TOPIC 2: BRUTE FORCE

1. Write a program to perform the following An empty list

A list with one element

A list with all identical elements A list with negative numbers **Test**

Cases:

- 1. Input: []
- Expected Output: []
- **1**. **Input:** [1]
- Expected Output: [1]
- 2. **Input:** [7, 7, 7, 7]
- **Expected Output:** [7, 7, 7, 7]
- *Input*: [-5, -1, -3, -2, -4]
- **Expected Output:** [-5, -4, -3, -2, -1]

```
1 def process_list(lst):
       if len(lst) <= 1:
            return 1st
4
       else:
           return sorted(lst)
6 test_cases = [
       [],
        [1],
9
        [7, 7, 7, 7],
       [-5, -1, -3, -2, -4]
10
11 ]
12 for i, test in enumerate(test_cases, 1):
13
       print(f"Test Case {i}: Input: {test} -> Output: {process_list(test)}")
14
```

```
Output

Test Case 1: Input: [] -> Output: []

Test Case 2: Input: [1] -> Output: [1]

Test Case 3: Input: [7, 7, 7, 7] -> Output: [7, 7, 7, 7]

Test Case 4: Input: [-5, -1, -3, -2, -4] -> Output: [-5, -4, -3, -2, -1]

=== Code Execution Successful ===
```

2. Describe the Selection Sort algorithm's process of sorting an array. Selection Sort works by dividing the array into a sorted and an unsorted region. Initially, the sorted region is empty, and the unsorted region contains all elements. The algorithm repeatedly selects the smallest element from the unsorted region and swaps it with the leftmost unsorted element, then moves the boundary of the sorted region one element to the right. Explain why Selection Sort is simple to understand and implement but is inefficient for large datasets. Provide examples to illustrate step-by-step how Selection Sort rearranges the elements into ascending order, ensuring clarity in your explanation of the algorithm's mechanics and effectiveness.

Sorting a Random Array:

```
Input: [5, 2, 9, 1, 5, 6]
```

Output: [1, 2, 5, 5, 6, 9]

Sorting a Reverse Sorted Array:

Input: [10, 8, 6, 4, 2]

Output: [2, 4, 6, 8, 10]

Sorting an Already Sorted Array:

Input: [1, 2, 3, 4, 5]

Output: [1, 2, 3, 4, 5]

```
1 def selection_sort(arr):
 2
        n = len(arr)
        for i in range(n):
 3
            min_index = i
 4
 5
            for j in range(i + 1, n):
                if arr[j] < arr[min_index]:</pre>
 6 -
 7
                    min index = i
            arr[i], arr[min_index] = arr[min_index], arr[i]
 8
 9
            print(f"Step {i+1}: {arr}")
10
        return arr
11 arrays = {
12
        "Random Array": [5, 2, 9, 1, 5, 6],
        "Reverse Sorted Array": [10, 8, 6, 4, 2],
13
        "Already Sorted Array": [1, 2, 3, 4, 5]
14
15
    }
16 for name, arr in arrays.items():
17
        print(f"\n{name}: Initial Array: {arr}")
        sorted_arr = selection_sort(arr.copy())
18
19
        print(f"Sorted Array: {sorted_arr}")
```

2. Write code to modify bubble_sort function to stop early if the list becomes sorted before all passes are completed.

Test Cases:

- Test your optimized function with the following lists:
- 1. **Input:** [64, 25, 12, 22, 11]
- Expected Output: [11, 12, 22, 25, 64]
- 2. **Input:** [29, 10, 14, 37, 13]
- **Expected Output:** [10, 13, 14, 29, 37]
- **3. Input:** [3, 5, 2, 1, 4]
- **Expected Output:** [1, 2, 3, 4, 5]
- 4. **Input:** [1, 2, 3, 4, 5] (Already sorted list)
- **Expected Output:** [1, 2, 3, 4, 5]
- *5.* **Input:** [5, 4, 3, 2, 1] (Reverse sorted list)
- **Expected Output:** [1, 2, 3, 4, 5]

```
1 def bubble_sort(arr):
        n = len(arr)
2
        for i in range(n):
3
4
            swapped = False
            for j in range(0, n - i - 1):
5 -
                if arr[j] > arr[j + 1]:
6
                    arr[j], arr[j + 1] = arr[j + 1], arr[j]
                    swapped = True
8
9
            print(f"After pass {i+1}: {arr}")
10 -
            if not swapped:
                print("List is already sorted. Stopping early.")
11
12
                break
13
        return arr
14
   arr = [5, 2, 9, 1, 5, 6]
   print("Initial Array:", arr)
15
   sorted_arr = bubble_sort(arr.copy())
   print("Sorted Array:", sorted_arr)
```

```
Output

Initial Array: [5, 2, 9, 1, 5, 6]

After pass 1: [2, 5, 1, 5, 6, 9]

After pass 2: [2, 1, 5, 5, 6, 9]

After pass 3: [1, 2, 5, 5, 6, 9]

After pass 4: [1, 2, 5, 5, 6, 9]

List is already sorted. Stopping early.

Sorted Array: [1, 2, 5, 5, 6, 9]

=== Code Execution Successful ===
```

4. Write code for Insertion Sort that manages arrays with duplicate elements during the sorting process. Ensure the algorithm's behavior when encountering duplicate values, including whether it preserves the relative order of duplicates and how it affects the overall sorting outcome.

Examples:

- 1. Array with Duplicates:
- **Input**: [3, 1, 4, 1, 5, 9, 2, 6, 5, 3]
- **Output**: [1, 1, 2, 3, 3, 4, 5, 5, 6, 9]
- 1. All Identical Elements:
- **Input**: [5, 5, 5, 5, 5]
- **Output**: [5, 5, 5, 5, 5]
- 2. Mixed Duplicates:
- **Input**: [2, 3, 1, 3, 2, 1, 1, 3]

• **Output**: [1, 1, 1, 2, 2, 3, 3, 3]

```
1 def insertion_sort(arr):
 2
        n = len(arr)
        for i in range(1, n):
 4
            key = arr[i]
            j = i - 1
 5
            while j >= 0 and arr[j] > key:
 6
 7
                arr[j + 1] = arr[j]
 8
                j -= 1
9
            arr[j + 1] = key
10
            print(f"Step {i}: {arr}")
11
        return arr
12 test_cases = [
        [3, 1, 4, 1, 5, 9, 2, 6, 5, 3],
13
14
        [5, 5, 5, 5, 5],
15
        [2, 3, 1, 3, 2, 1, 1, 3]
16 ]
17 for idx, arr in enumerate(test_cases, 1):
18
        print(f"\nTest Case {idx}: Initial Array: {arr}")
19
        sorted_arr = insertion_sort(arr.copy())
        print(f"Sorted Array: {sorted_arr}")
20
```

```
Output
Test Case 1: Initial Array: [3, 1, 4, 1, 5, 9, 2, 6, 5, 3]
Step 1: [1, 3, 4, 1, 5, 9, 2, 6, 5, 3]
Step 2: [1, 3, 4, 1, 5, 9, 2, 6, 5, 3]
Step 3: [1, 1, 3, 4, 5, 9, 2, 6, 5, 3]
Step 4: [1, 1, 3, 4, 5, 9, 2, 6, 5, 3]
Step 5: [1, 1, 3, 4, 5, 9, 2, 6, 5, 3]
Step 6: [1, 1, 2, 3, 4, 5, 9, 6, 5, 3]
Step 7: [1, 1, 2, 3, 4, 5, 6, 9, 5, 3]
Step 8: [1, 1, 2, 3, 4, 5, 5, 6, 9, 3]
Step 9: [1, 1, 2, 3, 3, 4, 5, 5, 6, 9]
Sorted Array: [1, 1, 2, 3, 3, 4, 5, 5, 6, 9]
Test Case 2: Initial Array: [5, 5, 5, 5, 5]
Step 1: [5, 5, 5, 5, 5]
Step 2: [5, 5, 5, 5, 5]
Step 3: [5, 5, 5, 5, 5]
Step 4: [5, 5, 5, 5, 5]
Sorted Array: [5, 5, 5, 5, 5]
Test Case 3: Initial Array: [2, 3, 1, 3, 2, 1, 1, 3]
Step 1: [2, 3, 1, 3, 2, 1, 1, 3]
Step 2: [1, 2, 3, 3, 2, 1, 1, 3]
Step 3: [1, 2, 3, 3, 2, 1, 1, 3]
Step 4: [1, 2, 2, 3, 3, 1, 1, 3]
Step 5: [1, 1, 2, 2, 3, 3, 1, 3]
Step 6: [1, 1, 1, 2, 2, 3, 3, 3]
Step 7: [1, 1, 1, 2, 2, 3, 3, 3]
Sorted Array: [1, 1, 1, 2, 2, 3, 3, 3]
```

5. Given an array arr of positive integers sorted in a strictly increasing order, and an integer k. return the kth positive integer that is missing from this array.

Example 1:

```
Input: arr = [2,3,4,7,11], k = 5
```

Output: 9

Explanation: The missing positive integers are [1,5,6,8,9,10,12,13,...]. The 5th missing positive integer is 9.

Example 2:

```
Input: arr = [1,2,3,4], k = 2 Output: 6
```

Explanation: The missing positive integers are [5,6,7,...]. The 2nd missing positive integer is 6.

```
1 def find_kth_missing(arr, k):
        missing_count = 0
 2
 3
        current = 1
        i = 0
 4
 5
        n = len(arr)
        while True:
 6 -
            if i < n and arr[i] == current:</pre>
 7 -
                 i += 1
 8
9 -
            else:
                missing_count += 1
10
                 if missing_count == k:
11 -
12
                     return current
13
            current += 1
   arr1 = [2, 3, 4, 7, 11]
14
    k1 = 5
15
    print(find_kth_missing(arr1, k1))
```

Output 9 === Code Execution Successful ===

- 6. A peak element is an element that is strictly greater than its neighbors. Given a 0-indexed integer array nums, find a peak element, and return its index. If the array contains multiple peaks, return the index to any of the peaks. You may imagine that nums[-1] = nums[n] =
- -∞. In other words, an element is always considered to be strictly greater than a neighbor that is outside the array. You must write an algorithm that runs in O(log n) time.

Example 1:

Input: nums = [1,2,3,1] Output: 2

Explanation: 3 is a peak element and your function should return the index number 2.

Example 2:

Input: nums = [1,2,1,3,5,6,4]

Output: 5

Explanation: Your function can return either index number 1 where the peak element is 2, or index number 5 where the peak element is 6.

```
1 - def find_peak_element(nums):
2    left, right = 0, len(nums) - 1
3    while left < right:
4        mid = (left + right) // 2
5        if nums[mid] < nums[mid + 1]:
6        left = mid + 1
7        else:
8             right = mid
9        return left
10    nums1 = [1, 2, 3, 1]
11    print(find_peak_element(nums1)) # Output: 2
12</pre>
```

```
Output

2
=== Code Execution Successful ===
```

7. Given two strings needle and haystack, return the index of the first occurrence of needle in haystack, or -1 if needle is not part of haystack.

Example 1:

```
Input: haystack = "sadbutsad", needle = "sad" Output: 0
```

Explanation: "sad" occurs at index 0 and 6.

The first occurrence is at index 0, so we return 0.

Example 2:

```
Input: haystack = "leetcode", needle = "leeto" Output: -
1
```

Explanation: "leeto" did not occur in "leetcode", so we return -1.

```
def strStr(haystack, needle):
       if needle == "":
2
            return 0
3
       n, m = len(haystack), len(needle)
4
       for i in range(n - m + 1):
5
            if haystack[i:i + m] == needle:
6 -
7
                return i
8
        return -1
   haystack1 = "sadbutsad"
9
10
   needle1 = "sad"
   print(strStr(haystack1, needle1))
11
```

```
Output

O === Code Execution Successful ===
```

8. Given an array of string words, return all strings in words that is a substring of another word. You can return the answer in any order. A substring is a contiguous sequence of characters within a string

Example 1:

```
Input: words = ["mass", "as", "hero", "superhero"]
```

Output: ["as","hero"]

Explanation: "as" is substring of "mass" and "hero" is substring of "superhero".

```
["hero", "as"] is also a valid answer.
```

```
Example 2:

Input: words = ["leetcode","et","code"]

Output: ["et","code"]

Explanation: "et", "code" are substring of "leetcode".

Example 3:

Input: words = ["blue","green","bu"] Output:

[]
```

Explanation: No string of words is substring of another string.

```
1 def string_matching(words):
2    result = set()
3    n = len(words)
4    for i in range(n):
5         for j in range(n):
6             if i != j and words[i] in words[j]:
7                  result.add(words[i])
8    return list(result)
9    words1 = ["mass", "as", "hero", "superhero"]
10    print(string_matching(words1))
```

```
Output
['hero', 'as']
=== Code Execution Successful ===
```

9. Write a program that finds the closest pair of points in a set of 2D points using the brute force approach. Input:

A list or array of points represented by coordinates (x, y). Points:

Output:

The two points with the minimum distance between them. The minimum distance itself.

Closest pair: (1, 2) - (3, 1) Minimum distance: 1.4142135623730951

```
import math
2 def distance(p1, p2):
        """Calculate Euclidean distance between two points"""
       return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])**2)
5 def closest_pair(points):
       min_dist = float('inf')
       pair = (None, None)
       n = len(points)
9
       for i in range(n):
           for j in range(i + 1, n):
11
               dist = distance(points[i], points[j])
12
               if dist < min_dist:</pre>
13
                   min_dist = dist
14
                   pair = (points[i], points[j])
15
        return pair, min_dist
16 points = [(1, 2), (4, 5), (7, 8), (3, 1)]
17 pair, min_dist = closest_pair(points)
18 print(f"Closest pair: {pair[0]} - {pair[1]} Minimum distance: {min_dist}")
```

```
Output

Closest pair: (1, 2) - (3, 1) Minimum distance: 2.23606797749979

=== Code Execution Successful ===
```

10. Write a program to find the closest pair of points in a given set using the brute force approach. Analyze the time complexity of your implementation. Define a function to calculate the Euclidean distance between two points. Implement a function to find the closest pair of points using the brute force method. Test your program with a sample set of points and verify the correctness of your results. Analyze the time complexity of your implementation. Write a brute-force algorithm to solve the convex hull problem for the following set S of points? P1 (10,0)P2 (11,5)P3 (5, 3)P4 (9, 3.5)P5 (15, 3)P6 (12.5, 7)P7 (6,

6.5)P8 (7.5, 4.5).How do you modify your brute force algorithm to handle multiple points that are lying on the sameline?

Given points: P1 (10,0), P2 (11,5), P3 (5, 3), P4 (9, 3.5), P5 (15, 3), P6 (12.5, 7), P7 (6, 6.5), P8 (7.5, 4.5).

output: P3, P4, P6, P5, P7, P1

```
1 import math
 2 def euclidean_distance(p1, p2):
        """Compute Euclidean distance between two points"""
        return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])**2)
 4
 5 def closest_pair(points):
 6
        min_dist = float('inf')
 8
        pair = (None, None)
 9
        n = len(points)
10 -
        for i in range(n):
11 -
            for j in range(i+1, n):
12
                dist = euclidean_distance(points[i], points[j])
                if dist < min_dist:</pre>
14
                    min_dist = dist
                    pair = (points[i], points[j])
16
        return pair, min_dist
17 points1 = [(1,2),(4,5),(7,8),(3,1)]
18 pair, min_dist = closest_pair(points1)
19 print(f"Closest pair: {pair[0]} - {pair[1]}, Minimum distance: {min_dist}")
20 def cross_product(a, b, c):
        """Return cross product of AB x AC"""
21
22
        return (b[0]-a[0])*(c[1]-a[1]) - (b[1]-a[1])*(c[0]-a[0])
23 def convex_hull_brute_force(points):
24
25
        hull_points = set()
26
        n = len(points)
27 -
        for i in range(n):
28
            for j in range(i+1, n):
29
                left = right = False
30
                for k in range(n):
```

```
31
                    if k==i or k==j:
32
                        continue
33
                    cp = cross_product(points[i], points[j], points[k])
34
                    if cp > 0:
                        left = True
35
36
                    elif cp < 0:
37
                        right = True
38
                if not (left and right):
39
                    hull_points.add(points[i])
40
                    hull_points.add(points[j])
41
        return list(hull_points)
42 def sort_points_clockwise(points):
43
        """Sort points in clockwise order around centroid"""
44
        cx = sum(p[0] for p in points)/len(points)
45
        cy = sum(p[1] for p in points)/len(points)
46
        points.sort(key=lambda p: math.atan2(p[1]-cy, p[0]-cx))
47
        return points
48 points_s = [
        (10,0), (11,5), (5,3), (9,3.5),
50
        (15,3), (12.5,7), (6,6.5), (7.5,4.5)
51 ]
52 hull = convex_hull_brute_force(points_s)
53 hull_sorted = sort_points_clockwise(hull)
   print("Convex Hull Points in clockwise order:")
55 for p in hull_sorted:
56
        print(p)
```

```
Output

Closest pair: (1, 2) - (3, 1), Minimum distance: 2.23606797749979

Convex Hull Points in clockwise order:
(5, 3)
(10, 0)
(15, 3)
(12.5, 7)
(6, 6.5)

=== Code Execution Successful ===
```

11. Write a program that finds the convex hull of a set of 2D points using the brute force approach.

Input:

A list or array of points represented by coordinates (x, y).

Points: [(1, 1), (4, 6), (8, 1), (0, 0), (3, 3)]

Output:

The list of points that form the convex hull in counter-clockwise order. Convex Hull: [(0, 0), (1, 1), (8, 1), (4, 6)]

```
1 def cross_product(a, b, c):
        return (b[0]-a[0])*(c[1]-a[1]) - (b[1]-a[1])*(c[0]-a[0])
3 def convex_hull_brute_force(points):
       hull_points = set()
5
       n = len(points)
       for i in range(n):
6
            for j in range(i+1, n):
8
                left = right = False
9
                for k in range(n):
                    if k == i or k == j:
10
11
                        continue
12
                    cp = cross_product(points[i], points[j], points[k])
13
                    if cp > 0:
14
                        left = True
15
                    elif cp < 0:
16
                        right = True
17
                if not (left and right):
18
                    hull_points.add(points[i])
19
                    hull_points.add(points[j])
20
        return list(hull_points)
```

```
21 def sort_counter_clockwise(points):
22          cx = sum(p[0] for p in points)/len(points)
23          cy = sum(p[1] for p in points)/len(points)
24          points.sort(key=lambda p: math.atan2(p[1]-cy, p[0]-cx))
25          return points
26          import math
27          points = [(1, 1), (4, 6), (8, 1), (0, 0), (3, 3)]
28          hull = convex_hull_brute_force(points)
29          hull_ccw = sort_counter_clockwise(hull)
30          print("Convex Hull (counter-clockwise):", hull_ccw)
```

```
Output

Closest pair: (1, 2) - (3, 1), Minimum distance: 2.23606797749979

Convex Hull Points in clockwise order:
(5, 3)
(10, 0)
(15, 3)
(12.5, 7)
(6, 6.5)

=== Code Execution Successful ===
```

- 12. You are given a list of cities represented by their coordinates. Develop a program that utilizes exhaustive search to solve the TSP. The program should:
- 1. Define a function distance(city1, city2) to calculate the distance between two cities (e.g., Euclidean distance).
- 2. Implement a function tsp(cities) that takes a list of cities as input and performs the following:
- Generate all possible permutations of the cities (excluding the starting city) using itertools.permutations.
- For each permutation (representing a potential route):
- Calculate the total distance traveled by iterating through the path and summing the distances between consecutive cities.
- Keep track of the shortest distance encountered and the corresponding path.
- Return the minimum distance and the shortest path (including the starting city at the beginning and end).

3. Include test cases with different city configurations to demonstrate the program's functionality. Print the shortest distance and the corresponding path for each test case.

Test Cases:

Simple Case: Four cities with basic coordinates (e.g., [(1, 2), (4, 5), (7, 1), (3, 6)])

More Complex Case: Five cities with more intricate coordinates (e.g., [(2, 4), (8, 1), (1, 7), (6, 3), (5, 9)])

Output:

Test Case 1:

Shortest Distance: 7.0710678118654755

Shortest Path: [(1, 2), (4, 5), (7, 1), (3, 6), (1, 2)]

Test Case 2:

Shortest Distance: 14.142135623730951

Shortest Path: [(2, 4), (1, 7), (6, 3), (5, 9), (8, 1), (2, 4)]

```
import itertools, math
 2 def distance(a, b):
        return math.hypot(a[0] - b[0], a[1] - b[1])
4 def tsp(cities):
        start = cities[0]
 6
        best_dist, best_path = float('inf'), None
        for perm in itertools.permutations(cities[1:]):
 7
            path = [start] + list(perm) + [start]
9
            dist = sum(distance(path[i], path[i+1]) for i in range(len(path)-1))
10 -
            if dist < best_dist:</pre>
11
                best_dist, best_path = dist, path
        return best_dist, best_path
12
13 cities1 = [(1, 2), (4, 5), (7, 1), (3, 6)]
14 cities2 = [(2, 4), (8, 1), (1, 7), (6, 3), (5, 9)]
15 print("Test Case 1:", tsp(cities1))
16 print("Test Case 2:", tsp(cities2))
```

```
Output

Test Case 1: (16.969112047670894, [(1, 2), (7, 1), (4, 5), (3, 6), (1, 2)])

Test Case 2: (23.12995011084934, [(2, 4), (1, 7), (5, 9), (8, 1), (6, 3), (2, 4)])

=== Code Execution Successful ===
```

23. You are given a cost matrix where each element cost[i][j] represents the cost of assigning worker i to task j. Develop a program that utilizes exhaustive search to solve the assignment problem. The program should Define a function total_cost(assignment, cost_matrix) that takes an assignment (list representing worker-task pairings) and the cost matrix as input. It iterates through the assignment and calculates the total cost by summing the corresponding costs from the cost matrix Implement a function assignment_problem(cost_matrix) that takes the cost matrix as input and performs the following Generate all possible permutations of worker indices (excluding repetitions).

Test Cases:

Input

Simple Case: Cost Matrix:

[[3, 10, 7],

[8, 5, 12],

[4, 6, 9]]

More Complex Case: Cost Matrix:

[[15, 9, 4],

[8, 7, 18],

[6, 12, 11]]

Output:

Test Case 1:

Optimal Assignment: [(worker 1, task 2), (worker 2, task 1), (worker 3, task 3)]

Total Cost: 19

Test Case 2:

Optimal Assignment: [(worker 1, task 3), (worker 2, task 1), (worker 3, task 2)]

Total Cost: 24

```
import itertools
 2 def total_cost(assignment, cost_matrix):
        return sum(cost_matrix[i][assignment[i]] for i in range(len(assignment)))
 4 def assignment_problem(cost_matrix):
        n = len(cost_matrix)
 5
 6
        workers = range(n)
        min_cost = float("inf")
        best_assignment = None
 8
 9
        for perm in itertools.permutations(range(n)):
10
            cost = total_cost(perm, cost_matrix)
11-
            if cost < min_cost:</pre>
12
                min_cost = cost
13
                best_assignment = perm
14
        result = [(f"worker {i+1}", f"task {best_assignment[i]+1}") for i in
            workers]
15
        return result, min_cost
16 if __name__ == "__main__":
17 -
        cost_matrix1 = [
18
            [3, 10, 7],
19
            [8, 5, 12],
20
            [4, 6, 9]
21
```

```
22
        assignment1, cost1 = assignment_problem(cost_matrix1)
23
        print("Test Case 1:")
24
        print("Optimal Assignment:", assignment1)
25
        print("Total Cost:", cost1)
26 -
        cost_matrix2 = [
27
            [15, 9, 4],
28
            [8, 7, 18],
29
            [6, 12, 11]
30
        1
31
        assignment2, cost2 = assignment_problem(cost_matrix2)
32
        print("\nTest Case 2:")
33
        print("Optimal Assignment:", assignment2)
        print("Total Cost:", cost2)
34
```

14. You are given a list of items with their weights and values. Develop a program that utilizes exhaustive search to solve the 0-1 Knapsack Problem. The program should:

Define a function total_value(items, values) that takes a list of selected items (represented by their indices) and the value list as input. It iterates through the selected items and calculates the total value by summing the corresponding values from the value list.

Define a function is_feasible(items, weights, capacity) that takes a list of selected items (represented by their indices), the weight list, and the knapsack capacity as input. It checks if the total weight of the selected items exceeds the capacity.

Test Cases:

Simple Case:

Items: 3 (represented by indices 0, 1, 2)

Weights: [2, 3, 1]

Values: [4, 5, 3]

Capacity: 4

More Complex Case:

Items: 4 (represented by indices 0, 1, 2, 3)

Weights: [1, 2, 3, 4]

Values: [2, 4, 6, 3]

Capacity: 6

Output:

Test Case 1:

Optimal Selection: [0, 2] (Items with indices 0 and 2)

Total Value: 7

Test Case 2:

Optimal Selection: [0, 1, 2] (Items with indices 0, 1, and 2)

Total Value: 10

```
import itertools
 2 def total_value(items, values):
        return sum(values[i] for i in items)
 4 def is_feasible(items, weights, capacity):
        return sum(weights[i] for i in items) <= capacity</pre>
 6 def knapsack(weights, values, capacity):
        n = len(weights)
 8
        best value = 0
 9
        best selection = []
10
        for r in range(n+1):
11
            for subset in itertools.combinations(range(n), r):
                if is_feasible(subset, weights, capacity):
12
13
                    val = total_value(subset, values)
14
                    if val > best value:
15
                        best_value = val
16
                        best_selection = list(subset)
17
        return best_selection, best_value
18 - if __name__ == "__main__":
19
20
        weights1 = [2, 3, 1]
21
        values1 = [4, 5, 3]
22
        capacity1 = 4
23
        selection1, value1 = knapsack(weights1, values1, capacity1)
24
        print("Optimal Selection:", selection1)
25
        print("Total Value:", value1)
```

Output

```
Optimal Selection: [1, 2]
Total Value: 8
=== Code Execution Successful ===
```