <p>$= \frac{49 - 2(5)}{5} = \frac{39}{5}$</p>

	<p>and $\left(\frac{\alpha}{\beta}\right)\left(\frac{\beta}{\alpha}\right) = 1$</p> <p>Thus, required equation is</p> $x^2 - \frac{39}{5}x + 1 = 0$ <p>or $5x^2 - 39x + 5 = 0$</p>
34.	$x^2 - 5 x + 6 = 0$ $\Rightarrow x ^2 - 5 x + 6 = 0$ $\Rightarrow (x - 3)(x - 2) = 0$ $\Rightarrow x = 3 \text{ or } x = 2$ $\Rightarrow x = \pm 3 \text{ or } x = \pm 2$
35.	<p>If α is a common root, then</p> $a\alpha^2 + c\alpha - b = 0 \quad (1)$ <p>and $a\alpha^2 - 3b\alpha + \frac{c}{3} = 0 \quad (2)$</p> <p>Subtracting (2) from (1), we get</p> $(c + 3b)\alpha - b - \frac{c}{3} = 0$ $\Rightarrow \alpha = \frac{1}{3} \because 3b + c \neq 0$ <p>Putting in (1), we get</p> $a\left(\frac{1}{9}\right) + c\left(\frac{1}{3}\right) - b = 0$ $\Rightarrow a + 3c - 9b = 0$
36.	$\tan 27^\circ + \tan 18^\circ = -2a$ $\tan 27^\circ \tan 18^\circ = b$ <p>Now,</p> $1 = \tan 45^\circ = \tan (27^\circ + 18^\circ)$ $= \frac{\tan(27^\circ) + \tan(18^\circ)}{1 - \tan 27^\circ \tan 18^\circ}$ $= \frac{-2a}{1 - b}$ $\Rightarrow 1 - b = -2a$

	$\Rightarrow 2a-b = -1$
37.	$y = 1 + \frac{1}{x^2 + 3x + 3} = 1 + \frac{1}{\left(x + \frac{3}{2}\right)^2 + \frac{3}{4}}$ $\Rightarrow y > 1$ <p>Also, $\frac{1}{y-1} = \left(x + \frac{3}{2}\right)^2 + \frac{3}{4} \geq \frac{3}{4}$</p> $\Rightarrow y-1 \leq \frac{4}{3} \Rightarrow y \leq \frac{7}{3}$ <p>Thus, $1 < y \leq \frac{7}{3}$</p> <p>[Maximum value $\frac{7}{3}$ is attained when $x = -\frac{3}{2}$]</p>
38.	$8x^2 - 14x + 3 = 0$ $\Rightarrow 8x^2 - 12x - 2x + 3 = 0$ $\Rightarrow 4x(2x-3) - (2x-3) = 0$ $\Rightarrow (4x-1)(2x-3) = 0$ $\Rightarrow x = \frac{1}{4}, \frac{3}{4}$ <p>Now, $\sum_{n=1}^{\infty} (\alpha^n + \beta^n) = \frac{\alpha}{1-\alpha} + \frac{\beta}{1-\beta}$</p> $= \frac{1}{3} + 3 = \frac{10}{3}$
39.	<p>As the roots of $x^2 + bx + c = 0$ are two consecutive odd numbers,</p> <p>We take $\alpha = 2m-1, \beta = 2m+1$</p> <p>Then $2 = \alpha - \beta = \sqrt{(\alpha + \beta)^2 - 4\alpha\beta}$</p> $2 = \alpha - \beta = \sqrt{(\alpha + \beta)^2 - 4\alpha\beta}$ $\Rightarrow 4 = (-b)^2 - 4c = b^2 - 4c$
40.	<p>Put $x+4 = t$. The equation becomes</p> $(t-1)^4 + (t+1)^4 = 16$ $\Rightarrow 2(t^4 + 6t^2 + 1) = 16$ $\Rightarrow t^4 + 6t^2 - 7 = 0$

	$\Rightarrow (t^2+7)(t^2-1) = 0$ $\Rightarrow t^2=1, -7$ $\Rightarrow t = \pm 1, \pm\sqrt{7}i$ <p>Thus, real roots of the equation are $x = -4 \pm 1 = -3, -5$ and their sum is -8.</p>
41.	<p>Since $(1-p)$ is the root of the given equation,</p> $\therefore (1-p)^2 + p(1-p) + (1-p) = 0$ $\Rightarrow (1-p)(1-p+p+1) = 0$ $2(1-p) = 0$ $\Rightarrow (1-p) = 0 \Rightarrow p = 1$ <p><i>substituting in the given equation</i></p> $x^2 + 1x + (1-1) = 0$ $\Rightarrow x^2 + x = 0$ $\Rightarrow x(x+1) = 0$ $\Rightarrow x = 0, -1$
42.	<p>Let the roots be α and $\frac{1}{\alpha}$</p> <p>Since the equation is</p> $x^2 - 5x + P = 0$ $\Rightarrow \alpha + \frac{1}{\alpha} = -\frac{13}{5}$ <p>and $\alpha \cdot \frac{1}{\alpha} = \frac{k}{5} \Rightarrow \frac{k}{5} = 1$</p> $\Rightarrow k = 5$
43.	<p>Let the correct equation be</p> $x^2 + ax + b = 0 \quad \text{----- (1)}$ <p>Ramesh, $S = 10$, $P = 16$</p> $\therefore \text{Equation is } x^2 - 10x + 16 = 0 \quad \text{-----(2)}$ <p>Since the committed mistake only in constant term</p> $\therefore a = -10, b \text{ is wrong}$ <p>Mahesh, $S = -10$, $P = 9$</p> $\therefore \text{Equation is } x^2 + 10x + 9 = 0$ <p>Since the committed mistake in the coefficient of x</p> $\therefore b = 9, a \text{ was wrong}$ $\therefore x^2 - 10x + 9 = 0$

	Roots are (9,1)
44.	$4x^2 + 3x + 7 = 0$ $\Rightarrow \alpha + \beta = \frac{-3}{4}, \alpha\beta = \frac{7}{4}$ $\frac{\alpha^3 + \beta^3}{\alpha^3 \beta^3} = \frac{(\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)}{(\alpha\beta)^3}$ $= \frac{\left(\frac{-3}{4}\right)^3 - 3\left(\frac{7}{4}\right)\left(\frac{-3}{4}\right)}{\left(\frac{7}{4}\right)^3}$ $= \frac{\frac{-27}{64} + \frac{63}{16}}{\frac{343}{64}}$ $= \frac{-27 + 252}{64} \times \frac{64}{343}$ $= \frac{225}{343}$
45.	$D = b^2 - 4ac$ $= (c-a)^2 - 4(b-c)(a-b)$ $= (c+a)^2 - 4ac - 4(ab+bc-ca-b^2)$ $= (c+a)^2 + 4b^2 - 4b(c+a)$ $= (c+a-2b)^2$ $= \text{perfect square}$ $\therefore \text{Roots are rational}$