

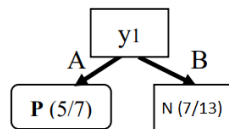
I. Pen-and-paper

1) $\#P = 5 + 3 + 3 = 11$

$\#N = 2 + 5 + 2 = 9$

	P	N
P	8	4
N	3	5

2)



$$P = \frac{TP}{TP + FP} = \frac{5}{5 + 2} = \frac{5}{7} \sim 0.71428$$

	P	N
P	5	2
N	6	7

$$R = \frac{TP}{TP + FN} = \frac{5}{5 + 6} = \frac{5}{11} \sim 0.45454$$

$$\frac{1}{F1} = \frac{1}{2} \left(\frac{1}{P} + \frac{1}{R} \right) = \frac{1}{2} \left(\frac{7}{5} + \frac{11}{5} \right) = \frac{9}{5}$$

$$F1 = \frac{5}{9} \sim 0.55556$$

3) The left tree path wasn't further decomposed in order to avoid overfitting and because further splitting would increase the impurity of the node.

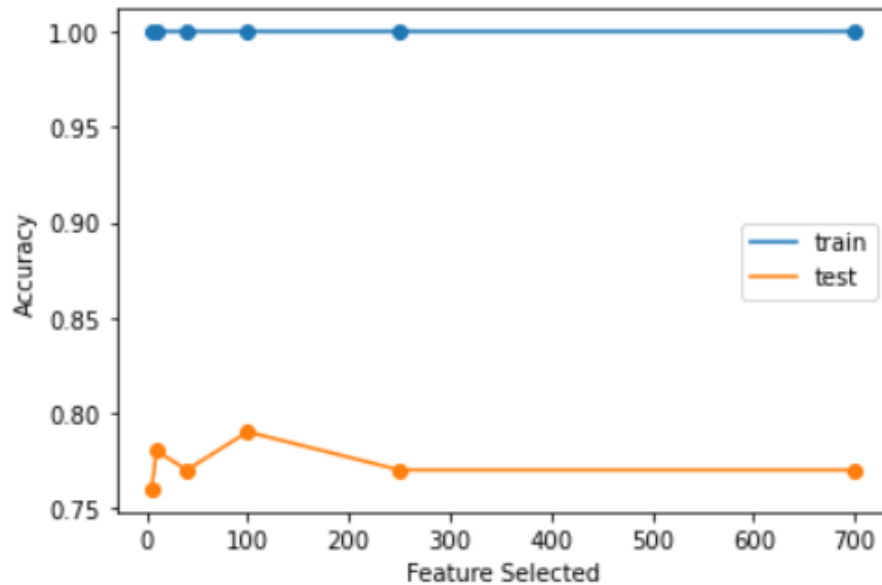
4) $IG(y_1) = H(X) - \sum_{i=1}^k \frac{|X_i|}{|X|} H(y_i) \quad H(X) = -\frac{11}{20} \log_2 \left(\frac{11}{20} \right) - \frac{9}{20} \log_2 \left(\frac{9}{20} \right) \sim 0.99277$

$$\sum_{i=1}^k \frac{|X_i|}{|X|} H(y_i) = \frac{7}{20} \left[-\frac{5}{7} \log_2 \left(\frac{5}{7} \right) - \frac{2}{7} \log_2 \left(\frac{2}{7} \right) \right] + \frac{13}{20} \left[-\frac{6}{13} \log_2 \left(\frac{6}{13} \right) - \frac{7}{13} \log_2 \left(\frac{7}{13} \right) \right] \approx 0.94932$$

$$IG(y_1) = 0.99277 - 0.94932 = 0.04345$$

II. Programming and critical analysis

1. [1.0, 1.0, 1.0, 1.0, 1.0, 1.0]
 [0.77, 0.76, 0.82, 0.81, 0.80, 0.81]



2. Training accuracy is consistently 1 because it is the set used to train the decision tree.

III. APPENDIX

```
import pandas as pd
import numpy as np
from sklearn import metrics, datasets, tree
from sklearn.feature_selection import mutual_info_classif
from sklearn.feature_selection import SelectKBest
from sklearn.model_selection import train_test_split
from sklearn.tree import DecisionTreeClassifier
import matplotlib.pyplot as plt
from scipy.io.arff import loadarff

# Loading data from arff file
data = loadarff('pd_speech.arff')
df = pd.DataFrame(data[0])
df['class'] = df['class'].str.decode('utf-8')

# Splitting data into X and y
X = df.drop("class", axis=1)
y = df['class']
df.head()

feats = [5, 10, 40, 100, 250, 700]
train = np.zeros(len(feats))
```

Aprendizagem 2021/22
Homework I – Group XXX

```
test = np.zeros(len(feats))

# For loop to iterate through the different number of features
for index, el in enumerate(feats):

    # Feature selection using mutual information
    X_newbest = SelectKBest(score_func=mutual_info_classif, k=el).fit_transform(X, y)

    # Splitting the data into training and testing sets
    X_train, X_test, y_train, y_test = train_test_split( X_newbest, y, train_size=0.3,
random_state=1)

    # Creating the decision tree
    D_Tree = DecisionTreeClassifier()

    # Training the decision tree
    predictor = D_Tree.fit(X_train, y_train)

    # Predicting the training and testing sets
    y_train_predict = predictor.predict(X_train)
    y_test_predict = predictor.predict(X_test)

    # Calculating the accuracy of the training and testing sets
    train[index] = round(metrics.accuracy_score(y_train, y_train_predict), 2)
    test[index] = round(metrics.accuracy_score(y_test, y_test_predict), 2)

# plot train and test
plt.plot(feats, train, label='train')
plt.plot(feats, test, label='test')
plt.xlabel('Feature Selected')
plt.ylabel('Accuracy')

# scatter train and test
plt.scatter(feats, train)
plt.scatter(feats, test)
plt.legend()
plt.show()
```

END