

1) if  $A = \{x : x \text{ is a prime number between 4 and 16}\}$

$$A = \{5, 7, 11, 13\}$$

So all possible subset of  $A$  are

$$\left( \{\emptyset\}, \{5\}, \{7\}, \{11\}, \{13\}, \{5, 7\}, \{5, 11\}, \{5, 13\}, \{7, 11\}, \{7, 13\}, \{11, 13\}, \{5, 7, 11\}, \{5, 7, 13\}, \{5, 11, 13\}, \{7, 11, 13\}, \{5, 7, 11, 13\} \right)$$

2)  $f(x) : \mathbb{Z} \rightarrow \mathbb{Z}$      $f(x) = x + 5$

One one <sup>test</sup> of  $f(x)$

$$\begin{aligned} f(x) &= f(y) \\ x + 5 &= y + 5 \\ x &= y \end{aligned}$$

So  $f$  is one - one

onto test    such that  $f(x) = y$

$$x + 5 = y$$

$$x = y - 5 \in \mathbb{Z}$$

So  $f$  is onto function

Since they are both one-one & onto so the it is bijective.

hence it is invertible

3)  $n = 100$   
 $m = 26$

so by applying pigeon hole  $\left\lfloor \frac{n-1}{m} \right\rfloor + 1$

$$\left\lfloor \frac{100-1}{26} \right\rfloor + 1$$

$$\left\lfloor \frac{99}{26} \right\rfloor + 1$$

$$= 3 + 1$$

$$= \underline{\underline{4}}$$

4) ~~so~~ there are 2 methods to represent a graph.

- 1) 0-1 matrix : we represent the order by 0 or 1
- 2) Adjacency matrix :- we represent by writing the edge ~~at the~~ which is making connection

inverse

5)

$$i^0 = 1$$

$$i^1 = 1$$

$$i^2 = 1 + 1 = 2$$

$$i^3 = 1 + 1 + 1 = 3$$

$$i^1 = -1$$

$$i^{-2} = -1 - 1 = -2$$

$$i^{-3} = -1 - 1 - 1 = -3$$



6) Semi group

i) closure law:- if  $(a,b) \in \mathbb{Z}$ ,  $a+b \in \mathbb{Z}$ 

ii) Associative law

 $(a,b,c) \in \mathbb{Z}$ 

$$a+(b+c) = (a+b)+c$$

Monoid.

closure law

Associative law

Identity law.

$$1 \in \mathbb{Z}$$

7) ~~Q~~  $n=0$ 

$$F(1) = 2 * F(0) + 3 = 2 * 3 + 3 = 6 + 3 = 9$$

$$F(2) = 2 * F(1) + 3 = 2 * 9 + 3 = 18 + 3 = 21$$

$$F(3) = 2 * F(2) + 3 = 2 * 21 + 3 = 42 + 3 = 45$$