

a) Calculate the relative error

$$\text{Absolute error} = \text{Measured reading} - \text{True reading}$$

$$\text{Absolute error} = 1.46 - 1.5$$

$$\text{Absolute error} = -0.04 \text{ V}$$

Thus,

$$\text{Relative error} = \frac{\text{Absolute error}}{\text{true value}}$$

$$\text{Relative error} = -\frac{0.04}{1.5}$$

$$\text{Relative error} = -0.026$$

$$\text{Relative error} = 2.67\%$$

### **Sensitivity:-**

- It is defined as the ratio of the changes in the output of an instrument to a change in the value of the quantity being measured.
- It denotes the smallest change in the measured variable to which the instrument responds.

Sensitivity = change in output/unit change in input =  $\Delta\text{output}/\Delta\text{input}$

Given :- linear relationship between temperature and resistance

For a change in temperature of  $30^{\circ}\text{C}$ , the change in resistance is 7 ohm. Hence the measurement sensitivity is equal to  $7/30 = 0.233 \text{ ohms}/^{\circ}\text{C}$

Answer:-

Given that:-

→ The temperature ' $T_x$ ' at an altitude of ' $x$ ' meter and relation  $T_x = T_0 - 0.01x$

• We know that

→ Relation for temperature is :-

$$T_r = \frac{T_x}{1 + \tau D}$$

$$= \frac{T_0 - 0.01x}{1 + \tau D}$$

$$T_r = \frac{10 - 0.01x}{1 + 1.5D}$$

→ At  $x = 5t$

$$T_r = \frac{10 - 0.01(5t)}{1 + 1.5D}$$

$$T_r = \frac{10 - 0.05t}{1 + 15D}$$

→ Now, by solving, we get

→ Complementary function :-

$$T_{xf} = Ce^{-t/15}$$

particular integral :-

$$T_{rpi} = 10 - 0.05(t - 15)$$

thus,

$$T_r = T_{xf} + T_{rpi}$$

$$T_r = Ce^{-t/15} + 10 - 0.05(t - 15)$$

Evaluate the value of 'c', by Applying the boundary conditions.

$$\text{let, } t = 0$$

$$T_r = 10$$

$$T_r = Ce^{-t/15} + 10 - 0.05(t-15)$$

$$10 = Ce^{-0/15} + 10 - 0.05(0-15)$$

$$C = -0.75$$

→ Substitute the 'C' value in above

$$T_r = -0.75e^{-t/15} + 10 - 0.05(t-15)$$

$$T_r = 10 - 0.75e^{-t/15} - 0.05(t-15)$$

a) Given that:-

→ The balloon is released at time zero, and thereafter rises upwards at a velocity = 5 metres/second.

→ Tabulated the value of temperature for different values of 't'

| Time | Altitude | Temperature reading | Temperature error |
|------|----------|---------------------|-------------------|
| 0    | 0        | 10                  | 0                 |
| 10   | 50       | 9.86                | 0.36              |
| 20   | 100      | 9.55                | 0.55              |
| 30   | 150      | 9.15                | 0.65              |
| 40   | 200      | 8.70                | 0.70              |
| 50   | 250      | 8.22                | 0.72              |

b) Given that:-

→ The temperature does the balloon report an altitude = 5000 metres.

→ Where, 5000m,  $t = 1000s$ .

$$\begin{aligned}
 T_r &= 10 - 0.75e^{-t/15} - 0.05(t-15) \\
 &= 10 - 0.75e^{-1000/15} - 0.05(1000 - 15)
 \end{aligned}$$

$$T_r = -39.25^{\circ}\text{C}$$