

# Analog Circuits FISAC

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Q1] as reg. no. = 36 (last 2 digits)

- input impedance =  $50\text{ k}\Omega = Z_{in}$
- power budget =  $5\text{ mW}$
- $\mu_n C_{ox} = 100\text{ }\mu\text{A/V}^2$
- $V_{TH} = 0.5\text{ V}$
- $\lambda = 0$  (no channel length modulation)
- $V_{DD} = 1.8\text{ V}$
- $V_{RS} = 400\text{ mV} = 0.4\text{ V}$

required gain:

-36

given

given circuit

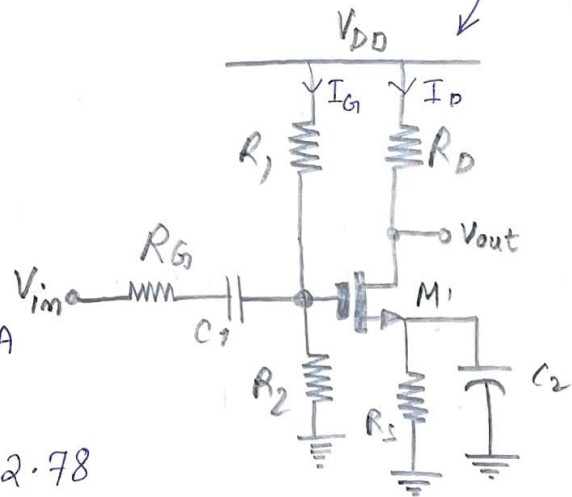
①. power budget =  $V_{DD} \times I_D$

$$\Rightarrow 5 \times 10^{-3} = 1.8 \times I_D$$

$$\Rightarrow I_D = \frac{5 \times 10^{-3}}{1.8} = 0.36 \times 10^{-3}$$

$$\Rightarrow I_D = \frac{5 \times 10^{-3}}{1.8} = 2.778 \times 10^{-3}\text{ A}$$

$$\therefore I_D = 2.778\text{ mA} \approx 2.78$$



②. need to assign maximum current to MOS

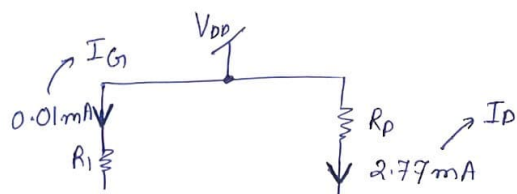
$$\therefore I_D = 2.787\text{ mA}$$

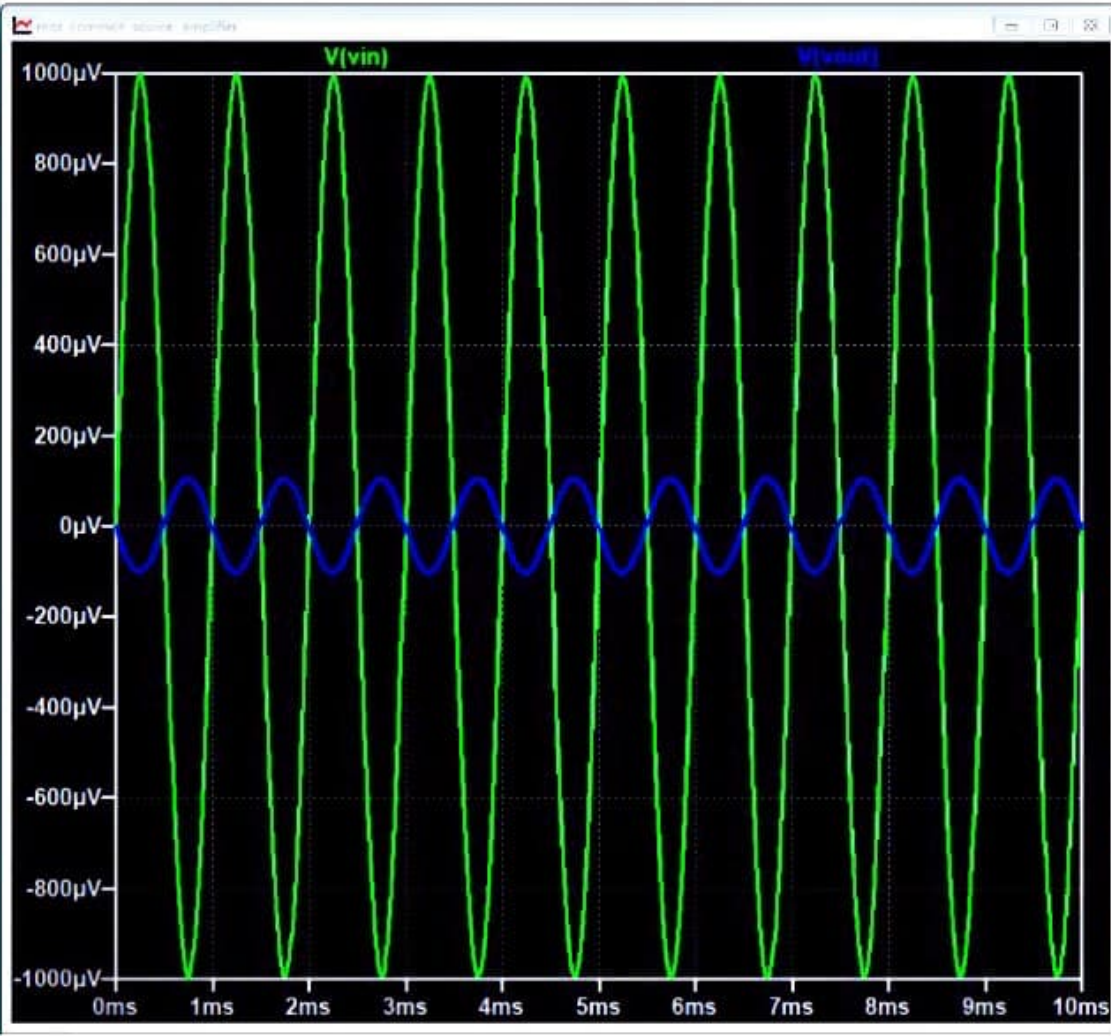
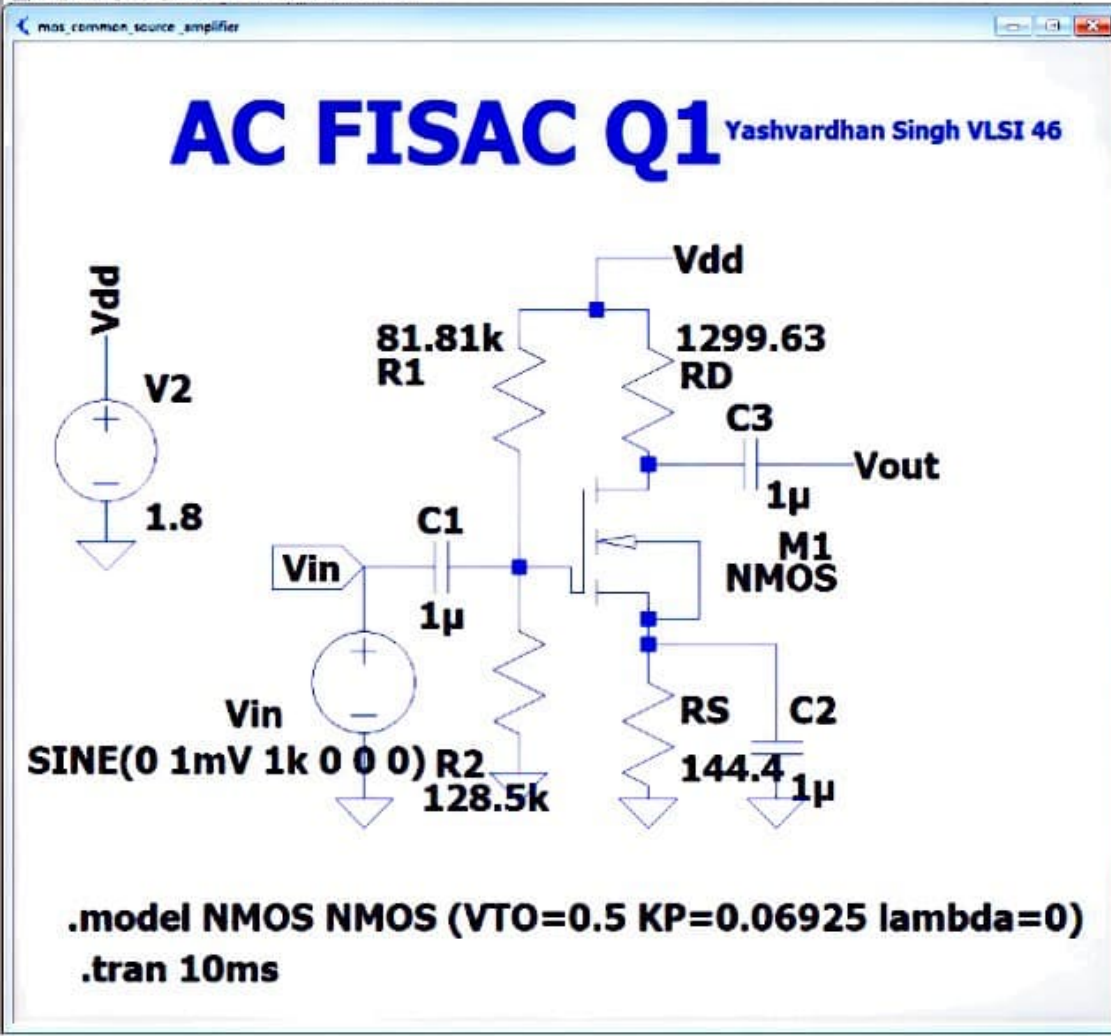
$$\therefore I_{G1} = 0.01\text{ mA}$$

let's assume  $V_{GS} = 0.7\text{ V}$

$$A_V = -g_m R_D = -36$$

$$g_m = \frac{2I_{DS}}{V_{GS} - V_{TH}} = \frac{2(2.78 \times 10^{-3})}{0.7 - 0.5} = 27.7 \frac{\text{mA}}{\text{V}}$$





$$g_m = 27.7 \text{ mA/V}$$

$$③. g_m R_D = 36 = 27.7 \text{ mA/V}$$

$$R_D = \frac{36}{27.7 \times 10^{-3}} = 1299.638 \Omega$$

$$R_D = 1299.63 \Omega$$

$$④. V_S = \text{voltage drop across } R_S = V_{PS} = 400 \text{ mV} = 0.4 \text{ V}$$

$$V_S = 0.4 \text{ V}$$

$$I_{DS} = \frac{V_S}{R_S} \Rightarrow R_S = \frac{V_S}{I_{DS}} = \frac{0.4}{2.77 \times 10^{-3}} = 144.4 \Omega$$

$$R_S = 144.4 \Omega$$

$$⑤. I_{DS} = \frac{\mu_n C_{ox} W}{2L} (V_{GS} - V_{TH})^2$$

$$2.77 \times 10^{-3} = \frac{1}{2} \times 100 \times 10^{-6} \times \frac{W}{L} (0.2)^2 \Rightarrow \frac{W}{L} = 1385$$

$$\frac{W}{L} = 1385$$

$$⑥. V_{GS} = 0.7 \text{ V} = V_G - 0.4 \Rightarrow V_G = 0.7 + 0.4 = 1.1 \text{ V}$$

$$V_G = 1.1 \text{ V}$$

$$\frac{R_1 R_2}{R_1 + R_2} = R_1 \parallel R_2$$

$$V_G = \frac{V_{DD} \times R_2}{R_1 + R_2} = 1.1 \text{ V} \Rightarrow \frac{1.8 R_1 R_2}{R_1 + R_2} = 1.1 (R_1)$$

multiply  $R_1$  on both sides

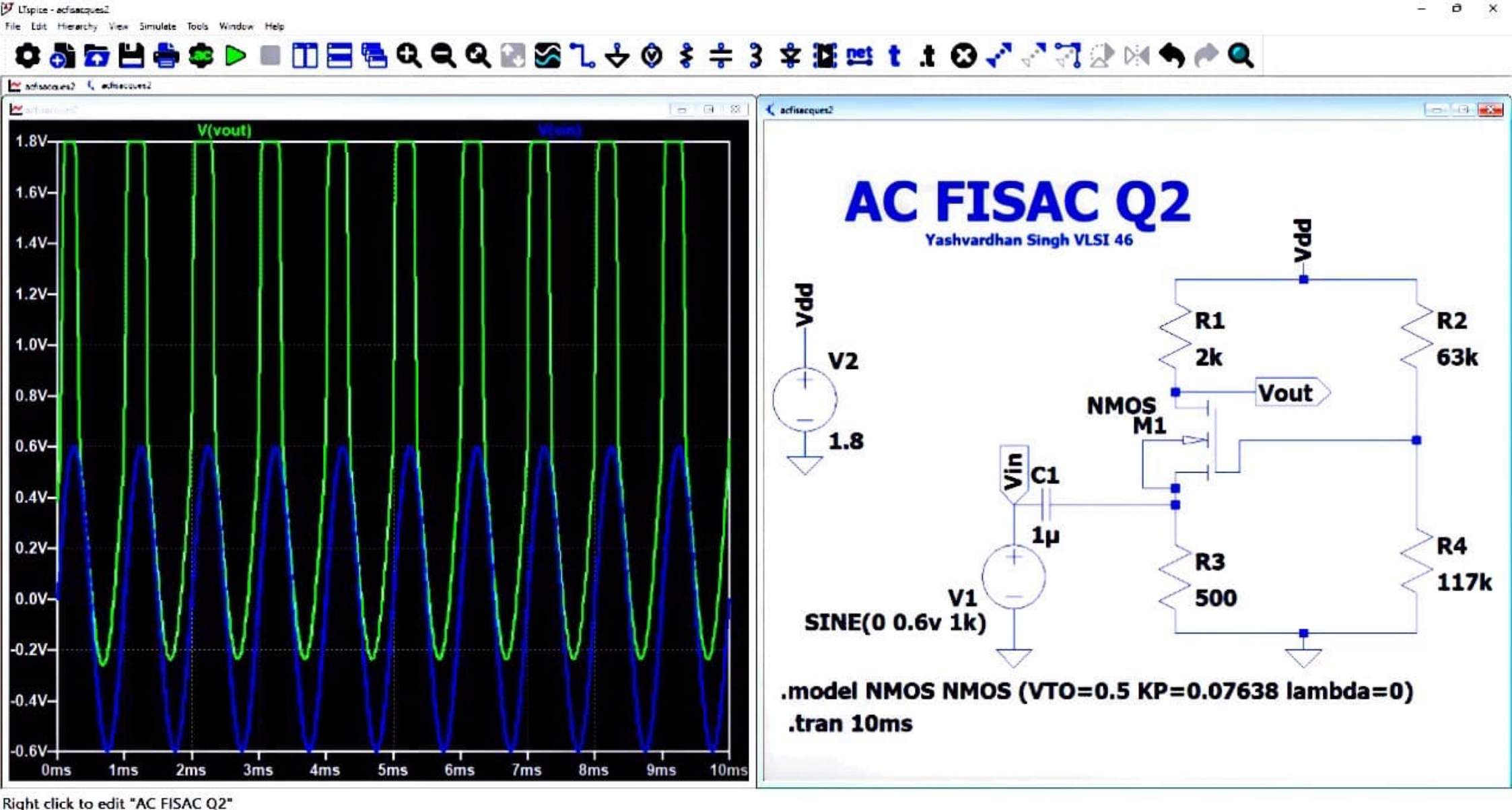
$$= 1.8 (R_1 \parallel R_2) = 1.1 R_1 \leftarrow \text{here } R_1 \parallel R_2 \text{ is } Z_{in} = 50 \text{ k}\Omega$$

$$= 1.8 \times 50 \times 10^3 = 1.1 R_1$$

$$\Rightarrow R_1 = 81.81 \text{ k}\Omega$$

$$\text{and } R_2 = 128.5 \text{ k}\Omega$$

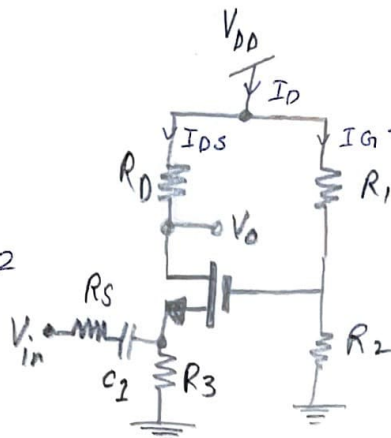




Q2

Given:

- voltage gain  $\Rightarrow A_v = 36$
- $R_S = 0$
- $R_3 = 500 \Omega$
- $R_{in} = 50 \Omega$
- $P_B = 2 \text{ mW}$
- $V_{DD} = 1.8 \text{ V}$
- $\mu_n C_{ox} = 100 \text{ MA/V}^2$
- $V_{TH} = 0.5 \text{ V}$
- $\lambda = 0$  (no CLM)



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$$\Rightarrow P_B = 2 \times 10^{-3} = V_{DD} \times I_D = 1.8 \times I_D$$

$$I_D = 1.111 \times 10^{-3} \text{ A} = 1.11 \text{ mA}$$

$$I_{DS} = 1.10 \text{ mA} \quad I_G = 0.01 \text{ mA}$$

$$\Rightarrow R_{in} = \frac{1}{g_m \parallel R_3} \rightarrow g_m = R_{in}^{-1} - R_3^{-1}$$

$$I_D = 1.11 \text{ mA}$$

$$g_m = 0.018 \Omega^{-1}$$

$$V_{GS} = 0.62 \text{ V}$$

$$\Rightarrow g_m = 0.018 \Omega^{-1}$$

$$\Rightarrow g_m = \frac{2 I_{DS}}{V_{GS} - V_{TH}} \Rightarrow V_{GS} = \frac{2 \times 1.10 \times 10^{-3}}{0.018} + 0.5 = 0.62 \text{ V}$$

$$\Rightarrow I_{DS} = \frac{\mu_n C_{ox}}{2} \cdot \frac{W}{L} (V_{GS} - V_{TH})^2 = \frac{100 \times 10^{-6}}{2} (0.62 - 0.5)^2 \frac{W}{L}$$

$$\frac{W}{L} = \frac{1.1 \times 10^{-3} \times 2 \times 10^4}{(0.12)^2} = 1527.778 \quad \frac{W}{L} = 1527.78$$

$$\Rightarrow V_{GS} + V_S = 0.62 + I_{DS} R_3 = 0.62 + 1.1 \times 10^{-3} (500)$$

$$V_G = 1.17 \text{ V}$$

$$V_G = 1.17 \text{ V}$$

$$\Rightarrow A_v = g_m R_D = 0.018 \times R_D = 36 \Rightarrow R_D = \frac{36}{0.018} = 2000$$

$$R_D = 2000 = 2 \text{ k}\Omega$$

$$\Rightarrow R_2 = \frac{V_G}{I_G} = \frac{1.17}{0.01} \times 1000 = 117 \text{ k}\Omega$$

$$R_2 = 117 \text{ k}\Omega$$

$$\Rightarrow R_1 = \frac{V_{DD} - V_G}{I_G} = \frac{1.8 - 1.17}{0.01} \times 1000 = 63 \times 10^3$$

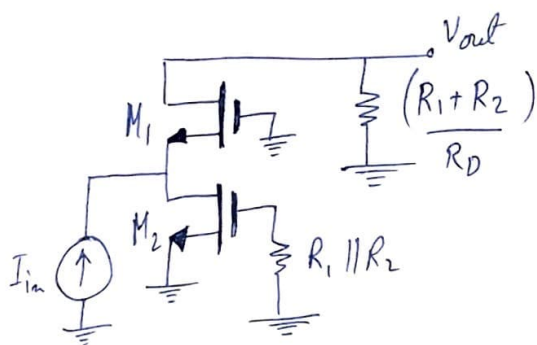
$$R_1 = 63 \text{ k}\Omega$$

$$\Rightarrow \text{all parameters found!} \quad K_p = \frac{100 \times 10^{-6} \times 1527.78}{2} = 0.07638$$

03]

$R_1 + R_2$  is very large  $\rightarrow$  given  
 $\therefore \lambda = 0 \rightarrow$

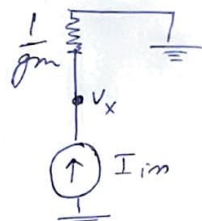
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$$R_{o, open} = \frac{V_{out}}{I_{in}}$$

$$V_{out}/V_x = g_m R_D$$

$$V_x = I_{in} / g_m$$



$$\frac{V_{out}}{I_{in}/g_m} = g_m R_D$$

$$\therefore R_{o, open} = \frac{V_{out}}{I_{in}} = R_D$$

$$R_{in, open} = V_x / I_{in}$$

$\Rightarrow$

$$R_{in, open} = 1/g_m$$

input impedance

$$R_{out, open} = R_D \parallel R_1 + R_2$$

Since  $R_1 + R_2 \gg R_D$

$R_D \parallel R_1 + R_2 \approx R_D$  (anything parallel to  $\infty$  is that thing itself).

$$R_{out, open} = R_D \rightarrow \text{output impedance}$$

Closed loop parameters

$$K = \frac{V_F}{V_{out}} = \frac{R_2}{R_1 + R_2}$$

$$R_{out, closed} = \frac{R_D}{1 + K R_D} = \frac{R_D}{1 + \frac{R_2 R_D g_{m2}}{R_1 + R_2}}$$

$R_{out, closed}$

$$= \frac{R_{out, open}}{1 + K R_D} =$$

$$\boxed{\frac{R_D}{1 + \frac{R_D R_2 g_{m2}}{R_1 + R_2}}}$$

$$R_{in, closed} = \frac{R_{in, open}}{1 + k R_D} \Rightarrow k = \frac{g_{m2} R_2}{R_1 + R_2}$$



Q4.]

4<sup>th</sup> order Butterworth LPF

$$f_c = 1 \text{ kHz}$$

$$\text{passband gain} = 5$$

$$C = 0.1 \mu\text{F}$$

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yes

$$\text{order} = 4 \Rightarrow \therefore N = 4 \quad H_0 = 5 \text{ (given)}$$

$$f_c = 1 \times 10^3 \text{ Hz} \rightarrow \omega_c = 2\pi f_c = 6283.1853 \text{ rad/s}$$

Transfer function: for 4<sup>th</sup> order

$$H(s) = \frac{H_0}{(s^2 + \alpha_1 \omega_c s + \omega_c^2)(s^2 + \alpha_2 \omega_c s + \omega_c^2)}$$

$\alpha_1, \alpha_2$  damping factors, for 4<sup>th</sup> order are:

$$\alpha_1 = 0.765$$

$$\alpha_2 = 1.848$$

$$H(s) = \frac{5}{(s^2 + 4806.24s + 39478417.38)(s^2 + 11605.83s + 39478417.38)}$$

$$f_{c \text{ stage } 1} = \frac{f_c}{0.924}$$

$$f_{c \text{ stage } 2} = \frac{f_c}{0.383}$$

lets assume  $R_1 = R_2 = R_3 = R_4 = R_7 = 1 \text{ k}\Omega$

$$A = 1 + \frac{R_6}{R_1} \Rightarrow R_6 = \underset{5}{(A-1)} \underset{1000}{R_1} = \underline{\underline{4 \text{ k}\Omega}}$$

$$R_1, R_2, R_3, R_4, R_5, R_7 = 1 \text{ k}\Omega$$

$$R_6 = 4 \text{ k}\Omega$$

$$PS_1 = \frac{1}{Q_1 k_1 \omega} + \frac{1}{Q_2 k_2 \omega} \Rightarrow \begin{matrix} k_1 = k_2 = 1 \\ Q_1 = 0.5412 \text{ quality} \\ Q_2 = 1.3066 \text{ factors} \end{matrix}$$

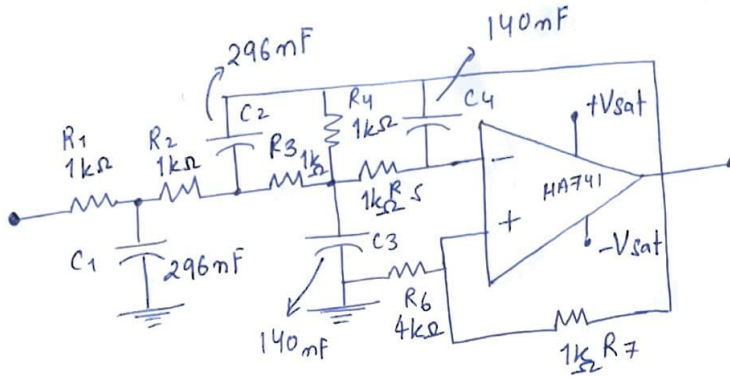
for simplicity, assume  $C_1 = C_2$  &  $C_3 = C_4$

$$C_1 = C_2 = \frac{1}{R\omega Q_1} = 296.23 \text{ nF} \quad (R \text{ considered as } 1 \text{ k}\Omega)$$

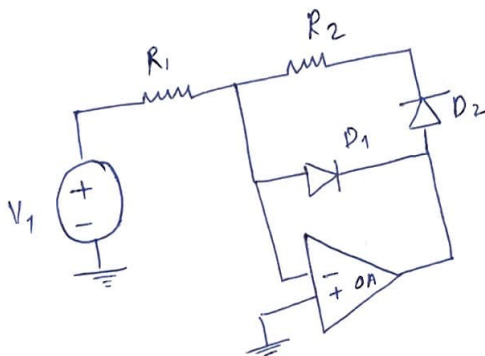
$$C_3 = C_4 = \frac{1}{R\omega Q_2} = 139.37 \text{ nF} \quad (R = 1 \text{ k}\Omega)$$

# 4th Order Butterworth LPF dkt. :

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Q5]

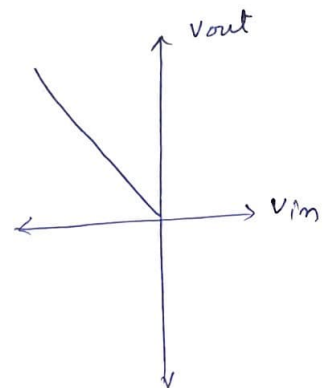
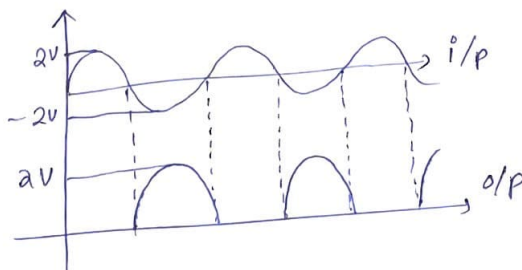


$$R_1 = R_2$$

$$\pm V_{sat} = \pm 12V$$

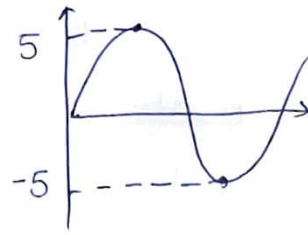
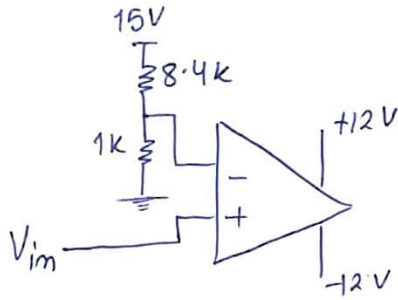
- The given circuit is a precision half-wave rectifier.
- When i/p voltage is greater than 0,  $D_1$  is conductive &  $D_2$  is non-conductive, so the voltage is 0.
- When input voltage is less than 0,  $D_1$  doesn't conduct whereas  $D_2$  conducts, and the op-amp works in inverting configuration.

$$\therefore V_{out} = -\frac{R_2}{R_1} V_{in} \text{ or } V_1$$





Q6)



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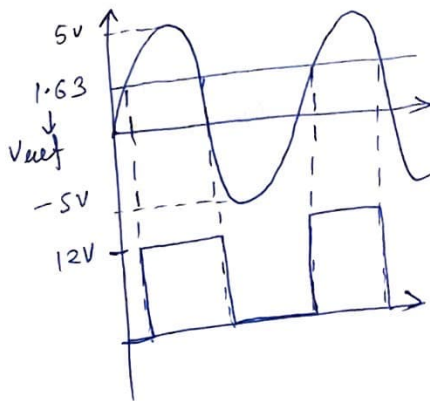
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This is a non-inverting comparator.

i/p : non-inverting terminal

~~o/p~~ reference : inverting terminal  
i/p

$$V_{ref} = \frac{15 \times R_2}{R_1 + R_2} = \frac{16}{9.2} = 1.63V$$



Q7)

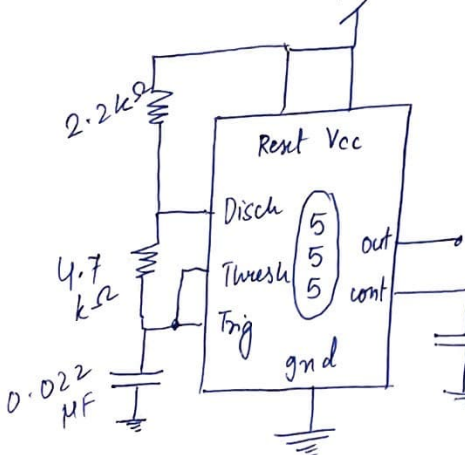
①  $R_1 = 2.2k\Omega$

$R_2 = 4.7k\Omega$

$C_2 = 0.022\mu F$

$C_1 = 0.01\mu F$

$V_{cc} = 5.5V$



$$F = \frac{1}{RC} = \frac{1}{6.9 \times 10^3 \times 0.022 \times 10^{-6}}$$

$$R = R_1 + R_2 = 2.2 + 4.7 = 6.9k\Omega$$

$$f = 6.587kHz$$

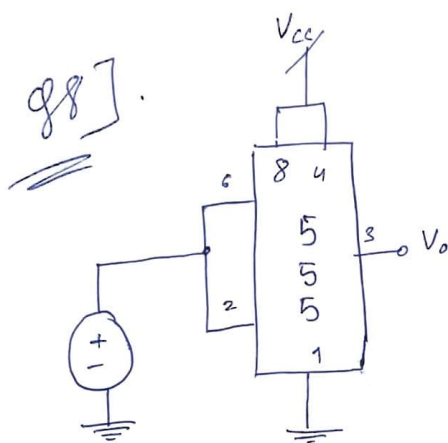
$$T = \frac{1}{f} = 0.176ms$$

$$T_{on} = 0.69(R_A + R_B)C = 0.1047ms$$

Duty-cycle :  $\frac{T_{on}}{T} = \frac{0.1047}{0.176} = 59.48\%$

Q7] ⑪ when a diode is connected b/w the discharge & threshold pins of a 555 timer configured as an astable multivibrator the output frequency will remain the same but the duty cycle reduces to less than 50%.

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$$V_{cc} = 6V$$

$$V_i = 3 + 3 \sin \pi t$$

555 timer  
threshold voltage

$$= \frac{1}{3} V_{cc} \text{ \& \#39; } \frac{2}{3} V_{cc}$$

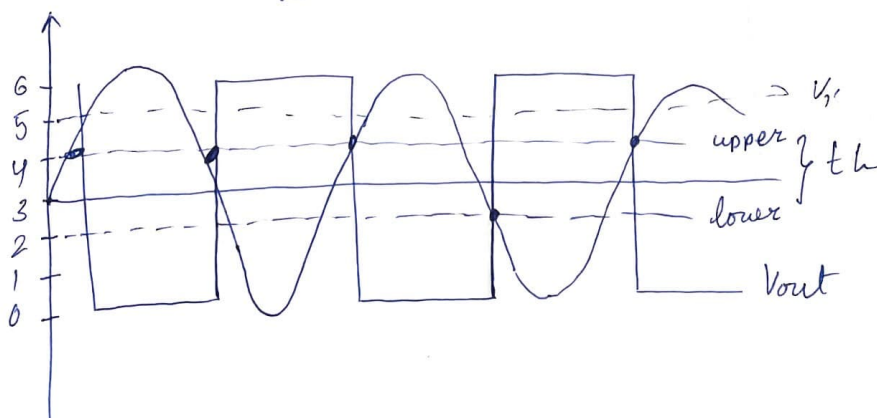
$$\frac{1}{3} \times 6 = 2V \text{ [lower th]}$$

$$\frac{2}{3} \times 6 = 4V \text{ [upper th]}$$

$$V_i = 3 + 3 \sin(\pi t)$$

$$\text{range} = -1 \text{ to } 1$$

$$V_i = 0V \quad V_i = 3 + 3 = 6V$$



Q9.

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Monostable  
multivibrator circuit

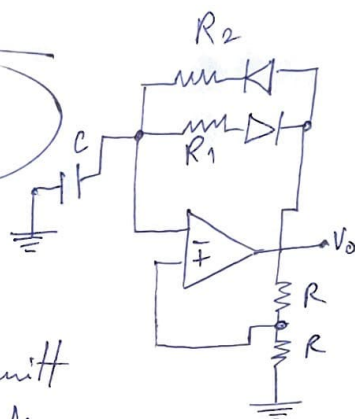
$$V_{im}(1 - e^{-t/R_1 C_1}) \rightarrow \text{charging}$$

$$V_{th} = V_{im}(1 - e^{-T/R_1 C_1})$$

$$e^{-T/R_1 C_1} = 1 - \frac{V_{th}}{V_{im}}$$

$$T = \frac{-T}{R_1 C_1} \ln\left(1 - \frac{V_{th}}{V_{im}}\right)$$

$$T = R_1 C_1 \ln\left(\frac{V_{im}}{V_{im} - V_{th}}\right)$$



Q10.)

- ①  $C = 0.1 \mu F$   
 $R = 1 k\Omega$   
 $R_1 = 2 k\Omega$   
 $R_2 = 1 k\Omega$

given ckt. is  
similar to Schmitt  
trigger relaxation  
oscillator.

Since the diodes face opposite directions  
only one of them will conduct behaving  
as a rectified waveform and oscillator

$$T = 2R_F C \ln\left(1 + \frac{2R}{R}\right) \rightarrow \text{Time period}$$

Half of waveform  $\Rightarrow R_F = 2 k\Omega$

$$T = 2 \times 2000 \times 0.1 \times 10^{-6} \times \ln(1 + 2000)$$

$$T = 3.04 \text{ ms}$$

other half  $= 7R_F = 1 k\Omega$

$$T = 2 \times 1000 \times 0.1 \times 10^{-6} \ln(1 + 2000)$$

$$T = 1.52 \text{ ms}$$



Q10) ii)

$$R_1 = R_2 = 2k\Omega$$

repeating above,

when

$$R = 2k\Omega$$

$$T = 3.04ms$$

and,

since both  $R = 2k\Omega$ ,

$$T_{total} = (3.04)_2 = \underline{\underline{6.08ms}}$$

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