

## Programming Homework 5: Unsupervised Learning, Clustering, Density Estimation, Mixture of Independent Gaussians, K-means; Application: Clustering for Robot Localization

### Clustering by Gaussian Naive-Bayes Models

#### Estimates for $\pi_c$

Cluster 1	Cluster 2	Cluster 3
0.5669	0.3384	0.0947

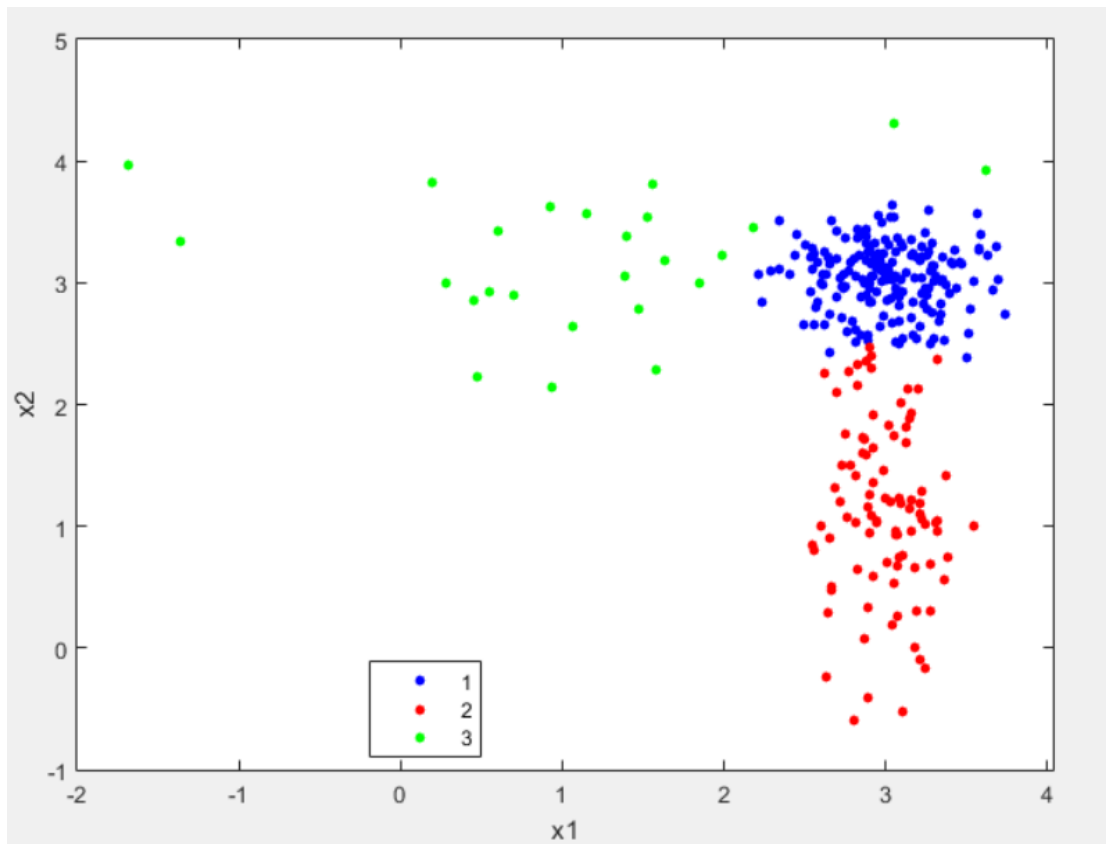
#### Estimates for $\mu_{i|c}$

	Cluster 1	Cluster 2	Cluster 3
$x_1$	3.0079	2.9972	1.2977
$x_2$	3.0503	1.2824	3.1541

#### Estimates for $\sigma^2_{i|c}$

	Cluster 1	Cluster 2	Cluster 3
$x_1$	0.1000	0.0473	1.3766
$x_2$	0.0733	0.7215	0.2566

### Plot of Gaussian Clustered Data



## Clustering by Generalized K-Means

### Estimates for $\pi_c$

Cluster 1	Cluster 2	Cluster 3
0.6067	0.3100	0.0833

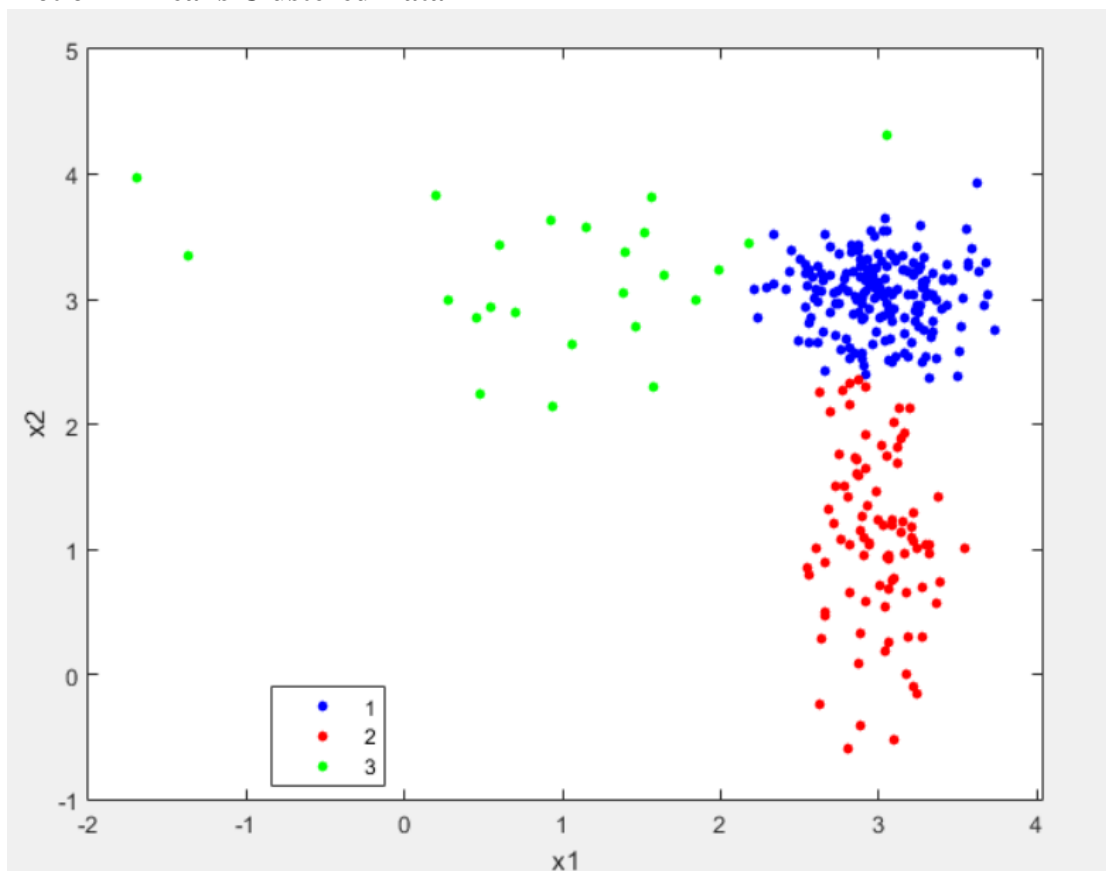
### Estimates for $\mu_{i|c}$

	Cluster 1	Cluster 2	Cluster 3
$x_1$	3.0048	2.9926	1.1013
$x_2$	3.0386	1.1302	3.2172

### Estimates for $\sigma^2_{i|c}$

	Cluster 1	Cluster 2	Cluster 3
$x_1$	0.0985	0.0464	1.2327
$x_2$	0.0732	0.4972	0.2980

### Plot of K-Means Clustered Data



## Analysis

The result of the two methods was very similar, but a few things were slightly different. Three points were changed from cluster 2 to cluster 1 and one point was changed from cluster 3 to cluster 1. In the Gaussian method,  $\sigma_{2|2}^2$  was 0.7215, but it sharply decreased to 0.4972 in the K-Means method. The values for  $\pi_c$  and  $\mu_{i|c}$  only had very slight differences.

## Running the Code

The code to run the Gaussian Naive-Bayes method of clustering is found in `em.m`, and the code to run the K-Means method is found in `kmeans.m`. `fcondjoin.m` is the function to find the conditional joint probability of two  $x$  values based on provided  $\sigma_{i|c}^2$  and  $\mu_{i|c}$ , and is used by both `em.m` and `kmeans.m`. This code was written, tested, and can be run in Matlab. `kmeans.m` should be run after `em.m` because it makes use of the variables saved in the workspace after `em.m` finishes running.