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Pen and Paper Assignment

Vocabulary = {~~cute~~, funny, ~~dogs~~, animals, cats, dogs
 are, and, rarely, get, along}

Word vector = [cats, dogs, cute, funny, animals, rarely, get, along]
 are, and

Dimension of Word Vector = 10

Count vector 1 = [1, 0, 1, 1, 0, 0, 0, 1, 1]

Count vector 2 = [0, 1, 0, 1, 1, 0, 0, 1, 0]

Count vector 3 = [1, 1, 0, 0, 0, 1, 1, 0, 1]

Matrix P_x =
$$\begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 \end{bmatrix}$$

Shape: 3 X 10 Matrix

Rows relate with Posts and Column relate with word vector

$P(\text{cat}) = p$ for each word

If post has 10 words, probability of no occurrence
 of "cat"

$$= (1-p)^{10}$$

$P(\text{at least one occurrence of cat in 10 words}) = 1 - (1-p)^{10}$

$P(\text{cat-type host for a host of length } L) = 1 - (1-p)^L$

Count vector 1: $[1, 0, 1, 1, 0, 0, 0, 0, 0, 1, 1]$

Probability vector 1: $[0.25, 0, 0.25, 0.25, 0, 0, 0, 0]$
 $[0.2, 0, 0.2, 0.2, 0, 0, 0, 0, 0.2, 0.2]$

Count vector 2: $[0, 1, 0, 1, 1, 0, 0, 0, 1, 0]$

Probability vector 2: $[0, 0.33, 0, 0.33, 0.33, 0, 0, 0]$
 $[0, 0.25, 0, 0.25, 0.25, 0, 0, 0, 0.25, 0]$

Count vector 3: $[1, 1, 0, 0, 0, 1, 1, 1, 0, 1]$

Probability vector 3: $[0.2, 0.2, 0, 0, 0, 0.2, 0.2, 0.2]$
 $[\frac{1}{6}, \frac{1}{6}, 0, 0, 0, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, 0, \frac{1}{6}]$

Probability of Post A being a cat-type post

$$\begin{aligned} P(A) &= 1 - (1-p)^5 \\ &= 1 - (1-0.2)^5 \\ &= 1 - (0.8)^5 \\ &= 0.67232 \end{aligned}$$

Probability of Post C being cat type

$$\begin{aligned} P(C) &= 1 - (1 - \frac{1}{6})^5 \\ &= 1 - (\frac{5}{6})^5 = 0.998714 \end{aligned}$$

$$P(\text{contains word cute} \mid \text{given it is a cat type post}) = \frac{1}{2} = 0.5$$

$$\begin{aligned} P(\text{cat type given it contains word cute}) &= \frac{P(\text{cute} \mid \text{cat type post}) \cdot P(\text{cat type post})}{P(\text{cute containing})} \\ &= \frac{(0.5) \cdot \left(\frac{2}{3}\right)}{\left(\frac{1}{3}\right)} = 1 \end{aligned}$$

Upvotes defined by :-

$$U(L) = -\frac{1}{20}L^2 + 3L$$

$$U'(L) = -\frac{L}{10} + 3 = 0$$

Max upvotes $\Rightarrow L = 30$

$$U''(L) = -\frac{1}{10} < 0 \text{ So, maxima}$$

$$P(L, p) = 1 - (1-p)^L$$

$$G(L, p) = (1 - (1-p)^L) \left(-\frac{1}{20}L^2 + 3L \right)$$

Taking p very small and L tending to ∞

$$= \left(1 - \left(1 - LP + \frac{L(L-1)}{2} p^2 \right) \right) \left(-\frac{1}{20}L^2 + 3L \right)$$

$$= \left(LP + \frac{L^2}{2}p^2 - \frac{L}{2}p^2 \right) \left(-\frac{1}{20}L^2 + 3L \right)$$

$$= \left(\frac{P}{L} + \frac{P^2}{2} - \frac{P^2}{2L} \right) \left(\frac{3L}{L} - \frac{1}{20}L^2 \right)$$

As $L \rightarrow \infty$

$$= \frac{P^2}{2} \left(-\frac{1}{20} \right) = -\frac{P^2}{40}$$

Can't seem find the solution