

EE2025 Independent Project (2019-20)

Programming Assignment - 1

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1 Simulation results :

| $\frac{E_b}{N_o}$ in dB | Bit Error rate | $Q(\sqrt{\frac{2E_b}{N_o}})$ |
|-------------------------|----------------|------------------------------|
| 10 | 0.3298 | 0.32736 |
| -5 | 0.2141 | 0.21322 |
| 0 | 0.07927 | 0.07868 |
| 5 | 0.005090 | 0.005953 |

Table 1: results

As value of $\frac{E_b}{N_o}$ in dB increases the BER(bit error rate) decreases.
The obtained energy per information bit is T/2.

$$s(t) = x_1 \cos(2\pi f_c t) + x_2 \sin(2\pi f_c t)$$

$$variance = f_s(\frac{N_o}{2})$$

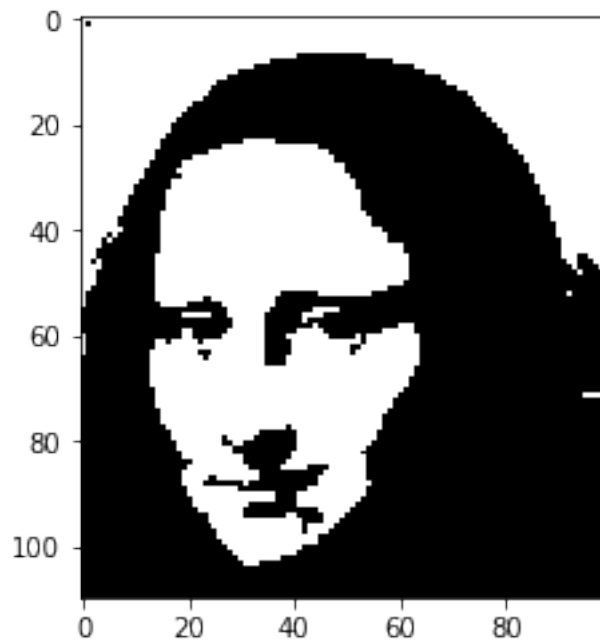
Simulation Results

January 29, 2020

```
[9]: #printing the given original MONALISA using matplotlib
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy')
print('The given image:')

plt.imshow(MonaLisa,'gray')
plt.show()
```

The given image:



```
[39]: #calculating the energy per information bit
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy') #Loads the Input
    ↳bits given as a matrix          from given .npy file
```

```

b = np.reshape(MonaLisa, (1,np.product(MonaLisa.shape)))[0] # b converts
↳ (110,100) matrix to 1d array
T=(10)**(-6)
x=np.zeros(11000) # Creates a row matrix with
↳ 11000 elements as zeroes
T_s=2*(10**(-8)) # Defining Time period
↳ of signal
f_c=2*(10**(6)) # Defining
↳ Frequency of the signal
f_s=50*(10**(6)) # Defining Sampling
↳ frequency

# This for loop encodes bits into constellations

for i in range (0,11000):
    if (b[i]==0):
        x[i]=1
    else:
        x[i]=(-1)

# Modulation
# Discrete time model
s_t=[]
for j in range (0,5500): # Creates a waveform to transmit
    for n in range(50*(j),50*(j+1)):
        s_t.append(x[2*j]*(np.cos(2*(np.
↳ pi)*(f_c)*(n*(T_s))))+(x[(2*j)+1]*(np.sin(2*(np.pi)*(f_c)*(n*(T_s))))))

# Energy Calculation per information bit
l=0
for k in range(0,275000):
    l=l+((s_t[k])**2)
m=(l/550000)*(T)
print('The energy per information bit is :',m)

```

('The energy per information bit is :', 5.000000000000075e-07)

```

[43]: #computes bit error rate,no of error bits and final recieved image for E_b/N_o
↳ = 5 in dB
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy') #Loads the Input
↳ bits given as a matrix from given .npy file

```

```

b = np.reshape(MonaLisa, (1,np.product(MonaLisa.shape)))[0] # b converts
↳ (110,100) matrix to 1d array
T=(10)**(-6)
x=np.zeros(11000) # Creates a row matrix with
↳ 11000 elements as zeroes
T_s=2*(10**(-8)) # Defining Time period
↳ of signal
f_c=2*(10**(6)) # Defining
↳ Frequency of the signal
f_s=50*(10**(6)) # Defining Sampling
↳ frequency

# This for loop encodes bits into constellations

for i in range (0,11000):
    if (b[i]==0):
        x[i]=1
    else:
        x[i]=(-1)

# Modulation
# Discrete time model
s_t=[]
for j in range (0,5500): # Creates a waveform to transmit
    for n in range(50*(j),50*(j+1)):
        s_t.append(x[2*j]*(np.cos(2*(np.
↳ pi)*(f_c)*(n*(T_s))))+(x[(2*j)+1]*(np.sin(2*(np.pi)*(f_c)*(n*(T_s))))))

# Energy Calculation per informtion bit
l=0
for k in range(0,275000):
    l=l+((s_t[k])**2)
m=(l/550000)*(T)
print('The energy per information bit is :',m)

# Calculating power spectral Density of Gaussian Random process from Obtained
↳ E_b
k=int(input('enter the value of E_b/N_o :'))
v=m/2
k_1=float(k/10)
sigma=np.sqrt((v)*(f_s)/((10)**(k_1)))

```

```

# Creates Discrete AWGN channel with mean:0 and variance:N_o/2
w=np.random.normal(0,np.sqrt(3.952),275000)

# Recieved wave form Through AWGN channel
r=s_t+w

# Demodulation by minimum distance decoding
# Creating four signals s1,s2,s3,s4 as constellation in 4-QAM modulation scheme
s1=np.zeros(275000)
s2=np.zeros(275000)
s3=np.zeros(275000)
s4=np.zeros(275000)
# u1,u2,u3,u4 are distances of r from constellations s1,s2,s3,s4 respectively
u1=np.zeros(5500)
u2=np.zeros(5500)
u3=np.zeros(5500)
u4=np.zeros(5500)
# This for loop calculate distances u1,u2,u3,u4
# Calcualting distances of 50 samples from both s_i(i=1,2,3,4) and r and
→ storing it in u1,u2,u3,u4 respectively

for e in range(0,5500):
    for n in range(50*(e),50*(e+1)):
        s1[n]=((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s2[n]=(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s3[n]=-(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s4[n]=-(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        u1[e]=u1[e]+(r[n]-s1[n])**2
        u2[e]=u2[e]+(r[n]-s2[n])**2
        u3[e]=u3[e]+(r[n]-s3[n])**2
        u4[e]=u4[e]+(r[n]-s4[n])**2

# Taking the minimum values from [u1[i],u2[i],u3[i],u4[i] ] for i from 0 to 5499
y_1=[]
for o in range(0,5500):
    y=[u1[o],u2[o],u3[o],u4[o]]
    y_1.append(min(y))

# Codes u1,u2,u3,u4 to 1,2,3,4 and stores the values in y_2

```

```

y_2=[]
for h in range(0,5500):
    if (y_1[h]== u1[h]):
        y_2.append(1)
    elif (y_1[h]==u2[h]):
        y_2.append(2)
    elif (y_1[h]==u3[h]):
        y_2.append(3)
    elif (y_1[h]==u4[h]):
        y_2.append(4)
c=np.zeros(11000)

# assigning bits to corresponding constellation points and stores it in array c
for p in range(0,5500):
    if (y_2[p]==1):
        c[2*p]=0
        c[2*(p)+1]=0
    elif (y_2[p]==2):
        c[2*p]=0
        c[2*(p)+1]=1
    elif (y_2[p]==3):
        c[2*p]=1
        c[2*(p)+1]=0
    elif (y_2[p]==4):
        c[2*p]=1
        c[2*(p)+1]=1

# Reshapes the array c to matrix(110,100)
d = c.reshape(110,100)

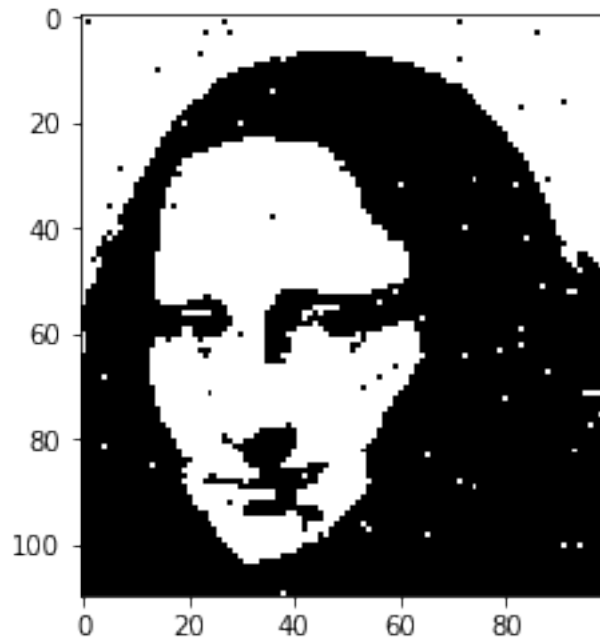
#Calculates bit error rate and no.of error bits
z_1=np.zeros(11000)
for q in range(0,11000):
    if (c[q]==b[q]):
        z_1[q]=0
    else :
        z_1[q]=1
k_1=np.count_nonzero(z_1)
k=0
for i in range(0,11000):
    k=k+z_1[i]
print('The number of error bits is:',k_1)
print('The bit error rate is:',k/11000)

# plots the final image
plt.imshow(d,'gray')

```

```
plt.show()
```

```
('The energy per information bit is :', 5.000000000000075e-07)
enter the value of E_b/N_o :5
('The number of error bits is:', 67)
('The bit error rate is:', 0.006090909090909091)
```



```
[41]: #computes bit error rate,no of error bits and final recieved image for E_b/N_o
      ↪ = 0 in dB
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy') #Loads the Input
      ↪bits given as a matrix      from given .npy file

b = np.reshape(MonaLisa, (1,np.product(MonaLisa.shape)))[0] # b converts
      ↪(110,100) matrix to 1d array
T=(10)**(-6)
x=np.zeros(11000) # Creates a row matrix with
      ↪11000 elements as zeroes
T_s=2*(10**(-8)) # Defining Time period
      ↪of signal
f_c=2*(10**(6)) # Defining
      ↪Frequency of the signal
f_s=50*(10**(6)) # Defining Sampling
      ↪frequency
```

```

# This for loop encodes bits into constellations

for i in range (0,11000):
    if (b[i]==0):
        x[i]=1
    else:
        x[i]=(-1)

# Modulation
# Discrete time model
s_t=[]
for j in range (0,5500):
    # Creates a waveform to transmit
    for n in range(50*(j),50*(j+1)):
        s_t.append(x[2*j]*(np.cos(2*(np.
→pi)*(f_c)*(n*(T_s))))+(x[(2*j)+1]*(np.sin(2*(np.pi)*(f_c)*(n*(T_s))))))

# Energy Calculation per informtion bit
l=0
for k in range(0,275000):
    l=l+((s_t[k])**2)
m=(l/550000)*(T)
print('The energy per information bit is :',m)

# Calculating power spectral Density of Gaussian Random process from Obtained
→E_b
k=int(input('enter the value of E_b/N_o :'))
v=m/2
k_1=float(k/10)
sigma=np.sqrt((v)*(f_s)/((10)**(k_1)))

# Creates Discrete AWGN channel with mean:0 and variance:N_o/2
w=np.random.normal(0,sigma,275000)

# Recieved wave form Through AWGN channel
r=s_t+w

# Demodulation by minimum distance decoding
# Creating four signals s1,s2,s3,s4 as constellation in 4-QAM modulation scheme
s1=np.zeros(275000)
s2=np.zeros(275000)

```



```

s3=np.zeros(275000)
s4=np.zeros(275000)
# u1,u2,u3,u4 are distances of r from constellations s1,s2,s3,s4 respectively
u1=np.zeros(5500)
u2=np.zeros(5500)
u3=np.zeros(5500)
u4=np.zeros(5500)
# This for loop calculate distances u1,u2,u3,u4
# Calculating distances of 50 samples from both s_i(i=1,2,3,4) and r and
→ storing it in u1,u2,u3,u4 respectively

for e in range(0,5500):
    for n in range(50*(e),50*(e+1)):
        s1[n]=((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s2[n]=(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s3[n]=-((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s4[n]=-((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        u1[e]=u1[e]+(r[n]-s1[n])**2
        u2[e]=u2[e]+(r[n]-s2[n])**2
        u3[e]=u3[e]+(r[n]-s3[n])**2
        u4[e]=u4[e]+(r[n]-s4[n])**2

# Taking the minimum values from [u1[i],u2[i],u3[i],u4[i] ] for i from 0 to 5499
y_1=[]
for o in range(0,5500):
    y=[u1[o],u2[o],u3[o],u4[o]]
    y_1.append(min(y))

# Codes u1,u2,u3,u4 to 1,2,3,4 and stores the values in y_2
y_2=[]
for h in range(0,5500):
    if (y_1[h]== u1[h]):
        y_2.append(1)
    elif (y_1[h]==u2[h]):
        y_2.append(2)
    elif (y_1[h]==u3[h]):
        y_2.append(3)
    elif (y_1[h]==u4[h]):
        y_2.append(4)
c=np.zeros(11000)

# assigning bits to corresponding constellation points and stores it in array c

```

```

for p in range(0,5500):
    if (y_2[p]==1):
        c[2*p]=0
        c[2*(p)+1]=0
    elif (y_2[p]==2):
        c[2*p]=0
        c[2*(p)+1]=1
    elif (y_2[p]==3):
        c[2*p]=1
        c[2*(p)+1]=0
    elif (y_2[p]==4):
        c[2*p]=1
        c[2*(p)+1]=1

# Reshapes the array c to matrix(110,100)
d = c.reshape(110,100)

#Calculates bit error rate and no.of error bits
z_1=np.zeros(11000)
for q in range(0,11000):
    if (c[q]==b[q]):
        z_1[q]=0
    else :
        z_1[q]=1
k_1=np.count_nonzero(z_1)
k=0
for i in range(0,11000):
    k=k+z_1[i]
print('The number of error bits is:',k_1)
print('The bit error rate is:',k/11000)

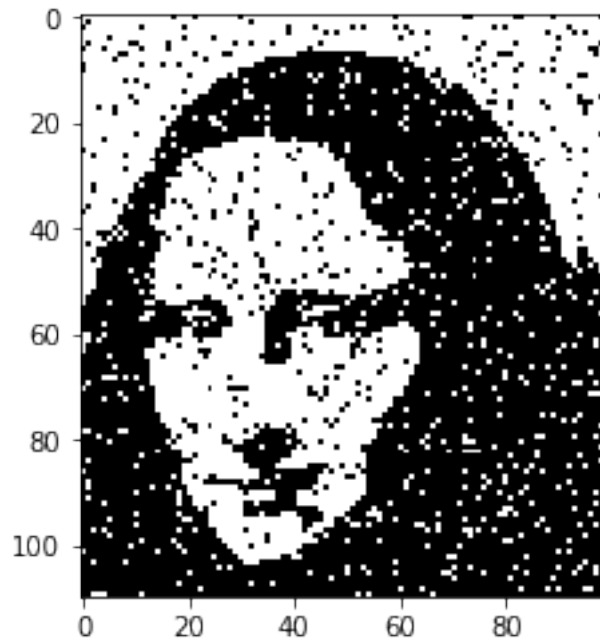
# plots the final image
plt.imshow(d,'gray')
plt.show()

```

```

('The energy per information bit is :', 5.000000000000075e-07)
enter the value of E_b/N_o :0
('The number of error bits is:', 865)
('The bit error rate is:', 0.07863636363636364)

```



```
[44]: #computes bit error rate,no of error bits and final recieved image for E_b/N_o
      ↪ = -5 in dB
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy') #Loads the Input
      ↪ bits given as a matrix      from given .npy file

b = np.reshape(MonaLisa, (1,np.product(MonaLisa.shape)))[0] # b converts
      ↪ (110,100) matrix to 1d array
T=(10)**(-6)
x=np.zeros(11000) # Creates a row matrix with
      ↪ 11000 elements as zeroes
T_s=2*(10**(-8)) # Defining Time period
      ↪ of signal
f_c=2*(10**(6)) # Defining
      ↪ Frequency of the signal
f_s=50*(10**(6)) # Defining Sampling
      ↪ frequency

# This for loop encodes bits into constellations

for i in range (0,11000):
    if (b[i]==0):
        x[i]=1
    else:
```

```

x[i]=(-1)

# Modulation
# Discrete time model
s_t=[]
for j in range (0,5500):          # Creates a waveform to transmit
    for n in range(50*(j),50*(j+1)):
        s_t.append(x[2*j]*(np.cos(2*(np.
→pi)*(f_c)*(n*(T_s))))+(x[(2*j)+1]*(np.sin(2*(np.pi)*(f_c)*(n*(T_s))))))

# Energy Calculation per informtion bit
l=0
for k in range(0,275000):
    l=l+((s_t[k])**2)
m=(l/550000)*(T)
print('The energy per information bit is :',m)

# Calculating power spectral Density of Gaussian Random process from Obtained
→E_b
k=int(input('enter the value of E_b/N_o :'))
v=m/2
k_1=float(k/10)
sigma=np.sqrt((v)*(f_s)/((10)**(k_1)))

# Creates Discrete AWGN channel with mean:0 and variance:N_o/2
w=np.random.normal(0,np.sqrt(39.5284),275000)

# Recieved wave form Through AWGN channel
r=s_t+w

# Demodulation by minimum distance decoding
# Creating four signals s1,s2,s3,s4 as constellation in 4-QAM modulation scheme
s1=np.zeros(275000)
s2=np.zeros(275000)
s3=np.zeros(275000)
s4=np.zeros(275000)
# u1,u2,u3,u4 are distances of r from constellations s1,s2,s3,s4 respectively
u1=np.zeros(5500)
u2=np.zeros(5500)
u3=np.zeros(5500)
u4=np.zeros(5500)

```

```

# This for loop calculate distances u1,u2,u3,u4
# Calculating distances of 50 samples from both s_i(i=1,2,3,4) and r and
→ storing it in u1,u2,u3,u4 respectively

for e in range(0,5500):
    for n in range(50*(e),50*(e+1)):
        s1[n]=((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s2[n]=(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s3[n]=-(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s4[n]=-(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        u1[e]=u1[e]+(r[n]-s1[n])**2
        u2[e]=u2[e]+(r[n]-s2[n])**2
        u3[e]=u3[e]+(r[n]-s3[n])**2
        u4[e]=u4[e]+(r[n]-s4[n])**2

# Taking the minimum values from [u1[i],u2[i],u3[i],u4[i] ] for i from 0 to 5499
y_1=[]
for o in range(0,5500):
    y=[u1[o],u2[o],u3[o],u4[o]]
    y_1.append(min(y))

# Codes u1,u2,u3,u4 to 1,2,3,4 and stores the values in y_2
y_2=[]
for h in range(0,5500):
    if (y_1[h]== u1[h]):
        y_2.append(1)
    elif (y_1[h]==u2[h]):
        y_2.append(2)
    elif (y_1[h]==u3[h]):
        y_2.append(3)
    elif (y_1[h]==u4[h]):
        y_2.append(4)
c=np.zeros(11000)

# assigning bits to corresponding constellation points and stores it in array c
for p in range(0,5500):
    if (y_2[p]==1):
        c[2*p]=0
        c[2*(p)+1]=0
    elif (y_2[p]==2):
        c[2*p]=0
        c[2*(p)+1]=1

```

```

        elif (y_2[p]==3):
            c[2*p]=1
            c[2*(p)+1]=0
        elif (y_2[p]==4):
            c[2*p]=1
            c[2*(p)+1]=1

# Reshapes the array c to matrix(110,100)
d = c.reshape(110,100)

#Calculates bit error rate and no.of error bits
z_1=np.zeros(11000)
for q in range(0,11000):
    if (c[q]==b[q]):
        z_1[q]=0
    else :
        z_1[q]=1
k_1=np.count_nonzero(z_1)
k=0
for i in range(0,11000):
    k=k+z_1[i]
print('The number of error bits is:',k_1)
print('The bit error rate is:',k/11000)

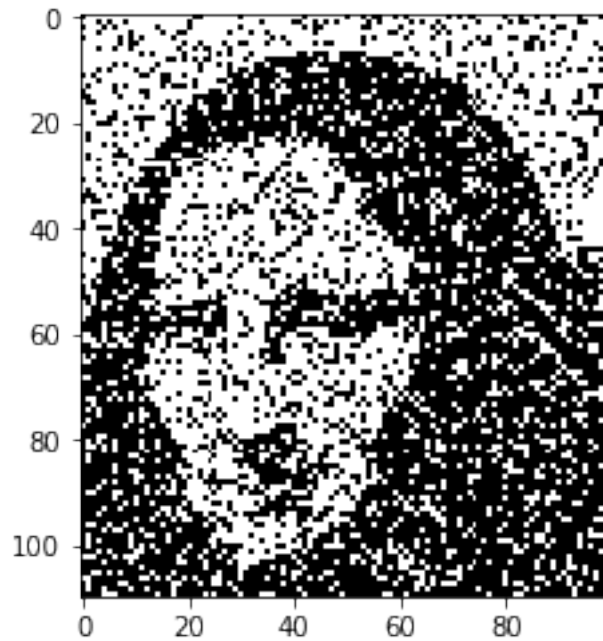
# plots the final image
plt.imshow(d,'gray')
plt.show()

```

```

('The energy per information bit is :', 5.000000000000075e-07)
enter the value of E_b/N_o :-5
('The number of error bits is:', 2362)
('The bit error rate is:', 0.21472727272727274)

```



```
[42]: #computes bit error rate,no of error bits and final recieved image for  $E_b/N_o$ 
      ↪ = -10 in dB
import numpy as np
import matplotlib.pyplot as plt
MonaLisa=np.load('binary_image.npy') #Loads the Input
      ↪ bits given as a matrix      from given .npy file

b = np.reshape(MonaLisa, (1,np.product(MonaLisa.shape)))[0] # b converts
      ↪ (110,100) matrix to 1d array
T=(10)**(-6)
x=np.zeros(11000) # Creates a row matrix with
      ↪ 11000 elements as zeroes
T_s=2*(10**(-8)) # Defining Time period
      ↪ of signal
f_c=2*(10**(6)) # Defining
      ↪ Frequency of the signal
f_s=50*(10**(6)) # Defining Sampling
      ↪ frequency

# This for loop encodes bits into constellations

for i in range (0,11000):
    if (b[i]==0):
        x[i]=1
    else:
```

```

x[i]=(-1)

# Modulation
# Discrete time model
s_t=[]
for j in range (0,5500):          # Creates a waveform to transmit
    for n in range(50*(j),50*(j+1)):
        s_t.append(x[2*j]*(np.cos(2*(np.
→pi)*(f_c)*(n*(T_s))))+(x[(2*j)+1]*(np.sin(2*(np.pi)*(f_c)*(n*(T_s))))))

# Energy Calculation per informtion bit
l=0
for k in range(0,275000):
    l=l+((s_t[k])**2)
m=(l/550000)*(T)
print('The energy per information bit is :',m)

# Calculating power spectral Density of Gaussian Random process from Obtained
→E_b
k=int(input('enter the value of E_b/N_o :'))
v=m/2
k_1=float(k/10)
sigma=np.sqrt((v)*(f_s)/((10)**(k_1)))

# Creates Discrete AWGN channel with mean:0 and variance:N_o/2
w=np.random.normal(0,sigma,275000)

# Recieved wave form Through AWGN channel
r=s_t+w

# Demodulation by minimum distance decoding
# Creating four signals s1,s2,s3,s4 as constellation in 4-QAM modulation scheme
s1=np.zeros(275000)
s2=np.zeros(275000)
s3=np.zeros(275000)
s4=np.zeros(275000)
# u1,u2,u3,u4 are distances of r from constellations s1,s2,s3,s4 respectively
u1=np.zeros(5500)
u2=np.zeros(5500)
u3=np.zeros(5500)
u4=np.zeros(5500)

```



```

# This for loop calculate distances u1,u2,u3,u4
# Calculating distances of 50 samples from both s_i(i=1,2,3,4) and r and
→ storing it in u1,u2,u3,u4 respectively

for e in range(0,5500):
    for n in range(50*(e),50*(e+1)):
        s1[n]=((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s2[n]=(np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s3[n]=-((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))+(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        s4[n]=-((np.cos(2*(np.pi)*(f_c)*(n*(T_s))))-(np.sin(2*(np.
→ pi)*(f_c)*(n*(T_s)))))
        u1[e]=u1[e]+(r[n]-s1[n])**2
        u2[e]=u2[e]+(r[n]-s2[n])**2
        u3[e]=u3[e]+(r[n]-s3[n])**2
        u4[e]=u4[e]+(r[n]-s4[n])**2

# Taking the minimum values from [u1[i],u2[i],u3[i],u4[i] ] for i from 0 to 5499
y_1=[]
for o in range(0,5500):
    y=[u1[o],u2[o],u3[o],u4[o]]
    y_1.append(min(y))

# Codes u1,u2,u3,u4 to 1,2,3,4 and stores the values in y_2
y_2=[]
for h in range(0,5500):
    if (y_1[h]== u1[h]):
        y_2.append(1)
    elif (y_1[h]==u2[h]):
        y_2.append(2)
    elif (y_1[h]==u3[h]):
        y_2.append(3)
    elif (y_1[h]==u4[h]):
        y_2.append(4)
c=np.zeros(11000)

# assigning bits to corresponding constellation points and stores it in array c
for p in range(0,5500):
    if (y_2[p]==1):
        c[2*p]=0
        c[2*(p)+1]=0
    elif (y_2[p]==2):
        c[2*p]=0
        c[2*(p)+1]=1

```

```

        elif (y_2[p]==3):
            c[2*p]=1
            c[2*(p)+1]=0
        elif (y_2[p]==4):
            c[2*p]=1
            c[2*(p)+1]=1

# Reshapes the array c to matrix(110,100)
d = c.reshape(110,100)

#Calculates bit error rate and no.of error bits
z_1=np.zeros(11000)
for q in range(0,11000):
    if (c[q]==b[q]):
        z_1[q]=0
    else :
        z_1[q]=1
k_1=np.count_nonzero(z_1)
k=0
for i in range(0,11000):
    k=k+z_1[i]
print('The number of error bits is:',k_1)
print('The bit error rate is:',k/11000)

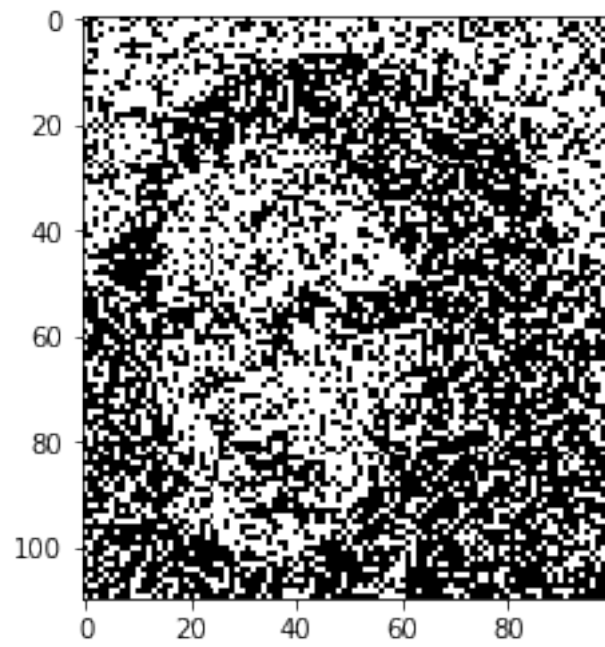
# plots the final image
plt.imshow(d,'gray')
plt.show()

```

```

('The energy per information bit is :', 5.000000000000075e-07)
enter the value of E_b/N_o :-10
('The number of error bits is:', 3525)
('The bit error rate is:', 0.32045454545454544)

```



[]: