

# PLANNING AND SEARCH

## CLASSICAL PLANNING

# Outline

- ◇ Search vs. planning
- ◇ STRIPS operators
- ◇ PDDL
- ◇ Forward (progression) state-space search
- ◇ Backward (regression) relevant-states search

# Planning

**Planning** is the process of computing several steps of a problem-solving procedure before executing any of them

This problem **can** be solved by search

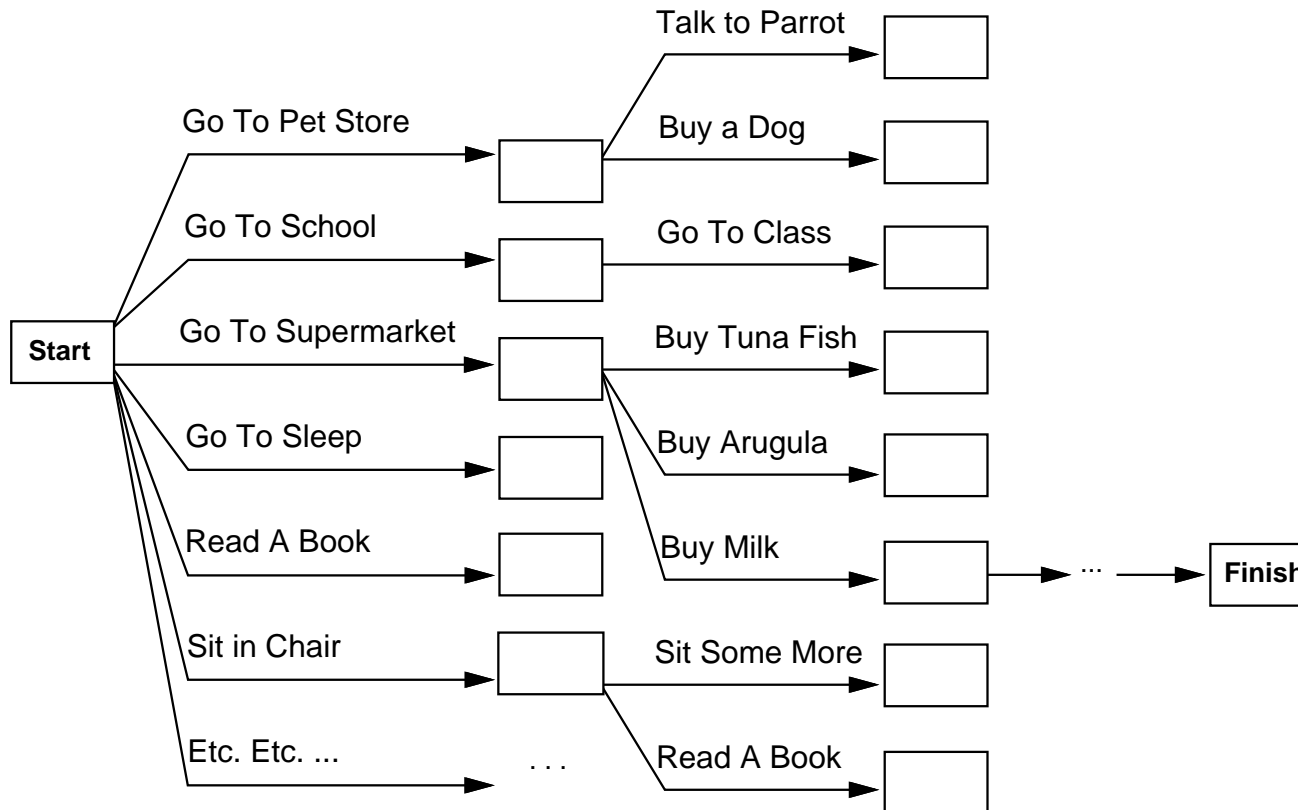
The main difference between search and planning is the representation of states

In search, states are represented as a single entity (which may be quite a complex object, but its internal structure is not used by the search algorithm)

In planning, states have structured representations (collections of properties) which are used by the planning algorithm

# Search vs. planning

Consider the task *get milk, bananas, and a cordless drill*  
Standard search algorithms seem to fail miserably:



After-the-fact heuristic/goal test inadequate

## Search vs. planning contd.

Planning systems do the following:

- 1) open up action and goal representation to allow selection
- 2) divide-and-conquer by subgoaling
- 3) relax requirement for sequential construction of solutions

	Search	Planning
States	data structures	Logical sentences
Actions	code	Preconditions/outcomes
Goal	code	Logical sentence (conjunction)
Plan	Sequence from $S_0$	Constraints on actions

# Classical planning

Assumptions are:

- (1) Environment is deterministic
- (2) Environment is observable
- (3) Environment is static (it only in response to the agent's actions)

# STRIPS operators

STRIPS planning language (Fikes and Nilsson, 1971)

Tidily arranged actions descriptions, restricted language

ACTION:  $Buy(x)$

PRECONDITION:  $At(p), Sells(p, x)$

EFFECT:  $Have(x)$

[Note: this abstracts away many important details!]

Restricted language  $\Rightarrow$  efficient algorithm

Precondition: conjunction of positive literals

Effect: conjunction of literals

$At(p) \ Sells(p, x)$

**Buy(x)**

$Have(x)$

# PDDL

Planning Domain Definition Language

A bit more relaxed than STRIPS

Preconditions and goals can contain negative literals

ACTION:  $Buy(x)$

PRECONDITION:  $At(p), Sells(p, x)$

EFFECT:  $Have(x)$

is called an **action schema**



## Planning domain

States are sets of fluents (ground, functionless atoms). Fluents which are not mentioned are false (this is called closed world assumption).

$$a \in \text{ACTIONS}(s) \text{ iff } s \models \text{PRECOND}(a)$$

$$\text{RESULT}(s, a) = (s - \text{DEL}(a)) \cup \text{ADD}(a)$$

where  $\text{DEL}(a)$  is the list of literals which appear negatively in the effect of  $a$ , and  $\text{ADD}(a)$  is the list of positive literals in the effect of  $a$ .

## Example (slightly modified)

ACTION:  $Buy(x)$

PRECONDITION:  $At(p), Sells(p, x), Have(Money)$

EFFECT:  $Have(x), \neg Have(Money)$

$DEL(Buy(Jaguar)) = \{Have(Money)\}$

$ADD(Buy(Jaguar)) = \{Have(Jaguar)\}$

If  $s = \{At(JDealer), Sells(JDealer, Jaguar), Blue(Sky), Have(Money)\}$ ,

$Buy(Jaguar) \in ACTIONS(s)$

$RESULT(s, Buy(Jaguar)) = (s - \{Have(Money)\}) \cup \{Have(Jaguar)\}$

$= \{At(JDealer), Sells(JDealer, Jaguar), Blue(Sky), Have(Jaguar)\}$

## Planning problem

Planning problem = planning domain + initial state + goal

Goal is a conjunction of literals:  $Have(Jaguar) \wedge \neg At(Jail)$

Can solve planning problem using search

## Backward and forward search

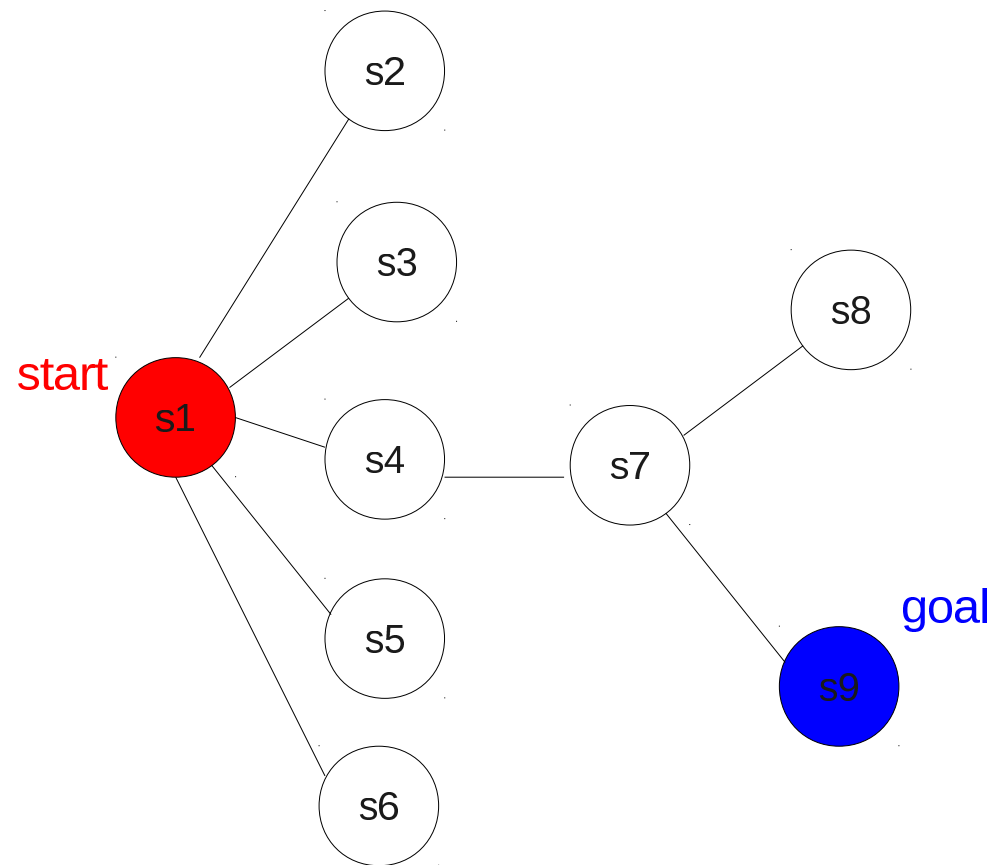
So far in the search lectures we only looked at forward search from the initial state to a goal state

Nothing prevented us from searching from a goal state to the initial state

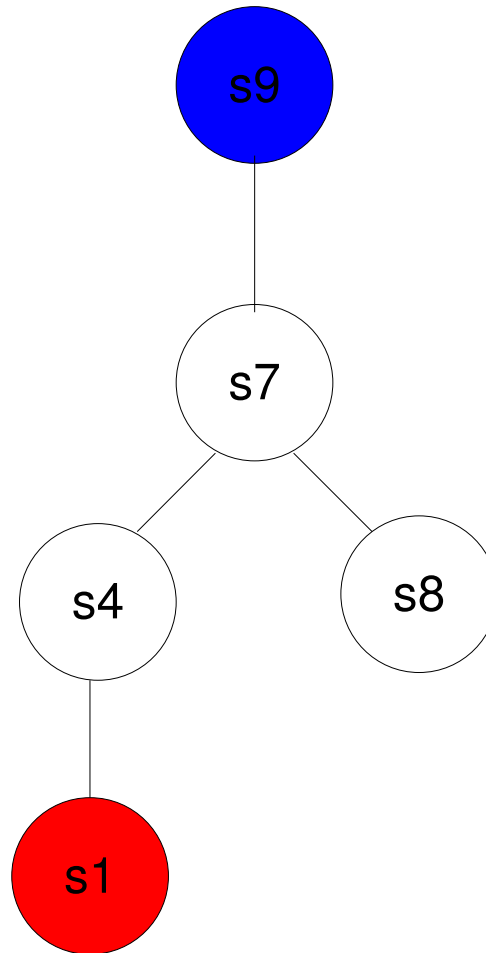
Sometimes given the branching factor it is more efficient to search backward

Motivating example: imagine trying to figure out how to get to some small place with few traffic connections from somewhere with a lot of traffic connections

# Example



## Example: backward search tree



## Backward search

Can use any search method, breadth-first or depth-first or iterative deepening or  $A^*$ ...

If there are several goal states, search backwards from each in turn

Planning can use both forward and backward search (progression and regression planning)

## Simple example of forward planning

Planning domain:

Predicates: *At*, *Sells*, *Have*

Two action schemas:

ACTION: *Buy*( $x$ )

PRECONDITION:  $At(p), Sells(p, x), Have(Money)$

EFFECT:  $Have(x), \neg Have(Money)$

ACTION: *Go*( $x, y$ )

PRECONDITION:  $At(x)$

EFFECT:  $At(y), \neg At(x)$



## Simple example of forward planning 2

Planning problem: planning domain above plus

Objects: *Money*, *J* (for Jaguar), *Home*, *G* (for Garage)

Initial state:  $At(Home) \wedge Have(Money) \wedge Sells(G, J)$

Goal state:  $Have(J)$

Note: state descriptions are always ground (no variables). Goal description may have variables:  $At(x) \wedge Have(y)$ . A property with a variable such as  $At(x)$  is satisfied at a state if there is a way of substituting an object for  $x$  so that the resulting formula is true in the state. An atomic ground formula  $At(Home)$  is true iff it is in the state description. A negation of a ground atom  $\neg At(G)$  is true iff the atom  $At(G)$  is not in the state description.

## Simple example of forward planning 3

-----		-----		-----
At(Home)	Go(Home,G)	At(Garage)	Buy(J)	At(Garage)
Have(Money)	----->	Have(Money)	----->	Have(J)
Sells(G,J)		Sells(G,J)		Sells(G,J)
-----		-----		-----

Go(Home,Home)  
applicable and  
does not change  
the state)

Go(Garage,Home) and  
Go(Garage,Garage)  
also available

Buy(x) not  
available for  
any x (don't have  
Sells(Home, x))

## Backward (regression) planning

Also called **relevant-states** search

Start at the goal state(s) and do **regression** (go back).

To be precise, there we start with a ground goal description  $g$  which describes a set of states (all those where  $Have(J)$  holds but  $Have(Money)$  may or may not hold, for example).

## Backward (regression) planning 2

Given a goal description  $g$  and a ground action  $a$ , the regression from  $g$  over  $a$  gives a state description  $g'$ :

$$g' = (g - \text{ADD}(a)) \cup \{\text{PRECOND}(a)\}$$

For example, if the goal is  $Have(J)$

$$\begin{aligned} g' &= (\{Have(J)\} - \{Have(J)\}) \cup \\ &\{At(p), Sells(p, J), Have(Money)\} = \\ &\{At(p), Sells(p, J), Have(Money)\} \end{aligned}$$

note that  $g'$  is partially uninstantiated ( $p$  is a free variable). In our example, there is only one match for  $p$ , namely  $G$ , but in general there may be several.

## Backward (regression) planning 3

Which actions to regress over?

**Relevant** actions: have an effect which is in the set of goal elements and no effect which negates an element of the goal.

For example, *Buy(Jaguar)* is a relevant action.

Search backwards from  $g$ , remembering the actions and checking whether we reached an expression applicable to the initial state.

## Simple example of backward planning

Have(J)      Buy(J)  
                  <-----

At(x)      Go(y,x)  
                  <-----  
 Have(Money)  
 Sells(x,J)

At(y)  
 Have(Money)  
 Sells(x,J)

Does not match  
 the initial  
 state yet

Matches the  
 initial state  
 with y/Home and x/G

## Slightly more elaborate example

if the goal is  $Have(Jaguar) \wedge \neg At(Jail)$ ,

$$g' = (\{Have(Jaguar), \neg At(Jail)\} - \{Have(Jaguar)\}) \cup$$

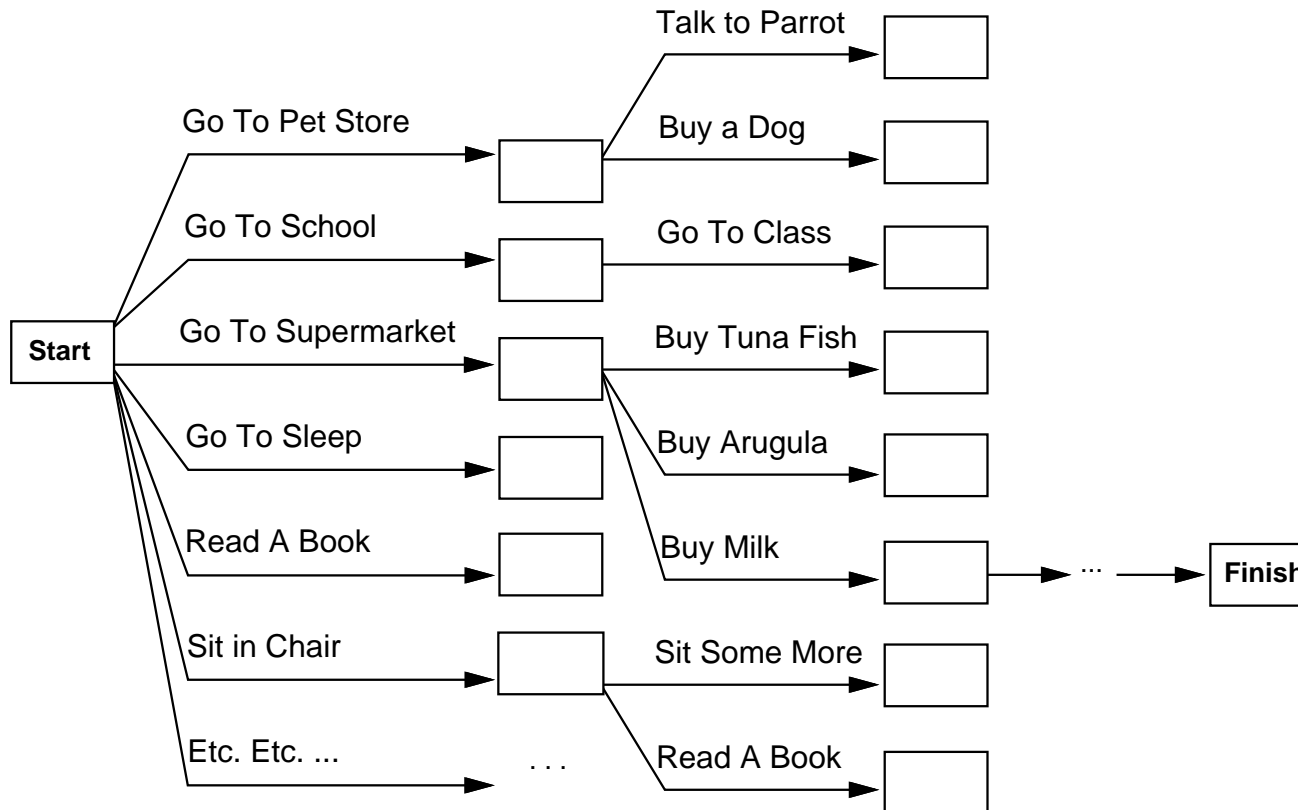
$$\{At(p), Sells(p, Jaguar), Have(Money)\} =$$

$$\{\neg At(Jail), At(p), Sells(p, Jaguar), Have(Money)\}$$

$Buy(Jaguar)$  is a relevant action. If we had an extra action  $Steal(Jaguar)$  which also resulted in  $Have(Jaguar)$  but had an additional effect of  $At(Jail)$ , it would not be a relevant action.

# Comparison of forward and backward planning

If there are lots of actions, searching for a solution starting from the initial state looks hopeless





## Comparison of forward and backward planning 2

However, it turns out we can automatically derive good heuristics (and remember how much better  $A^*$  is compared to uninformed search)

Two basic approaches:

1) add more edges to the graph (make more actions possible), and use solutions to the resulting problem as a heuristic. (There are often more efficient algorithms to solve the relaxed problem.)

Examples: remove (some) preconditions, ignore delete lists...

ACTION  $Slide(t, s_1, s_2)$

PRECOND:  $On(t, s_1) \wedge Tile(t) \wedge Blank(s_2) \wedge Adjacent(s_1, s_2)$

EFFECT:  $On(t, s_2) \wedge Blank(s_1) \wedge \neg On(t, s_1) \wedge \neg Blank(s_2)$

removing  $Blank(s_2)$  will enable tiles to move to occupied places: Manhattan distance heuristic

2) abstract the problem (make the search space smaller).

## Comparison of forward and backward planning 3

Backward planning considers a lot fewer actions/relevant states than forward search, but uses sets of states  $(g, g')$  - hard to come up with good heuristics.

## Use of logic and deduction

In situation calculus (lecture 8), planning **is** deduction

In 'normal' planning, we only need to check whether a state description entails some property:  $s \models P(A, B) \wedge \neg Q(A)$  for example

In simple cases, like in this lecture, this just involves checking that  $P(A, B)$  is in the list of properties  $s$  has, and  $Q(A)$  is not (closed world assumption: if  $Q(A)$  is not listed, then  $\neg Q(A)$  must be true)

However, often planning domains are described using additional axioms, and then checking  $s \models P(A, B)$  may involve more complex reasoning (whether  $P(A, B)$  follows from the description of  $s$  and the axioms).

## Next lecture

More classical planning

Goal-stack planning (based on another textbook: Elaine Rich and Kevin Knight, Artificial Intelligence).

Sussman anomaly