

MATLAB: Vectors and Matrices

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<https://yasirbhutta.github.io/matlab/docs/vectors-matrices.html>

Vector Products

Important: To perform matrix multiplication, the first matrix must have the same number of columns as the second matrix has rows. The number of rows of the resulting matrix equals the number of rows of the first matrix, and the number of columns of the resulting matrix equals the number of columns of the second matrix. [1]

Important: In MATLAB, the concept of conjugate refers to the complex conjugate of a number or element within a matrix. The complex conjugate of a complex number is a new number with the same real part but the imaginary part negated.

Vectors in MATLAB

Vectors are one-dimensional arrays used to store a collection of numbers. You can create them in different ways:

1. Using square brackets `[]`:

```
myVector = [1 2 3 4 5];
```

2. Using the colon operator `:`:

```
rangeVector = 1:5; % Creates a vector from 1 to 5 (inclusive)
```

Accessing Elements

There are two main ways to access individual elements within a vector:

1. Using Indices:

- MATLAB uses **one-based indexing**, meaning the first element has an index of 1, the second has an index of 2, and so on.
- To access a specific element, enter the vector name followed by the index in parentheses:

```
myVector(2) % Accesses the second element (value 2)  
rangeVector(4) % Accesses the fourth element (value 4)
```

2. Using Colon Operator ::

- The colon operator allows you to select a range of elements:
 - `vector(start:end)`: Accesses elements from `start` (inclusive) to `end` (inclusive).
 - `vector(start:step:end)`: Accesses elements with a specific `step` between them (similar to Python slicing).
 - `vector(:)`: Accesses all elements of the vector.

```
myVector(2:4) % Accesses elements from index 2 (value 2) to index 4 (value 4)
rangeVector(1:2:5) % Accesses elements 1, 3, and 5 (with a step of 2)
myVector(:) % Accesses all elements (same as `myVector`)
```

3. Creating and Accessing a Vector:

```
fruits = ["apple" "banana" "orange"]; % Create a vector of strings
secondFruit = fruits(2); % Access the second element ("banana")
```

4. Extracting Sub-vectors:

```
temperatures = [20 32 25 18];
firstTwo = temperatures(1:2); % Extract the first two elements ([20 32])
evenIndices = temperatures(2:2:end); % Extract elements at even indices ([32 18])
```

Tips

- Remember one-based indexing.
- Use `end` as an index to refer to the last element: `myVector(end)`.
- The colon operator is versatile for selecting elements or creating new vectors.

See also:

- [Matrix Indexing in MATLAB - MathWorks Docs](#)

Generating Row Vectors with Even Spacing in MATLAB

a. linspace

Linspace in MATLAB is a function used to generate a row vector containing **evenly spaced values** between two specified endpoints.

Syntax:

- `y = linspace(x1, x2)`: This creates a row vector with 100 (default) points between `x1` and `x2`.

- `y = linspace(x1, x2, n)`: This allows you to specify the number of points (`n`) in the vector.

Key Points:

- The spacing between values is calculated as: $(x2 - x1) / (n - 1)$.
- It includes both the starting (`x1`) and ending (`x2`) points in the output vector.
- `Linspace` is similar to the colon operator (`:`) but offers more control over the number of points.

Use Cases:

- Creating data points for plotting functions.
- Setting up evenly spaced grid points for numerical calculations.
- Controlling the sampling rate for simulations.

See also:

- **MATLAB Documentation:** <https://www.mathworks.com/help/matlab/ref/linspace.html>

b. logspace

In MATLAB, the `logspace` function is used to generate a row vector containing **logarithmically spaced values** between two specified points. It's the logarithmic counterpart of the `linspace` function you saw earlier.

Syntax:

- `y = logspace(a, b)`: This creates a row vector with 50 points (default) between decades of 10^a and 10^b .
- `y = logspace(a, b, n)`: This allows you to specify the number of points (`n`) in the vector.
- `y = logspace(a, pi)`: This is useful for creating logarithmically spaced frequencies (especially in digital signal processing) in the interval $[10^a, \pi]$.

Key Points:

- The spacing is based on logarithms, not linear values. Points are closer together at lower values and farther apart at higher values.
- It includes an approximation of the starting point (10^a) and the ending point (might not be exactly π if used) in the output vector.
- **Use Cases:**
 - Generating frequencies for simulations or filter design.
 - Sampling data across a wide range of values.
 - Creating logarithmic axes for plotting data that exhibits exponential growth or decay.

See also

- **MATLAB Documentation:** <https://www.mathworks.com/help/matlab/ref/logspace.html>

Vector Functions

1. sum(x)

```
v = [1, 2, 3, 4, 5];
total_sum = sum(v);
disp(total_sum) % Output: 15
```matlab

2. mean(x)

```matlab
v = [4, 6, 7, 3, 5];
average_value = mean(v);
disp(average_value) % Output: 5
```

3. length(x)

```
v = [1, 2, 3, 4, 5];
vector_length = length(v);
disp(vector_length) % Output: 5
```

4. max(x)

Example #: Finding the maximum element

```
v = [1, 5, 2, 8, 3];
max_element = max(v);
disp(max_element) % Output: 8
```

5. min

Example #: Finding the minimum element

```
v = [5, 2, 8, 1, 3];
minimum_value = min(v);
disp(minimum_value) % Output: 1
```

6. prod(x)

Example #: Product of all elements

```
v = [2, 3, 4, 1];
total_product = prod(v);
disp(total_product) % Output: 24
```

7. sign(x)

- The `sign` function in MATLAB is useful for determining the sign (positive, negative, or zero) of elements in vectors and arrays.

Example #: Finding the sign of each element:

```
v = [1, -2, 0, 3.5, -4];  
element_signs = sign(v);  
disp(element_signs) % Output: 1 -1 0 1 -1
```

This code creates a vector `v` and uses `sign(v)` to determine the sign of each element. The results are stored in `element_signs`. The output shows 1 for positive values, -1 for negative values, and 0 for zero.

8. find(x)

- The `find` function in MATLAB is a versatile tool for finding specific elements or their indices within a vector.

1. Finding Non-Zero Elements:

- The simplest usage is `k = find(v)`. This returns a vector `k` containing the linear indices of all non-zero elements in vector `v`.

Example:

```
v = [1, 0, 3, 0, 5];  
k = find(v);  
disp(k) % Output: 1 3 5
```

2. Finding a Specific Number of Elements:

- You can specify the number of elements to find:
 - `k = find(v, n)` returns the first `n` indices of non-zero elements.
 - `k = find(v, n, 'last')` returns the last `n` indices of non-zero elements.

Example:

```
v = [2, 0, -1, 4, 0];  
first_two = find(v, 2); % Find the first two non-zero elements  
last_two = find(v, 2, 'last'); % Find the last two non-zero elements  
disp(first_two) % Output: 1 3  
disp(last_two) % Output: 3 4
```

3. Finding Elements Based on Conditions:

- Use relational operators (`<`, `>`, `<=`, `>=`, `==`, `~=`) within `find` to locate elements meeting specific criteria.

Example:

```
v = [8, 2, 6, 1, 9];  
greater_than_5 = find(v > 5); % Find indices of elements greater than 5  
equal_to_2 = find(v == 2); % Find indices of elements equal to 2  
disp(greater_than_5) % Output: 1 4 5  
disp(equal_to_2) % Output: 2
```

Remember, the `find` function is a powerful tool for manipulating vectors in MATLAB. Explore the documentation <https://www.mathworks.com/help/matlab/ref/find.html> for more details and advanced usage scenarios.

9. fix(x)

Example #: Fixing all elements in a vector

```
v = [-2.5 1.8 4.3 -7.1];  
fixed_v = fix(v);  
disp(fixed_v) % Output: -2 1 4 -7
```

This code creates a vector `v` with decimal values. `fix(v)` applies the `fix` function to each element, rounding them towards zero and storing the result in `fixed_v`.

10. floor

The `floor` function in MATLAB is useful for rounding down elements in vectors (and arrays) to the nearest integer less than or equal to that element.

Important: `floor` always rounds down towards negative infinity, regardless of the sign of the input value.

Example #: Rounding down elements in a vector

```
v = [1.5, 2.8, 3.1, 4.9, 5.2];  
floored_vector = floor(v);  
disp(floored_vector) % Output: 1 2 3 4 5
```

Example #: Rounding down negative decimals

```
v = [-1.5, 2.8, -3.1, 4.9, -5.2];  
floored_vector = floor(v);  
disp(floored_vector) % Output: -2 2 -4 4 -6
```

11. ceil

Important point: ceil always rounds up towards positive infinity.

Example #: Rounding towards positive infinity

```
v = [-1.5, 2.8, -3.1, 4.9, -5.2];
ceiling_vector = ceil(v);
disp(ceiling_vector) % Output: -1 3 -3 5 -5
```

In this example, ceil(v) rounds each element in v towards positive infinity. So:

- Negative decimals are rounded up to the nearest negative integer (closer to zero).
- Positive decimals are rounded up to the nearest positive integer.

12. round

Example #: Rounding to nearest integers

```
v = [1.5, 2.8, -3.7, 4.9, -5.2];
rounded_vector = round(v);
disp(rounded_vector) % Output: 2 3 -4 5 -5
```

13. sort

Example #: Sorting in ascending order (default)

```
v = [5, 1, 4, 2, 3];
sorted_vector = sort(v);
disp(sorted_vector) % Output: 1 2 3 4 5
```

This code creates a vector v and uses sort(v) to sort its elements in ascending order. The result is stored in sorted_vector.

Example #: Sorting in descending order You can specify 'descend' as the second argument to sort in descending order:

```
sorted_descending = sort(v, 'descend');
disp(sorted_descending) % Output: 5 4 3 2 1
```

14. mod

The mod function in MATLAB is useful for finding the remainder after element-wise division of vectors. Here are some examples of how to use it with vectors:

1. Modulo with a Scalar:

- This calculates the remainder for each element of the vector divided by the scalar value.

Example:

```
v = [10, 5, 18, 3, 12];  
mod_result = mod(v, 4); % Find remainder after dividing each element by 4  
disp(mod_result) % Output: 2 1 2 3 0
```

2. Modulo Between Vectors:

- You can perform modulo between two vectors of the same size. The operation is performed element-wise.

Example:

```
v1 = [7, 11, 15];  
v2 = [3, 4, 5];  
mod_result = mod(v1, v2);  
disp(mod_result) % Output: 1 3 0 (Remainder of v1(i) / v2(i))
```

Key points:

- The `mod` function follows the convention that `mod(a,0)` returns `a`. In other words, the remainder when dividing by zero is the original dividend itself.
- For floating-point input arguments, the output data type of `mod` is the same as the inputs.

By understanding these examples, you can effectively use the `mod` function to perform modulo operations on vectors in MATLAB.

15. rem

The `rem` function in MATLAB behaves very similarly to `mod` for vectors, but with a subtle difference. Here's how to use it with vectors:

1. Rem with a Scalar:

- This calculates the remainder for each element of the vector divided by the scalar value.

Example:

```
v = [10, 5, 18, 3, 12];  
rem_result = rem(v, 4); % Find remainder after dividing each element by 4  
disp(rem_result) % Output: 2 1 2 3 0
```

2. Rem Between Vectors:

- You can perform element-wise modulo between two vectors of the same size.

Example:

```
v1 = [7, 11, 15];  
v2 = [3, 4, 5];  
rem_result = rem(v1, v2);  
disp(rem_result) % Output: 1 3 0 (Remainder of v1(i) / v2(i))
```

3. Key Difference from mod:

- The key difference between `rem` and `mod` lies in the handling of negative dividends.
 - `mod` always returns a non-negative remainder between 0 and the divisor minus one.
 - `rem` however, signs the remainder according to the sign of the dividend.

Example:

```
v = [-10, 5, -18, 3, -12];  
rem_result = rem(v, 4); % Remainder considering sign of dividend  
disp(rem_result) % Output: -2 1 -2 3 -0
```

Matrices

Creating Matrices: Entering elements directly

Example #: Creating a 2x2 Matrix

```
A = [1 2; 3 4];  
disp(A);
```

This creates a 2x2 matrix `A` with elements:

```
1  2  
3  4
```

Example #: Creating a 3x3 Matrix

```
% Create a 3x3 matrix  
matrix = [1 2 3; 4 5 6; 7 8 9]
```

Example #: Create a 2x3 matrix

```
C = [1 2 3; 4 5 6]
```

Example #: Specifying elements with spaces or commas

Elements within a row can be separated by either commas (,) or spaces. Both notations achieve the same result.

```
% Using commas
matrix_comma = [1, 4, 7; 2, 5, 8; 3, 6, 9]

% Using spaces
matrix_space = [1 4 7; 2 5 8; 3 6 9]
```

Example #: Creating a 4x2 Matrix

```
C = [2, 4; 6, 8; 10, 12; 14, 16];
```

This creates a 4x2 matrix **C** with elements:

```
2   4
6   8
10  12
14  16
```

Example #: Creating a 3x4 Matrix

```
D = [1, 2, 3, 4; 5, 6, 7, 8; 9, 10, 11, 12];
```

This creates a 3x4 matrix **D** with elements:

```
1   2   3   4
5   6   7   8
9   10  11  12
```

Example #: Creating a 1x5 Row Vector

```
E = [1, 2, 3, 4, 5];
```

This creates a 1x5 row vector **E** with elements:

```
1  2  3  4  5
```

Example #: Creating a 5x1 Column Vector:

```
F = [6; 7; 8; 9; 10];
```

This creates a 5x1 column vector **F** with elements:

```
6
7
8
9
10
```

See also:

- [Creating Matrices and Arrays - MathWorks Help Center](#)

Matrix Indexing in MATLAB

In MATLAB, indexing into matrices allows you to access and manipulate specific elements, rows, columns, or subsets of a matrix. Here are some examples of matrix indexing in MATLAB:

Example #: Accessing single elements:

```
A = [1, 2, 3; 4, 5, 6; 7, 8, 9];
element = A(2, 3); % Accesses the element in the second row and third column
disp(element); % Displays: 6
```

Example #: Accessing entire rows or columns:

```
A = [1, 2, 3; 4, 5, 6; 7, 8, 9];
row = A(2, :); % Accesses the entire second row
disp(row); % Displays: 4 5 6

column = A(:, 3); % Accesses the entire third column
disp(column); % Displays: 3 6 9
```

Example #: Assigning values to specific elements:

```
A = [1, 2, 3; 4, 5, 6; 7, 8, 9];
A(1, 2) = 10; % Assigns the value 10 to the element in the first row and second
```

```
column
disp(A); % Displays the updated matrix

% Resulting matrix:
% 1  10  3
% 4   5  6
% 7   8  9
```

Example #: Indexing with linear indices:

```
A = [1, 2, 3; 4, 5, 6; 7, 8, 9];
linear_index = [1, 4, 7]; % Linear indices of elements to access
elements = A(linear_index); % Accesses elements using linear indices
disp(elements); % Displays elements corresponding to linear indices
```

The Output of the code is:

```
1     2     3
```

Example #: Indexing with logical arrays:

```
A = [1, 2, 3; 10, 5, 1; 4, 8, 9];
logical_index = A > 5; % Creates a logical array indicating elements greater than 5
disp(logical_index); % Displays the logical array

% Resulting logical array:
% 0   0   0
% 1   0   0
% 0   1   1

% Using logical array to access elements
elements_gt_5 = A(logical_index);
disp(elements_gt_5); % Displays elements greater than 5

% Output
% 10
% 8
% 9
```

Key Terms

True/False (Mark T for True and F for False)

Answer Key (True/False):

Multiple Choice (Select the best answer)

Fill in the Blanks

Answer Key (Fill in the Blanks):

Practice Exercises

1. Create a vector of your favorite numbers and access the third element.
2. Create a vector of temperatures and extract the elements for Monday and Wednesday (assuming even indices represent Wednesdays).
3. Experiment with the colon operator to create sub-vectors with different intervals.

Review Questions

References and Bibliography

[1] "M.2 Matrix Arithmetic | STAT ONLINE," PennState: Statistics Online Courses.
<https://online.stat.psu.edu/statprogram/reviews/matrix-algebra/arithmetic>