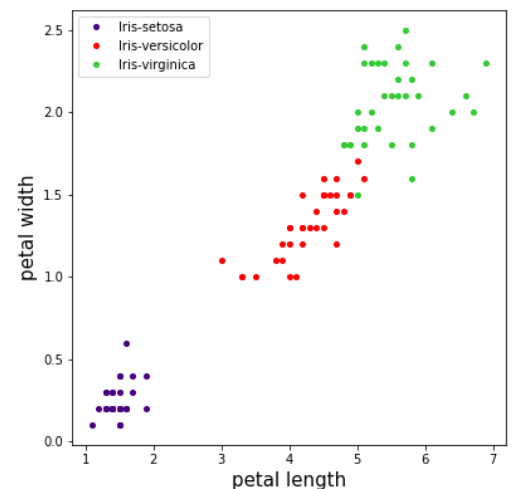
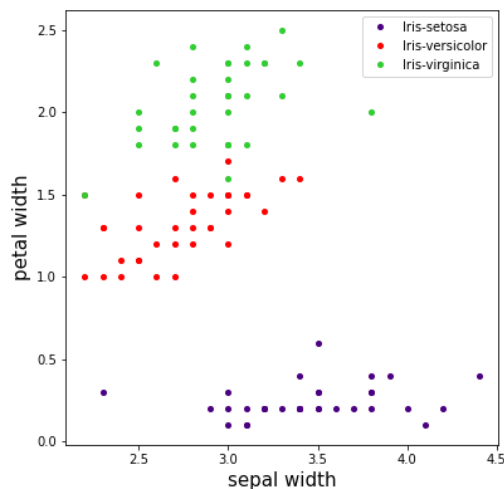
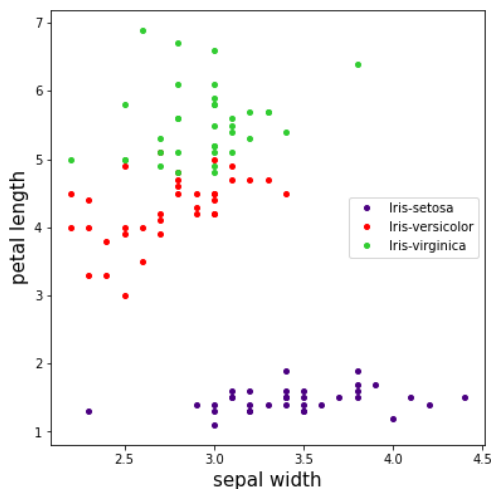
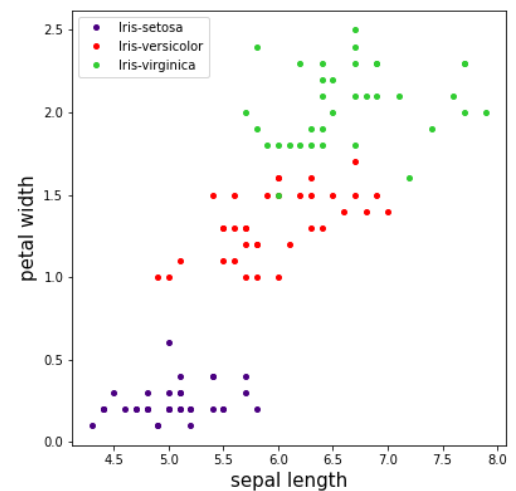
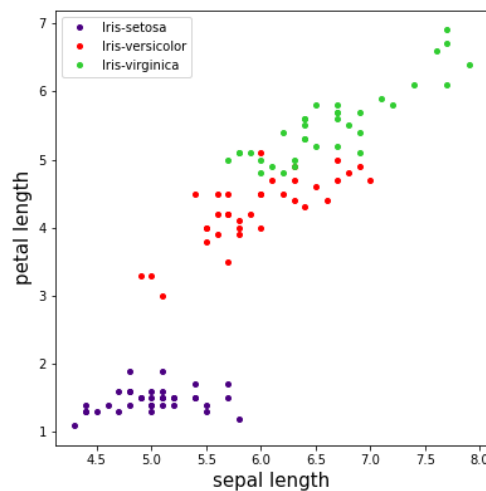
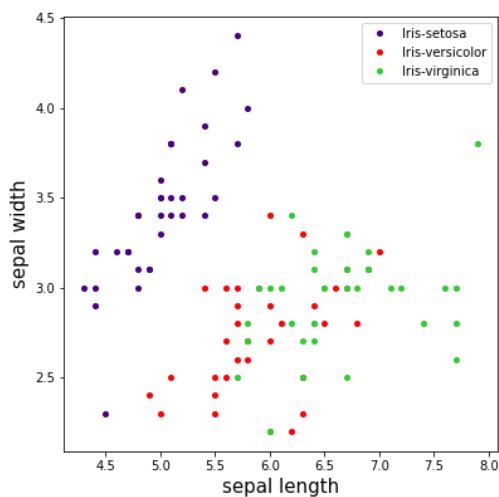


## ML Lab 5 Report

### Question 1 :

#### 1. Preprocessing and Visualisation :

- There were no NULL values or unuseful data. So nothing to drop.
- Then plotted distributions of all the features pair-wise for analysing them.



## 2. Training QDA:

- After visualising the plots, selected 3 pairs which gave the most separation among the classes and used them for training the QDA model.

## 3. Mean and Covariance Matrix for QDAs :

- Calculated Mean and Covariance matrix for the selected pairs according to the classes.
- One of the 3 pairs is shown here :

```
For features [sepal length, petal width] :
```

```
Mean :
```

```
[[5.01428571 0.24      ]  
 [5.96      1.32571429]  
 [6.64571429 2.04857143]]
```

```
Covariance of Distributions :
```

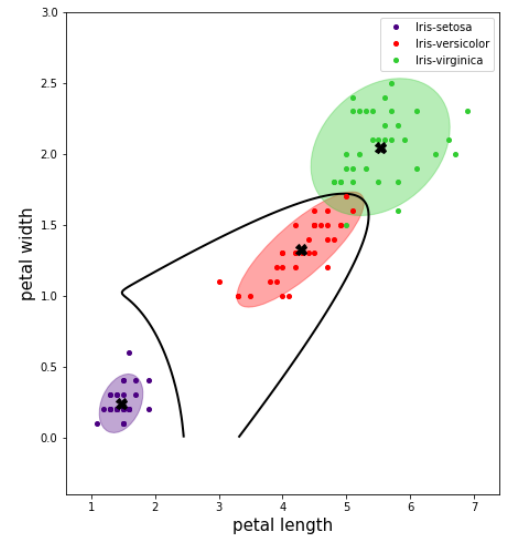
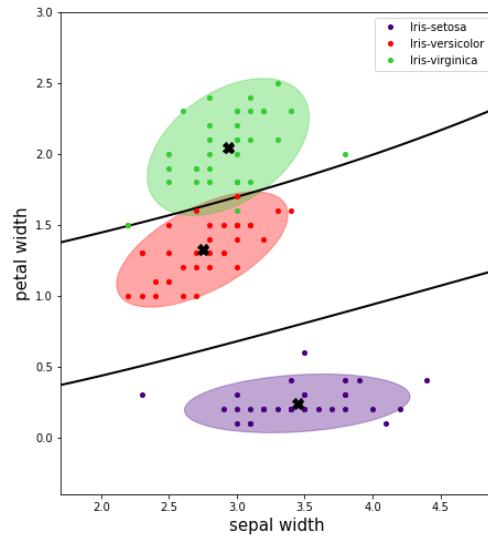
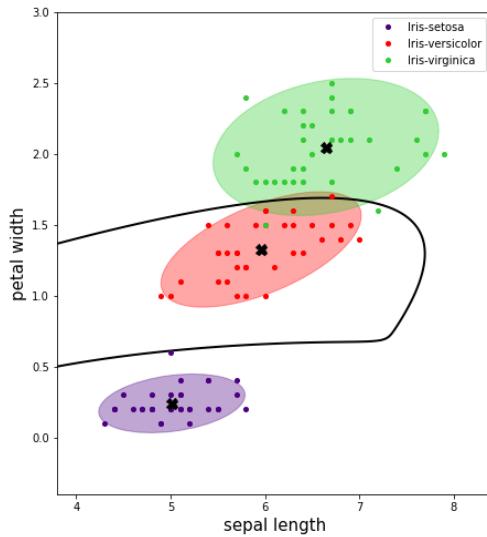
```
[[[0.15008403 0.01147059]  
 [0.01147059 0.01070588]]
```

```
[[0.28129412 0.06311765]  
 [0.06311765 0.04137815]]
```

```
[[0.35667227 0.03359664]  
 [0.03359664 0.05845378]]]
```

## 4. Decision Boundary:

- From the obtained means, covariance matrices, I plotted the elliptical distributions and then using the predicted probabilities from QDA models, plotted the decision boundary.



## 5. Class Predictions :

- Using the trained QDA models, predicted the classes for the testing data.
- Found that petal length and petal width pair gives maximum accuracy and minimum error rate. (  $\text{err\_rate} = 1 - \text{accuracy\_score}$  )

We got following Error Rates for the following pairs :

```
For [sepal length , petal width] : 0.0667
For [sepal width , petal width] : 0.0667
For [petal length , petal width] : 0.0444
```

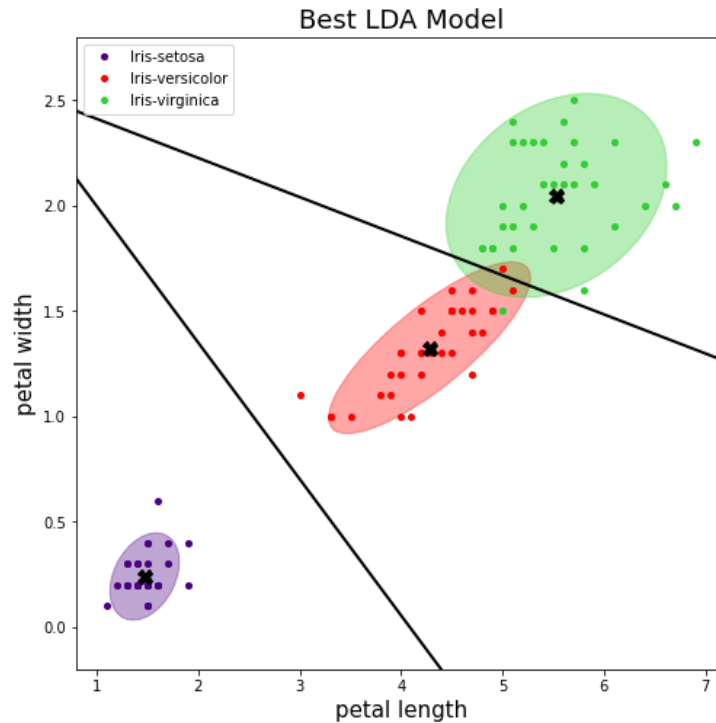
```
Hence the best model is obtained from the pair [petal width , petal length]
Minimum Error Rate : 0.0444
Maximum Accuracy : 95.56 %
```

## 6. LDA model :

- Trained a LDA model for the best pair using training data.

## 7. Decision boundary by LDA :

- Predicted probabilities by the LDA and used them for plotting the decision boundaries for all the classes.

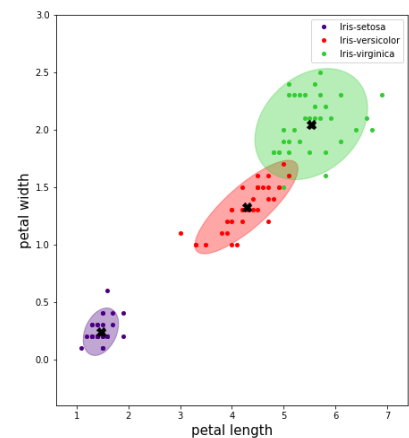
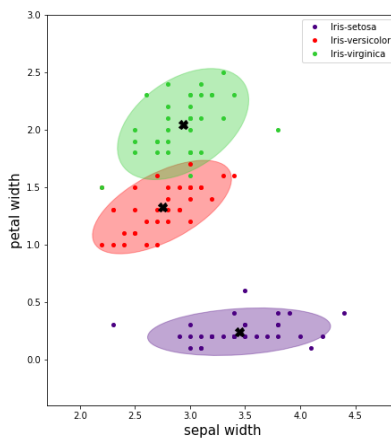
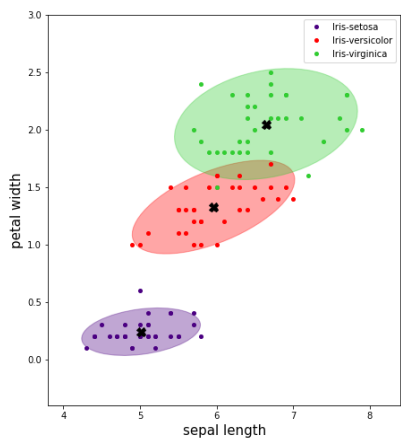


## 8. Error Rate for LDA :

- Predicted the classes of the testing data and calculated error rates of the same. Found that LDA performs worse than QDA as expected. ( LDA underfits the given dataset )

```
For best LDA Model, following are the metrics :
Error Rate : 0.0889
Accuracy score : 91.11 %
```

## 9. Visualisation of Distributions :

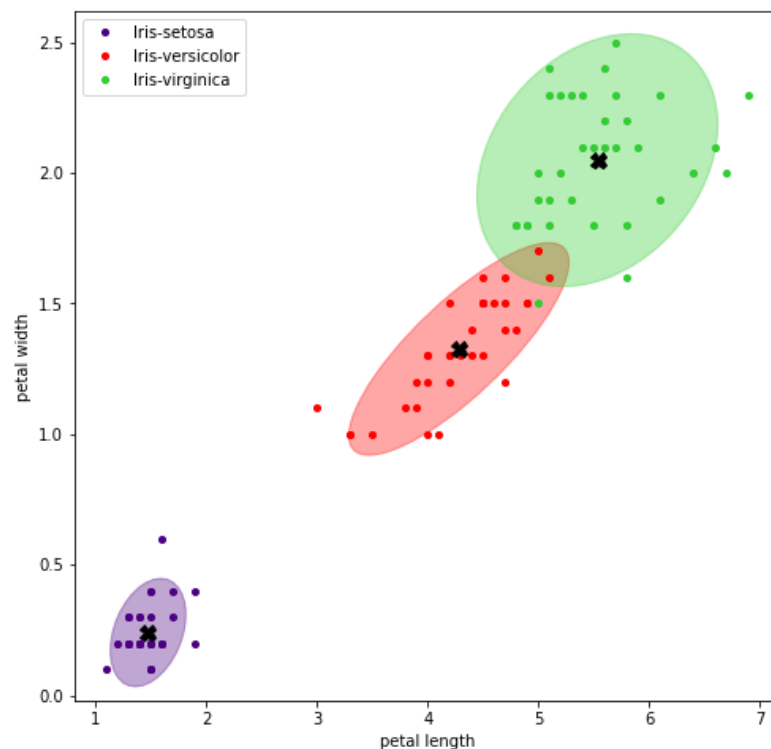


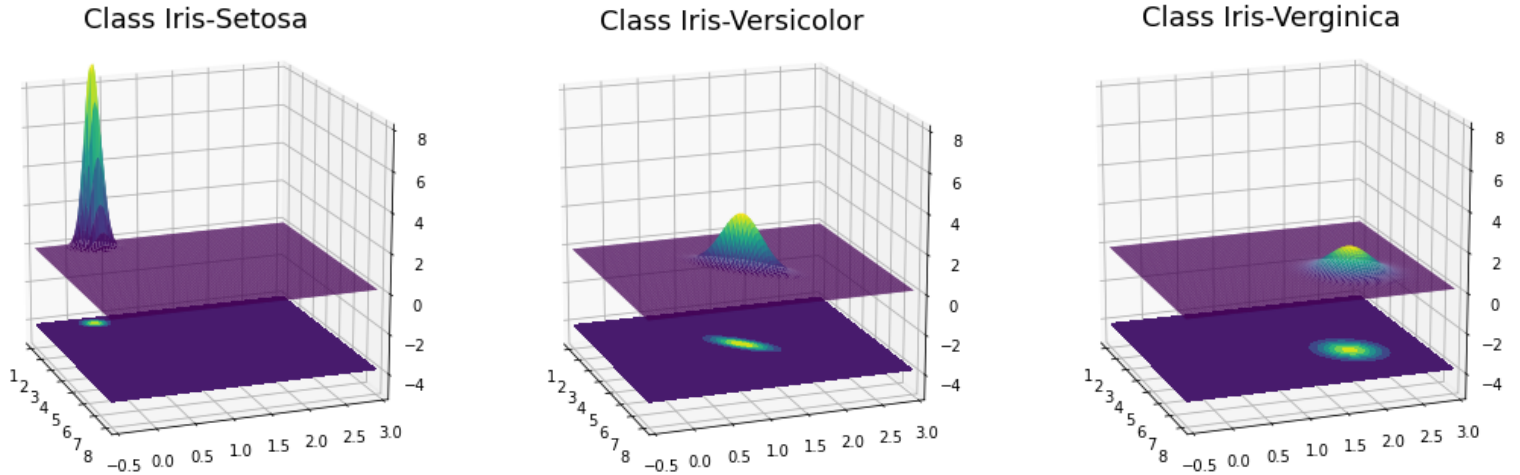
## Question 2 :

### A. Visualising Gaussian Distributions [ petal length, petal width ] :

- Calculated Mean and Covariance Matrices and used them to plot ellipses for the class distributions.
- Then plotted gaussian distribution for all the classes in 3 dimensions for better visualisation.

```
Sample Mean for Petal Length and Petal Width :  
[[1.47142857 0.24      ]  
 [4.28      1.32571429]  
 [5.53142857 2.04857143]]  
  
Sample Covariance Matrix for Petal Length and Petal Width :  
[[[0.02915966 0.00588235]  
  [0.00588235 0.01070588]]  
  
 [[0.24752941 0.08258824]  
  [0.08258824 0.04137815]]  
  
 [[0.2957479  0.03695798]  
  [0.03695798 0.05845378]]]
```





## B. Compute Likelihood :

- Made a function `compute_likelihood()` for calculating the likelihoods keeping multivariate distribution into account.

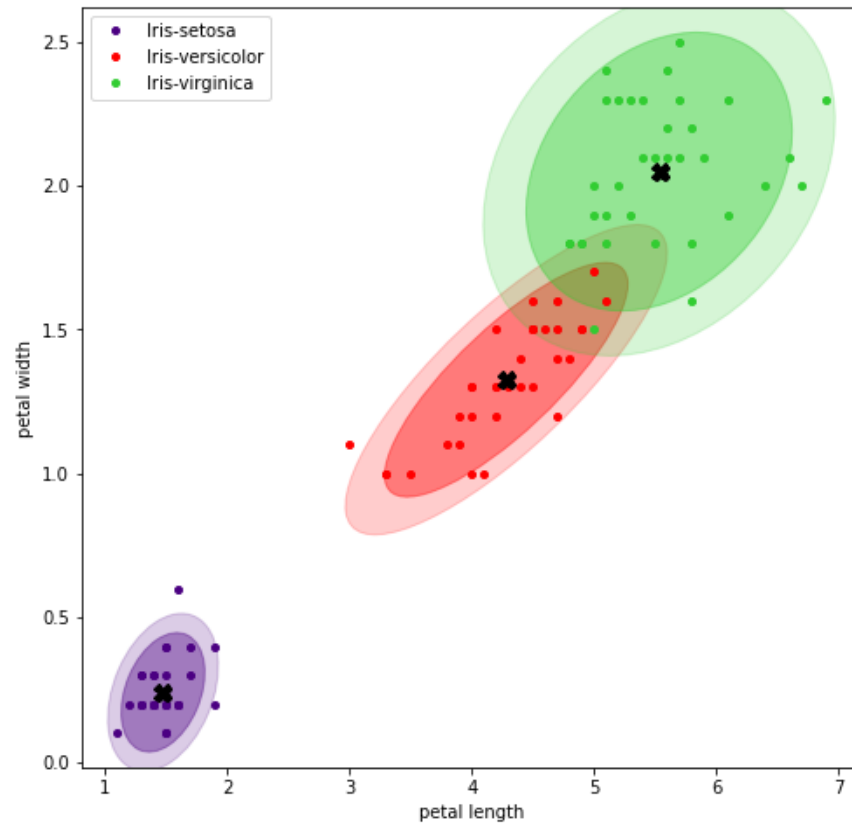
$$p(x|\mu, \Sigma) = \frac{1}{(2\pi)^{n/2}|\Sigma|^{1/2}} \exp \left\{ -\frac{1}{2}(x - \mu)^T \Sigma^{-1}(x - \mu) \right\}$$

## C. Maximum Likelihood Estimation :

Performed MLE by calculating the class-wise mean and covariance matrix and using them while calculating the likelihoods.

## D. Visualising the Distributions of ( A and C ):

From mean and covariances obtained in part A and C, plotted ellipses for all the classes in the same plot as said. The ellipse represents the contour of the distribution at a certain height.



### E. Making Predictions :

Predicted the classes for the testing data points and compared the accuracy score with QDA's accuracy.

We find that QDA performs better than the Naive Bayesian model.

```
Accuracy obtained by Naive Bayes Classifier :  
Accuracy : 91.11 %
```

```
Accuracy obtained by QDA :  
Accuracy : 95.56 %
```

## Question 3 :

### 1. Likelihood Calculation :

- Calculated the likelihoods for all the data points in the training dataset.

### 2. Laplace Smoothing :

- For the probability to remain non-zero for the certain dataset entries, we use laplace smoothing to make the probability a small positive value.

$$p_{\lambda}(C_k) = p_{\lambda}(Y = C_k) = \frac{\sum_{i=1}^N I(y_i = C_k) + \lambda}{N + K\lambda}$$

### 3. Naive Bayes Classification :

- Classified the testing data to the corresponding classes and measured the accuracy scores.
- Also compared with the QDA accuracy, and we see that QDA performs better than the Naive Bayes Classifier.

```
Accuracy obtained by Naive Bayes Classifier :  
Accuracy : 91.67 %
```

```
Accuracy obtained by QDA :  
Accuracy : 95.56 %
```

*End of the Report !*