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A34 B155(150) C52166(2.13) D48 Vol. II ¶ 13

今有圓田，周三百步，徑一百步。問得田幾何？答曰：三十一畝，奇六十步。術曰：先置周三百步，半之，得一百五十步。又置徑一百步，半之，得五十步。相乘，得七千五百步。以畝法二百四十步除之，即得。又術：周自相乘，得九萬步。以一十二除之，得七千五百步。以畝法除之，得畝數。又術：徑自乘，得一萬。以三乘之，得三萬步。四除之，得七千五百步。以畝法除之，得畝數。

B has 又術曰 for 又術 : Here $\pi \simeq 3$, see Vol. I ¶ 5.

Now we have a circular field, with circumference three hundred 步, and diameter one hundred 步. We ask: how much field resulteth?
Answer saith: thirty-one 畝 remainder sixty 步.
Method saith: First put down the circumference, three hundred 步; halving it, resulteth in one hundred and fifty 步. Also put down the diameter, one hundred 步; halving it, resulteth in fifty 步. These multiplied with each other resulteth in seven thousand, five hundred 步. Dividing it by the 畝 divisor two hundred and forty 步, we are done.
Also a method: the circumference, multiplied with itself, resulteth in ninety thousand 步. Dividing it by twelve, resulteth in seven thousand five hundred 步. Dividing it by the 畝 divisor, resulteth in the number of 畝.
Also a method: the diameter, multiplied with itself, resulteth in ten thousand. Multiplying it by three, resulteth in thirty thousand 步. Dividing it by four, resulteth in seven thousand five hundred 步. Dividing it by the 畝 divisor, resulteth in the number of 畝.

$A = \frac{c}{2}\frac{d}{2} \simeq \frac{c^2}{12} \simeq \frac{3d^2}{4}$, with $1 = \frac{240\,步^2}{畝}$ END ¶ 13