

Iteration - 1

$x_i \ y_i$

sample - 1

7.6 157

7.1 174

Step 1 :- $[7.6, 157]$, $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned}\text{Step 2 :- } \frac{\partial E}{\partial m} \Big|_{m=1} &= - (y_i^a - m x_i^a - c) \times (-x_i^a) \\ &= + (157 - (1 \times 7.6) - (-1)) \times (7.6) \\ &= (158 - 7.6) (7.6) \\ &= (150.4) (7.6) \\ &= 1143.04\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} \Big|_{c=-1} &= - (y_i^a - m x_i^a - c) \\ &= - (157 - 1 \times 7.6 - (-1)) \\ &= - (158 - 7.6) \\ &= - 150.4\end{aligned}$$

$$\begin{aligned}\text{Step 3 :- } \Delta m &= -\eta \frac{\partial E}{\partial m} = - (0.01) (1143.04) \\ &= -11.430\end{aligned}$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = - (0.01) (-150.4) \\ &= 1.504\end{aligned}$$

$$\begin{aligned}\text{Step 4 :- } m &= m + \Delta m = 1 + (-11.43) = -10.43 \\ c &= c + \Delta c = -1 + (1.504) = 0.504\end{aligned}$$

sample-2

step-1 :- $[7.1, 174]$, $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned}\text{step 2 :- } \frac{\partial E}{\partial m} \Big|_{m=1} &= -(y_i^a - m x_i^a - c) - x_i^a \\ &= (174 - 1 \times (7.1) - (-1)) \times 7.1 \\ &= (175 - 7.1) \times 7.1 \\ &= 167.9 \times 7.1 \\ &= 1192.09\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} \Big|_{c=-1} &= -(y_i^a - m x_i^a - c) \\ &= -(174 - 1(7.1) - (-1)) \\ &= -167.9\end{aligned}$$

$$\begin{aligned}\text{step 3 :- } \Delta m &= -\eta \frac{\partial E}{\partial m} \\ &= -(0.01) 1192.09 \\ &= -11.220\end{aligned}$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01) (-167.9) \\ &= 1.679\end{aligned}$$

$$\begin{aligned}\text{step 4 :- } m &= m + \Delta m \\ &= 1 + (-11.220) \\ &= -10.220\end{aligned}$$

$$\begin{aligned}c &= c + \Delta c \\ &= -1 + 1.679 \\ &= 0.679\end{aligned}$$

Iteration - 2

Sample - 1

$$\text{Step 1: } [7.61, 151], \eta = 0.01 \quad m = -10.43 \quad c = 0.504$$

$$\text{Step 2: } -\frac{\partial E}{\partial m} \Big|_{m=-10.43}$$

$$= (151 - (-10.43)(7.61) - 0.504)(7.61)$$

$$= [151 + (10.43)(7.61) - 0.504](7.61)$$

$$= [156.496 + (10.43 \times 7.61)] \cdot 7.61$$

$$= (156.496 + 79.372) \cdot 7.61$$

$$= (235.868) \cdot 7.61$$

$$= 1794.955$$

$$\frac{\partial E}{\partial c} \Big|_{c=0.504} = - (151 - (-10.43)(7.61) - 0.504)$$

$$= -235.868$$

$$\text{Step 3: } \Delta m = -\eta \frac{\partial E}{\partial m} = (-0.01 \times 1794.955)$$

$$= -17.949$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = (-0.01) \times -235.868$$

$$= 2.358$$

$$\text{Step 4: } m = m + \Delta m$$

$$= -10.43 + (-17.949)$$

$$= -28.379$$

$$c = c + \Delta c$$

$$= 0.504 + 2.358$$

$$= 2.862$$

sample-2

Step 1:- $[7.1, 174]$, $\eta = 0.01$, $m = -10.92$, $c = 0.679$

Step 2:- $\frac{\partial E}{\partial m} \Big|_{m=-10.92}$

$$= (174 - (-10.92)) (7.1) - 0.679 (7.1)$$

$$= (173.321 + (10.92 \times 7.1)) \times 7.1$$

$$= 1781.056$$

$$\frac{\partial E}{\partial c} \Big|_{c=0.679} = -((174 - (-10.92)) (7.1) - (0.679)) / c^2$$

$$= -250.853$$

Step 3:- $\Delta m = -\eta \frac{\partial E}{\partial m} = (-0.01) \times 1781.056$

$$= -17.810$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = (-0.01) (-250.853)$$

$$= 2.508$$

Step 4:- $m = m + \Delta m$

$$= -10.92 - 17.81$$

$$= -28.73$$

$$c = c + \Delta c$$

$$= 0.679 + 2.508$$

$$= 3.187$$