

# CBCS SCHEME

USN

J M E 2 2 C S 0 1 6

BCS401

## Fourth Semester B.E./B.Tech. Degree Examination, June/July 2024 Analysis and Design of Algorithms

Time: 3 hrs.

Max. Marks: 100

*Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.  
2. M : Marks, L: Bloom's level, C: Course outcomes.*

| Module – 1 |    |                                                                                                                                                                                                                | M  | L  | C   |
|------------|----|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|----|-----|
| Q.1        | a. | What is an algorithm? Explain the fundamentals of algorithmic problem solving.                                                                                                                                 | 10 | L2 | CO1 |
|            | b. | Develop an algorithm to search an element in an array using sequential search. Calculate the best case, worst case and average case efficiency of this algorithm.                                              | 10 | L3 | CO1 |
| OR         |    |                                                                                                                                                                                                                |    |    |     |
| Q.2        | a. | Explain asymptotic notations with example.                                                                                                                                                                     | 10 | L2 | CO1 |
|            | b. | Give the general plan for analyzing the efficiency of the recursive algorithm. Develop recursive algorithm for computing factorial of a positive number. Calculate the efficiency in terms of order of growth. | 10 | L3 | CO1 |
| Module – 2 |    |                                                                                                                                                                                                                |    |    |     |
| Q.3        | a. | Explain Strassen's matrix multiplication approach with example and derive its time complexity.                                                                                                                 | 10 | L3 | CO2 |
|            | b. | What is divide and conquer? Develop the quick-sort algorithm and write its best case. Make use of this algorithm to sort the list of characters: E, X, A, M, P, L, E.                                          | 10 | L2 | CO2 |
| OR         |    |                                                                                                                                                                                                                |    |    |     |
| Q.4        | a. | Distinguish between decrease & conquer and divide & conquer algorithm design techniques with block diagram. Develop insertion sort algorithm to sort a list of integers and estimate the efficiency.           | 10 | L3 | CO2 |
|            | b. | Define topological sorting. List the two approaches of topological sorting and illustrate with examples.                                                                                                       | 10 | L2 | CO2 |
| Module – 3 |    |                                                                                                                                                                                                                |    |    |     |
| Q.5        | a. | Define AVL tree with an example. Give worst case efficiency of operations on AVL tree. Construct an AVL tree of the list of keys: 5, 6, 8, 3, 2, 4, 7 indicating each step of key insertion and rotation.      | 10 | L3 | CO3 |
|            | b. | Define Heap. Explain the bottom-up heap construction algorithm. Apply heap sort to sort the list of numbers 2, 9, 7, 6, 5, 8 in ascending order using array representation.                                    | 10 | L3 | CO3 |
| OR         |    |                                                                                                                                                                                                                |    |    |     |
| Q.6        | a. | Define 2-3 tree. Give the worst case efficiency of operations on 2-3 tree. Build 2-3 tree for the list of keys 9, 5, 8, 3, 2, 4, 7 by indicating each step of key insertion and node splits.                   | 10 | L3 | CO3 |
|            | b. | Design Horspool algorithm for string matching. Apply this algorithm to find the pattern BARBER in the text:<br>JIM SAW ME IN A BARBERSHOP                                                                      | 10 | L3 | CO3 |
| Module – 4 |    |                                                                                                                                                                                                                |    |    |     |
| Q.7        | a. | Apply Dijkstra's algorithm to find the single source shortest path for given graph [Fig.Q7(a)] by considering 's' as source vertex. Illustrate each step.                                                      | 10 | L3 | CO4 |



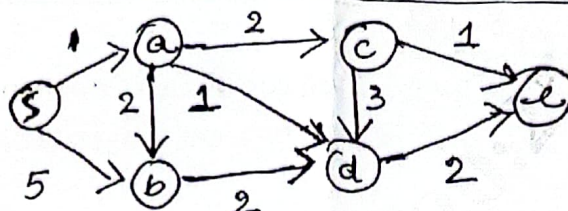


Fig.Q7(a)

- b. Define transitive closure. Write Warshall's algorithm to compute transitive closure. Illustrate using the following directed graph.

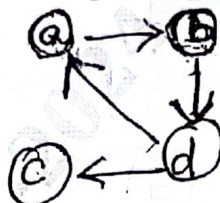


Fig.Q7(b)

OR

- Q.8 a. Define minimum spanning tree. Write Kruskal's algorithm to find minimum spanning tree. Illustrate with the following undirected graph.

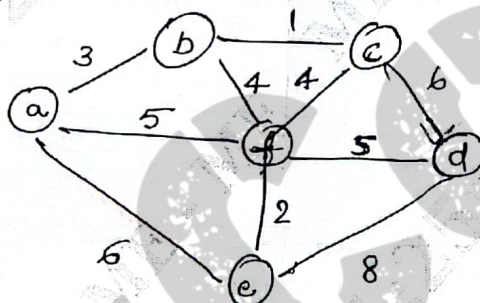


Fig.Q8(a)

- b. Construct Huffman Tree and resulting code for the following:

| Character   | A   | B   | C   | D    | E    |
|-------------|-----|-----|-----|------|------|
| Probability | 0.4 | 0.1 | 0.2 | 0.15 | 0.15 |

(i) Encode the text : ABACABAD

(ii) Decode the text : 100010111001010

Module – 5

- Q.9 a. Explain n-Queen's problem with example using backtracking approach.

- b. Solve the following instance of the knapsack problem by the branch-and-bound algorithm. Construct state-space tree.

| Item | Weight | Value |
|------|--------|-------|
| 1    | 4      | \$ 40 |
| 2    | 7      | \$ 42 |
| 3    | 5      | \$ 25 |
| 4    | 3      | \$ 12 |

The knapsack's capacity W is 10.

OR

- Q.10 a. Differentiate between Branch and Bound technique and Backtracking. Apply backtracking to solve the following instance of subset-sum problem  $S = \{3, 5, 6, 7\}$  and  $d = 15$ . Construct a state space tree.

- b. Explain greedy approximation algorithm to solve discrete knapsack problem.

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