

# Cattaneo, Jansson and Ma (2020, JASA)

---

Yasuyuki Matsumura (Kyoto University)

Last Updated: May 3, 2025

<https://yasu0704xx.github.io>



## Simple Local Polynomial Density Estimators

Matias D. Cattaneo<sup>a</sup>, Michael Jansson<sup>b</sup>, and Xinwei Ma<sup>c</sup>

<sup>a</sup>Department of Operations Research and Financial Engineering, Princeton University, Princeton, NJ; <sup>b</sup>Department of Economics, CREATES, University of California, Berkeley, CA; <sup>c</sup>Department of Economics, University of California, San Diego, CA

### ABSTRACT

This article introduces an intuitive and easy-to-implement nonparametric density estimator based on local polynomial techniques. The estimator is fully boundary adaptive and automatic, but does not require pre-binning or any other transformation of the data. We study the main asymptotic properties of the estimator, and use these results to provide principled estimation, inference, and bandwidth selection methods. As a substantive application of our results, we develop a novel discontinuity in density testing procedure, an important problem in regression discontinuity designs and other program evaluation settings. An illustrative empirical application is given. Two companion Stata and R software packages are provided.

### ARTICLE HISTORY

Received September 2017  
Accepted May 2019

### KEYWORDS

Density estimation; Local polynomial methods; Manipulation test; Regression discontinuity

This slide is available on

<https://github.com/yasu0704xx/ArticleReview>.

Introduction

Boundary Adaptive Density Estimation

Main Technical Results

Application to Manipulation Testing

Empirical Illustration

Conclusion

References

# Introduction

---

# Boundary Adaptive Density Estimation

---

## Main Technical Results

---

## Application to Manipulation Testing

---

## Empirical Illustration

---









## Conclusion





---




## References





---





-  Abadie, A., and Cattaneo, M. D. (2018). Econometric methods for program evaluation. *Annual Review of Economics*, **10**, 465-503.
-  Arai, Y., and Ichimura, H. (2018). Simultaneous selection of optimal bandwidths for the sharp regression discontinuity estimator. *Quantitative Economics*, **9**, 441-482.
-  Calonico, S., Cattaneo, M. D., and Farrell, M. H. (2018). On the effect of bias estimation on coverage accuracy in nonparametric inference. *Journal of the American Statistical Association*, **113**, 767-779.

-  Calonico, S., Cattaneo, M. D., and Titiunik, R. (2014). Robust nonparametric confidence intervals for regression-discontinuity designs. *Econometrica*, **82**, 2295-2326.
-  Cattaneo, M. D., Jansson, M., and Ma, X. (2018). Manipulation testing based on density discontinuity. *Stata Journal*, **18**, 234-261.
-  Cattaneo, M. D., Jansson, M., and Ma, X. (2019). *lpdfensity: Local Polynomial Density Estimation and Inference*. arXiv:1906.06529.

-  Cattaneo, M. D., Titiunik, R., and Vazquez-Bare, G. (2017). Comparing inference approaches for RD designs: A reexamination of the effect of Head Start on child mortality. *Journal of Policy Analysis and Management*, **36**, 643-681.
-  Cheng, M.-Y., Fan, J., and Marron, J. S. (1997). On automatic boundary corrections. *Annals of Statistics*, **25**, 1691-1708.
-  Dong, Y., Lee, Y.-Y., and Gou, M. (2019). Regression discontinuity designs with a continuous treatment. SSRN Working Paper No. 3167541.
-  Fan, J., and Gijbels, I. (1996). *Local Polynomial Modelling and Its Applications*. New York: Chapman & Hall/CRC.

-  Ganong, P., and Jager, S. (2018). A permutation test for the regression kink design. *Journal of the American Statistical Association*, **113**, 494-504.
-  Hyytinen, A., Merilainen, J., Saarimaa, T., Toivanen, O., and Tukiainen, J. (2018). When does regression discontinuity design work? Evidence from random election outcomes. *Quantitative Economics*, **9**, 1019-1051.
-  Imbens, G., and Lemieux, T. (2008). Regression discontinuity designs: A guide to practice. *Journal of Econometrics*, **142**, 615-635.

-  Imbens, G. W., and Rubin, D. B. (2015). *Causal Inference in Statistics, Social, and Biomedical Sciences*. New York: Cambridge University Press.
-  Karunamuni, R., and Alberts, T. (2005). On boundary correction in kernel density estimation. *Statistical Methodology*, **2**, 191-212.
-  Lee, D. S., and Lemieux, T. (2010). Regression discontinuity designs in economics. *Journal of Economic Literature*, **48**, 281-355.
-  Li, K.-C. (1987). Asymptotic optimality for  $C_p$ ,  $C_L$ , cross-validation and generalized cross-validation: Discrete index set. *Annals of Statistics*, **15**, 958-975.

-  Ludwig, J., and Miller, D. L. (2007). Does Head Start improve children ' s life chances? Evidence from a regression discontinuity design. *Quarterly Journal of Economics*, **122**, 159-208.
-  McCrary, J. (2008). Manipulation of the running variable in the regression discontinuity design: A density test. *Journal of Econometrics*, **142**, 698-714.
-  Otsu, T., Xu, K.-L., and Matsushita, Y. (2014). Estimation and inference of discontinuity in density. *Journal of Business and Economic Statistics*, **31**, 507-524.
-  Wand, M., and Jones, M. (1995). *Kernel Smoothing*. New York: Chapman & Hall/CRC.





Zhang, S., and Karunamuni, R. J. (1998). On kernel density estimation near endpoints. *Journal of Statistical Planning and Inference*, **70**, 301-316.