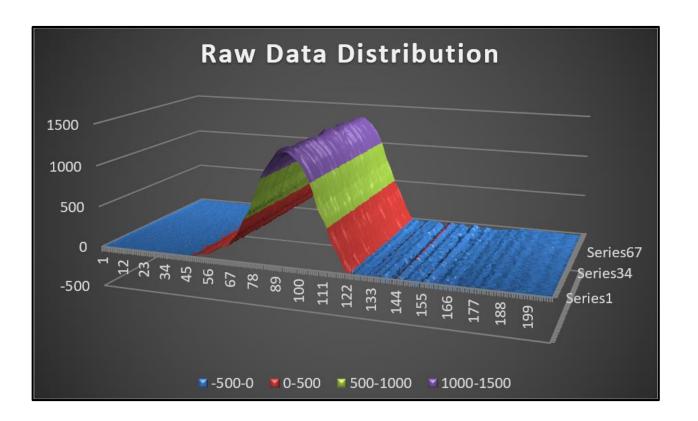


Phase I Analysis on Manufacturing process dataset

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Preliminary Analysis:



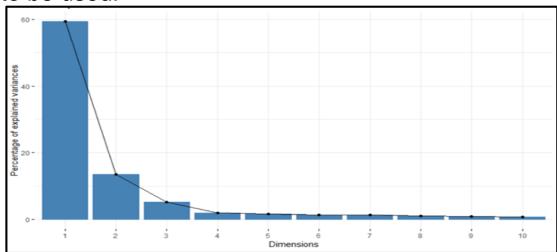


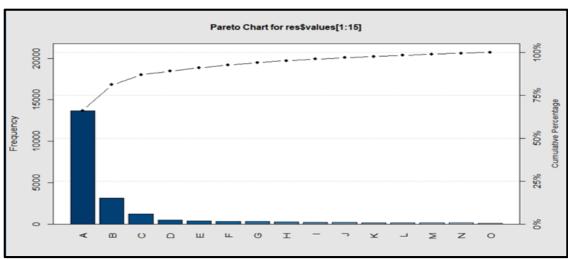
- Dataset contains of 552 observations for 209 attributes.
- The distribution for each attribute is normal distribution.
- By checking the co-variance and correlation matrix it was found that the attributes are highly correlated

Principal Component Analysis



- Since it is a high dimensional data and the attributes are highly correlated, the inherent noise in the data will drown the signals and make it harder to reject the null hypothesis.
- Use the concept of effect sparsity which states that it is always the "vital few" instead of the "trivial many" that matters.
- Used the PCA technique to reduce the dimension of the data.
- After finding the Principal Component Scores, scree plot and pareto plot were used to select the number of PCs to be used.



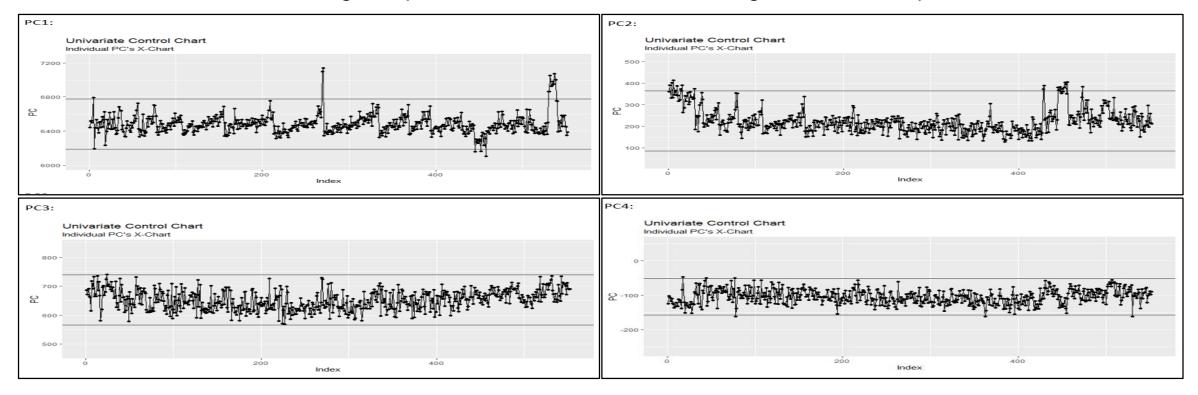


Based on these plots, we decided to use first 4 PCs that explained a total of 80% variance in the data.

Control charts



Univariate charts obtained using composite decision rules for obtaining a combined alpha level of 0.05

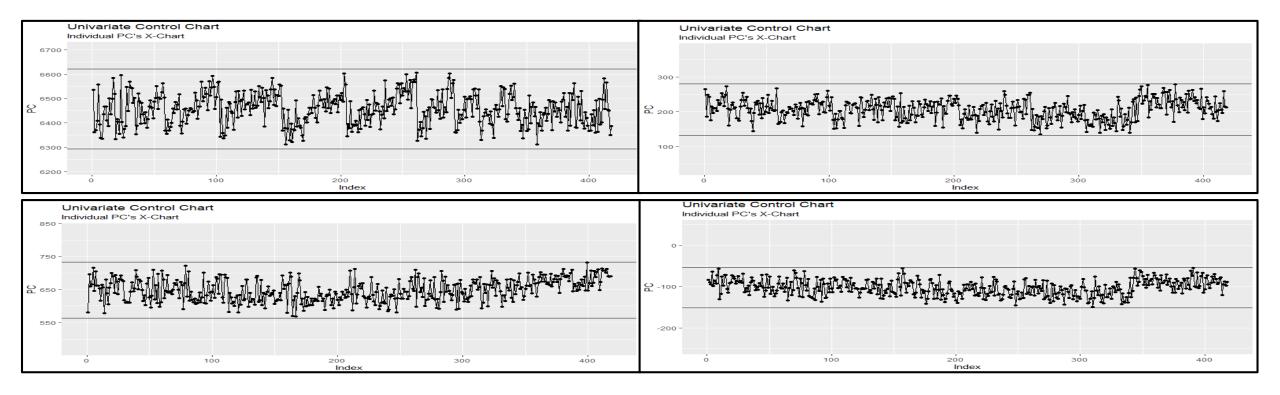


- Since, composite decision rules have to be used in case of multiple univariate charts, it leads to inflated α or β error unless parameters for individual charts are not tweaked.
- Therefore, we decided to use the Hotelling T² chart instead as it only has 1 decision rule and is unambiguous.

Control Charts



The univariate charts obtained after iteratively removing OOC points

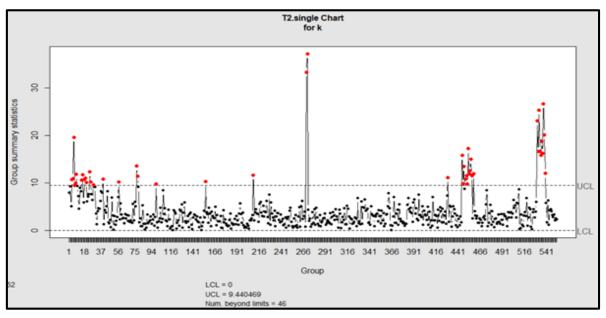


- It took 16 iterations to achieve the in-control data points.
- Since using univariate charts is computationally intensive and leads to ambiguity in interpretation, we decided to go ahead with Hotelling T² chart instead.

Hotelling T² chart



- Using the mean and covariance matrix from the PC scores, initial T² statistics were calculated.
- As the T² statistic in this case follows chi-square distribution, UCL was determined using chi-squared table at α level of 0.05
- The Out of Control(OOC) points were removed iteratively by recalculating the T² after each iteration using new mean and covariance matrix.



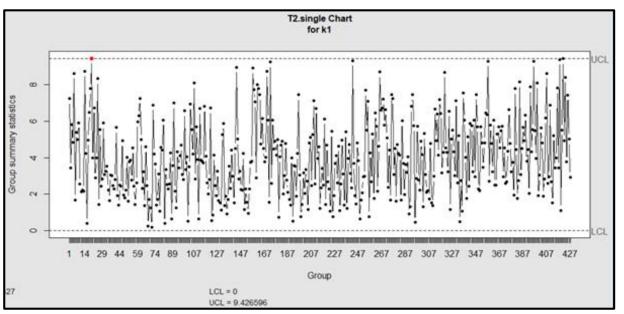


Fig: T² chart for original observations of PCs

Fig: T² chart after removing all OOC points

Using the IC data points, the IC mean and covariance matrix were calculated.

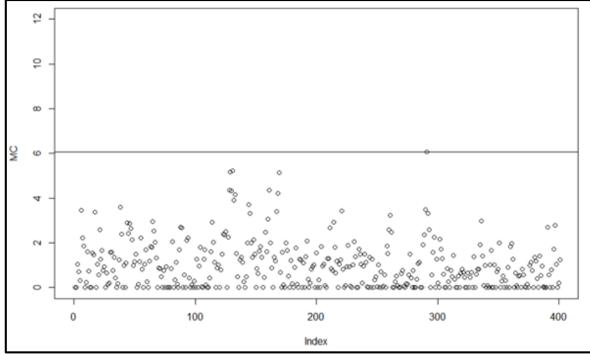
M-CUSUM chart



 To establish the parameters for future monitoring, M-CUSUM chart was used to set the control limits for detection of mean shift.

The control limits were designed to obtain an ARL₀ of 200 and ARL₁ of 4 for a mean shift of 5%using Monte Carlo

<u>simulation technique.</u>



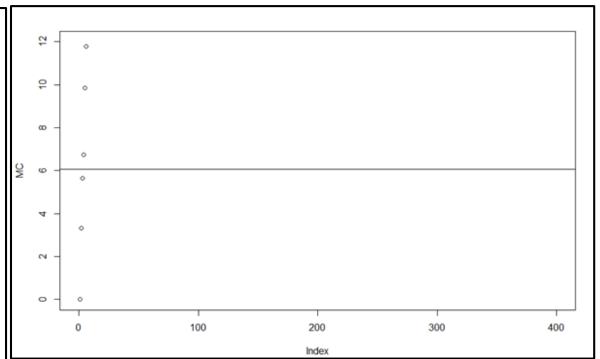


Fig: Data simulated using IC parameters

Fig: Data simulated using 5% mean shift parameters

Learnings and conclusions



- It is difficult to use high dimensional, highly correlated data for quality control purposes as it makes it harder to reject null hypothesis.
- Dimension reduction through PCA is a powerful tool to capture majority of the information in data in a fraction of its size.
- Even though multi-variate charts can be used on reduced data as it is un-correlated, it makes it difficult to determine appropriate control limits to achieve desired results.
- Hotelling T² chart is easy to use in case of multivariate data to detect OOC points in quality control process.
- M-CUSUM is useful in detecting a small mean shift in the process and should be used in conjunction with other charts for quality control process.



Thank You