

EE2703 END SEM

Yaswanth Bandi,EE20B020

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1 Pseudo Code for Question1

We are trying to compute points to work on.

1. Divide the wire into pieces of length dz and so, we have $2N$ pieces and $2N + 1$ points.
2. Then we are going to create an array "z" of length $2N + 1$ which contains point coordinates. This is done using "*linspace*" command.
3. We will take construct array of length $2N - 2$ which will not have coordinates $-0.5, 0, 0.5$ was done by deleting it from z.
4. We are going to compute at $N = 4$.

1.1 Matrices Obtained

Vector z :

$[-0.5 \quad -0.38 \quad -0.25 \quad -0.12 \quad 0. \quad 0.12 \quad 0.25 \quad 0.38 \quad 0.5]$

Vector u :

$[-0.38 \quad -0.25 \quad -0.12 \quad 0.12 \quad 0.25 \quad 0.38]$

2 Pseudo Code for Question2

We need an equation for each unknown current. These equations are obtained by calculating the Magnetic field in two different ways.

From Ampere's Law:

1. We have $H = M * J$. We will compute H at $r = a$
2. We will construct matrix M by using "*identity*" command to get unit matrix of size $(2N - 2, 2N - 2)$

2.1 Matrices Obtained

Matrix M:

$$\begin{bmatrix} 15.92 & 0. & 0. & 0. & 0. & 0. \\ 0. & 15.92 & 0. & 0. & 0. & 0. \\ 0. & 0. & 15.92 & 0. & 0. & 0. \\ 0. & 0. & 0. & 15.92 & 0. & 0. \\ 0. & 0. & 0. & 0. & 15.92 & 0. \\ 0. & 0. & 0. & 0. & 0. & 15.92 \end{bmatrix}$$

3 Pseudo Code for Question3

From Vector potential:

1. We have to construct two Matrices P and P_B .
 P is the contribution to the vector potential due to currents unknown. It is a matrix with $2N - 2$ columns and $2N - 2$ rows.
 P_B is the contribution to the vector potential due to current $z = 0$. It is a column vector.
2. To construct those we are going to need Rz, Ru, RN .
 Rz computes distances including distances to known current.
 Ru is a vector of distances to unknown currents.
 RN is distances with respect to $z = 0$ coordinate.
3. From Ru and RN we will get P and P_B .

3.1 Matrices Obtained

Matrix Rz :

```
[[0.01 0.13 0.25 0.38 0.5 0.63 0.75 0.88 1. ]
 [0.13 0.01 0.13 0.25 0.38 0.5 0.63 0.75 0.88]
 [0.25 0.13 0.01 0.13 0.25 0.38 0.5 0.63 0.75]
 [0.38 0.25 0.13 0.01 0.13 0.25 0.38 0.5 0.63]
 [0.5 0.38 0.25 0.13 0.01 0.13 0.25 0.38 0.5 ]
 [0.63 0.5 0.38 0.25 0.13 0.01 0.13 0.25 0.38]
 [0.75 0.63 0.5 0.38 0.25 0.13 0.01 0.13 0.25]
 [0.88 0.75 0.63 0.5 0.38 0.25 0.13 0.01 0.13]
 [1. 0.88 0.75 0.63 0.5 0.38 0.25 0.13 0.01]]
```

```
[1. +0.j 0.88+0.j 0.75+0.j 0.63+0.j 0.5 +0.j 0.38+0.j
 0.25+0.j 0.13+0.j 0.01+0.j]]
```

Matrix Ru :

```
[[0.01 0.13 0.25 0.5 0.63 0.75]
 [0.13 0.01 0.13 0.38 0.5 0.63]
 [0.25 0.13 0.01 0.25 0.38 0.5 ]
 [0.5 0.38 0.25 0.01 0.13 0.25]
 [0.63 0.5 0.38 0.13 0.01 0.13]
 [0.75 0.63 0.5 0.25 0.13 0.01]]
```

Vector RN :

```
[0.38+0.j 0.25+0.j 0.13+0.j 0.13+0.j 0.25+0.j 0.38+0.j]
```

Vector $P_B \times 1e8$:

```
[1.27-3.08j 3.53-3.53j 9.2 -3.83j 9.2 -3.83j 3.53-3.53j 1.27-3.08j]
```

Matrix P*1e8 :

```

[[124.94-3.93j    9.2 -3.83j    3.53-3.53j    -0.    -2.5j
 -0.77-1.85j
  -1.18-1.18j]
 [   9.2 -3.83j 124.94-3.93j    9.2 -3.83j    1.27-3.08j
 -0.    -2.5j
  -0.77-1.85j]
 [   3.53-3.53j    9.2 -3.83j 124.94-3.93j    3.53-3.53j
 1.27-3.08j
  -0.    -2.5j ]
 [  -0.    -2.5j    1.27-3.08j    3.53-3.53j 124.94-3.93j
 9.2 -3.83j
   3.53-3.53j]
 [  -0.77-1.85j  -0.    -2.5j    1.27-3.08j    9.2 -3.83j 124.94-3.93j
   9.2 -3.83j]
 [  -1.18-1.18j  -0.77-1.85j  -0.    -2.5j    3.53-3.53j
 9.2 -3.83j
 124.94-3.93j]]

```

4 Pseudo Code for Question4

1. We have to construct two Matrices Q and Qb .

Q is the contribution due to currents unknown. It is a matrix with $2N - 2$ columns and $2N - 2$ rows.

Pb is the contribution due to current at $z = 0$. It is a column vector.

2. To construct those we are going to need Rz, Ru, RN .

3. From Ru and RN we will get Q and Qb .

4.1 Matrices Obtained

Matrix Q :

```
[[9.952e+01-0.j 5.000e-02-0.j 1.000e-02-0.j 0.000e+00-0.j 0.000e+00-0.j
  0.000e+00-0.j]
 [5.000e-02-0.j 9.952e+01-0.j 5.000e-02-0.j 0.000e+00-0.j 0.000e+00-0.j
  0.000e+00-0.j]
 [1.000e-02-0.j 5.000e-02-0.j 9.952e+01-0.j 1.000e-02-0.j 0.000e+00-0.j
  0.000e+00-0.j]
 [0.000e+00-0.j 0.000e+00-0.j 1.000e-02-0.j 9.952e+01-0.j 5.000e-02-0.j
  1.000e-02-0.j]
 [0.000e+00-0.j 0.000e+00-0.j 0.000e+00-0.j 5.000e-02-0.j 9.952e+01-0.j
  5.000e-02-0.j]
 [0.000e+00-0.j 0.000e+00-0.j 0.000e+00-0.j 1.000e-02-0.j 5.000e-02-0.j
  9.952e+01-0.j]]
```

Matrix Qb :

```
[0. -0.j 0.01-0.j 0.05-0.j 0.05-0.j 0.01-0.j 0. -0.j]
```

5 Pseudo Code for Question5

1. Our final equation is $M * J = Q * J + QbIm$
i.e., $(MQ) * J = Qb * Im$
2. We will use $inv(M - Q)$ to solve for J .
3. We construct the another vector with known currents and unknown currents.
4. We will get the exact curves on increasing N value.

5.1 Matrices Obtained

I calculated :

```
[ 0.+0.j -0.+0.j -0.+0.j -0.+0.j  1.+0.j -0.+0.j -0.+0.j -0.+0.j
 0.+0.j ]
```

I assumed :

```
[0.    0.38 0.71 0.92 1.    0.92 0.71 0.38 0. ]
```

5.2 Plots

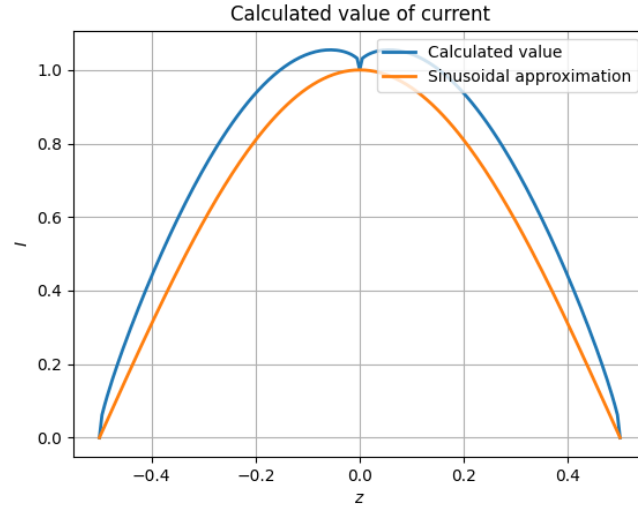


Figure 1: Antenna currents in a half-wave dipole antenna at N=100

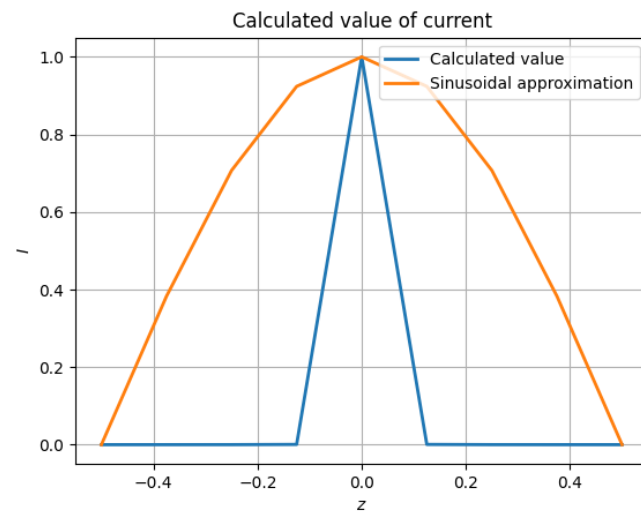


Figure 2: Antenna currents in a half-wave dipole antenna at $N=4$