

Sample Paper-02 (unsolved)**Mathematics****Class – XI**

Time allowed: 3 hours

Maximum Marks: 100

General Instructions:

- All questions are compulsory.
- The question paper consists of 26 questions divided into three sections A, B and C. Section A comprises of 6 questions of one mark each, Section B comprises of 13 questions of four marks each and Section C comprises of 7 questions of six marks each.
- All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
- Use of calculators is not permitted.

Section A

- Write a trigonometric function that is even, its domain and range.
- Prove that $f(x) - f(-x)$ is an odd function.
- Write the equation of tangent to the circle $x^2 + y^2 = 13$ at the point (3, 2)
- Evaluate i^{62}
- Write the condition that the ellipse represented by the equation $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ whose major axis coincides with the line $x = 0$
- In how many ways can 5 students be seated at a (1) round table (2) on a bench

Section B

- $f(x-1) = 3x^4 - 12x^3 + 13x^2 - 2x + 7$ Find $f(x)$
- Find the largest term in the expansion of $(3-2x)^9$ when $x=1$
- Find the condition that the equations $ax^2 + bx + c = 0$, $px^2 + qx + r = 0$ have a common root
- Prove by mathematical induction that for all positive integral values of n , $(10^n - 1)$ is divisible by 9
- Find the domain and range of the function $f(x) = \frac{1}{3 - \sin 3x}$
- Find the limit $\lim_{x \rightarrow 0} \frac{\sin 3x - \sin x}{\sin x}$
- Solve $\tan \theta + \tan 2\theta - \sqrt{3} \tan \theta \tan 2\theta = \sqrt{3}$
- If $f(x-1) = x^2 - 2x$ Find $f^{-1}(17)$

15. Prove that if a, b are the intercepts made by a line with x axis and y axis respectively such that $\frac{1}{a} + \frac{1}{b} = k$ where k is a constant then the line passes through a fixed point. Also find the fixed points
16. Find the least positive value of n if $\left(\frac{1+i}{1-i}\right)^n = -1$
17. Find the range of $f(x)$ when $f(x) = a \cos x + b \sin x$
18. Find the non-zero solutions of $|1 + 2i|^x = 5$
19. In single throw of two dies find the probability of getting a minimum sum of 9

Section C

20. Prove that A, G, H form a decreasing GP where A, G, H are the AM, GM, HM between two numbers (a, b)
21. A bag contains tickets numbered from 1 to 10. Two tickets are drawn at random. Find the probability that both are prime.
22. One reporter tells lie in 30% cases and the other in 35% cases. Find the probability that both contradict each other on the same report.
23. Differentiate $\cos x$ from the first principle with respect to x
24. Find the sum of n terms of the series $1^3 + 2^3 + 3^3 + \dots + n^3$
25. Find the foci and the equation to the directrix of the ellipse represented by the equation $\frac{x^2}{16} + \frac{y^2}{25} = 1$
26. Calculate the mean deviation from the median for the following data

Weight in Kg	58	59	60	61	62	63	64	65	66
No of men	10	8	15	20	35	35	22	20	15