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In[1]:= Clear[f1, g1, g2, g3, g4, g5, g6, g7]
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$$f1 = -2 \cos[x1] + 6 x1^2 x2 - 0.75 x2$$

$$g1 = 4 x1^2 + 10 x1 x2 - 1$$

$$g2 = -4 x1 + 6 x2^2 - 14$$

$$g3 = 6 x1^2 + 5 x1 + 12 x2 - 20$$

$$g4 = -2 - x1$$

$$g5 = x1 - 2$$

$$g6 = -2 - x2$$

$$g7 = x2 - 2$$

$$\text{Out[2]} = -0.75 x2 + 6 x1^2 x2 - 2 \cos[x1]$$

$$\text{Out[3]} = -1 + 4 x1^2 + 10 x1 x2$$

$$\text{Out[4]} = -14 - 4 x1 + 6 x2^2$$

$$\text{Out[5]} = -20 + 5 x1 + 6 x1^2 + 12 x2$$

$$\text{Out[6]} = -2 - x1$$

$$\text{Out[7]} = -2 + x1$$

$$\text{Out[8]} = -2 - x2$$

$$\text{Out[9]} = -2 + x2$$

$$L = -f1 + u1 (g1 + s1^2) + u2 (g2 + s2^2) + u3 (g3 + s3^2) + \\ u4 (-2 - x1 + s4^2) + u5 (x1 - 2 + s5^2) + u6 (-2 - x2 + s6^2) + u7 (x2 - 2 + s7^2) ;$$

$$lx1 = D[L, x1]$$

$$lx2 = D[L, x2]$$

$$lu1 = D[L, u1]$$

$$lu2 = D[L, u2]$$

$$lu3 = D[L, u3]$$

$$lu4 = D[L, u4]$$

$$lu5 = D[L, u5]$$

$$lu6 = D[L, u6]$$

$$lu7 = D[L, u7]$$

$$ls1 = D[L, s1]$$

$$ls2 = D[L, s2]$$

$$ls3 = D[L, s3]$$

$$ls4 = D[L, s4]$$

$$ls5 = D[L, s5]$$

$$ls6 = D[L, s6]$$

$$ls7 = D[L, s7]$$

$$\text{Out}[11]= -4 u2 - u4 + u5 + u3 (5 + 12 x1) - 12 x1 x2 + u1 (8 x1 + 10 x2) - 2 \text{Sin}[x1]$$

$$\text{Out}[12]= 0.75 + 12 u3 - u6 + u7 + 10 u1 x1 - 6 x1^2 + 12 u2 x2$$

$$\text{Out}[13]= -1 + s1^2 + 4 x1^2 + 10 x1 x2$$

$$\text{Out}[14]= -14 + s2^2 - 4 x1 + 6 x2^2$$

$$\text{Out}[15]= -20 + s3^2 + 5 x1 + 6 x1^2 + 12 x2$$

$$\text{Out}[16]= -2 + s4^2 - x1$$

$$\text{Out}[17]= -2 + s5^2 + x1$$

$$\text{Out}[18]= -2 + s6^2 - x2$$

$$\text{Out}[19]= -2 + s7^2 + x2$$

$$\text{Out}[20]= 2 s1 u1$$

$$\text{Out}[21]= 2 s2 u2$$

$$\text{Out}[22]= 2 s3 u3$$

$$\text{Out}[23]= 2 s4 u4$$

$$\text{Out}[24]= 2 s5 u5$$

$$\text{Out}[25]= 2 s6 u6$$

$$\text{Out}[26]= 2 s7 u7$$

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In[48]:= L = -f1 + u1 (g1 + s1) + u2 (g2 + s2) + u3 (g3 + s3) +
          u4 (-2 - x1 + s4) + u5 (x1 - 2 + s5) + u6 (-2 - x2 + s6) + u7 (x2 - 2 + s7);
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lx1 = D[L, x1];
lx2 = D[L, x2];
lu1 = D[L, u1];
lu2 = D[L, u2];
lu3 = D[L, u3];
lu4 = D[L, u4];
lu5 = D[L, u5];
lu6 = D[L, u6];
lu7 = D[L, u7];
ls1 = D[L, s1];
ls2 = D[L, s2];
ls3 = D[L, s3];
ls4 = D[L, s4];
ls5 = D[L, s5];
ls6 = D[L, s6];
ls7 = D[L, s7];
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In[44]:= case1 =
  NSolve[{lx1 == 0, lx2 == 0, lu1 == 0, lu2 == 0, lu3 == 0, lu4 == 0, lu5 == 0, lu6 == 0, lu7 == 0} /.
    {u1 → 0, s2 → 0, s3 → 0, u4 → 0, u5 → 0, u6 → 0, u7 → 0}, {x1, x2, s1, u2, u3, s4, s5, s6, s7}]
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Out[44]= {{x1 → -2.65461, x2 → -0.750728, s1 → -47.1168, u2 → -4.798,
  u3 → -0.141006, s4 → -0.654612, s5 → 4.65461, s6 → 1.24927, s7 → 2.75073},
 {x1 → 0.191234, x2 → 1.5687, s1 → -2.14616, u2 → -0.278601, u3 → 0.392827,
  s4 → 2.19123, s5 → 1.80877, s6 → 3.5687, s7 → 0.431299},
 {x1 → 2.31164, x2 → -1.96836, s1 → 25.1266, u2 → -2.29231, u3 → -1.90274,
  s4 → 4.31164, s5 → -0.31164, s6 → 0.0316437, s7 → 3.96836},
 {x1 → -1.51493, x2 → 1.15038, s1 → 9.24745, u2 → -0.771472, u3 → 1.97249,
  s4 → 0.485072, s5 → 3.51493, s6 → 3.15038, s7 → 0.849617}}
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In[45]:= case2 =
  NSolve[{lx1 == 0, lx2 == 0, lu1 == 0, lu2 == 0, lu3 == 0, lu4 == 0, lu5 == 0, lu6 == 0, lu7 == 0} /.
    {u1 → 0, s2 → 0, s5 → 0, u4 → 0, u3 → 0, u6 → 0, u7 → 0}, {x1, x2, s1, s3, u2, u5, s4, s6, s7}]
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Out[45]= {{x1 → 2., x2 → -1.91485, s1 → 23.2971, s3 → 8.97825,
  u2 → -1.01183, u5 → -48.1852, s4 → 4., s6 → 0.0851458, s7 → 3.91485},
 {x1 → 2., x2 → 1.91485, s1 → -53.2971, s3 → -36.9783, u2 → 1.01183,
  u5 → 51.8224, s4 → 4., s6 → 3.91485, s7 → 0.0851458}}
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In[47]:= case3 =
  NSolve[{lx1 == 0, lx2 == 0, lu1 == 0, lu2 == 0, lu3 == 0, lu4 == 0, lu5 == 0, lu6 == 0, lu7 == 0} /.
    {u5 -> 0, s1 -> 0, s2 -> 0, u4 -> 0, u3 -> 0, u6 -> 0, u7 -> 0}, {x1, x2, s5, s3, u2, u1, s4, s6, s7}]

Out[47]= {{x1 -> 6.49039, x2 -> -2.58075, s5 -> -4.49039, s3 -> -234.234,
  u2 -> -35.6913, u1 -> -13.1475, s4 -> 8.49039, s6 -> -0.580748, s7 -> 4.58075},
 {x1 -> 0.0638196, x2 -> 1.54139, s5 -> 1.93618, s3 -> 1.1598, u2 -> -0.0416993,
  u1 -> 0.0716637, s4 -> 2.06382, s6 -> 3.54139, s7 -> 0.458611},
 {x1 -> -0.0649659, x2 -> -1.51328, s5 -> 2.06497, s3 -> 38.4589, u2 -> 0.0426964,
  u1 -> -0.0779864, s4 -> 1.93503, s6 -> 0.486718, s7 -> 3.51328},
 {x1 -> -2.32257, x2 -> 0.885974, s5 -> 4.32257, s3 -> -11.3849, u2 -> 4.66124,
  u1 -> 0.772451, s4 -> -0.322575, s6 -> 2.88597, s7 -> 1.11403}}

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