

Iteration-1

Find the minimum value of  $f(x) = x^4 + 3x^2 + 10$

Let  $x = 2$  and  $\eta = 0.02$

$$\frac{\partial f(x)}{\partial x} = 4x^3 + 6x$$

$$= 4 \times 2^3 + 6 \times 2$$

$$= 44 \Rightarrow \text{step length} = -0.01 \times 44 = -0.44$$

$$\therefore x = 2 - 0.44$$

$$= 1.56$$

Iteration-2

Let  $x = 1.56$  and  $\eta = 0.02$

$$\frac{\partial f(x)}{\partial x} \bigg|_{x=1.56} = 4 \times (1.56)^3 + 6 \times 1.56$$

$$= 24.545664$$

$$\text{Step length} = -0.01 \times 24.545664$$

$$= -0.2454566$$

$$\therefore x = 1.56 - 0.2454566$$

$$= 1.31454336$$