

Assignment 2

AI1110: Probability and Random Variables
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12.13.6.18: Question. Consider the experiment of throwing a die, if a multiple of 3 comes up, throw the die again and if any other number comes, toss a coin. Find the conditional probability of the event 'the coin shows a tail', given that 'at least one die shows a 3'.

Answer: 0

Solution: The sample space for the given experiment is:

$$S = \{(3, 1), (3, 2), \dots, (3, 6)(6, 1), \dots, (6, 6), (1, T), (2, T), (4, T), (5, T)(1, H), (2, H), (4, H), (5, H)\} \quad (1)$$

Now,

1) Let A be an event such that 'The coin shows a tail' .

$$A = \{(1, T), (2, T), (4, T), (5, T)\} \quad (2)$$

2) Let B be an event such that 'At least one die shows a 3' .

$$B = \{(3, 1), (3, 2), (3, 3), (3, 4), (3, 5), (3, 6), (6, 3)\} \quad (3)$$

To Find,

$$\Pr(A | B) \quad (4)$$

And we know that,

$$\Pr(A | B) = \frac{\Pr(AB)}{\Pr(B)} \quad (5)$$

From (2) and (3),

$$\Rightarrow AB = \phi \quad (6)$$

$$\Rightarrow \Pr(AB) = 0 \quad (7)$$

Putting the value from (7) in (5),

$$\Pr(A | B) = \frac{(0)}{\Pr(B)} \quad (8)$$

$$\Rightarrow \Pr(A | B) = 0 \quad (9)$$