

Question 1:

The output is : 1st column is the size, second is the average #operations for naive algorithm and the third is the average #operations for Karatsuba algorithm.

1	1	1
2	7	9
3	34	39
4	34	39
5	145	135
6	145	135
7	148	141
8	148	141
9	595	435
10	595	435
11	598	441
12	598	441
13	613	465
14	613	465
15	616	471

The karatsuba algorithm make less recursive calls than the naive algorithm however it does make twice addition and subtraction operations, hence why it is less efficient to calculate the multiplication of numbers with small size. As for big sizes (larger than 4), the Karatsuba algorithm is more efficient as the gap between the #operations keep increasing as the size increase.

