



## Department of Computer Science and Engineering (Data Science)

### Image Processing and Computer Vision I (DJ19DSL603) Lab

#### 4: Histogram Equalisation

**Aim:** To Perform Histogram Equalisation and stretching.

**Theory:** Histogram equalization is used to enhance contrast. It is not necessary that contrast will always be increase in this. There may be some cases were histogram equalization can be worse. In that cases the contrast is decreased.

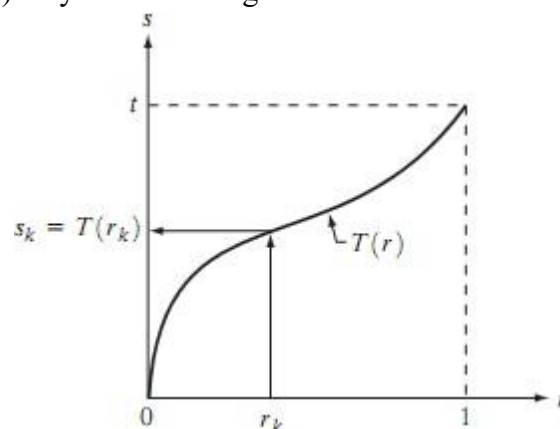
Consider for a moment continuous functions, and let the variable  $r$  represent the gray levels of the image to be enhanced. We assume that  $r$  has been normalized to the interval  $[0, 1]$ , with  $r=0$  representing black and  $r=1$  representing white. Later, we consider a discrete formulation and allow pixel values to be in the interval  $[0, L-1]$ . For any  $r$  satisfying the aforementioned conditions, we focus attention on transformations of the form

$$s = T(r) \quad 0 \leq r \leq 1 \quad \text{that produce a level } s \text{ for every pixel}$$

value  $r$  in the original image. For reasons that will become obvious shortly, we assume that the transformation function  $T(r)$  satisfies the following conditions: (a)  $T(r)$  is single-valued and monotonically increasing in the interval  $0 \leq r \leq 1$ ; and (b)  $0 \leq T(r) \leq 1$  for  $0 \leq r \leq 1$ . The requirement in (a) that  $T(r)$  be single valued is needed to guarantee that the inverse transformation will exist, and the monotonicity condition preserves the increasing order from black to white in the output image. A transformation function that is not monotonically increasing could result in at least a section of the intensity range being inverted, thus producing some inverted gray levels in the output image. Finally, condition (b) guarantees that the output gray levels will be in the same range as the input levels. Figure 4.1 gives an example of a transformation function that satisfies these two conditions. The inverse transformation from  $s$  back to  $r$  is denoted

$$r = T^{-1}(s) \quad 0 \leq s \leq 1$$

It can be shown by example that even if  $T(r)$  satisfies conditions (a) and (b), it is possible that the corresponding inverse  $T^{-1}(s)$  may fail to be single valued.



A gray-level transformation function that is both single valued and monotonically increasing.



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The gray levels in an image may be viewed as random variables in the interval  $[0, 1]$ . One of the most fundamental descriptors of a random variable is its probability density function (PDF). Let  $p_r(r)$  and  $p_s(s)$  denote the probability density functions of random variables  $r$  and  $s$ , respectively, where the subscripts on  $p$  are used to denote that  $p_r$  and  $p_s$  are different functions. A basic result from an elementary probability theory is that, if  $p_r(r)$  and  $T(r)$  are known and  $T^{-1}(s)$  satisfies condition (a), then the probability density function  $p_s(s)$  of the transformed variable  $s$  can be obtained using a rather simple formula:

$$p_s(s) = p_r(r) \left| \frac{dr}{ds} \right|$$

Thus, the probability density function of the transformed variable,  $s$ , is determined by the gray-level PDF of the input image and by the chosen transformation function. A transformation function of particular importance in image processing has the form

$$s = T(r) = \int_0^r p_r(w) dw$$

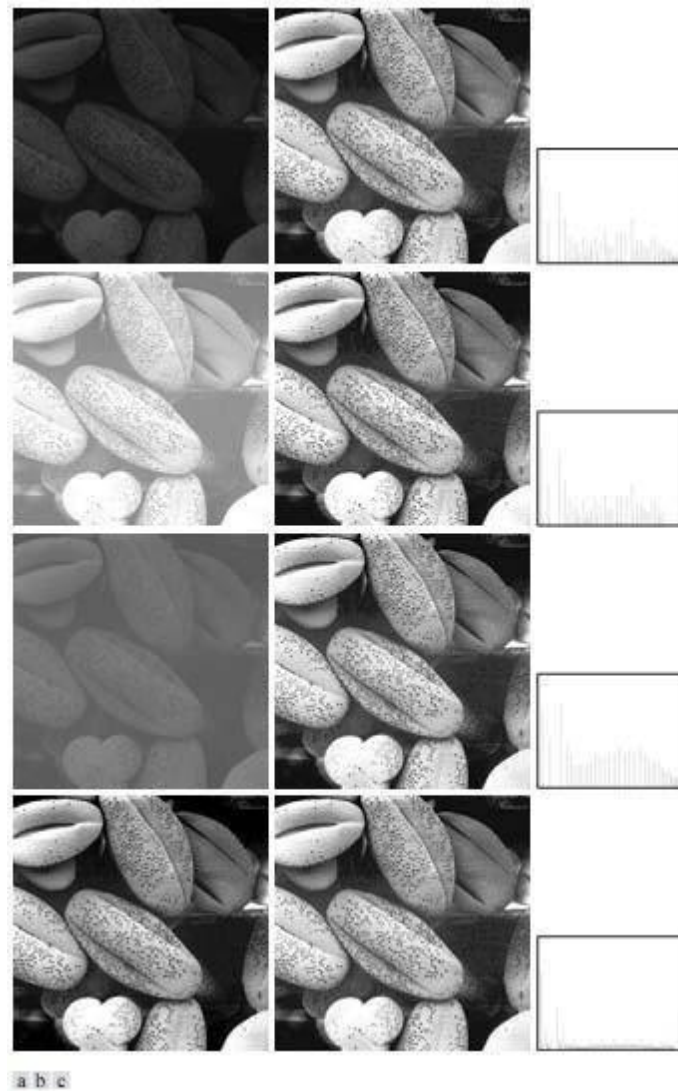
where  $w$  is a dummy variable of integration. The right side of Eq. above is recognized as the cumulative distribution function (CDF) of random variable  $r$ . Since probability density functions are always positive, and recalling that the integral of a function is the area under the function, it follows that this transformation function is single valued and monotonically increasing, and, therefore, satisfies condition (a). Similarly, the integral of a probability density function for variables in the range  $[0, 1]$  also is in the range  $[0, 1]$ , so condition (b) is satisfied as well.

Thus, a processed (output) image is obtained by mapping each pixel with level  $r_k$  in the input image into a corresponding pixel with level  $s_k$  in the output image. As indicated earlier, a plot of  $p_r(r_k)$  versus  $r_k$  is called a histogram. The transformation (mapping) is called histogram equalization or histogram linearization. It is not difficult to show that the transformation in Eq. satisfies conditions (a) and (b) stated previously. Unlike its continuous counterpart, it cannot be proved in general that this discrete transformation will produce the discrete equivalent of a uniform probability density function, which would be a uniform histogram.

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(a) Images from Fig.3 (b) Results of histogram equalization. (c) Corresponding histograms.

## Histogram Stretching

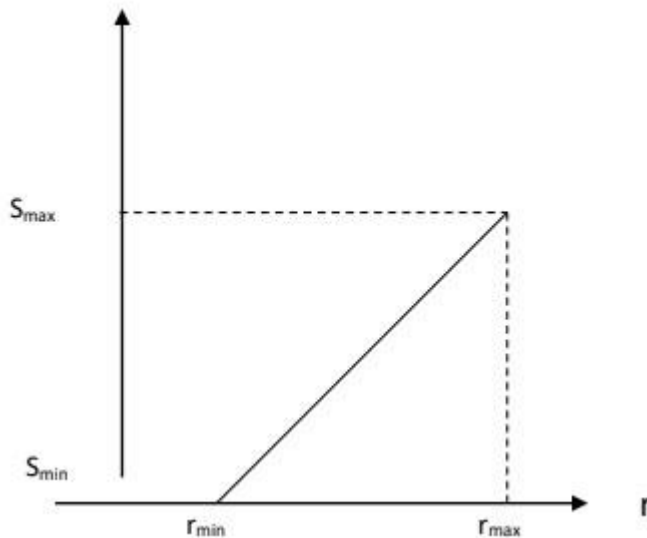
It is a method to increase the dynamic range of the image. Here we do not alter the basic shape of the histogram, but we spread it so as to cover the entire dynamic range. We do this by using a straight line equation having a slope  $(s_{\max} - s_{\min}) / (r_{\max} - r_{\min})$



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$s_{max}$  = Maximum grey level of output image

$s_{min}$  = Minimum grey level of output image.

$r_{max}$  = Maximum grey level of input image

$r_{min}$  = Minimum grey level of input image.

$$S = T(r) = \frac{(s_{max} - s_{min})}{(r_{max} - r_{min})} (r - r_{min}) + s_{min}$$

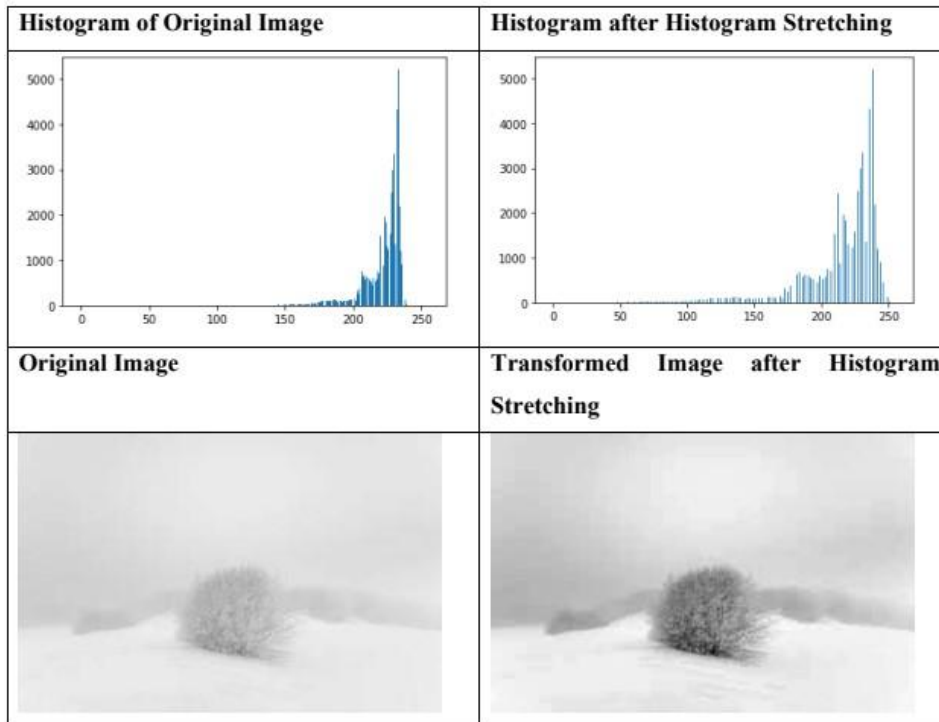
This transformation stretches and shifts the grey level range of input image to occupy the entire dynamic range ( $s_{max}$ ,  $s_{min}$ ).



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The steps followed in histogram equalisation are as followed:

1. Calculate the histogram of the image.
2. Calculate the probability mass function. ( $PMF = [\text{histogram value}] / 255$ )
3. Calculate the cumulative distribution function.
4. Find the new gray value of each original gray value by multiplying the found CDF with 255.
5. Convert the image using this new found gray level value for each pixel.

#### Lab Assignments to complete in this session

**Problem Statement:** Develop a Python program utilizing the OpenCV library to manipulate images from the Fashion MNIST digits dataset. The program should address the following tasks:

1. Read random image(s) from the MNIST fashion dataset.
2. **Dataset Link:** [Fashion MNIST Github](#)
3. Display the before & after image(s) used in the task below.
4. Perform Histogram equalisation by following the steps above.
5. Show the difference in the histograms of the images used and thus produced.
6. Note the difference and provide a conclusion of why the image contrast increased or decreased for the image(s) used.



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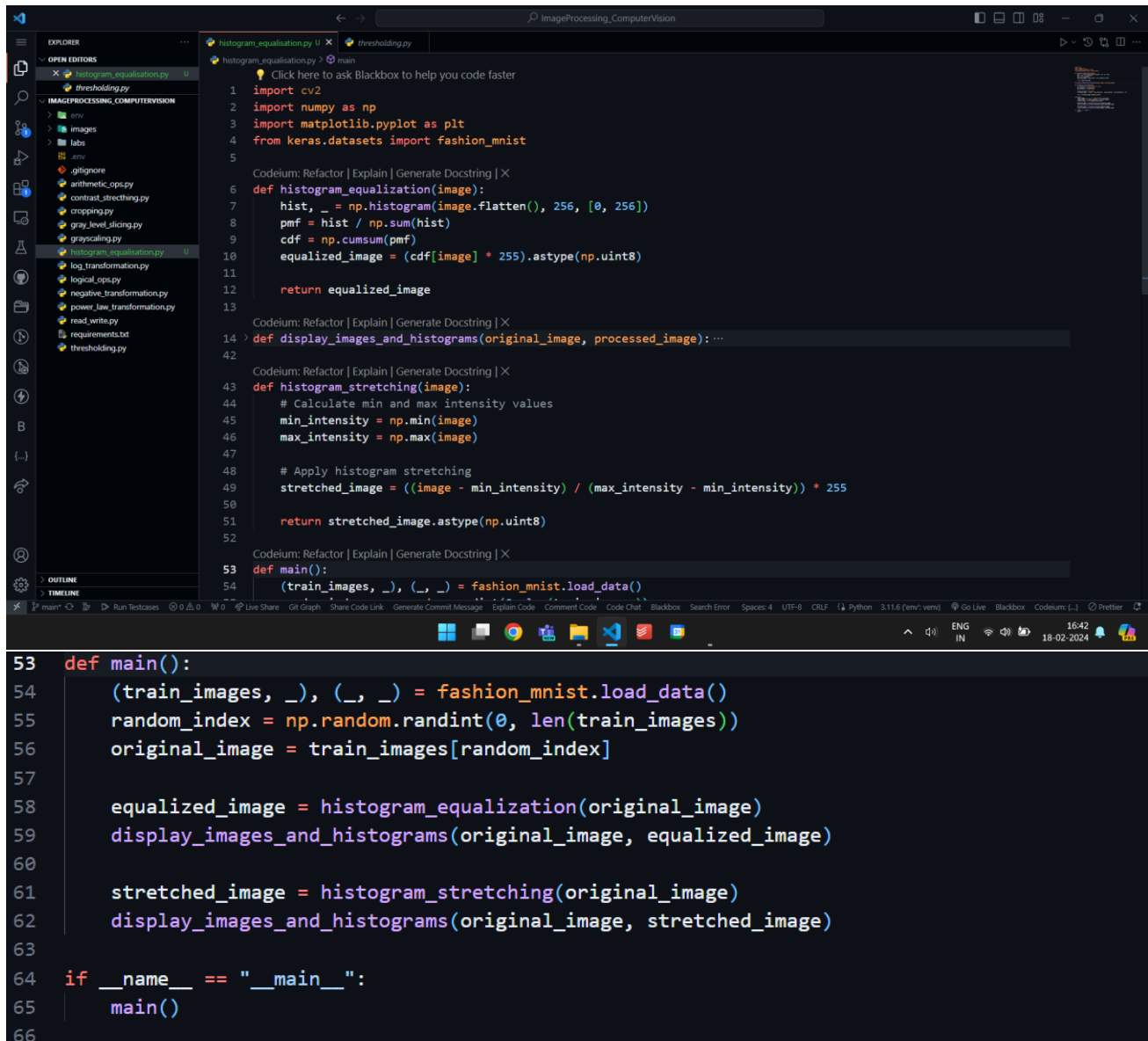
7. Perform Histogram stretching to increase contrast. Observe the original dynamic range is then stretched to (0-255). Thus, the dynamic range of the values increases while the shape of the histogram is maintained.

The solution to the operations performed must be produced by scratch coding without the use of built-in OpenCV methods.





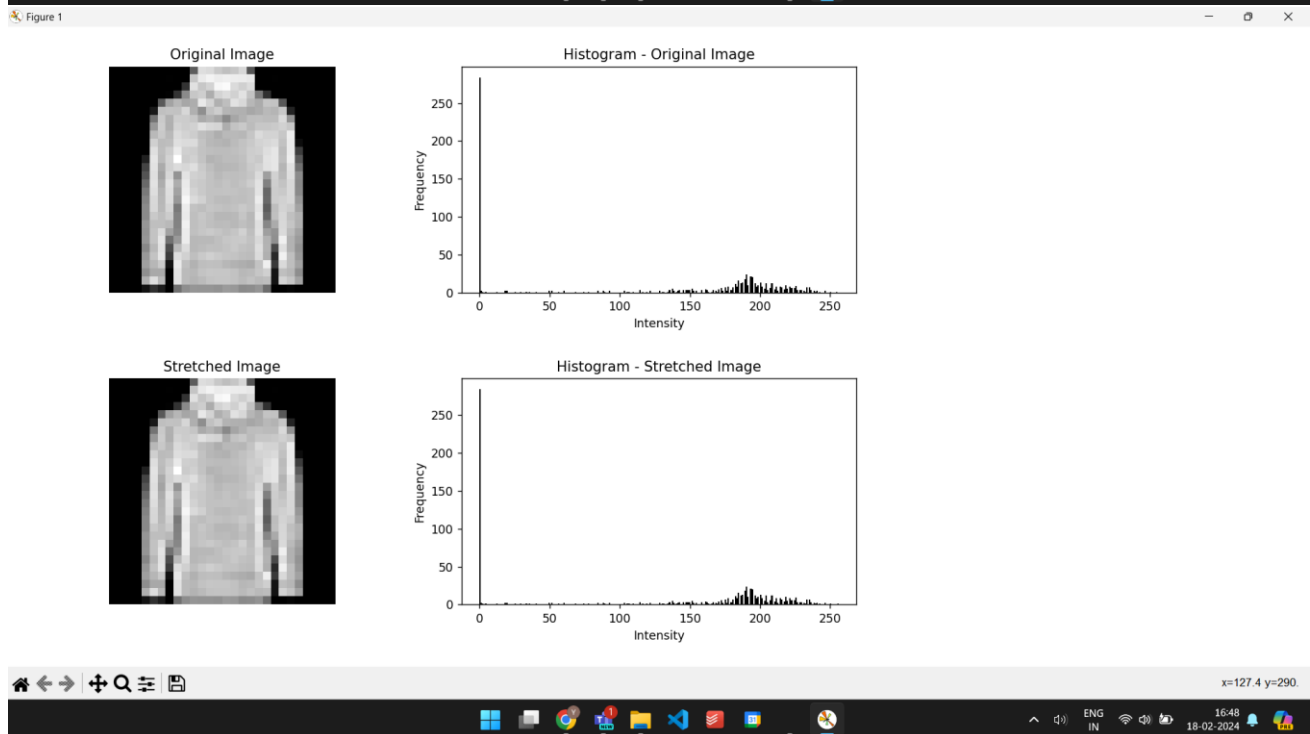
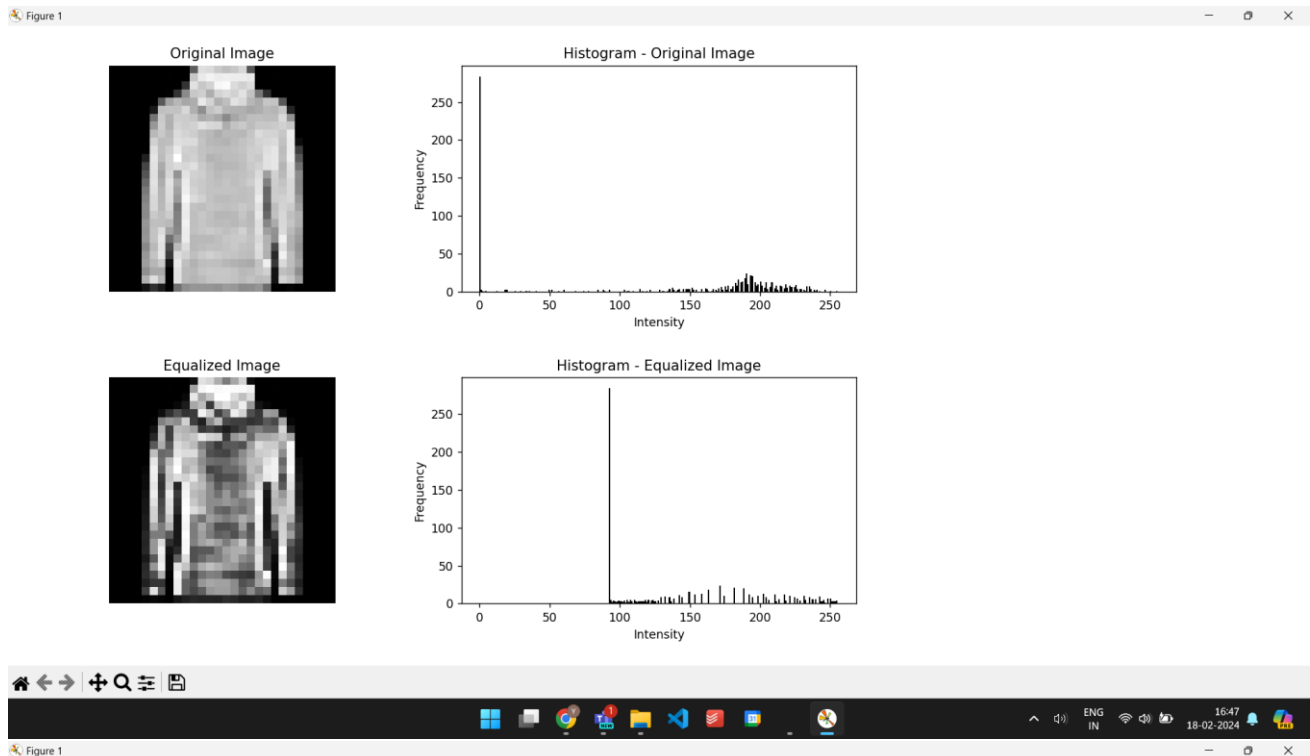
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```
1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4 from keras.datasets import fashion_mnist
5
6 def histogram_equalization(image):
7     hist, _ = np.histogram(image.flatten(), 256, [0, 256])
8     pmf = hist / np.sum(hist)
9     cdf = np.cumsum(pmf)
10    equalized_image = (cdf[image] * 255).astype(np.uint8)
11
12    return equalized_image
13
14 def display_images_and_histograms(original_image, processed_image): ...
15
16 def histogram_stretching(image):
17     # Calculate min and max intensity values
18     min_intensity = np.min(image)
19     max_intensity = np.max(image)
20
21     # Apply histogram stretching
22     stretched_image = ((image - min_intensity) / (max_intensity - min_intensity)) * 255
23
24     return stretched_image.astype(np.uint8)
25
26 def main():
27     (train_images, _), (_, _) = fashion_mnist.load_data()
28
29     random_index = np.random.randint(0, len(train_images))
30     original_image = train_images[random_index]
31
32     equalized_image = histogram_equalization(original_image)
33     display_images_and_histograms(original_image, equalized_image)
34
35     stretched_image = histogram_stretching(original_image)
36     display_images_and_histograms(original_image, stretched_image)
37
38 if __name__ == "__main__":
39     main()
```



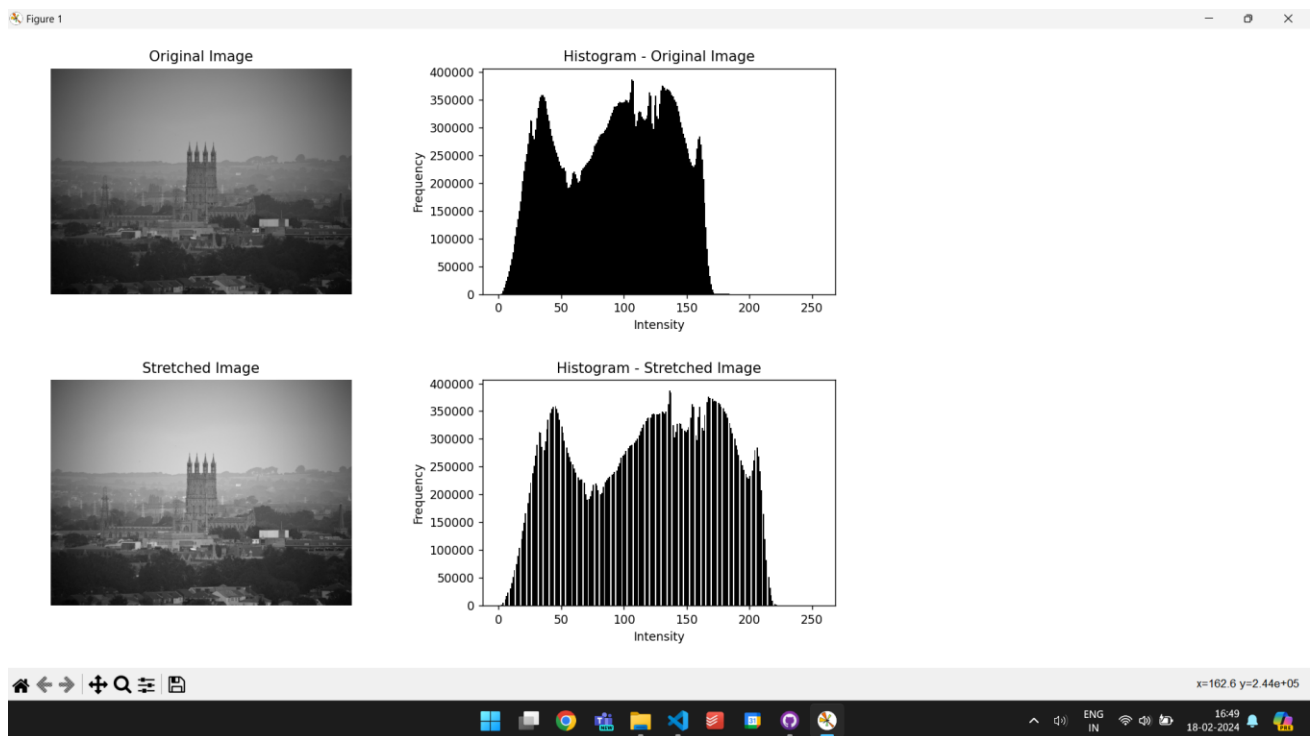
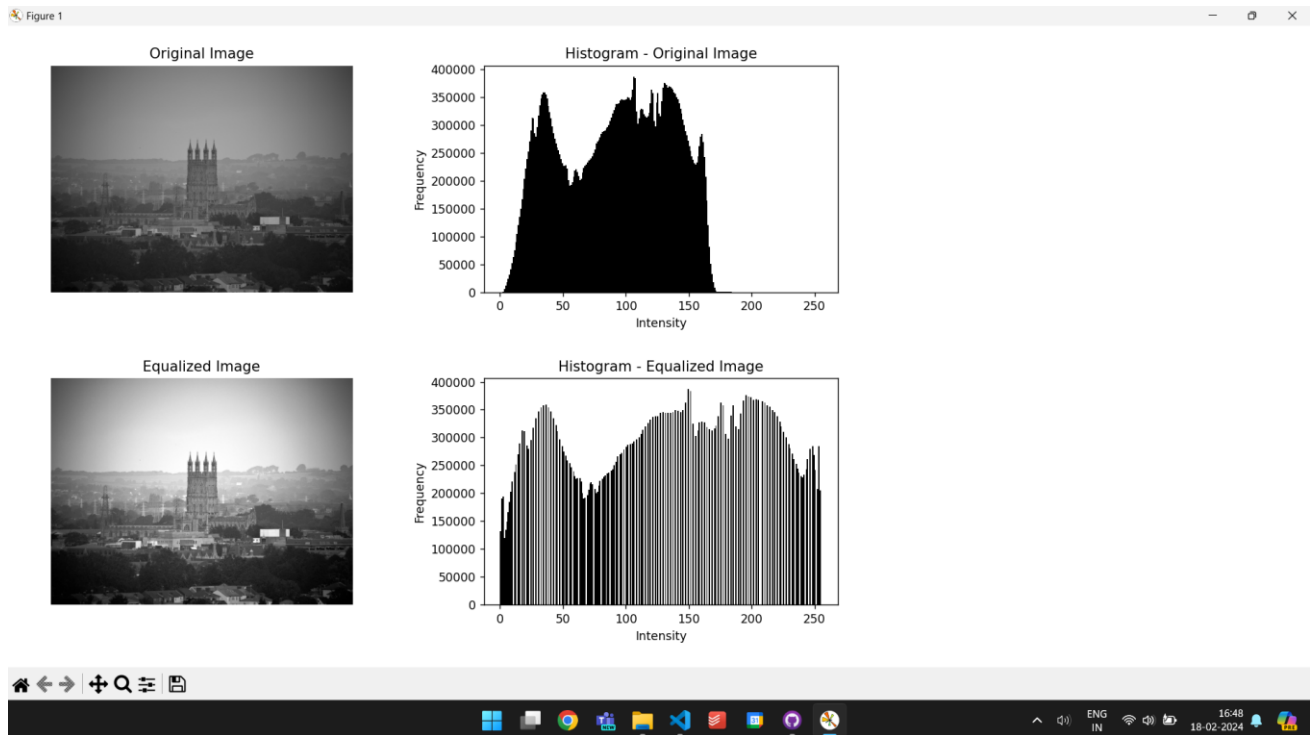
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