Linear Regression Analysis of MTCARS Data

Ivan Li

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```r
# Load ggplot2 and caret
library(ggplot2)
library(caret)
```

```
## Warning: package 'caret' was built under R version 4.2.3
```

```
## Loading required package: lattice
```

```r
# Load mtcars dataset
data(mtcars)
# Display the head of the dataset
head(mtcars)
```

```
##                    mpg cyl disp  hp drat    wt  qsec vs am gear carb
## Mazda RX4         21.0   6  160 110 3.90 2.620 16.46  0  1    4    4
## Mazda RX4 Wag     21.0   6  160 110 3.90 2.875 17.02  0  1    4    4
## Datsun 710        22.8   4  108  93 3.85 2.320 18.61  1  1    4    1
## Hornet 4 Drive    21.4   6  258 110 3.08 3.215 19.44  1  0    3    1
## Hornet Sportabout 18.7   8  360 175 3.15 3.440 17.02  0  0    3    2
## Valiant           18.1   6  225 105 2.76 3.460 20.22  1  0    3    1
```

```r
# Summary statistics of the dataset
summary(mtcars)
```

```
##       mpg             cyl             disp             hp
##  Min.   :10.40   Min.   :4.000   Min.   : 71.1   Min.   : 52.0
##  1st Qu.:15.43   1st Qu.:4.000   1st Qu.:120.8   1st Qu.: 96.5
##  Median :19.20   Median :6.000   Median :196.3   Median :123.0
##  Mean   :20.09   Mean   :6.188   Mean   :230.7   Mean   :146.7
##  3rd Qu.:22.80   3rd Qu.:8.000   3rd Qu.:326.0   3rd Qu.:180.0
##  Max.   :33.90   Max.   :8.000   Max.   :472.0   Max.   :335.0
##       drat             wt             qsec             vs
##  Min.   :2.760   Min.   :1.513   Min.   :14.50   Min.   :0.0000
##  1st Qu.:3.080   1st Qu.:2.581   1st Qu.:16.89   1st Qu.:0.0000
##  Median :3.695   Median :3.325   Median :17.71   Median :0.0000
##  Mean   :3.597   Mean   :3.217   Mean   :17.85   Mean   :0.4375
##  3rd Qu.:3.920   3rd Qu.:3.610   3rd Qu.:18.90   3rd Qu.:1.0000
##  Max.   :4.930   Max.   :5.424   Max.   :22.90   Max.   :1.0000
##       am             gear             carb
##  Min.   :0.0000   Min.   :3.000   Min.   :1.000
##  1st Qu.:0.0000   1st Qu.:3.000   1st Qu.:2.000
##  Median :0.0000   Median :4.000   Median :2.000
##  Mean   :0.4062   Mean   :3.688   Mean   :2.812
##  3rd Qu.:1.0000   3rd Qu.:4.000   3rd Qu.:4.000
##  Max.   :1.0000   Max.   :5.000   Max.   :8.000
```

```r
# Generate pairwise scatter plots for relationship visualization
pairs(mtcars, panel = panel.smooth, main = "Pairwise Scatter Plots")
```
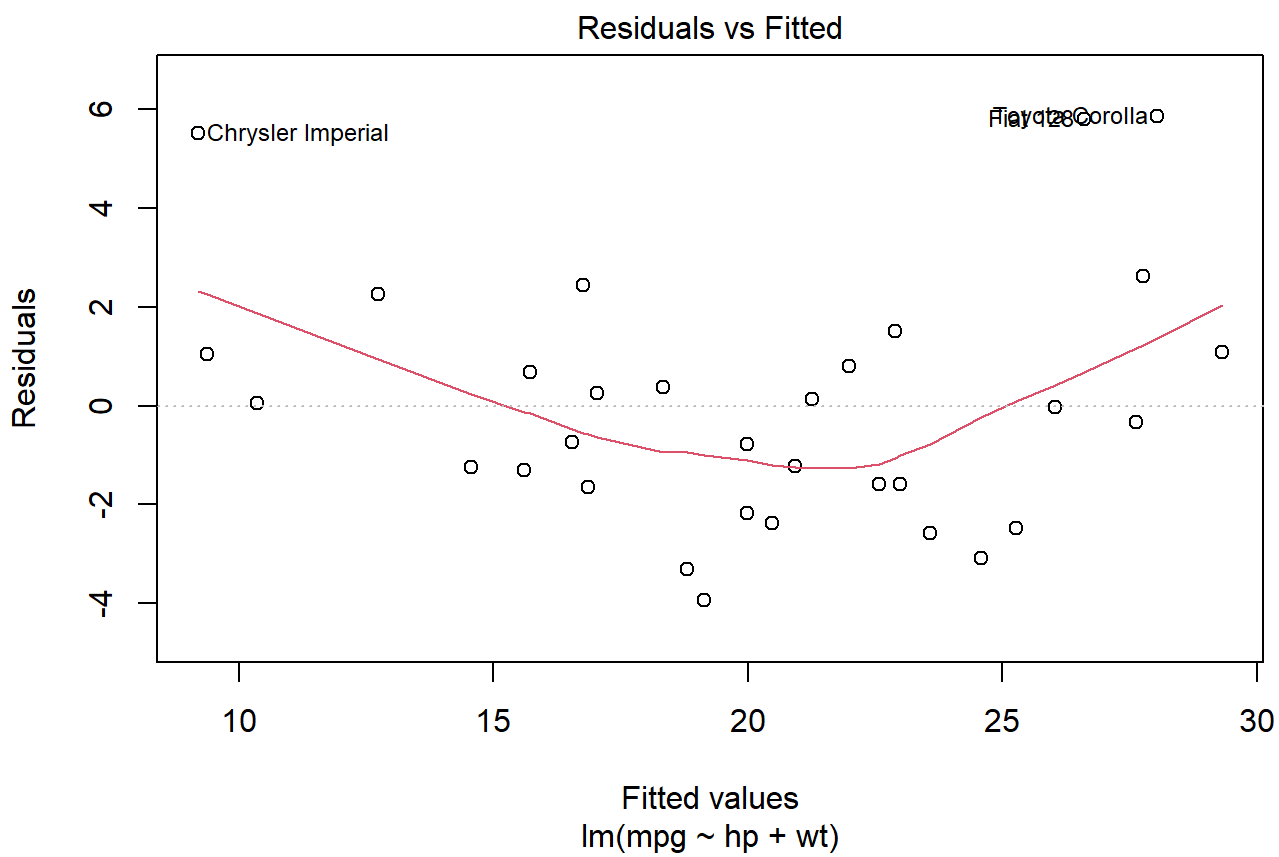

Pairwise Scatter Plots
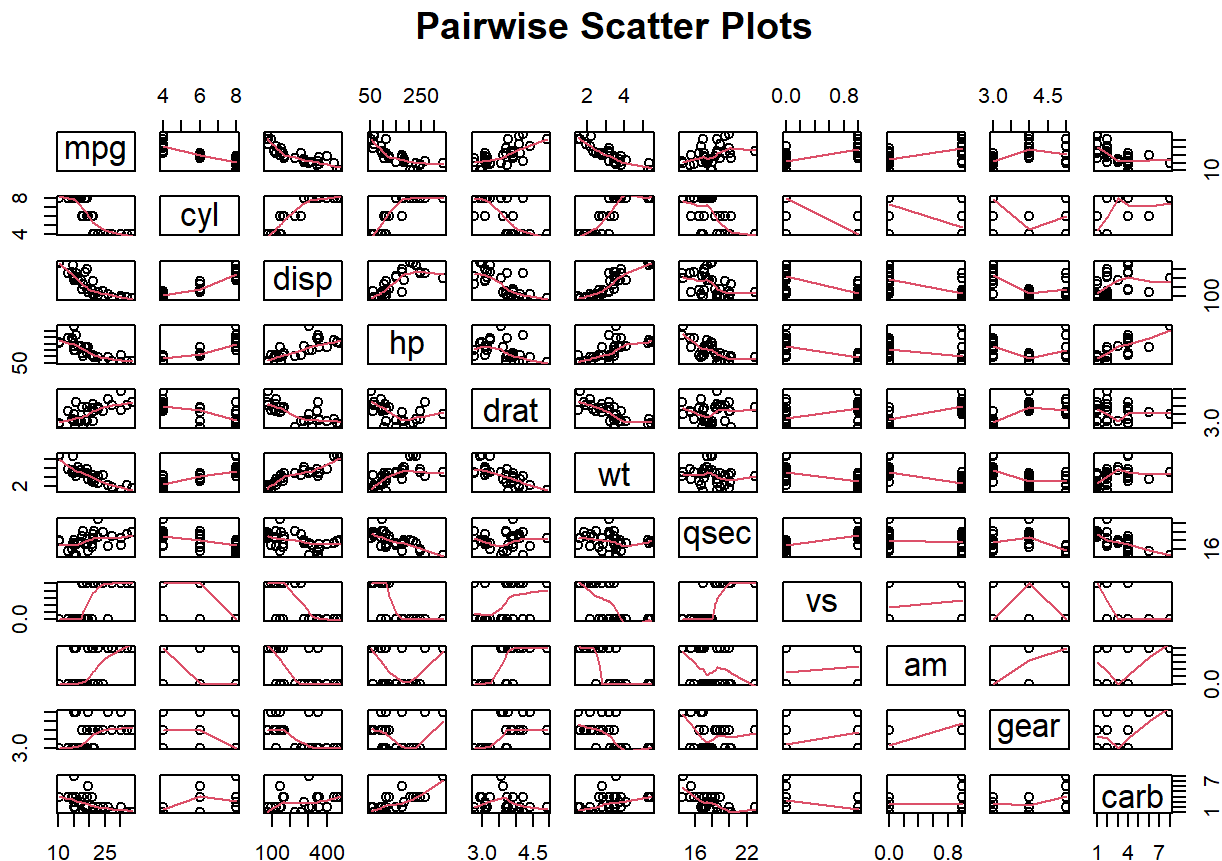
```r
# Choose the linear regression model to fit
model <- lm(mpg ~ hp + wt, data = mtcars)

# Show a summary of the model
summary(model)
```
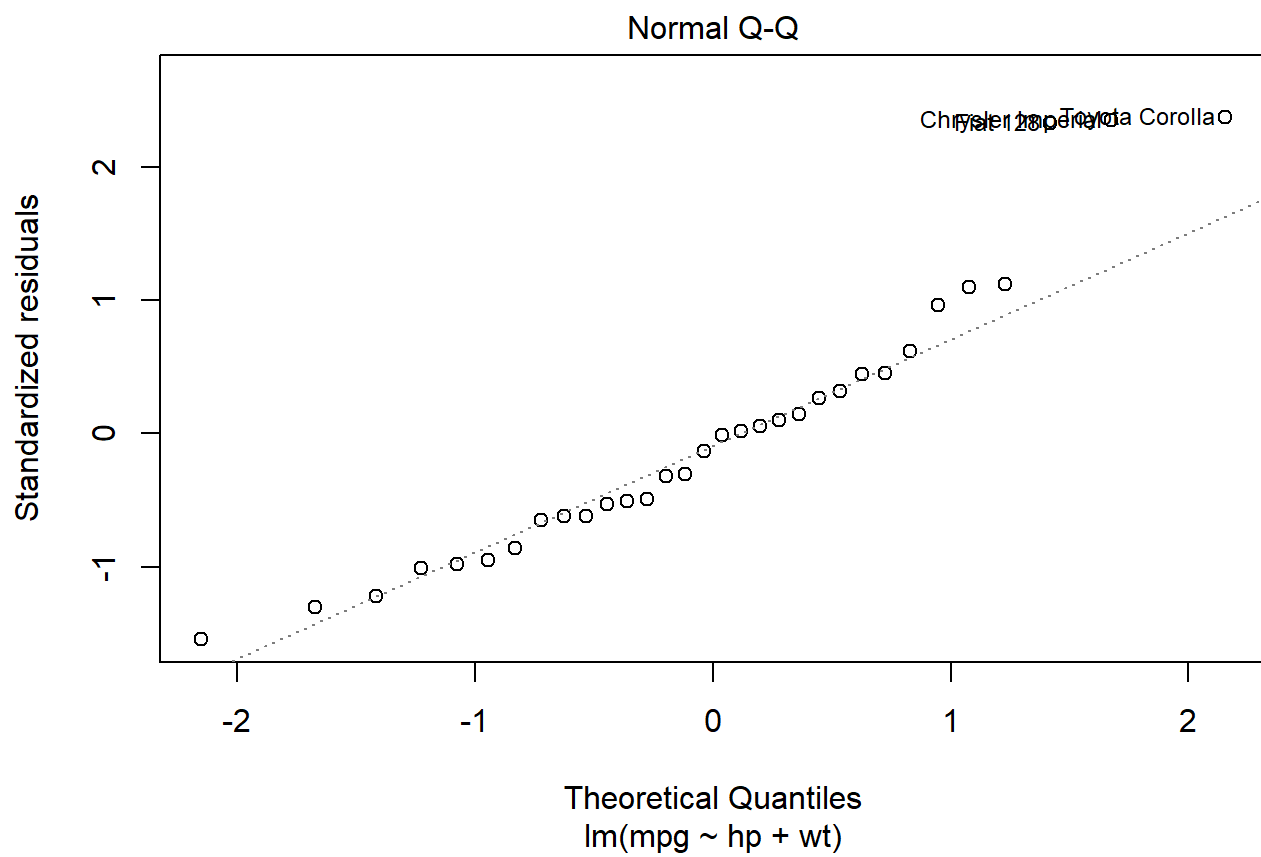
```
##
## Call:
## lm(formula = mpg ~ hp + wt, data = mtcars)
##
## Residuals:
##     Min      1Q Median      3Q     Max
## -3.941 -1.600 -0.182  1.050   5.854
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 37.22727    1.59879  23.285  < 2e-16 ***
## hp          -0.03177    0.00903  -3.519  0.00145 **
## wt          -3.87783    0.63273  -6.129 1.12e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.593 on 29 degrees of freedom
## Multiple R-squared:  0.8268, Adjusted R-squared:  0.8148
## F-statistic: 69.21 on 2 and 29 DF,  p-value: 9.109e-12
```
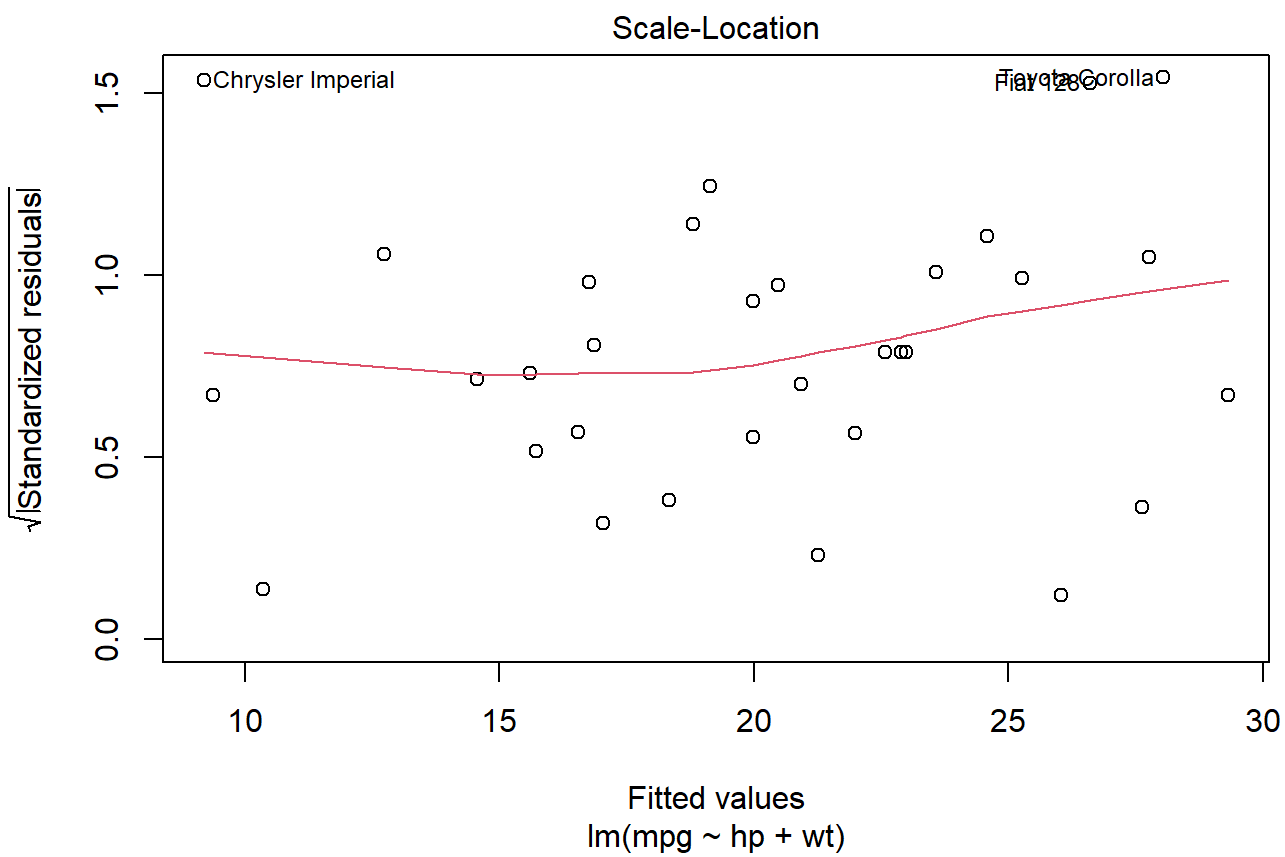
```r
# Residuals vs Fitted plot for checking homoscedasticity
plot(model, which = 1)
```

Residuals vs Fitted

Residuals

6

4

2

0

-2

-4

○Chrysler Imperial

TeyotaCorolla○
Fiat 128○

10   15   20   25   30

Fitted values
lm(mpg ~ wt)

```
# Normal Q-Q plot to check normality of residuals
plot(model, which = 2)
```

Normal Q-Q

Standardized residuals

Chrysler Imperial Toyota Corolla
Fiat 128

Theoretical Quantiles
lm(mpg ~ hp + wt)

```r
# Scale-Location plot to check homoscedasticity
plot(model, which = 3)
```

Scale-Location

√|Standardized residuals|

Chrysler Imperial   Toyota Corolla
                           Fiat 128

Fitted values
lm(mpg ~ hp + wt)

```
# Residuals vs Leverage plot to find influential points
plot(model, which = 5)
```

Residuals vs Leverage

lm(mpg ~ hp + wt)
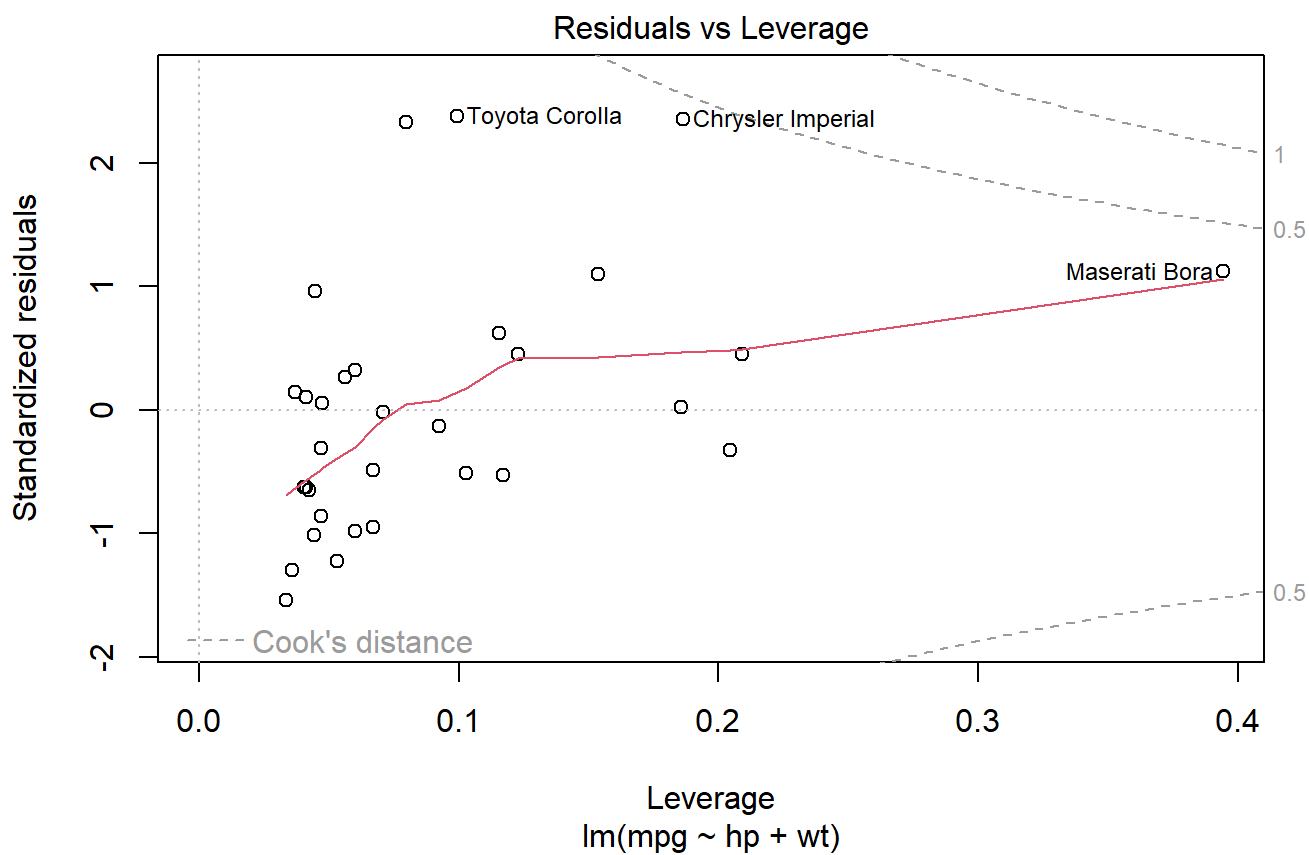
```r
# New data for prediction
new_data <- data.frame(hp = c(110, 150), wt = c(2.5, 3.0))

# Use the model to predict mpg for the new data
predictions <- predict(model, new_data)
# Show the predictions
predictions
```

```
##        1        2
## 24.03767 20.82784
```