

Question 3 :

The goal of the algorithm is to find the longest monotonically increasing subsequence of a sequence of n numbers. To do this, first we'll start we'll use two arrays M and P such that;

$M[j]$ will store the index k of the smallest value $X[k]$ such that there is an increasing subsequence of length j ending at $X[k]$ on the range $k \leq i$.

And

$P[k]$ will store the index of the predecessor of $X[k]$ in the longest increasing subsequence ending at $X[k]$

Pseudo-code :

```
def longestIncreasingSubsequence(sequence, subsequence, elem):
    P = array of length N
    M = array of length N + 1

    L = 0
    for i in range 0 to N-1:
        // Binary search
        lo = 1
        hi = L
        while lo ≤ hi:
            mid = ceil((lo+hi)/2)
            if sequence[M[mid]] < X[i]:
                lo = mid+1
            else:
                hi = mid-1

        // After searching, lo is 1 greater than the
        // length of the longest prefix of sequence[i]
        newL = lo

        // The predecessor of sequence[i] is the last index of the subsequence of
        length newL-1
        P[i] = M[newL-1]
        M[newL] = i

    if newL > L:
        L = newL
```

```
Solution = array of length L
k = M[L]
for i in range L-1 to 0:
    Solution[i] = X[k]
    k = P[k]

return Solution
```

The binary search is be done in time $O(\log n)$ since the subsequences are in increasing order . The loop will run $O(n)$ times, resulting in a running time of $O(n \log n)$.

Help from wikipedia page.

Question 4 :

W1 = AACT & W2 = GAT. The optimal alignment with a minimum score of 0 using the edit score is :

AACT

GA-T

$$d(x,y) = \begin{cases} -1 & \text{if } x = y \\ 1 & \text{otherwise.} \end{cases}$$

	-	A	A	C	T
-	0	1	2	3	4
G	1	1	2	3	4
A	2	0	0	1	2
T	3	1	1	1	0

