

$$\begin{aligned}
& \sqrt{2} \sqrt{-\frac{\mathbb{L}_{\#}}{\mathbb{r}_{\#} (4 + \mathbb{L}_{\#})}} \sqrt{\xi} + \frac{(-36 - 4 \mathbb{L}_{\#} + \mathbb{L}_{\#}^2) \xi^{3/2}}{6 \sqrt{2} \sqrt{-\mathbb{L}_{\#}} (\mathbb{r}_{\#} (4 + \mathbb{L}_{\#}))^{3/2}} + \frac{\mathbb{L}_{\#}^2 (144 - 3744 \mathbb{L}_{\#} - 1624 \mathbb{L}_{\#}^2 - 136 \mathbb{L}_{\#}^3 + 9 \mathbb{L}_{\#}^4) \xi^{5/2}}{240 \sqrt{2} \mathbb{r}_{\#}^2 (4 + \mathbb{L}_{\#})^2 \sqrt{-\mathbb{r}_{\#} \mathbb{L}_{\#}^7 (4 + \mathbb{L}_{\#})}} \\
& \frac{(\mathbb{L}_{\#} (12480 + 19776 \mathbb{L}_{\#} - 8592 \mathbb{L}_{\#}^2 - 10784 \mathbb{L}_{\#}^3 - 2732 \mathbb{L}_{\#}^4 - 188 \mathbb{L}_{\#}^5 + 5 \mathbb{L}_{\#}^6)) \xi^{7/2}}{448 \left(\sqrt{2} \mathbb{r}_{\#}^3 (4 + \mathbb{L}_{\#})^3 \sqrt{-\mathbb{r}_{\#} \mathbb{L}_{\#}^7 (4 + \mathbb{L}_{\#})} \right)} + \\
& \left((11439360 + 42347520 \mathbb{L}_{\#} + 56183040 \mathbb{L}_{\#}^2 + 17521920 \mathbb{L}_{\#}^3 - 4943392 \mathbb{L}_{\#}^4 - 3744704 \mathbb{L}_{\#}^5 - \right. \\
& \quad \left. 709936 \mathbb{L}_{\#}^6 - 41808 \mathbb{L}_{\#}^7 + 525 \mathbb{L}_{\#}^8) \xi^{9/2} \right) / \left(138240 \sqrt{2} \mathbb{r}_{\#}^4 (4 + \mathbb{L}_{\#})^4 \sqrt{-\mathbb{r}_{\#} \mathbb{L}_{\#}^7 (4 + \mathbb{L}_{\#})} \right) + \\
& \left((-60318720 + 192384000 \mathbb{L}_{\#} + 1011406080 \mathbb{L}_{\#}^2 + 1529840640 \mathbb{L}_{\#}^3 + 866594688 \mathbb{L}_{\#}^4 + \right. \\
& \quad \left. 157458048 \mathbb{L}_{\#}^5 - 33015648 \mathbb{L}_{\#}^6 - 18666944 \mathbb{L}_{\#}^7 - 2875220 \mathbb{L}_{\#}^8 - 147924 \mathbb{L}_{\#}^9 + 945 \mathbb{L}_{\#}^{10}) \xi^{11/2} \right) / \\
& \left(675840 \sqrt{2} \mathbb{r}_{\#}^5 (-\mathbb{L}_{\#})^{9/2} (4 + \mathbb{L}_{\#})^5 \sqrt{\mathbb{r}_{\#} (4 + \mathbb{L}_{\#})} \right) + \\
& \left((-632293724160 - 2155286568960 \mathbb{L}_{\#} - 2395199600640 \mathbb{L}_{\#}^2 + 236777748480 \mathbb{L}_{\#}^3 + \right. \\
& \quad \left. 3081436694784 \mathbb{L}_{\#}^4 + 2733581233152 \mathbb{L}_{\#}^5 + 1014268345088 \mathbb{L}_{\#}^6 + 127225805568 \mathbb{L}_{\#}^7 - \right. \\
& \quad \left. 25746179952 \mathbb{L}_{\#}^8 - 11039030176 \mathbb{L}_{\#}^9 - 1426991544 \mathbb{L}_{\#}^{10} - 64846440 \mathbb{L}_{\#}^{11} + 218295 \mathbb{L}_{\#}^{12}) \xi^{13/2} \right) / \\
& \left(402554880 \sqrt{2} \mathbb{r}_{\#}^6 \mathbb{L}_{\#}^2 (4 + \mathbb{L}_{\#})^6 \sqrt{-\mathbb{r}_{\#} \mathbb{L}_{\#}^7 (4 + \mathbb{L}_{\#})} \right) + \mathcal{O}[\xi]^{15/2}
\end{aligned}$$