



## Digital Communication #ELC3253

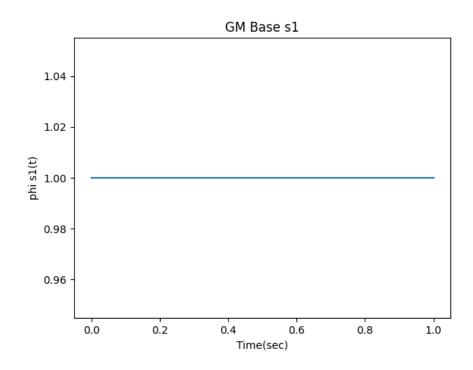
**Assignment Three** 

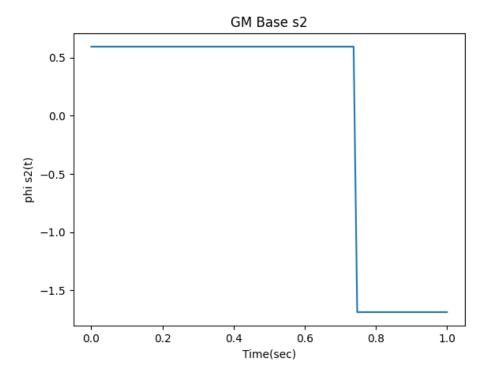
Signal Space

#### **STUDENTS INFORMATION**

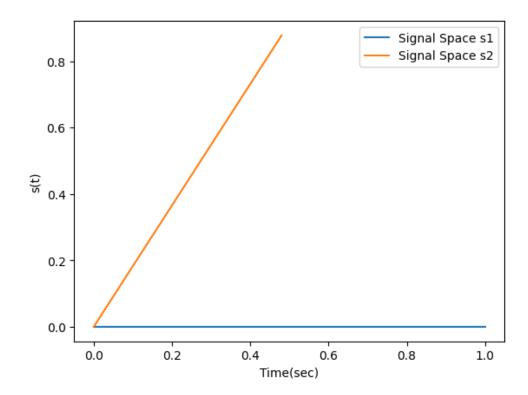
Name	Section	Bench Number
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1) Use your "GM\_Bases" function to get the bases functions of s1(t) & s2(t) Figure 1.1. Plot the obtained bases functions.



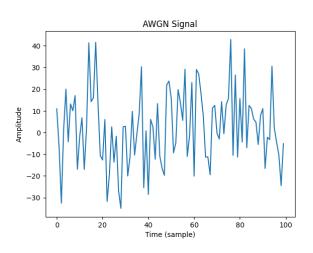


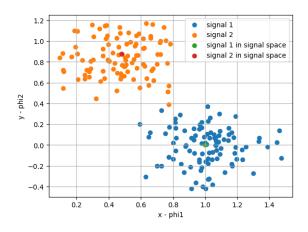
2) Use your "signal\_space" function (along with the bases from 1) to get the signal space representation of s1(t) & s2(t) in Figure 1.1. Plot the signal space representation.



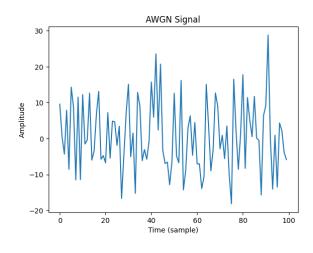
# 3) Generate samples of r1 (t) and r2 (t) using s1(t) & s2(t) and random noise samples. Plot the signal points of the generated samples of r1 (t) and r2 (t) at E $\sigma2 = -5$ dB, 0 dB, 10 dB, where E is the energy of s1 (t) or s2(t).

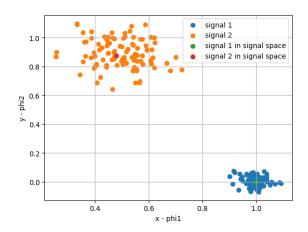
a) At 
$$E/\sigma^2 = -5$$



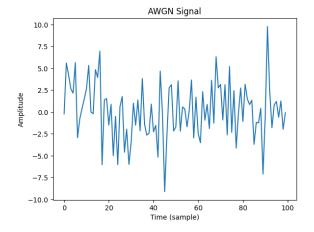


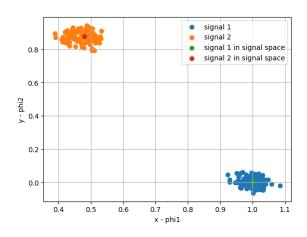
#### b) At $E/\sigma^2 = 0$





#### c) At $E/\sigma^2 = 10$





### 4) How does the noise affect the signal space? Does the noise effect increase or decrease with increasing $\sigma$ 2 ?

The noise distorts the signal space very much when introduced to it.

As the variance increases the noise effect decreases and the signal tends to go more to its original value. Therefore it's inversely proportional/correlated.

#### 1-"GM\_Bases" function

```
def GM_Bases(s1,s2):
    '''
    The function calculates the Gram-Schmidt orthonormal bases functions
(phil & phi 2) for two input signals (s1 & s2)
    The inputs s1 and s2: are two 1×N vectors that represent the input
signals
    The outputs phil & phi2: are two 1×N vectors that represent the two
orthonormal bases functions (using Gram-Schmidt).
    If s1 & s2 have one basis function, then phi2 is 1×N zero vector

""

#We set the first vector same as original & then normalize the rest on
it

phil = s1 / np.linalg.norm(s1) # Normalize s1 to get phi1

v2 = s2 - np.dot(s2, phil) * phil # Calculate the orthogonal
component of s2 to phil
    if np.linalg.norm(v2) > 0: # Check if v2 is non-zero
        phi2 = v2 / np.linalg.norm(v2) # Normalize v2 to get phi2
else:
        phi2 = np.zeros_like(s2) # phi2 is a zero vector if v2 is zero

return phil, phi2
```

#### 2- "signal\_space" function

#### 4- Helper Functions

```
#HELPER FUNCTIONS

# Generate the unit step signals

def unit_step(t):
    return np.heaviside(t, 1)

# Plot signals

def plot_signal(x,y,labelx,labely,title,type='plot'):
    if(type == 'scatter'):
        plt.scatter(x, y)
    else:
        plt.plot(x, y)
    plt.xlabel(labelx)
    plt.ylabel(labely)
    plt.title(title)
    plt.show()
    return
```

```
def plot points(x,y,labelx,labely,title1,title2):
   ___, ax = plt.subplots()
    ax.plot([x[0][0],x[0][1]], [x[1][0],x[1][1]], label = title1)
    ax.plot([y[0][0],y[0][1]], [y[1][0],y[1][1]], label = title2)
    ax.set xlabel(labelx)
    ax.set ylabel(labely)
    ax.legend()
    plt.show()
def scatter signals(x1,y1,x2,y2,labelx,labely,title1,title2):
   \underline{\phantom{a}}, ax = plt.subplots()
    ax.scatter(x1, y1, label = title1)
    ax.scatter(x2, y2, label = title2)
    ax.set xlabel(labelx)
    ax.set ylabel(labely)
    ax.legend()
    plt.show()
```

#### 4- Generating Signals

```
# Generate s1
tS1 = np.linspace(0, 1, 100)
s1 = unit_step(tS1)
plot_signal(tS1,s1,'Time(sec)','s1(t)','1st Signal')

# Generate s2
tS2_1 = np.linspace(0, 0.74, 74)
tS2_2 = np.linspace(0.75, 1, 26)

s2_a = unit_step(tS2_1)
s2_b = -(unit_step(tS2_2))

s2 = np.concatenate((s2_a,s2_b),axis=0)
tS2 = np.concatenate((tS2_1, tS2_2), axis=0)
plot_signal(tS2,s2,'Time(sec)','s2(t)','2nd Signal')
```

#### 5- Calculating GM Bases

```
GM_Base_s1, GM_Base_s2 = GM_Bases(s1,s2)

T = np.linspace(0,1, 100)

plot_signal(T,GM_Base_s1, 'Time(sec)', 'phi s1(t)', 'GM Base s1')
plot_signal(T,GM_Base_s2, 'Time(sec)', 'phi s2(t)', 'GM Base s2')
```

#### 6- Calculating Signal Spaces

```
GM_Base_s1_a, GM_Base_s1_b = signal_space(s1,GM_Base_s1,GM_Base_s2)
GM_Base_s2_a, GM_Base_s2_b = signal_space(s2,GM_Base_s1,GM_Base_s2)

T = np.linspace(0, 1, 10)
#Signal space of s1 over GM_Base s1 and s2 respectively
# & Signal space of s2 over GM_Base s1 and s2 respectively
plot_points([[0,GM_Base_s1_a],[0,GM_Base_s1_b]],[[0,GM_Base_s2_a],[0,GM_Base_s2_b]], 'Time(sec)', 's(t)', 'Signal Space s1', 'Signal Space s2')
```

#### 7- Generating the r signals with noise and calculating energy of s1

```
#1- Generate the AWGN signal
variance = 0.5
num samples = 100 #No. of samples
w t = np.random.normal(loc=0, scale=np.sqrt(variance), size=num samples)
t = np.arange(num samples)
plot signal(t,w t,'Sample','Amplitude','AWGN Signal','scatter')
# #2- Generate r1(t) & r2(t)
r1 = s1 + w t
plot signal(t,r1,'Time (sec*10^-2)','Amplitude r1(t)','r1(t)
Signal','scatter')
r2 = s2 + w t
plot signal(t,r2,'Time (sec*10^-2)','Amplitude r2(t)','r2(t)
Signal','scatter')
#3- Get energy of s1 & s2
e1 = np.sum(s1**2)/len(s1)
e2 = np.sum(s2**2)/len(s2)
```

#### 8- Calculating the effect of AWGN on different values of E/^2

```
v1 = e1/(10**(-5/10))
v2 = e2/(10**(-5/10))

#1- Generate the AWGN signal
w_t1 = np.random.normal(loc=0, scale=np.sqrt(v1), size=num_samples)
w_t2 = np.random.normal(loc=0, scale=np.sqrt(v2), size=num_samples)
t = np.arange(num_samples)
plot_signal(t,w_t,'Time (sample)','Amplitude','AWGN Signal')

#2- Generate r1(t) & r2(t)
r1_1 = [signal_space(s1 + np.random.normal(loc=0, scale=np.sqrt(v1), size=num_samples), GM_Base_s1, GM_Base_s2)[0] for x in range(100)]
r1_2 = [signal_space(s1 + np.random.normal(loc=0, scale=np.sqrt(v1), size=num_samples), GM_Base_s1, GM_Base_s2)[1] for x in range(100)]
r2_1 = [signal_space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2), size=num_samples), GM_Base_s1, GM_Base_s2)[0] for x in range(100)]
r2_2 = [signal_space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2), size=num_samples), GM_Base_s1, GM_Base_s2)[1] for x in range(100)]
scatter_signals(r1_1,r1_2,r2_1,r2_2,'Time(sec*10^-2)','Amplitude','r1(t)','r2(t)')
```

```
vv1 = e1/(10**(0/10))
v2 = e2/(10**(0/10))
w_t1 = np.random.normal(loc=0, scale=np.sqrt(v1), size=num samples)
w t2 = np.random.normal(loc=0, scale=np.sqrt(v2), size=num samples)
t = np.arange(num samples)
plot signal(t,w t,'Time (sample)','Amplitude','AWGN Signal')
rl 1 = [signal space(s1 + np.random.normal(loc=0, scale=np.sgrt(v1),
size=num samples), GM Base s1, GM Base s2)[0] for x in range(100)]
r1 2 = [signal space(s1 + np.random.normal(loc=0, scale=np.sgrt(v1),
size=num samples), GM Base s1, GM Base s2)[1] for x in range(100)]
r2 1 = [signal space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2),
size=num samples), GM Base s1, GM Base s2)[0] for x in range(100)]
r2 2 = [signal space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2),
size=num samples), GM Base s1, GM Base s2)[1] for x in range(100)]
scatter signals(r1 1,r1 2,r2 1,r2 2,'Time
(sec*10^-2)','Amplitude','r1(t)','r2(t)')
```

```
\#At E/\sigma2 = 10 dB
v1 = e1/(10**(10/10))
v2 = e2/(10**(10/10))
w_t1 = np.random.normal(loc=0, scale=np.sqrt(v1), size=num samples)
w t2 = np.random.normal(loc=0, scale=np.sqrt(v2), size=num samples)
c = np.arange(num samples)
plot signal(t,w t,'Time (sample)','Amplitude','AWGN Signal')
rl 1 = [signal space(s1 + np.random.normal(loc=0, scale=np.sqrt(v1),
size=num samples), GM Base s1, GM Base s2)[0] for x in range(100)]
r1 2 = [signal space(s1 + np.random.normal(loc=0, scale=np.sqrt(v1),
size=num samples), GM Base s1, GM Base s2)[1] for x in range(100)]
r2 1 = [signal space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2),
size=num samples), GM Base s1, GM Base s2)[0] for x in range(100)]
r2 2 = [signal space(s2 + np.random.normal(loc=0, scale=np.sqrt(v2),
size=num samples), GM Base s1, GM Base s2)[1] for x in range(100)]
scatter signals(r1 1,r1 2,r2 1,r2 2,'Time
(sec*10^-2)','Amplitude','r1(t)','r2(t)')
```