

Peaks in $|X[k]|$ when $F_s < \text{frequency of } x[n]$

$$x = (\omega t) \% 2\pi$$

$$\text{Here, } \omega = 20\pi$$

$$\text{After sampling, } t = \frac{n}{F_s}$$

$$\text{Thus, } x = 2\pi \cdot (10n/F_s) \% 1, \text{ for } n = 1, 2, \dots, [5F_s]$$

Now, when we take a Fourier transform,

$$X[k] \propto \sum_n x[n] e^{-2\pi \frac{k}{N} n}$$

$$X[k] \propto \sum_n (10n/F_s) \% 1 \times e^{-2\pi \frac{k}{N} n}$$

Now, depending upon the frequency of $x[n]$, we get peaks in $|X|$

E.g., when $F_s = 7.5$,

$$X[k] \propto \sum_n (n/3) \% 1 \times e^{-2\pi \frac{k}{N} n}$$

The period of $x[n]$ is 3, or the frequency is $1/3$.

The peak will occur when the second term (exp), will also have the same frequency, i.e., when $k/N = 1/3$.

If you choose $N=512$, then $k=512/3 = 171$.

