

Control Systems

G V V Sharma*

CONTENTS

1	Mason's Gain Formula	1
2	Bode Plot	1
2.1	Introduction	1
2.2	Example	1
3	Second order System	1
3.1	Damping	1
3.2	Example	1
3.3	Example 2	1
4	Routh Hurwitz Criterion	2
4.1	Routh Array	2
4.2	Marginal Stability	2
4.3	Stability	2
5	State-Space Model	2
5.1	Controllability and Observability	2
5.2	Second Order System	2
6	Nyquist Plot	2
7	Compensators	2
8	Phase Margin	2
9	Gain Margin	2

Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

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*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All content in this manual is released under GNU GPL. Free and open source.

1 MASON'S GAIN FORMULA

2 BODE PLOT

2.1 Introduction

2.2 Example

3 SECOND ORDER SYSTEM

3.1 Damping

3.2 Example

3.3 Example 2

3.1. A second-order real system has the following properties:

a) the damping ratio $\zeta = 0.5$ and undamped natural frequency $\omega_n = 10\text{rad/s}$

b) the steady state value of the output, to a unit step input, is 1.02.

The transfer function of the system is

$$(A) \frac{1.02}{s^2+5s+100} \quad (B) \frac{102}{s^2+10s+100}$$

$$(C) \frac{100}{s^2+10s+100} \quad (D) \frac{102}{s^2+5s+100}$$

Solution: Characteristic equation of second order system is as follows

$$s^2 + 2\zeta\omega_n s + \omega_n^2 = 0 \quad (3.1.1)$$

Given

$$\zeta = 0.5 \quad (3.1.2)$$

$$\omega_n = 10\text{rad/s} \quad (3.1.3)$$

Therefore the equation becomes

$$s^2 + 10s + 100 = 0 \quad (3.1.4)$$

Denominator of the Transfer Function is characteristic equation. Considering this, we can eliminate A and D options.

We know that output of the system in s domain is

$$(3.1.5)$$

$$C(s) = T(s)R(s) \quad (3.1.6)$$

$$R(s) = \frac{1}{s} \quad (3.1.7)$$

as it is unit step input.

Steady state output is given by

$$C(\infty) = \lim_{s \rightarrow 0} sC(s) \quad (3.1.8)$$

Given, steady state output is 1.02 and is the same for only option B

Therefore, transfer function of the system is

$$\frac{102}{s^2 + 10s + 100} \quad (3.1.9)$$

4 ROUTH HURWITZ CRITERION

4.1 Routh Array

4.2 Marginal Stability

4.3 Stability

5 STATE-SPACE MODEL

5.1 Controllability and Observability

5.2 Second Order System

6 NYQUIST PLOT

7 COMPENSATORS

8 PHASE MARGIN

9 GAIN MARGIN