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# Semi-Supervised Statistical Approach for Network Anomaly Detection

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#### **Abstract**

Intrusion Detection Systems (IDS) have become a very important defense measure against security threats. In recent years, computer networks are widely deployed for critical and complex systems, which make them more vulnerable to network attacks. In this paper, we propose a two-stage Semi-supervised Statistical approach for Anomaly Detection (SSAD). The first stage of SSAD aims to build a probabilistic model of normal instances and measures any deviation that exceeds an established threshold. This threshold is deduced from a regularized discriminant function of Maximum Likelihood (ML). The purpose of the second stage is to reduce False Alarm Rate (FAR) through an iterative process that reclassifies anomaly cluster, from the first stage, using a similarity distance and anomaly's cluster dispersion rate. We evaluate the proposed approach on the well-known intrusion detection dataset NSL-KDD and Kyoto 2006+. The experimental results show that SSAD outperforms the Naïve Bayes methods in terms of Detection Rate and False Positive Rate.

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Keywords: Network Security, Anomaly Detection; Maximum Likelihood; chi-square statistic; NSL-KDD dataset; Kyoto 2006+ dataset

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#### 1. Introduction

An intrusion is defined as "any set of actions that attempt to compromise the integrity, confidentiality or availability of a resource". An Intrusion Detection System (IDS) is a set of components and techniques that aim to monitor network resources or computer activities in order to detect and react to any suspicious action.

IDSs are usually classified into two categories<sup>2, 3</sup>: i) Misuse-based and ii) Anomaly-based. Systems that use misuse-base techniques need a database of known attacks' signature (description) to match against observed activities or audit data. These systems provide very good detection results for specified well-known attacks. However, their inability to detect the unknown attacks is a major drawback. Anomaly-based systems, rely on models of normal behavior of the protected target, any deviation from this model is considered as suspicious. These systems are able to detect previously unknown attacks. However, the number of their false alarms is still high.

Several methods have been proposed to detect anomalies<sup>4</sup>, some are based upon computational intelligence (evolutionary computation<sup>5, 6</sup>, artificial immune systems<sup>7</sup>...), others use pattern matching or rely on statistical approaches representing normal behavior<sup>8</sup>. These methods can be mainly grouped into three approaches: i) unsupervised approach where intrusions are detected with no prior knowledge of a normal/attack behavior. ii) Supervised approach where both normal and abnormal behaviors are modeled based on a pre-labeled data tagged as normal or abnormal. iii) In the third semi-supervised approach, only normal behavior is modeled using a pre-labeled data. The challenge of this last approach is to find an optimal discriminant function that can efficiently distinguish the target's normal behavior from abnormal instances.

In this paper, we propose a two-stage Semi-supervised Statistical approach for Anomaly Detection (SSAD). In the first stage, we build a probabilistic model based on pre-labeled normal instances, and we classify as anomaly any deviation that exceeds a defined threshold. This threshold is deduced from the Maximum Likelihood (ML) function and the p-value of chi-square ( $\chi^2$ ) distribution. We introduce, for optimization, a variance-covariance matrix's regularization coefficient into the ML function. To reduce the false alarm rate, we propose as second stage, an iterative process based on a similarity distance and the dispersion rate of first stage's output classes.

The remainder of this paper is organized as follows: Section 2 presents some related work on statistical approaches for anomaly detection. Section 3 describes, in details, our proposed approach. Section 4 shows and discusses experimental results. We briefly conclude our work in Section 5.

### 2. Statistical Approaches for Anomaly Detection

Statistical approaches are commonly based on probabilistic models associated with training data. Several approaches to modeling normal and anomalous data have been applied to intrusion detection: Eleazar Eskin<sup>9</sup> presented a mixture model based technique for detecting anomalies within a dataset that contains a large number of normal instances and relatively few anomalies. His approach uses machine-learning techniques to estimate a probability distribution over this dataset and applies a statistical test to detect anomalies. 10 presents an anomaly detection technique based on a chi-square statistic for intrusion detection into information systems. The authors highlight the great computational cost when using Hotelling's T<sup>2</sup> statistic and discussed the use of a distance measure based on chi-square test statistic instead. Authors in 11 proposed a prototype of a network anomaly detection system, with hierarchical architecture, that uses statistical models and neural network classifiers to detect intrusions. Data are gathered from network traffic, system logs as well as hardware reports. In 12, authors discussed the use of a multivariate statistical analysis of audit trails for host-based intrusion detection. They also discussed and compared the performance of Hotelling's T<sup>2</sup> test and chi-squared test. <sup>13</sup> proposes a statistical processing unit, that utilize application specific knowledge of the network services, to detect anomalous network traffic, specifically the less frequent attacks such as R2L and U2R. A metric is developed which allows the system to automatically search identical characteristics of different service requests. Where authors in 14 used Kolmogorov-Smirnov statistics to model and detect DoS as well as probing attacks. Authors in <sup>15</sup> proposed an approach based on Adaptive Bayesian Algorithm (ABA) for anomaly intrusion detection and compared it with Naïve Bayesian Algorithm using KDD99 dataset. Krueggel and al. 16 suggested an event classification scheme based on Bayesian networks to mitigate two main reasons for large false alarm. According to them, the first reason is the simplistic aggregation of model outputs in the decision phase. The second reason is the lack of integration of additional information into the

decision process. The approach in <sup>17</sup> flows multiple steps. First, Kalman filter is performed on raw data. Then a Gaussian Mixture Model (GMM) is built, since authors assumed that the real distribution is a mixture of normal densities. Hidden Markov Model is, after that, applied to find the temporal dependencies above the different Gaussian components. Finally, Viterbi algorithm is used to detect anomalous events.

Our work presented in this paper is strongly related to those cited above to the extent that statistical methods are applied. However, our approach slightly differs from theirs as we build a statistical model from normal instances only and consider instances of the rejected class as attacks. To improve the decision rule, we introduced regularization into the discriminant function of Maximum Likelihood.

#### 3. Proposed approach

The main idea is to build a model representing the normal instances from which we define a discriminant function. A new instance is identified as anomaly if it does not comply with the predefined pattern under the hypothesis Null Ho and the alternative H1, regarding a threshold T. Instances identified as anomaly are then reclassified under some conditions based on a similarity distance and anomaly class's dispersion. Fig.I. and pseudocode.1. illustrate the block diagram of the process's main steps and the corresponding pseudocode.

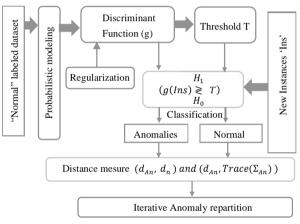


Fig. 1. Bloc diagram of the SSAD

#### Pseudocode, 1. SSAD Input: TrainDatasetNormal, TestDataset Output: TestDatasetLabeled Initialize parameters: precision $\varepsilon$ , p( $C_i$ ), $\alpha$ Compute $\hat{\Sigma}_{i}^{reg}$ , $\mu_{i}$ Create the Discriminant Function Compute the threshold T for each instance inst in TestDataset { Compute $g(X^{Ins})$ if $(g(X^{Ins}) \ge T)$ inst is labeled "normal" else inst is labeled "anomaly" } Stage 2: Compute $\mu_{normal}$ , $\mu_{anomaly}$ trace $(\Sigma_{anomaly})$ Repeat for each instance inst in anomaly cluster if $(d(inst, \mu_{an}) < d(inst, \mu_{nor}) && d(inst, \mu_{an}) < tr(\Sigma_{an}))$ label inst as « anomaly » else label inst as « normal » Until number of changed label < 5

#### 3.1. Discriminant Function

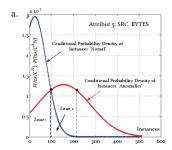
Let  $X^{Ins} = [x_1, x_2, ... x_n]^T$  be an instance featured by n attributes. Attribute's value of this instance are assumed to be possible values from a random variable whose conditional density function is given by  $p(X^{Ins}/C^N)$ . Considering a unidimensional case, Fig.II.a shows the probability density of the attribute "src\_bytes" in nsl-kdd dataset. The overlapping zones of the two distributions are indicators of instances' separability. This overlap is even more pronounced in fig.II.b whose probabilities are calculated on the attribute "dst\_bytes" of a subset with higher detection difficulty.

Furthermore, knowing the class  $C^N$ , we can calculate the a posteriori probability  $p(C^N/X^{Ins})$  expressed by Bayes rule <sup>18</sup> and given as follow:  $p(C^N/X^{Ins}) = p(X^{Ins}/C^N) * p(C^N)$  (1)

Where  $p(C^N)$  is the a priori probability of normal instances.

The posteriori probability gives the likelihood that the instance  $X^{Ins}$  belongs to the class  $C^N$ . In the general case, the logarithmic expression of  $p(C^i/X^{Ins})$  is given by:

$$g_i(X) = \log\left(p(C^i/X^{lns})\right) = Log\left(p(X^{lns}/C_i) + \log\left(p(C_i)\right)\right) \tag{2}$$



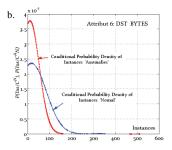


Fig. II. Probability density function of training dataset (a) Low difficulty (b) Hight difficulty instances

Where  $g_i(X)$  represents the discriminant function.

The decision rule in a multiclass case is as follows:

$$X \in C_i$$
 si  $g_i(X) > g_i(X)$  for  $i \neq j$ 

We assume that the data follows a multivariate Gaussian distribution. In this case, the discriminant function shall be as follows:

$$g_i(X) = -\frac{1}{2}(X - \mu_i)^T \Sigma_i^{-1}(X - \mu_i) - \frac{1}{2}\log(|\Sigma_i| - \frac{1}{n}\log(2\pi) + \log\{p(C_i)\}$$
 (3)

Where  $\mu_i$  is mean vector and  $\Sigma_i$  is the variance-covariance matrix.

To handle non-modeled instances and make the process semi-automatic, we introduce threshold verification in the decision rule. The goal of using threshold is to create an anomaly class with this decision rule:

$$\left\{ \begin{array}{ll} g_i(X) \geq T_i & X \in normal\ class & (H_1) \\ \text{Otherwise} & X \in anomaly\ class & (H_0) \end{array} \right.$$

From equations 3 and 4, we may put:

$$-\frac{1}{2}(X - \mu_i)^T \Sigma_i^{-1}(X - \mu_i) - \frac{1}{2} \log(|\Sigma_i|) + \log\{p(C_i)\} > T_i$$

The expression  $(X - \mu_i)^T \Sigma_i^{-1} (X - \mu_i) = d$  follows a chi square  $\chi^2$  distribution with n degree of freedom. Threshold expression becomes:  $T_i = -\frac{d}{2} - \frac{1}{2} \log(|\Sigma_i|) + \log\{p(C_i)\}$  (5)

#### 3.2. Regularization

The accuracy of the detection in the first step depends mainly on the discriminant function of normal instances. It relies on the representativeness of the variance-covariance matrix  $\Sigma_i$  of "normal" cluster. In order to optimize this function, we introduced regularization for  $\Sigma_i$  with the overall matrix variance-covariance  $\Sigma_g$ . The regularization term is given by:  $\Sigma_i^{reg} = \alpha \Sigma_i + (1-\alpha) \Sigma_g$ , where  $\alpha$  is a weighting parameter and  $\alpha \in [0\ 1]$ . Two clusters  $\{Cluster(N), Cluster(AN)\}$  result from the first detection phase.

#### 3.3. Iterative Anomaly repartition

In order to reduce false alarm rate, we added an iterative process that reclassifies first stage's anomaly cluster. Each instance in this cluster will either be kept as "anomaly" or relabeled as "normal".

Let  $\mu_{normal}$  and  $\mu_{anomaly}$  be the mean of normal and anomaly clusters respectively.  $\Sigma_{anomaly}$  is the variance of anomaly cluster. An instance *inst* is labeled as anomaly if, and only if, *distance* (*inst*,  $\mu_{anomaly}$ ) is smaller than *distance* (*inst*,  $\mu_{anomaly}$ ) and *distance* (*inst*,  $\mu_{anomaly}$ ) is smaller than *trace*( $\Sigma_{anomaly}$ ). Otherwise, *inst* is labeled as normal. The process is repeated until a stable configuration is met (no changing labels).

#### 4. Experimental Results and Discussion

#### 4.1. Datasets

Experiments were carried out using NSL-KDD<sup>19</sup> and Kyoto 2006+ <sup>20</sup> datasets.

#### 4.1.1. NSL-KDD

NSL-KDD dataset is the refined version of KDDcup99 known for some deficiencies mentioned in <sup>21</sup>. It has numerous advantages over the original KDD data set like the absence of redundant records or the estimation of the difficulty level of each instance.

The dataset contains a large volume of network TCP connections, the results of 5 weeks of capture in the Air force network. Each connection consists of 41 attributes plus a label of either normal or a type of attack. Simulated attacks fall into one of the four following categories <sup>5</sup> DOS, U2R, R2L or PROBE.

#### 4.1.2. Kyoto 2006+

Kyoto 2006+ dataset is built on 3 years of real traffic data (from Nov. 2006 to Aug. 2009) which are obtained from diverse types of honeypots in Kyoto University<sup>22</sup>. It consists of 14 statistical features derived from KDD Cup 99' dataset as well as 10 additional features to further analyse and evaluate network IDSs<sup>23</sup>. Traffic was collected to/from 348 honeypots deployed inside and outside of Kyoto University. All traffic was thoroughly inspected using three security softwares: SNS7160 IDS, Clam AntiVirus, Ashula and since Apr.2010, snort was added. We used in our experiments traffic data from 2009 captures.

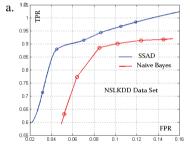
Table.1 and Table.2 describe the composition of multiple subsets, from the data described above, used to test and compare SSAD to other statistical methods.

Table 1. Experimental subsets of NSL-KDD

Subset	Normal	Anomaly	Size
Kdd_1	9711	12833	22544
Kdd_2	8131	6720	14851
Kdd_3	23881	5822	29703
Kdd_4	25844	18711	44555
Kdd_5	48366	11040	59406
Kdd_6	50165	24093	74258

Table 2. Experimental subsets of Kyoto 2006+

Subset	Normal	Anomaly	Size
Kyoto_1	60341	8912	69253
Kyoto_2	120806	17701	138507
Kyoto_3	181119	26641	207760
Kyoto_4	241430	35584	277014
Kyoto_5	301784	44483	346267
Kyoto_6	1605096	213910	1819006



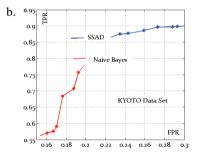


Fig. III. Experimental results (a) nsIKDD dataset (b) Kyoto 2006+ dataset

#### 4.2. Experimental Results

Experiments were carried out using Windows® 8-64 bit operating system with core i7 processor running at 2.40 GHz and 8 GB RAM. The first phase parameters were set to:  $\alpha = 0.8$ ,  $p(C_n) = 0.6$ ,  $\epsilon$  (precision) =80%. These values were chosen after several tests and were selected to be those that give the best results.

The accuracy of any intrusion detection system is determined by true positive rate (TPR = TP/(TP + FN)) and false positive rate (FPR = FP/(FP + TN)). The detection rate is expected to be as high as possible, while the false positive rate is expected to be as low as possible.

As can be seen in fig.III, SSAD outperforms Naïve Bayes in terms of TPR and FPR. Even though, Kyoto 2006+dataset is more challenging than nslKDD, which was created more than a decade ago.

#### 5. Conclusion

In this paper, we present a semi-supervised statistical approach for network anomaly detection (SSAD). The first step of the approach is to build a model of normal instances, a threshold is then established and a classification is made based on H0 and H1 hypothesis. A second step is proposed to reduce the false positive rate. It consists on reclassifying anomaly instances (from the first step) using a similarity distance and anomaly class's dispersion. Comparative tests using nslKDD and Kyoto 2006+ datasets show that this approach has promising results. As future work, we plan to explore other probabilistic distribution, consider the online detection and evaluate our solution using more challenging datasets.

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