

TSegFormer: 3D Tooth Segmentation in Intraoral Scans with Geometry Guided Transformer

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Abstract. Optical Intraoral Scanners (IOS) are widely used in digital dentistry to provide detailed 3D information of dental crowns and the gingiva. Accurate 3D tooth segmentation in IOSs is critical for various dental applications, while previous methods are error-prone at complicated boundaries and exhibit unsatisfactory results across patients. In this paper, we propose TSegFormer which captures both local and global dependencies among different teeth and the gingiva in the IOS point clouds with a multi-task 3D transformer architecture. Moreover, we design a geometry-guided loss based on a novel point curvature to refine boundaries in an end-to-end manner, avoiding time-consuming post-processing to reach clinically applicable segmentation. In addition, we create a dataset with 16,000 IOSs, the largest ever IOS dataset to the best of our knowledge. The experimental results demonstrate that our TSegFormer consistently surpasses existing state-of-the-art baselines. The superiority of TSegFormer is corroborated by extensive analysis, visualizations and real-world clinical applicability tests. Our code is available at https://github.com/huiminxiong/TSegFormer.

Keywords: 3D tooth segmentation \cdot IOS mesh scans \cdot Transformer

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Supplementary Information The online version contains supplementary material available at https://doi.org/10.1007/978-3-031-43987-2 41.

[©] The Author(s), under exclusive license to Springer Nature Switzerland AG 2023 H. Greenspan et al. (Eds.): MICCAI 2023, LNCS 14225, pp. 421–432, 2023. https://doi.org/10.1007/978-3-031-43987-2_41

1 Introduction

Deep learning is becoming increasingly popular in modern orthodontic treatments for tooth segmentation in intraoral scans (IOS), cone-beam CT (CBCT) and panoramic X-ray [9,15]. Accurate tooth segmentation in 3D IOS dental models is crucial for orthodontics treatment such as diagnosis, tooth crown-root analysis and treatment simulation [10,25]. Specifically, tooth segmentation classifies each triangular face of a 3D IOS tooth model with about 100,000 to 400,000 faces and a spatial resolution of 0.008-0.02mm into teeth and gingiva categories, following the Federation Dentaire Internationale (FDI) standard [8].

There are two main categories for tooth segmentation in IOS: conventional methods that handle 2D image projections [10,21,24] or directly operate on 3D IOS meshes [17,22,25,29], and deep learning methods that operate on meshes or point clouds [1,3,6,7,11,12,14,18,23,27,30]. However, many challenges persist. Complicated morphological topology or dental diseases (e.g. crowded or erupted teeth) can lead to unsatisfactory segmentation performance [6]. Additionally, current methods often fail to recognize mesh faces between adjacent teeth or the tooth and gingiva, requiring time-consuming post-processing to refine the noisy boundary segmentation [6,12,23]. Moreover, the state-of-the-art works such as MeshSegNet [12], TSGCNet [27] and DCNet [6] have only been evaluated with a limited amount of data samples and the clinical applicability need to be evaluated with large-scale dataset or in real-world scenarios.

Inspired by the success of transformers in various tasks [2,4,5,13,19,28], we propose a novel 3D transformer framework, named TSegFormer, to address the aforementioned challenges. In particular, the tooth segmentation task on 3D IOSs is formulated as a semantic segmentation task on point clouds sampled from raw IOS meshes. We design the 3D transformer with tailored self-attention layers to capture long-range dependencies among different teeth, learning expressive representations from inherently sophisticated structures across IOSs. In addition, we design a multi-task learning paradigm where another auxiliary segmentation head is introduced to assist in delimiting teeth and gingiva. Furthermore, in view of the confusing boundary segmentation, we devise a novel geometry guided loss based on a newly-defined point curvature to help learn accurate boundaries. The network is trained in an end-to-end manner and requires no complicated post-processing during inference, making it appealing to practical applications.

We collect a large-scale, high-resolution and heterogeneous 3D IOS dataset with 16,000 dental models where each contains over 100,000 triangular faces. To the best of our knowledge, it is the largest IOS dataset to date. Experimental results show that TSegFormer has reached 97.97% accuracy, 94.34% mean intersection over union (mIoU) and 96.01% dice similarity coefficient (DSC) on the large-scale dataset, outperforming previous works by a significant margin. To summarize, our main contributions are:

- We design a novel framework for 3D tooth segmentation with a tailed 3D transformer and a multi-task learning paradigm, aiming at distinguishing the permanent teeth with divergent anatomical structures and noisy boundaries.

- We design a geometry guided loss based on a novel point curvature for endto-end boundary refinement, getting rid of the two-stage and time-consuming post-processing for boundary smoothing.
- We collect the largest ever 3D IOS dataset for compelling evaluation. Extensive
 experiments, ablation analysis and clinical applicability test demonstrate the
 superiority of our method, which is appealing in real-world applications.

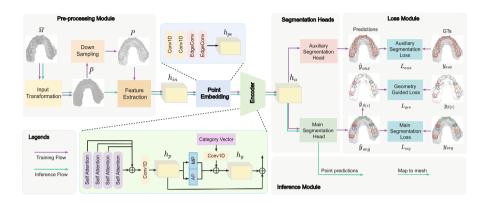


Fig. 1. The pipeline of our proposed TSegFormer for 3D tooth segmentation

2 Method

2.1 Overview

The overall pipeline is illustrated in Fig. 1. The original mesh M is converted to a point cloud \widetilde{P} by taking the gravity center point of each mesh face. We down-sample a point cloud P with N=10,000 points from \widetilde{P} , and extract the input feature matrix $h_{in} \in \mathbb{R}^{N \times 8}$ as defined below. The network first employs a point embedding module to capture abundant local structure information h_{pe} from h_{in} . Thereafter, we design the 3D transformer encoder with self-attention layers to capture high-level semantic representations h_a . With h_a , the main segmentation head produces prediction scores $\hat{y}_{seg} \in \mathbb{R}^{N \times 33}$ (32 permanant teeth and the gingiva), while the auxiliary head generates prediction scores $\hat{y}_{aux} \in \mathbb{R}^{N \times 2}$ to assist distinguishing the tooth-gingiva boundary. Furthermore, we devise a geometry guided loss L_{geo} , which is integrated with the main segmentation loss L_{seg} and the auxiliary loss L_{aux} to attain superior performance. During inference, we will extract the features $h_{in} \in \mathbb{R}^{\tilde{N} \times 8}$ for all points in \tilde{P} , process \tilde{P} into multiple sub-point clouds each with N points, then generate predictions for each point with $\lceil \frac{\tilde{N}}{N} \rceil$ rounds of inference, and map them back to raw mesh \tilde{M} .

2.2 TSegFormer Network Architecture

Feature Extraction. We first transform input meshes to point clouds as directly handling meshes with deep nets is computationally expensive, especially for high-resolution IOSs. To compensate for potential topology loss, we extract 8-dimensional feature vectors $h_{in} \in \mathbb{R}^{\widetilde{N} \times 8} / \mathbb{R}^{N \times 8}$ for each point to preserve sufficient geometric information, including the point's 3D Cartesian coordinates, 3-dimensional normal vector of mesh face, the Gaussian curvature and a novel point "curvature" m_i . The m_i is defined as $m_i = \frac{1}{|K(i)|} \sum_{j \in K(i)} \theta(n_i, n_j)$, where n_i is the i-th point's normal vector, K(i) is the second-order neighborhood of the i-th point, |K(i)| is the number of points in K(i), and $\theta(\cdot, \cdot)$ denotes the angle in radians between two vectors. By definition, the curvature of a point reflects how much the local geometric structure around this point is curved, i.e., the local geometry on 3D tooth point clouds.

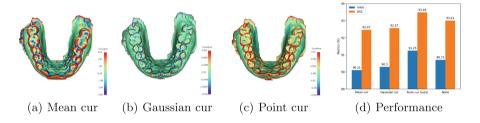


Fig. 2. Visualization and performance comparison of different curvatures(cur).

Backbone Network. Delineating complicated tooth-tooth or tooth-gingiva boundaries requires decent knowledge of local geometry in IOS. Hence, we first learn local dependencies from the input h_{in} . In particular, we design a point embedding module composed of two linear layers and two EdgeConv layers [20], which takes h_{in} as input and learn local features $h_{pe} \in \mathbb{R}^{N \times d_e}$. The point embedding module enriches point representations with local topological information, with ablation results in the Supplementary Material (SM) Table 1.

Meantime, in view of the inherently sophisticated and inconsistent shapes and structures of the teeth, and the ability of attention mechanism to capture long-range dependencies and suitability for handling unordered point cloud data [2,4,13,19,28], we build an encoder module based on it. The encoder module, composed of four successive self-attention layers and a linear transformation, further yields the high-level point feature maps h_p . To avoid misjudging jaw categories, an extra 2D category vector V is fed as input to help distinguish the maxillary and mandible and obtain the global feature maps h_g . Specifically, $h_g = \sigma(V) \oplus MP(h_p) \oplus AP(h_p)$, where "MP" and "AP" respectively denote the max and average pooling; \oplus denotes concatenation and $\sigma(\cdot)$ is a linear layer. Finally, we obtain feature maps h_g for all points, where $h_g = h_p \oplus h_g$.

Segmentation Heads. To improve the network's ability to recognize different tooth and gingiva categories, we design two segmentation heads. The main segmentation head, an MLP (MLP_{seg}) , generates point classification scores for 33 classes $\hat{y}_{seg} = MLP_{seg}(h_a) \in \mathbb{R}^{N\times 33}$ for tooth segmentation. Meanwhile, considering the prevalence of incorrect prediction of tooth-gingiva boundaries, we design an auxiliary segmentation head MLP_{aux} to provide binary classification scores for each point belonging to either tooth or gingiva, i.e., $\hat{y}_{aux} = MLP_{aux}(h_a) \in \mathbb{R}^{N\times 2}$. Experimental results indicate that the cooperation with MLP_{aux} can refine tooth-gingiva segmentation boundary.

Geometry Guided Loss. Previous methods are usually unsatisfactory to delineate the complicated tooth-tooth boundaries. Observing that points with high point curvatures often lie on the upper sharp ends of tooth crowns and the teeth boundaries (Fig. 2(c)), where mispredictions usually occur, we define the novel geometry guided loss L_{geo} encourages TSegFormer to adaptively focus more on error-prone points with higher point curvatures with negligible extra computations. Specifically, we define it as

$$L_{geo} = -\sum_{i \in S(r)} \sum_{c=1}^{33} (1 - \hat{p}_{ic}^{geo})^{\gamma} \cdot \Phi(y_{S(r)_i}, c) \cdot log(\hat{p}_{ic}^{geo}), \tag{1}$$

where γ is the modulating factor (empirically set to 2 in experiments); $y_{S(r)_i} \in \mathbb{R}^{33}$ represents the gold label of the *i*-th point in the point set S(r); \hat{p}_{ic}^{geo} denotes the predicted probability of the *i*-th point belonging to the *c*-th class, and $\Phi(y_i,c)$ is an indicator function which outputs 1 if $y_i=c$ and 0 otherwise. Concretely, S(r) is a set of points whose point curvatures m_i are among the top $r\cdot 100\%$ ($0 < r \le 1$) of all N points, i.e., $S(r) := \{a_1, a_2, \cdots, \lceil a_{rN} \rceil\}$, where $m_{a_1} \ge m_{a_2} \ge \cdots > m_{a_{rN}} \ge m_{a_{rN+1}} \ge \cdots \ge m_{a_N}$. The experimental results (Fig. 2(d)) on a dataset of 2,000 cases indicate that L_{geo} is more effective with our point curvature over traditional mean and Gaussian curvatures, even they are worst than no curvature. This is because our point curvature provides more clear tooth-tooth and tooth-gingiva boundary indications (Fig. 2(a)-2(c)), thus avoiding misleading the model to focus too much on unimportant non-boundary points.

We employ the cross entropy loss as the loss of main segmentation head (L_{seg}) and the loss of auxiliary segmentation head (L_{aux}) . The total loss L_{total} is computed by combining L_{seg} , L_{aux} for all points and L_{geo} for hard points: $L_{total} = L_{seg} + \omega_{geo} \cdot L_{geo} + \omega_{aux} \cdot L_{aux}$. We set the weights $\omega_{geo} = 0.001$, $\omega_{aux} = 1$ and the ratio r = 0.4, and detailed hyperparameter search results in SM Fig. 1 indicate that the performance is stable across different hyperparameter settings.

3 Experiments

3.1 Dataset and Experimental Setup

We construct a large-scale 3D IOS dataset consisting of 16,000 IOS meshes with full arches (each with 100,000 to 350,000 triangular faces) collected between 2018-

2021 in China, with evenly distributed maxillary and mandible scans labeled by human experts. Detailed data statistics are presented in SM Table 2, and 39.8% of the data have third-molars, 16.8% suffer from missing teeth, which all reveal the complexity of the dataset. The dataset is randomly split into training (12,000 IOSs), validation (2,000 IOSs) and test sets (2,000 IOSs). Furthermore, we collect an external dataset with 200 complex cases (disease statistics shown in SM Table 3) to evaluate the real-world clinical applicability of TSegFormer. Detailed training and architecture settings are in SM Tables 4 and 5.

3.2 Main Results on Tooth Segmentation

To our best knowledge, there has been no prior work on Transformer-based segmentation on non-Euclidean 3D tooth point clouds/meshes. Hence, we compare our TSegFormer to seven representative and state-of-the-art baselines from three categories: 1) neural networks for point clouds, including PointNet++ [16] and DGCNN [20]; 2) transformers for point clouds, including point transformer [28] and PVT [26]; 3) domain-specific architectures for 3D tooth segmentation, including MeshSegNet [12], TSGCNet [27] and DC-Net [6]. For fair comparison, baselines that cannot achieve raw-resolution mesh prediction followed the same inference protocols in 2.1, while the rest kept their original inference schemes.

Method	Mandible			Maxillar	У		All		
	mIoU ↑	$DSC\uparrow$	Acc ↑	mIoU ↑	DSC ↑	Acc ↑	mIoU ↑	DSC ↑	Acc ↑
${\bf PointNet}{+}{+}$	81.11	85.33	94.96	83.89	87.12	96.28	82.57	86.27	95.65
DGCNN	92.41	94.49	97.68	93.82	95.61	98.01	93.15	95.08	97.85
point transformer	92.61	94.83	97.55	93.93	95.72	98.06	93.3	95.3	97.81
PVT	90.66	93.59	96.64	92.46	94.72	97.44	91.6	94.19	97.06
MeshSegNet	82.21	86.55	91.98	85.37	89.28	93.72	83.87	87.98	92.90
TSGCNet	80.71	85.23	92.78	80.97	85.28	93.86	80.85	85.25	93.34
DCNet	91.18	93.89	97.11	92.78	95.18	97.44	92.02	94.57	97.28
TSegFormer (Our)	93.53	95.36	97.72	95.07	96.60	98.20	94.34	96.01	97.97

Table 1. Main segmentation results (Tested on 1,000 patients).

Table 2. Ablation study on different main components.

Component		Mandible			Maxillary			All		
Geometry guided loss	Auxiliary branch	mIoU	DSC	Acc	mIoU	DSC	Acc	mIoU	DSC	Acc
		92.19	94.27	97.35	94.02	95.69	97.96	93.15	95.01	97.67
	✓	92.53	94.57	97.43	94.45	96.10	98.02	93.54	95.37	97.74
✓		92.46	94.47	97.37	94.45	96.12	98.02	93.51	95.33	97.71
✓	✓	92.95	94.88	97.57	94.46	96.07	98.14	93.77	95.51	97.87

We can firstly observe that TSegFormer outperforms existing best-performing point transformer model [28] by 0.16% in accuracy, 1.04% in mIoU and 0.71%

in DSC (Table 1). Such an improvement is surely significant considering the complicated real-world cases in our large-scale dataset and the relatively high performance of point transformer with an mIoU of 93.30%. Moreover, TSeg-Former consistently surpassed all baselines on both mandible and maxillary in terms of all metrics, demonstrating its universal effectiveness.

It is important to integrate advanced architectures with domain-specific design for superior performance. We can notice that though MeshSegNet, TSGC-Net, and DCNet are all domain-specific 3D tooth segmentation models, their performance, though on par with PVT and DGCNN, is worse than the point transformer. This is also consistent with the superior performance of transformer-based models on standard point cloud processing tasks, which could be mainly attributed to the larger dataset and powerful attention mechanism that better capture global dependencies. Hence, though models like MeshSegNet adopt some task-specific designs to achieve good performance, they still lag behind point transformer when a huge amount of data samples are available. In contrast, our TSegFormer employs the attention mechanism for point representation learning, and meanwhile, adopted task-specific architectures and geometry guided loss to further boost the performance. More statistical results are in SM Table 2.

Table 3. Segmentation performance of DCNet [6] with our geometry guided loss.

Model	Mandible			Maxillary			All		
	mIoU	DSC	Acc	mIoU	DSC	Acc	mIoU	DSC	Acc
DCNet	87.72	91.00	95.99	90.77	93.50	96.87	89.32	92.31	96.46
$\mathrm{DCNet}{+}L_{geo}$	89.66	92.58	96.46	91.75	94.28	97.14	90.75	93.47	96.82

Table 4. Segmentation performance of TSegFormer under different training set scales.

Training set scale	Mandible			Maxillary			All		
	mIoU	DSC	Acc	mIoU	DSC	Acc	mIoU	DSC	Acc
500	86.36	89.74	95.45	89.22	91.69	96.57	87.86	90.76	96.04
1,000	90.60	93.13	96.72	92.84	94.77	97.50	91.78	93.99	97.13
2,000	92.15	94.28	97.31	94.05	95.79	97.92	93.15	95.08	97.63
4,000	93.10	95.05	97.69	94.68	96.28	98.12	93.93	95.70	97.92
8,000	93.27	95.15	97.67	94.83	96.40	98.16	94.09	95.81	97.92
12,000	93.53	95.36	97.72	95.07	96.60	98.20	94.34	96.01	97.97

3.3 Ablation Studies

Effectiveness of Geometry Guided Loss. Table 2 shows that introducing the geometry guided loss can improve the performance under all three metrics, e.g., around 0.4% improvement in mIoU. Besides, we show the universal effectiveness of the geometry guided loss by adding it to DCNet [6]. The performance of DCNet is also enhanced by 1.43% in mIoU (Table 3) with this additional loss.

Effectiveness of the Auxiliary Segmentation Head. The auxiliary segmentation head is designed to rectify the inaccuracy brought by mislabeling teeth and gingiva near their boundaries. Adding a loss for the auxiliary branch leads to about 0.4% mIoU performance improvement (Table 2).

Effectiveness on Training Data Efficiency. In real-world orthodontic applications, large-scale training data may not be directly accessible due to privacy concerns. Therefore, to show our model's data efficiency, we train our model on datasets with different sizes (Table 4). With only 500 training samples, TSeg-Former is able to surpass PointNet++, MeshSegNet and TSGCNet trained on 12,000 samples. Furthermore, TSegFormer trained with only 2,000 samples can almost outperform all previous models trained on 12,000 samples. Overall, these results demonstrate the exceptional data efficiency of our TSegFormer.

Effectiveness of Local Point Embedding. SM Table 1 shows purely MLP-based structures perform worst due to the lack of local contexts, while EdgeConv layers can make up for this, and the collaboration of both performs best.

Table 5. Clinical applicability test on the external IOS dataset (200 cases). "#success"/"#fail": number of segmentation that meets/does not meet the clinical criteria. #param: number of parameters in the network. Inf-T: inference time for 200 cases.

Model	#success ↑	#fail ↓	clinical error rate (%) \downarrow	#param ↓	Inf-T(s) ↓
MeshSegNet	65	135	67.5	1.81M	128.56
TSGCNet	15	185	92.5	4.13M	31.40
Point Transformer	97	103	51.5	6.56M	437.21
DCNet	109	91	45.5	1.70M	5.79
TSegFormer (Our)	152	48	24.0	4.21M	23.15

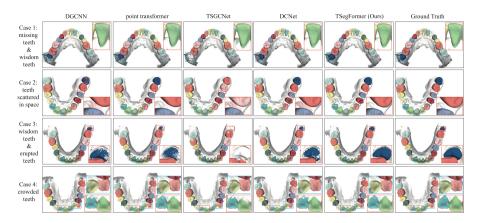


Fig. 3. Visualization of segmentation of different methods across different diseases.

3.4 Clinically Applicability Test and Visualization

To show the effectiveness of TSegFormer in real-world scenarios, we conducted a clinical applicability test (Table 5) on a dataset with 200 complex IOS scans, whose diseases statistics are in SM Table 3. The segmentation with five different models were evaluated by a committee of dentists with more than 5-year experience. We can notice that TSegFormer significantly outperforms the other models regarding the clinical error rate.

The feedback from dentists indicates that models such as TSGCNet cannot meet the requirement when dealing with complicated boundaries, while TSeg-Former apparently handles them better. The point transformer and DCNet also showed promising performance, but they are yet far behind our TSegFormer. As for the number of parameters and inference time, though TSegFormer has the second most parameters among all methods we tested, it is the second fastest method that only takes around 23 s to complete inference for 200 cases, which is certainly acceptable in real-world clinical scenarios.

By visualization, we show the superiority of TSegFormer on various complicated dental diseases in Fig. 3. The baselines unavoidably produce false predictions or even fail to identify an entire third-molar, while TSegFormer can yield more accurate segmentation and smoother boundaries (see SM Fig. 2 for details), corroborating great potential for clinical applications. Specifically, SM Fig. 3 shows that with our geometry guided loss and auxiliary head, the isolated mispredictions and boundary errors are greatly reduced. However, TSegFormer fails in some complex samples, e.g. the missing tooth, the erupted wisdom tooth and sunken gingiva and alveolar bone regions, as illustrated in SM Fig. 4, which needs to be further studied.

4 Conclusion

We propose TSegFormer, a 3D transformer-based model for high-resolution IOS segmentation. It combines a point embedding module and attention mechanism to effectively capture local and global features, and introduces a geometry guided loss based on a novel point curvature to handle boundary errors and multi-task segmentation heads for boundary refinement. Results of comprehensive experiments on a large-scale dataset and clinical applicability tests demonstrate TSeg-Former's state-of-the-art performance and its great potential in digital dentistry.

Acknowledgements. This work is supported by the National Natural Science Foundation of China (Grant No. 62106222), the Natural Science Foundation of Zhejiang Province, China (Grant No. LZ23F020008) and the Zhejiang University-Angelalign Inc. R&D Center for Intelligent Healthcare.

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